CSI 747 – Midterm Submission

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Introduction:

The midterm required implementing Support Vector Machine with primal soft-margin method, dual-soft margin method and a dual soft-margin method with a radial basis kernel. This document mentions the process used to prepare data, models implemented in AMPL to train the models; and to test the results obtained from training data.

The following sections discuss each of these implementations – Training and Testing - in more detail:

- 1. Preparing Data for questions (2), (3), and (4), and Preparing Data for question (5).
- 2. Implementation of Primal soft-margin SVM to differentiate 3s and 6s.
- 3. Implementing Dual soft-margin SVM to differentiate 3s and 6s.
- 4. Dual soft-margin SVM using a Radial Basis Kernel.
- 5. Dual soft-margin SVM using a Radial Basis Kernel to differentiate even numbers from odd numbers.

Preparing Data Sets:

The data for questions (2),(3) and (4) was taken from files "train3.txt", "train6.txt" for training the SVM, and "test3.txt", "test6.txt" for Testing the values obtained from SVM.

500 vectors from each of the above mentioned files were used for forming the training and test set.

These vectors were each normalized before running through the SVM.

The code - implemented in MATLAB - used for forming datasets for (2),(3) and (4) is given below:

Form_3and6_DataSets.m

```
clear all; clc;
train3 = dlmread('midtermdata/train3.txt');
train3 subset = train3(1:500,:);
clear train3;
train6 = dlmread('midtermdata/train6.txt');
train6 subset = train6(1:500,:);
clear train6;
```

```
test3 = dlmread('midtermdata/test3.txt');
test3 subset = test3(1:500,:);
clear test3;
test6 = dlmread('midtermdata/test6.txt');
test6 subset = test6(1:500,:);
clear test6;
train set 20 = [train3 subset;train6 subset];
test set 20 = [test3_subset;test6_subset];
for i = 2:length(train_set_20(:,1))
    dr = 0;
    if (max(train set 20(i,2:end)) == 0)
        dr=1:
    else
        dr = max(train set 20(i, 2:end));
    train set 20(i,2:end) = train set 20(i,2:end)/dr;
end
for i = 2:length(test set 20(:,1))
    dr = 0;
    if (max(test set 20(i, 2:end)) == 0)
        dr=1;
    else
        dr = max(test set 20(i, 2:end));
    test_set_20(i,2:end) = test_set_20(i,2:end)/dr;
end
horz = 1:length(train set 20(1,:));
vert = 0:length(train set 20(:,1));
train set 20 = [horz;train set 20];
train set 20 = [vert',train set 20];
horz = 1:length(test_set_20(1,:));
vert = 0:length(test_set_20(:,1));
test_set_20 = [horz;test_set_20];
test set 20 = [vert', test set 20];
dlmwrite('3and6 Train set.txt', train set 20,' ');
dlmwrite('3and6 Test set.txt',test set 20,' ');
```

The Dataset for question 5 was formed by taking 100 first data points from each of the Training and Test datasets.

The code in MATLAB used for forming them is below:

Create_Full_DataSet.m

```
clear all; clc;
display 'creating subset of files';
display 'This might take some time!!';
files = dir('midtermdata/train*.txt');
train = [];
data set=[];
%Read in RAW data from files
for nm = 1:length(files)
    train data = dlmread(strcat('midtermdata/', files(nm).name));
    data_set = train_data(1:100,2:end);
    train = [train;data_set];
end
for i = 2:length(train(1,:))
    dr = 0;
    if (max(train(:,i)) ==0)
        dr = 1;
    else
        dr = max(train(:,i));
    train(:,i) = train(:,i)/dr;
end
horz = 1:length(train(1,:));
vert = 0:length(train(:,1));
train = [horz;train];
train = [vert',train];
dlmwrite('Train Set Full.txt',train,' ');
```

Implementing Primal Soft-Margin SVM:

The Primal Soft-Margin SVM was trained using the following AMPL code:

SVM-2.mod: include SVM-2-Train.mod

```
param n := 785;
param D := 1000;
param C := 100;
set POINTS := {2..n};
#set POINTS1 := {1..n-1};
set INPUT POINTS := {1..n};
set DATASET := {1..D};
param x{DATASET,POINTS1};
param y{DATASET};
data 3and6_Train_set.txt;
Setting the value of y: 1 if digit is 3 and -1 for 6
for {i in DATASET} {
      if x[i,1] = 3 then {let y[i] := 1} else{ let y[i] := -1};
}
var w{POINTS};
var b;
var eta{DATASET} >= 0;
minimize SVM {j in POINTS} : 0.5*(w[j]*w[j])+(C*sum {i in DATASET} eta[i]);
s.t. CONDITION {i in DATASET}: y[i]*( (sum {j in POINTS} (x[i,j]*w[j]))-b) >= 1-
eta[i];
option solver snopt;
solve;
```

The code was run, and gave the following values of w and b:

