

ASSIGNMENT 4

- 1) Formulate and solve this transportation problem using lpsolve, or any other equivalent library in R.

	Unit Shipping Cost			Unit	Monthly
	Warehouse 1	Warehouse 2	Warehouse 3	Production Cost	Production Capacity
Plant A	\$22	\$14	\$30	\$600	100
Plant B	\$16	\$20	\$24	\$625	120
Monthly Demand	80	60	70		

Formulation of the transportation Problem

Approach 1

Decision Variables:

X_{ij} = No. of units shipped from Plant i to Warehouse j

X_{AW1} = No. of units shipped from Plant A to Warehouse 1

X_{AW2} = No. of units shipped from Plant A to Warehouse 2

X_{AW3} = No. of units shipped from Plant A to Warehouse 3

X_{BW1} = No. of units shipped from Plant B to Warehouse 1

X_{BW2} = No. of units shipped from Plant B to Warehouse 2

X_{BW3} = No. of units shipped from Plant B to Warehouse 3

Obj Function:

$$\begin{aligned}\text{Min } C &= 22 \text{ XAW1} + 14 \text{ XAW2} + 30 \text{ XAW3} + 16 \text{ XBW1} + 20 \text{ XBW2} + 24 \text{ XBW3} + 600 \\ &\text{XAW1} + 600 \text{ XAW2} + 600 \text{ XAW3} + 625 \text{ XBW1} + 625 \text{ XBW2} + 625 \text{ XBW3} \\ &= 622 \text{ XAW1} + 614 \text{ XAW2} + 630 \text{ XAW3} + 641 \text{ XBW1} + 645 \text{ XBW2} + 649 \text{ XBW3}\end{aligned}$$

Constraints:

s.t)

Plant A Supply: $\text{XAW1} + \text{XAW2} + \text{XAW3} \leq 100$

Plant B Supply: $\text{XBW1} + \text{XBW2} + \text{XBW3} \leq 120$

Warehouse 1: $\text{XAW1} + \text{XBW1} = 80$

Warehouse 2: $\text{XAW2} + \text{XBW2} = 60$

Warehouse 3: $\text{XAW3} + \text{XBW3} = 70$

All $X_{ij} \geq 0$

Approach 2**Using Dummy Model approach:**

Now total Supply(220) > total demand(210) – Must add new dummy nodes(with difference of 10 units. New Constraints for this new node is :

$$\text{Min } C = 622 \text{ XAW1} + 614 \text{ XAW2} + 630 \text{ XAW3} + 641 \text{ XBW1} + 645 \text{ XBW2} + 649 \text{ XBW3}$$

Constraints:

Supply Constraints:

Plant A Supply: $\text{XAW1} + \text{XAW2} + \text{XAW3} + \text{XAD4} = 100$

Plant B Supply: $\text{XBW1} + \text{XBW2} + \text{XBW3} + \text{XBD4} = 120$

Demand Constraints:

Warehouse 1: $X_{AW1} + X_{BW1} = 80$

Warehouse 2: $X_{AW2} + X_{BW2} = 60$

Warehouse 3: $X_{AW3} + X_{BW3} = 70$

Warehouse 4: $X_{AW4} + X_{BW4} = 10$ (Dummy)

Solution:

The problem is solved using R and the code is in

Assignment_Quant4.Rmd file (Rmd and LP files folder) and

The knitted file (Assignment_Quant4_Solutions_Knitted.pdf) is in pdf folder

2.A) FORMULATION FOR TRANSSHIPMENT PROBLEM

Objective Function:

