EE5600 Assignment 3

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Abstract—This document contains the solution to a Linear-Programming question.

Download all python codes from

https://github.com/Jayanth9969/EE5600/tree/master/Assignment3/codes

1 Problem

Maximise Z = 3x + 2y subject to $x + 2y \le 10, 3x + y \le 15, x, y \ge 0$

2 Solution

$$Maximize: 3x_1 + 2x_2$$
 (2.0.1)

$$Subject - to: x_1 + 2x_2 \le 10$$
 (2.0.2)

$$3x_1 + x_2 \le 15 \tag{2.0.3}$$

The Problem is converted into canonical form by adding slack variables. Then Problem becomes,

Maximize :
$$3x_1 + 2x_2 + 0s_1 + 0s_2$$
 (2.0.4)

Constraints:
$$x_1 + 2x_2 + s_1 = 10$$
 (2.0.5)

$$3x_1 + x_2 + s_2 = 15$$
 (2.0.6)

we write the Simplex tableau,

$$\begin{pmatrix}
x_1 & x_2 & s_1 & s_2 & c \\
1 & 2 & 1 & 0 & 10 \\
3 & 1 & 0 & 1 & 15 \\
-3 & -2 & 0 & 0 & 0
\end{pmatrix}$$
(2.0.7)

Keeping the Pivot element as 3 and by using gauss-jordan Elimination we get

$$\begin{pmatrix}
x_1 & x_2 & s_1 & s_2 & c \\
0 & \frac{5}{3} & 1 & \frac{-1}{3} & 5 \\
1 & \frac{1}{3} & 0 & \frac{1}{3} & 5 \\
0 & -1 & 0 & 1 & 15
\end{pmatrix} (2.0.8)$$

Keeping the Pivot element as $\frac{5}{3}$ and by using gauss-jordan Elimination we get

$$\begin{pmatrix}
x_1 & x_2 & s_1 & s_2 & c \\
0 & 1 & \frac{3}{5} & \frac{-1}{5} & 2 \\
1 & 0 & \frac{-1}{5} & \frac{2}{5} & 3 \\
\hline
0 & 0 & \frac{3}{5} & \frac{4}{5} & 18
\end{pmatrix} (2.0.9)$$

In this tableau Since all indicators in last row are non-negative ,we found optimal solution to given problem. Therefore Optimal Solution will be:

$$(x_1, x_2) = (4, 3)$$
 (2.0.10)

$$Z = 3x_1 + 2x_2 \tag{2.0.11}$$

$$Z = 3 \times 4 + 2 \times 3 \tag{2.0.12}$$

$$Z = 18$$
 (2.0.13)

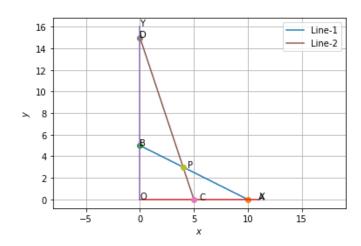


Fig. 2.0: Region OBPC is Valid region

This Problem can be represented in matrix form as follows,

$$\max_{\mathbf{x}} Z = \begin{pmatrix} 3 & 2 \end{pmatrix} \mathbf{x} \qquad (2.0.14)$$

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$$s.t. \quad \begin{pmatrix} 1 & 2 \\ 3 & 1 \end{pmatrix} \mathbf{x} \le \begin{pmatrix} 10 \\ 15 \end{pmatrix} \qquad (2.0.15)$$

$$\mathbf{x} \ge \mathbf{0} \qquad (2.0.16)$$

$$\mathbf{x} \succeq \mathbf{0} \tag{2.0.16}$$

$$\mathbf{y} \succeq \mathbf{0} \tag{2.0.17}$$

this is solved using cvxpy in python,we get

$$\mathbf{x} = \begin{pmatrix} 3.999999999 \\ 2.99999999 \end{pmatrix}, Z = 17.99999996$$
 (2.0.18)