Result: SVM-2-Train.mod

```
SNOPT 7.2-8: Optimal solution found.
7500 iterations, objective 0.9331388318
w [*] :=
 2 0
                 198 0
                                   394 0
                                                     590 0
 3 0
                 199 0
                                   395 0
                                                     591 0
 4 0
                 200 0.00632913
                                   396 0
                                                     592 0.00245573
 5 0
                 201 0.00476042
                                   397 0
                                                     593 0.0326093
                 202 0.0206777
 6 0
                                   398 -0.0125816
                                                     594 0.0533608
```

```
7
                                       399 -0.0467392
    0
                   203 0.0268085
                                                           595
                                                                 0.0389315
 8
                   204
                        0.0488274
                                       400 0.0187036
                                                           596
                                                                 0.034354
 9
                   205
                        0.0389903
                                       401 -0.0270946
                                                            597
                                                                 0.0242443
    a
10
                   206
                        0.0146756
                                       402 -0.057874
                                                            598
                                                                 0.0181352
11
    a
                   207
                        0.058661
                                       403 -0.0719348
                                                            599 -0.06953
12
    0
                   208
                        0.0150024
                                       404 -0.0270767
                                                           600 -0.0228797
13
    0
                   209
                        0.0560007
                                       405 -0.0164912
                                                           601
                                                                0.0171081
14
    0
                   210
                        0.00505681
                                       406 -0.0962813
                                                           602 -0.0804761
15
    0
                   211
                        0.0220115
                                       407 -0.0390875
                                                           603 -0.0980588
                        0.00560537
                                       408
                                           0.0305464
                                                           604
                                                                0.00454695
16
    0
                   212
17
                   213
                        0.0342548
                                       409
                                            0.0805546
                                                           605
                                                                 0.0279356
    0
                                       410 0.0147909
18
    a
                   214
                        0.110073
                                                           606
                                                                0.0222861
19
    0
                   215
                        0.0251302
                                       411 -0.0132871
                                                           607 -0.041661
20
    0
                   216
                        0.0641945
                                       412
                                           0.0957558
                                                           608
                                                                0.001856
                   217
                                       413
                                                           609
21
    0
                        0.0791721
                                            0.0190721
                                                                0.0339414
22
    0
                   218
                        0.0664382
                                       414 -0.0175872
                                                           610
                                                                 0.0873956
23
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                   219 0.0400187
                                       415 -0.0605229
                                                           611
                                                                 0.0320942
24
                   220 0.0294737
                                       416 -0.105098
                                                           612 -0.0156752
    0
25
                   221 0.0350157
                                       417 -0.0715644
                                                           613
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26
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                   222 -0.0145561
                                       418 -0.0579831
                                                            614
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27
                   223 -0.0145561
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28
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29
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                                       422
30
    0
                   226
                       0
                                            0
                                                            618
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31
    0
                   227
                                       423
                                                           619
                   228 -2.04021e-16
                                       424 0.0173691
                                                           620 -8.71776e-17
32
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33
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                   229
                        0.0314506
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                                            0.0155242
                                                           621 0.000265927
34
                        0.0404709
                                       426 0.00191582
                   230
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                                                                 0.0169571
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                                                                 0.0446649
36
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                        0.0270541
                                       428 -0.0246455
                                                           624
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                   233
                                       429 -0.0751222
                                                           625
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    8.79568e-17
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                                                                 0.0146861
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                                                           626 -0.00870476
                                       431 -0.133554
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                   235
                        0.0353612
                                                           627
                                                                 0.0317492
   6.67412e-14
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                        0.0147125
                                       432 -0.0382567
                                                           628 -0.0567996
41 -1.81259e-14
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                        0.0594455
                                       433 -0.00180544
                                                           629
                                                                 0.066188
42 -6.15046e-17
                   238
                        0.004127
                                       434 0.00770934
                                                           630
                                                                0.00800053
43 -9.73425e-17
                        0.0216688
                                       435
                                            0.0218571
                                                           631 -0.0207817
                   239
44 -8.26129e-17
                        0.0964585
                                       436
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                   240
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                                                                 0.0154795
45
    2.37239e-17
                   241
                        0.09235
                                       437
                                            0.0581184
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                                                                 0.0837469
                        0.132497
46
                                       438
                                            0.0838373
                                                           634
                                                                0.0316464
   9.25021e-17
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47
    5.13718e-16
                   243
                        0.130264
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                                                                 0.0368887
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48 -9.47724e-17
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                        0.187343
                                           0.00897118
                                                                 0.0652766
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49
    5.57601e-14
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                        0.0938227
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50
    1.42974e-17
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                        0.0340535
                                       442 -0.0135053
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51
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                                       443 -0.0525532
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52
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                       0.0346546
                                       444 -0.0653997
                                                           640
                                                                 7.69512e-05
53
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                                       445 -0.0809408
                                                           641 -2.0229e-16
    0
54
                   250 -0.0145561
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                                       453 0.0308292
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62 -4.17697e-16
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     0
                    259 -0.00142818
                                        455 -0.0353069
                                                                  0.016505
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 64
     a
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                    262 -0.0404722
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                    263 -0.0438159
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                    264 -0.0137555
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                                        466 -0.023971
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 78 -0.000284464
                    274 -0.011698
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                                                            666
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                    275 0.0186208
                                        471 -0.0100166
                                                            667
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                                        475 -0.00957026
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 89
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     7.26285e-18
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 93 -0.0199014
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                    291 -0.0395043
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 96 -0.0243646
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                                        491 -0.111723
                    295 -0.00412512
                                                            687
                                                                  0.103679
100 -0.0550355
                    296 -0.00923371
                                        492 -0.113189
                                                            688
                                                                  0.0957395
                                        493 0.0474106
101 -0.0266202
                    297
                         0.0995732
                                                            689
                                                                 0.0484958
102 -0.00184472
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                         0.134602
                                        494 -0.0331465
                                                            690
                                                                  0.0642631
103 -0.0335711
                    299
                                        495 -0.00656597
                         0.150611
                                                            691
                                                                  0.0714345
104 -0.0523784
                    300
                         0.154909
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                                                            692
                                                                  0.0699319
105 -0.0437697
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                         0.0910238
                                        497 -0.0440807
                                                            693
                                                                  0.0266299
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106 -0.0225182
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                                                            694
                                                                  0.0252161
107 -0.0412614
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                                        499 0.0370107
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109 -0.0247767
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110 0
                    306 -0.0220941
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111
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112
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113
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114
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115
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116
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                                                            704
```

