

Nearest Neighbour Method



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Abstract—This manual introduces the nearest neighbour method.

1 Dataset

1.1 Generate $S_x = \{\mathbf{m}_{xk}\}_{k=1}^{10}$ from the bivariate Gaussian distribution.

$$\mathcal{N}\left(\begin{pmatrix}1\\0\end{pmatrix},I\right).$$
 (1.1)

1.2 Generate $S_y = \left\{ \mathbf{m}_{yk} \right\}_{k=1}^{10}$ from the bivariate Gaussian distribution.

$$\mathcal{N}\left(\begin{pmatrix} 0\\1 \end{pmatrix}, I\right).$$
 (1.2)

1.3 Generate

$$\mathbf{x}_n = \mathcal{N}(\mathbf{m}_{xk}, I/5), n = 1, ..., 100$$
 (1.3)

such that \mathbf{m}_{xk} are picked uniformly from S_x .

1.4 Generate

$$\mathbf{y}_n = \mathcal{N}(\mathbf{m}_{yk}, I/5), n = 1, ..., 100$$
 (1.4)

such that \mathbf{m}_{yk} are picked uniformly from S_y .

1.5 Generate a scatterplot for \mathbf{x}_n in orange colour and \mathbf{y}_n in blue colour.

2 Nearest Neighbour

2.1 Find
$$\mathbf{y} = \begin{pmatrix} y_1 \\ y_2 \end{pmatrix}$$
,

$$y_2 = \frac{1}{k} \sum_{i \in N_k(y_1)} x_{2i} \tag{2.1}$$

where

$$N_k(y_1) = \{i : |x_{1i} - y_1| < \epsilon < |x_{1j} - y_1|\}, (2.2)$$

$$|N_k(y_1)| = k \tag{2.3}$$

- 2.2 Plot \mathbf{y}_m , $1 \le m \le 100$ for k = 15.
- 2.3 Repeat the exercise for k = 1.
- 2.4 Compare with the least squares estimate.

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