Min $C = 1.52 X_{1A} + 1.60 X_{1B} + 1.40 X_{1C} + 1.70 X_{2A} + 1.63 X_{2B} + 1.55 X_{2C} + 1.45 X_{3A} + 1.57 X_{3B} + 1.30 X_{3C} + 5.15 X_{AR1} + 5.69 X_{AR2} + 6.13 X_{AR3} + 5.63 X_{AR4} + 5.80 X_{AR5} + 5.12 X_{BR1} + 5.47 X_{BR2} + 6.05 X_{BR3} + 6.12 X_{BR4} + 5.71 X_{BR5} + 5.32 X_{CR1} + 6.16 X_{CR2} + 6.25 X_{CR3} + 6.17 X_{CR4} + 5.87 X_{CR5};$

Decision Variables: in (TBD= Thousand Barrels per Day)

Wells to Pump Stations:

X_{1A} = No. of units of oil barrels moved from Well 1 to Pump station A in TBD

X_{1B} = No. of units of oil barrels moved from Well 1 to Pump station B in TBD

X1C= No. of units of oil barrels moved from Well 1 to Pump station C in TBD

X2A= No. of units of oil barrels moved from Well 2 to Pump station A in TBD

X2B= No. of units of oil barrels moved from Well 2 to Pump station B in TBD

X2C= No. of units of oil barrels moved from Well 2 to Pump station C in TBD

X3A= No. of units of oil barrels moved from Well 3 to Pump station A in TBD

X3B= No. of units of oil barrels moved from Well 3 to Pump station B in TBD

X3C= No. of units of oil barrels moved from Well 3 to Pump station C in TBD

Pump Stations to Refineries:

XAR1= No. of units of oil barrels moved from Pump station A to Refinery 1 in TBD

XAR2= No. of units of oil barrels moved from Pump station A to Refinery 2 in TBD

XAR3= No. of units of oil barrels moved from Pump station A to Refinery 3 in TBD

XAR4= No. of units of oil barrels moved from Pump station A to Refinery 4 in TBD

XAR5= No. of units of oil barrels moved from Pump station A to Refinery 5 in TBD

XBR1= No. of units of oil barrels moved from Pump station B to Refinery 1 in TBD

XBR2= No. of units of oil barrels moved from Pump station B to Refinery 2 in TBD

XBR3= No. of units of oil barrels moved from Pump station B to Refinery 3 in TBD

XBR4= No. of units of oil barrels moved from Pump station B to Refinery 4 in TBD

XBR5= No. of units of oil barrels moved from Pump station B to Refinery 5 in TBD

XCR1= No. of units of oil barrels moved from Pump station C to Refinery 1 in TBD

XCR2= No. of units of oil barrels moved from Pump station C to Refinery 2 in TBD

XCR3= No. of units of oil barrels moved from Pump station C to Refinery 3 in TBD

XCR4= No. of units of oil barrels moved from Pump station C to Refinery 4 in TBD

XCR5= No. of units of oil barrels moved from Pump station C to Refinery 5 in TBD

Constraints:

S.t)

Supply = 276; Demand= 274

Supply > demand

Supply constraints :

$$X1A + X1B + X1C \leq 93;$$

$$X2A + X2B + X2C \leq 88;$$

$$X3A + X3B + X3C \leq 95;$$

Transshipment Nodes:

$$X1A + X2A + X3A = XAR1 + XAR2 + XAR3 + XAR4 + XAR5;$$

$$X1B + X2B + X3B = XBR1 + XBR2 + XBR3 + XBR4 + XBR5;$$

$$X1C + X2C + X3C = XCR1 + XCR2 + XCR3 + XCR4 + XCR5;$$

Demand Constraints:

$$XAR1 + XBR1 + XCR1 = 30;$$

$$XAR2 + XBR2 + XCR2 = 57;$$

$$XAR3 + XBR3 + XCR3 = 48;$$

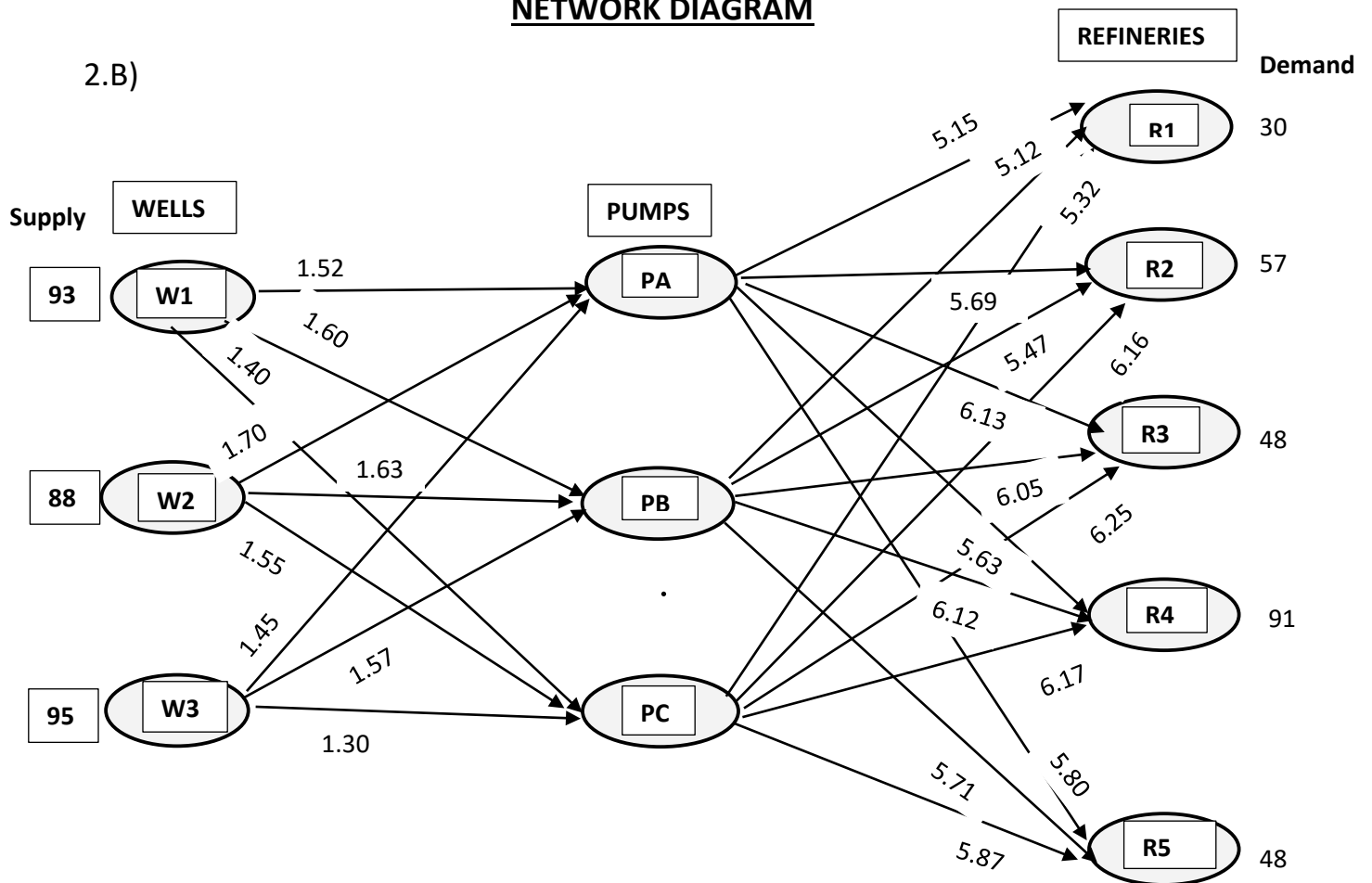
$$XAR4 + XBR4 + XCR4 = 91;$$

$$XAR5 + XBR5 + XCR5 = 48;$$

$$\text{All } X_{ij} \geq 0$$

NETWORK DIAGRAM

2.B)



Solution:

The problem is solved using R and the code is in

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