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117 0
                                                                   7.46019e-17
                    313 0.0501345
                                         509 0.0340338
                                                              705
                         0.0369451
                                         510
                                              0.0449696
                                                                   0.0245075
118 -1.53468e-14
                    314
                                                              706
119 -0.00943616
                    315
                                                              707
                                                                   0.0215537
                         0.00874006
                                         511
                                              0.0123433
120 -0.0107512
                    316
                         0.0230115
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                                                              708
                                                                   0.0223313
                         0.0082077
121
     0.0108339
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                                                                   0.0188472
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                                         514 -0.118481
                                                              710
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124
     0.0401592
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                                         516 -0.179158
                                                              712
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125
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                    321 0.058326
                                         517 -0.202646
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126
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                                                              715
127
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128 -0.0779316
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                                         520 -0.0572413
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129 -0.0344054
                    325
                         0.144185
                                         521 -6.06309e-06
                                                              717
                                                                   0.0134131
130
     0.0370221
                    326
                         0.0459134
                                         522 -0.0395031
                                                              718
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133 -0.133722
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                                         525 -0.064507
                                                              721
                                                                   0.0078615
134 -0.179007
                         0.03498
                                         526 -0.0236902
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135 -0.111586
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                                         527 -0.000111939
136 -0.0531318
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                    333 -0.0680615
                                         529 -0.0566487
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137 -0.0170078
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                                         530 -0.00942532
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139
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                         3.271e-14
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140
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142
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143
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144
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146 -0.00492316
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147 -0.0121125
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                                         539
                                              0.0123674
                                                              735
                                                                   0
148
     0.000705554
                    344
                         0.0285102
                                         540
                                              0.0396679
                                                              736
                                                                   0
149
                    345
                         0.0645023
                                         541
                                                              737
                                                                   0
     0.0793507
                                              0.0770845
     0.0551969
                                                              738
150
                    346
                         0.0337041
                                         542 -0.0141297
                                                                   0
     0.0266743
                                                              739
151
                    347 -0.02431
                                         543 -0.110427
                                                                   0
152
     0.0489251
                    348 -0.0152063
                                         544 -0.129196
                                                              740
                                                                   0.0116178
                                         545 -0.180832
                    349 0.0230228
                                                              741
                                                                   0.0116178
153
     0.0582853
                                         546 -0.111158
154
     0.0598178
                    350 -0.0408621
                                                              742
                                                                   0.0116178
155
     0.0818831
                    351 -0.00135278
                                         547 -0.0779778
                                                              743
                                                                   0.0116178
                    352 0.09315
                                         548 -0.0606605
156 -0.0126922
                                                              744
                                                                   0.0116178
157
     0.0545111
                    353
                         0.0355177
                                         549 -0.0624464
                                                              745
                                                                   0.0116178
                    354
                                         550
                                             0.00801447
                                                              746
158
     0.0850526
                         0.0123443
                                                                   0
159 -0.0386638
                    355
                         0.0305722
                                         551
                                              0.00708408
                                                              747
                                                                   0
160 -0.0319913
                    356
                         0.0619872
                                         552
                                              0.0544045
                                                              748
                                                                   0
                                         553
                                                              749
                                                                   0
161 -0.109335
                    357
                         0.0650978
                                              0.0175076
162 -0.132979
                    358
                        0.00981814
                                         554 -0.0185216
                                                              750
                                                                   0
                                         555 -0.0339329
163 -0.138792
                    359 -0.0494686
                                                              751
                                                                   0
164 -0.080498
                    360 -0.040193
                                         556
                                              0.0799483
                                                              752
                                                                   0
165 -0.0134477
                    361 -0.0504729
                                         557 -0.0171499
                                                              753
                                                                   a
166 -0.013419
                    362 -0.0699581
                                         558 -0.00957026
                                                              754
                                                                   a
                    363
                                         559 -0.00683594
                                                              755
167 -0.0145561
                         1.16723e-17
                                                                   0
168 -0.0145561
                    364
                         0
                                         560
                                              0
                                                              756
                                                                   0
169
     0
                    365
                         0
                                         561
                                              0
                                                              757
                                                                   0
                         0
                                              0
                                                                   0
170
     0
                    366
                                         562
                                                              758
171
     0
                    367
                         0
                                         563
                                              0
                                                              759
                                                                   0
```

