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EE5600 Assignment 1

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Abstract—This document contains the solution to a Lines and planes problem. Download all python codes from

https://github.com/Jayanth9969/EE5600/blob/master/Assignment1/code.py

1 Problem

Find the Angle between the following lines

$$(\sqrt{3} \quad 1) \mathbf{x} = 1$$

$$(1 \quad \sqrt{3}) \mathbf{x} = 4$$

2 Solution

The **Approach** is: For finding the Angle between these lines we will use dot-Product Formula and with the help of direction vectors we can find angle between these 2 lines.

a) We will make direction vectors from these line vectors form:

$$\mathbf{m}_1 = \begin{pmatrix} -\sqrt{3} & 1 \end{pmatrix} \tag{2.0.1}$$

$$\mathbf{m}_2 = \begin{pmatrix} -1 & \sqrt{3} \end{pmatrix} \tag{2.0.2}$$

Now we will find out magnitudes of each vectors $\mathbf{m}_1, \mathbf{m}_2$:

$$\|\mathbf{m}_1\| = \sqrt{3+1} = 2$$
 (2.0.3)

$$\|\mathbf{m}_2\| = \sqrt{1+3} = 2$$
 (2.0.4)

Thus angle between 2 vectors \mathbf{m}_1 , \mathbf{m}_2 can be found using dot-product using the formula below, Let θ be angle between vectors \mathbf{m}_1 , \mathbf{m}_2 then,

$$\theta = \cos^{-1}\left(\frac{\mathbf{m}_1 \mathbf{m}_2^T}{\|\mathbf{m}_1\| \|\mathbf{m}_2\|}\right)$$
 (2.0.5)

By,Putting values into above equation we get,

$$\theta = \cos^{-1}\left(\frac{\left(-\sqrt{3} \quad 1\right)\left(\frac{-1}{\sqrt{3}}\right)}{2\times 2}\right) \tag{2.0.6}$$

$$\theta = \cos^{-1}\left(\frac{2 \times \sqrt{3}}{4}\right) \tag{2.0.7}$$

$$\theta = \cos^{-1}\left(\frac{\sqrt{3}}{2}\right) \tag{2.0.8}$$

$$\theta = 30^{\circ} \tag{2.0.9}$$

Thus the angle between given lines is 30°

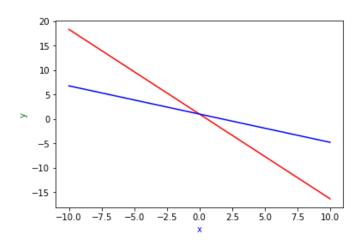


Fig. 2.0.1: Figure