```
172 0.0078615
                 368 0
                                  564 0.00727853
                                                   760 0
173 0.00702378
                 369 0.0436595
                                  565 0.0348105
                                                   761 0
                 370 0.0259214
174 -0.000951051
                                  566 0.0170382
                                                   762 0
175 -0.0102713
                 371 0.000171597
                                  567 0.00389667
                                                   763 0
                                  568 0.0244985
176 0.0242834
                 372 0.0390645
                                                   764 0
177 0.0742141
                 373 0.056723
                                  569 0.0695047
                                                   765
                                                       0
178 -0.0105544
                 374 0.015285
                                  570 0.0343081
                                                   766 0
179 -0.0208608
                 375 -0.0472017
                                  571 -0.0658294
                                                   767
                                                       0
376 -0.0398539
                                  572 -0.0483423
                                                   768 0
                 377 -0.00882352
                                  573 -0.0444746
                                                   769 0
                 378 -0.097911
                                  574 -0.0633916
                                                   770
                                  575 0.00575063
                 379 -0.0533587
                                                   771 0
184 0.0123267
                 380 0.0346085
                                  576 -0.00630118
                                                   772 0
185 -0.0149629
                 381 0.0329156
                                  577 -0.064012
                                                   773
                                                       0
                                                   774
186 0.0743554
                 382 -0.00408859
                                  578 -0.0358787
                                                       0
                                                   775
187 0.00388012
                 383 0.071261
                                  579 -0.0300458
                                                       0
188 0.0396797
                 384 0.0875986
                                  580 0.00311627
                                                   776 0
189 -0.028281
                 385 0.00465692
                                  581 -0.0209204
                                                   777 0
190 0.0275798
                 386 -0.00912711
                                  582 -0.0628325
                                                   778 0
191 0.0219908
                 387 -0.0826662
                                  583 -0.0105376
                                                   779
                                                       0
192 -0.0333734
                 388 -0.0783939
                                  584 0.0341486
                                                   780 0
193 0.00669146
                                  585 -0.00620682
                                                   781
                                                       0
                 389 -0.0564344
194 -0.0145561
                 390 -0.0650109
                                  586 -0.000743322
                                                   782 0
                 391 -0.00629943
                                  587 2.28871e-14
195 -0.0145561
                                                   783
                                                       0
196 -0.0145561
                 392 0
                                  588 0
                                                   784
                                                       0
                                  589 0
197 -0.0145561
                 393 0
                                                   785 0
b = -0.100834
```

These values of W and b were used on the Test Dataset to determine if the digit was 3 or 6. The model for Testing was implemented as follows:

SVM-2.mod: include SVM-2-Test.mod

```
param x_test{DATASET,INPUT_POINTS};
param y_test{DATASET};

param test{DATASET};

param hit3; param miss3;
param hit6; param miss6;

param total_hits; param total_misses;

data 3and6_Test_set.txt;

let hit3 := 0; let miss3 := 0;
let hit6:= 0; let miss6 := 0;
let total_hits :=0; let total_misses:=0;
```

```
#Checking number of misses for digit 3
for {i in {1..500}} {
      #Finding where the point is placed on the hyperplane
      let test[i] := sum {j in POINTS} (x_test[i,j]*w[j]) - b;
      if (test[i] >= 0) then
      {
             let y_test[i] := 1;
             let hit3 := hit3+1
      }
      else
      {
             let y_test[i] := -1;
             let miss3 := miss3+1
      };
};
#Checking number of misses for digit 6
for {i in {501..1000}} {
      #Finding where the point is placed on the hyperplane
      let test[i] := sum {j in POINTS} (x_test[i,j]*w[j]) - b;
      if (test[i] >= 0) then
      {
             let y_test[i] := 1;
             let miss6 := miss6+1
      }
      else
      {
             let y_test[i] := -1;
             let hit6 := hit6+1
      };
};
#Calculating Accuracy and Errors
for {i in DATASET}
{
      if(test[i] >= 0 and x_test[i,1] == 3) then
      {
             let total hits:=total hits+1;
      }
      else if(test[i] < 0 and x_test[i,1] == 6) then</pre>
      {
             let total_hits := total_hits+1;
      }
      else
      {
             let total_misses := total_misses + 1;
      };
};
display y_test;
display hit3, miss3, hit6, miss6;
```

The output generated by testing on the Test Data set was as follows:

SVM-2-Test.mod: Output

y_tes	+ [*] :=									
1	1	126	1	251	1	376	1	501 -1	626 -1	751 -1	876 -1
2	1	127	1	252	1	377	1	502 -1	627 -1	752 -1	877 -1
3	1	128	1	253	1	378	1	503 -1	628 -1	753 -1	878 -1
4	1	129	1	254	1	379	1	504 1	629 -1	754 -1	879 -1
5	1	130	1	255	1	380	1	505 -1	630 -1	755 -1	880 -1
6	1	131	1	256	1	381	1	506 -1	631 -1	756 -1	881 -1
7	1	132	1	257	1	382	1	507 -1	632 -1	757 -1	882 -1
8	1	133	1	258	1	383	1	508 -1	633 -1	758 -1	883 -1
9	1	134	1	259	1	384	1	509 -1	634 -1	759 -1	884 -1
10	1	135	1	260	1	385	1	510 -1	635 -1	760 -1	885 -1
11	1	136	1	261	1	386	1	511 -1	636 -1	761 -1	886 -1
12	1	137	1	262	1	387	1	512 -1	637 -1	762 -1	887 -1
13	1	138	1	263	1	388	1	513 -1	638 -1	763 -1	888 -1
14	1	139	1	264	1	389	1	514 -1	639 -1	764 -1	889 -1
15	1	140	1	265	1	390	1	515 -1	640 -1	765 -1	890 -1
16	1	141	1	266	1	391	1	516 -1	641 -1	766 -1	891 -1
17	1	141	1	267	1	392	1	510 -1 517 -1	642 -1	760 -1 767 -1	892 -1
18	1	143	1	268	1	393	1	517 -1	643 -1	767 -1 768 -1	893 -1
19	1	144	1	269	1	394	1	518 -1 519 -1	644 -1	768 -1 769 -1	894 -1
20	1	145	1	279	1	395	1	520 -1	645 -1	709 -1 770 -1	895 -1
21	1	146	1	270	1	396		521 -1	646 -1	770 -1 771 -1	896 -1
22	1	147	1	271	1	390	1	521 -1 522 -1	647 -1	771 -1 772 -1	897 -1
							1		647 -1 648 -1		898 -1
23 24	1	148 149	1	273 274	1	398 399	1	523 -1 524 -1	648 -1 649 -1	773 -1 774 -1	899 -1
	1		1	274 275	1	400	1				900 -1
25 26	1	150	1		1		1	525 -1	650 -1	775 -1	
26	1	151	1	276 277	1	401 402	1	526 -1	651 -1	776 -1	901 -1
27	1	152	1		1		1	527 -1	652 -1	777 -1	902 -1
28 29	1	153	1	278 279	1	403 404	1	528 -1 529 -1	653 -1	778 -1 779 -1	903 -1 904 -1
	1	154	1		1		1		654 -1		905 -1
30 31	1	155	1	280	1	405	1	530 -1 531 -1	655 -1	780 -1 781 -1	906 -1
32	1 1	156 157	1 1	281 282	1 1	406 407	1 1	531 -1 532 -1	656 -1 657 -1	781 -1 782 -1	907 -1
33	1	158	1	282	1	407	1	532 -1 533 -1	658 -1	782 -1 783 -1	908 -1
34		159	1	283 284				534 -1	659 -1	784 -1	909 -1
35	1 1	160	1	284 285	1 1	409 410	1 1	534 -1 535 -1	660 -1	784 -1 785 -1	910 -1
36		161	1	286	1	410	1	536 -1	661 -1	786 -1	910 -1
37		162	1	287		411	1		662 -1	786 -1 787 -1	
											912 -1
38	1	163	1	288	1	413	1	538 -1	663 -1 664 -1	788 -1	913 -1
39 40	1	164	1	289	1	414	1	539 -1		789 -1	914 -1
40	1	165	1	290	1	415	1	540 -1	665 -1	790 -1	915 -1
41	1	166	1	291	1	416	1	541 -1	666 -1	791 -1	916 -1
42	1	167		292	1	417	1	542 -1	667 -1	792 -1	917 -1
43	1	168	1	293	1	418	1	543 -1	668 1	793 -1	918 -1
44 45	1	169	1	294	1	419	1	544 -1	669 -1	794 -1	919 -1
45	1	170	1	295	1	420	1	545 -1	670 -1	795 -1	920 -1
46	1	171	1	296	1	421	1	546 -1	671 -1	796 -1	921 -1
47	1	172	1	297	1	422	1	547 -1	672 -1	797 -1	922 -1

48	1	173	1	298	1	423	1	548 -1	673 -1	798 -1	923 -1
49	1	174	1	299	1	424	1	549 -1	674 -1	799 -1	924 -1
50	1	175	1	300	1	425	1	550 -1	675 -1	800 -1	925 -1
51	1	176	1	301	1	426	1	551 -1	676 -1	801 -1	926 -1
52	1	177	1	302	1	427	1	552 -1	677 -1	802 -1	927 -1
53	1	178	1	303	1	428	1	553 -1	678 -1	803 -1	928 -1
54	1	179	1	304	1	429	1	554 -1	679 -1	804 -1	929 -1
55	1	180	1	305	1	430	1	555 -1	680 -1	805 -1	930 -1
56	1	181	1	306		431	1	556 1	681 -1	806 -1	931 -1
57	1	182	1	307	1	432	1	557 -1	682 -1	807 -1	932 -1
58	1	183	1	308	1	433	1	558 -1	683 -1	808 -1	933 -1
59	1	184	1	309	1	434	1	559 -1	684 -1	809 -1	934 -1
60	1	185	1	310	-1	435	1	560 -1	685 -1	810 -1	935 -1
61	1	186	1	311	1	436	1	561 -1	686 -1	811 -1	936 -1
62	1	187	1	312	1	437	1	562 -1	687 -1	812 -1	937 -1
63	1	188	1		-1	438	1	563 -1	688 -1	813 -1	938 -1
64	1	189	1	314		439	1	564 -1	689 -1	814 -1	939 -1
65	1	190	1	315	1	440	1	565 -1	690 -1	815 -1	940 -1
66	1	191	1	316	1	441	1	566 -1	691 -1	816 -1	941 -1
67	1	192	1	317	1	442	1	567 -1	692 -1	817 -1	942 -1
68	1	193	1	318	1	443	1	568 -1	693 -1	818 -1	943 -1
69	1	194	-1	319	1	444	1	569 -1	694 -1	819 -1	944 -1
70	1	195	1	320	1	445	1	570 -1	695 -1	820 -1	945 -1
71	1	196	1	321	1	446	1	571 -1	696 -1	821 -1	946 -1
72	1	197	1	322	1	447	1	572 -1	697 -1	822 -1	947 -1
73	1	198	1	323	1	448	1	573 -1	698 -1	823 -1	948 -1
74	1	199	1	324	1	449	1	574 -1	699 -1	824 -1	949 -1
75	1	200	1	325	1	450	1	575 -1	700 -1	825 -1	950 -1
76	1	201	1	326	1	450	1	576 -1	700 -1 701 -1	826 -1	951 -1
77	1	202	1	327	1	452	1	577 -1	702 -1	827 -1	952 -1
78	1	203	1	328	1	453	1	578 -1	703 -1	828 -1	953 -1
79	1	204	1	329	1	454	1	579 -1	704 -1	829 -1	954 -1
80	1	205	1	330	1	455	1	580 -1	705 -1	830 -1	955 -1
81	1	206	1	331	1	456	1	581 -1	706 -1	831 -1	956 -1
82	1	207	1	332	1	457	1	582 -1	707 -1	832 -1	957 -1
83	1	208	1	333	1	458	1	583 -1	708 -1	833 -1	958 -1
84	1	209	1	334	1	459	1	584 -1	709 -1	834 -1	959 -1
85	1	210	1	335	1	460	1	585 -1	710 -1	835 -1	960 -1
86	1	211	1	336	1	461	1	586 -1	711 -1	836 -1	961 -1
87	1	212	1	337	1	462	1	587 -1	712 -1	837 -1	962 -1
88	1	213	1	338	1	463	1	588 -1	712 1	838 -1	963 -1
89				339				589 -1	713 -1 714 -1	839 -1	
	1	214	1		1	464	1				964 -1
90	1	215	1	340	1	465	1	590 -1	715 -1	840 -1	965 -1
91	1	216	1	341	1	466	1	591 -1	716 -1	841 -1	966 -1
92	1	217	1	342	1	467	1	592 -1	717 -1	842 -1	967 -1
93	1	218	1	343	1	468	1	593 -1	718 -1	843 -1	968 -1
94	1	219	1	344	1	469	1	594 -1	719 -1	844 -1	969 -1
95	1	220	1	345	1	470	1	595 -1	720 -1	845 -1	970 -1
96	1	221	1	346	1	471	1	596 -1	721 -1	846 -1	971 -1
97	1	222	1	347	1	472	1	597 -1	722 -1	847 -1	972 -1
98	1	223	1	348	1	473	1	598 -1	723 -1	848 -1	973 -1
99	1	224	1	349	1	474	1	599 -1	724 1	849 -1	974 -1
100	1	225	1	350	1	475	1	600 -1	725 -1	850 -1	975 -1
101	1	226	1	351	1	476	1	601 -1	726 -1	851 -1	976 -1
102	1	227	1	352	1	470	1	602 -1	720 -1 727 -1	852 -1	970 -1 977 -1
TOZ	_	221	1	227	1	4//	1	00Z -I	/	U)	9// - 1

```
978 -1
 103
           228
                               478 1
      1
               1
                     353 1
                                         603 -1
                                                    728 -1
                                                              853 -1
 104
      1
           229
                1
                     354
                          1
                               479
                                    1
                                         604 -1
                                                    729 -1
                                                              854 -1
                                                                        979 -1
           230 1
                               480
                                                                        980 -1
 105
      1
                     355
                                         605 -1
                                                    730 -1
                                                              855 -1
                          1
                                    1
 106
      1
           231
               1
                     356
                          1
                               481
                                         606 -1
                                                    731 -1
                                                              856 -1
                                                                        981 -1
 107
      1
           232
               1
                     357
                          1
                               482
                                    1
                                         607 -1
                                                    732 -1
                                                              857 -1
                                                                        982 -1
 108
           233 -1
                               483
      1
                     358
                          1
                                    1
                                          608 -1
                                                    733 -1
                                                              858 -1
                                                                        983 -1
 109
      1
           234
               1
                     359
                          1
                               484
                                    1
                                         609 -1
                                                    734 -1
                                                              859 -1
                                                                        984 -1
      1
               1
                         1
 110
           235
                     360
                               485
                                    1
                                         610 -1
                                                    735 -1
                                                              860 -1
                                                                        985 -1
 111
     1
           236 1
                     361
                         1
                               486
                                    1
                                         611 -1
                                                    736 -1
                                                              861 -1
                                                                        986 -1
                                                    737 -1
 112
      1
           237 1
                     362
                         1
                               487
                                    1
                                         612 -1
                                                              862 -1
                                                                        987 -1
 113
      1
           238
               1
                     363
                          1
                               488
                                    1
                                         613 -1
                                                    738 -1
                                                              863 -1
                                                                        988 -1
 114
      1
           239 1
                     364
                         1
                               489
                                         614 -1
                                                    739 -1
                                                              864 -1
                                                                        989 -1
                                    1
 115
      1
           240 1
                     365
                         1
                               490
                                    1
                                         615 -1
                                                    740 -1
                                                              865 -1
                                                                        990 -1
 116
           241 1
                               491 -1
      1
                     366
                         1
                                         616 -1
                                                    741 -1
                                                              866 -1
                                                                        991 -1
                               492 -1
                                         617 -1
 117
      1
           242
                1
                     367
                                                    742 -1
                                                              867 -1
                                                                        992 -1
                          1
 118
      1
           243
               1
                     368
                               493
                                    1
                                         618 -1
                                                    743 -1
                                                                        993 -1
                          1
                                                              868 -1
 119
      1
           244 1
                     369 1
                               494 1
                                         619 1
                                                    744 -1
                                                              869 -1
                                                                        994 -1
 120 1
           245 1
                     370 1
                               495
                                    1
                                         620 -1
                                                    745 -1
                                                              870 -1
                                                                        995 -1
 121
     1
           246 1
                     371 1
                               496
                                         621 -1
                                                    746 -1
                                                              871 -1
                                                                        996 -1
                                    1
                                         622 -1
                                                                        997 -1
 122
      1
           247 1
                     372
                          1
                               497
                                    1
                                                    747 -1
                                                              872 -1
 123
      1
           248 1
                     373 1
                               498
                                    1
                                         623 -1
                                                    748 -1
                                                              873 -1
                                                                        998 -1
 124
      1
           249 1
                     374 1
                               499
                                    1
                                         624 -1
                                                    749 -1
                                                              874 -1
                                                                        999 -1
 125
      1
           250 1
                     375 1
                               500 1
                                         625 -1
                                                    750 -1
                                                              875 -1
                                                                       1000 -1
hit3 = 490
miss3 = 10
hit6 = 495
miss6 = 5
total_hits = 985
total misses = 15
Accuracy Percent = 98.5
Error Percent = 1.5
```

Dual-Soft Margin SVM:

Dual-Soft Margin SVM was implemented in AMPL and Tested the values using MATLAB.

The code used for training SVM in AMPL is as follows:

SVM-3.mod

```
param n := 785;
param D := 1000;
param C := 100;

set POINTS := {2..n};
set INPUT_POINTS := {1..n};
set DATASET := {1..D};
```

```
param x{DATASET,INPUT_POINTS};
param y{DATASET};
#param K{DATASET,DATASET};

data 3and6_Train_set.txt;

param K{i in DATASET, j in DATASET} := sum {t in POINTS} x[i,t]*x[j,t];

#Initializing Y[i]
for {i in DATASET} {
        if x[i,1] = 3 then {let y[i] := 1} else{ let y[i] := -1};
}

var alpha{DATASET} >= 0, <= C; #

maximize DUALSVM : (sum {i in DATASET} alpha[i]) - 0.5*(sum {i in DATASET,j in DATASET} alpha[i]*alpha[j]*y[i]*y[j]*K[i,j]);

s.t. CONDITION : sum {i in DATASET} alpha[i]*y[i] = 0;

option solver snopt;
solve;</pre>
```

The values for alpha generated by this SVM is as follows:

SVM-3.mod: Output

```
ampl: model SVM-3.mod;
SNOPT 7.2-8: Optimal solution found.
101 iterations, objective 0.9331388318
ampl: display alpha;
alpha [*] :=
   1 0
                    251 0
                                        501 0
                                                           751 0
   2 0
                    252 0
                                        502 0
                                                           752 0
   3 0
                    253 0
                                        503 0
                                                           753 0
   4 0
                    254 0
                                        504 0
                                                           754 0
   5 0
                    255 0
                                        505 0
                                                           755 0
   6 0
                    256 0
                                        506 0
                                                           756 0
   7 0
                    257 0
                                        507 0
                                                           757 0
  8 0
                    258 0
                                        508 0
                                                           758 0
  9 0
                    259 0
                                        509 0
                                                           759 0
                    260 0
                                                           760 0
 10 0
                                        510 0
 11 0
                    261 0
                                        511 0
                                                           761 0
 12 0
                    262 0
                                        512 0
                                                           762 0
 13 0
                    263 0
                                        513 0
                                                           763 0
                                                           764 0
 14 0
                    264 0
                                        514 0
                    265 0
                                        515 0
                                                           765 0
 15 0
 16 0
                    266 0.00762124
                                        516 0
                                                           766 0
 17 0
                    267 0
                                        517 0
                                                           767 0
 18 0
                    268 0
                                        518 0
                                                           768 0
```

19 0.0229393	269 0	519 0.010818	769 0.00438357
20 0	270 0	520 0	770 0
21 0.0158137	271 0	521 0	771 0
22 0	272 0	522 0	772 0
23 0	273 0	523 0	773 0
24 0	274 0	524 0	774 0
25 0	275 0	525 0.0396946	775 0
26 0	276 0.0138238	526 0.00981295	776 0
27 0	277 0	527 0	777 0
28 0	278 0	528 0	778 0
29 0	279 0	529 0	779 0
30 0	280 0.0116178	530 0	780 0
31 0	281 0.018492	531 0	781 0
32 0	282 0	532 0	782 0
33 0	283 0.0643798	533 0	783 0
34 0	284 0	534 0	784 0
35 0	285 0	535 0	785 0
36 0	286 0	536 0	786 0
37 0.036598	287 0	537 0	787 0
38 0	288 0	538 0	788 0
39 0	289 0	539 0.020362	789 0.00778625
40 0	290 0	540 0	790 0.00504809
41 0	291 0	541 0	791 0
42 0	292 0	542 0	792 0
43 0	293 0	543 0	793 0
44 0	294 0	544 0	794 0.0659321
45 0	295 0	545 0	795 0
46 0	296 0	546 0	796 0
47 0	297 0	547 0	797 0
48 0	298 0	548 0	798 0
49 0	299 0	549 0.0330524	799 0
50 0	300 0	550 0	800 0
51 0	301 0	551 0	801 0
52 0	302 0	552 0	802 0
53 0	303 0	553 0	803 0
54 0.00313437	304 0	554 0	804 0
55 0	305 0	555 0	805 0
56 0	306 0	556 0	806 0
57 0	307 0	557 0	807 0
58 0	308 0	558 0	808 0
59 0	309 0	559 0	809 0
60 0	310 0	560 0	810 0.0457639
61 0	311 0	561 0	811 0
62 0	312 0	562 0	812 0
63 0	313 0	563 0	813 0
64 0	314 0	564 0	814 0
65 0	315 0.00878912		815 0
66 0	316 0	566 0	816 0
67 0	317 0	567 0	817 0
68 0	318 0.0206537	568 0	818 0
69 0	319 0	569 0	819 0
70 0	320 0	570 0	820 0.0472099
71 0	321 0	571 0	821 0
72 0	322 0	572 0	822 0.0413412
73 0	323 0.0509329	573 0	823 0

74 0	324 0	574 0	824 0
75 0	325 0	575 0	825 0
76 0.0836223	326 0	576 0	826 0
77 0.0171851	327 0	577 0	827 0
78 0	328 0	578 0	828 0
79 0	329 0	579 0	829 0
80 0	330 0	580 0	830 0
81 0	331 0	581 0	831 0
82 0	332 0	582 0	832 0
83 0	333 0	583 0	833 0
84 0	334 0	584 0	834 0
85 0	335 0	585 0	835 0
86 0	336 0	586 0	836 0
87 0	337 0	587 0	837 0
88 0	338 0	588 0	838 0
89 0.00757683	339 0	589 0	839 0
90 0	340 0.0160459	590 0	840 0
91 0	341 0	591 0	841 0
92 0	342 0	592 0	842 0
93 0	343 0.0166185	593 0	843 0
94 0	344 0	594 0	844 0
95 0	345 0	595 0	845 0
96 0	346 0	596 0	846 0
97 0	347 0	597 0	847 0
98 0	348 0	598 0	848 0
99 0	349 0	599 0	849 0
100 0	350 0	600 0.0326473	850 0
101 0	351 0	601 0	851 0
102 0	352 0	602 0	852 0
103 0	353 0	603 0	853 0.042452
104 0	354 0	604 0	854 0
105 0 106 0	355 0 356 0	605 0	855 0
107 0	356 0 357 0	606 0 607 0	856 0 857 0
108 0	358 0	608 0	858 0
109 0	359 0	609 0	859 0
110 0	360 0	610 0	860 0
111 0	361 0	611 0.0550584	861 0
112 0	362 0	612 0	862 0.068372
113 0	363 0	613 0	863 0
114 0	364 0	614 0	864 0
115 0	365 0	615 0	865 0
116 0	366 0	616 0	866 0
117 0	367 0	617 0.0178404	867 0
118 0	368 0	618 0	868 0
119 0	369 0	619 0	869 0
120 0	370 0	620 0.0111894	870 0
121 0	371 0	621 0	871 0
122 0	372 0	622 0	872 0
123 0	373 0	623 0	873 0
124 0	374 0	624 0	874 0
125 0.0466636	375 0	625 0	875 0
126 0	376 0	626 0	876 0.0440758
127 0	377 0	627 0	877 0
128 0	378 0	628 0	878 0.0379009

129 0	379 0	629 0	879 0
130 0	380 0	630 0	880 0
131 0.00406832	381 0	631 0	881 0.0125816
132 0	382 0	632 0	882 0
133 0	383 0	633 0	883 0
134 0	384 0	634 0	884 0
135 0	385 0	635 0	885 0
136 0	386 0	636 0	886 0
137 0	387 0	637 0	887 0
138 0	388 0	638 0	888 0
139 0	389 0.0449771	639 0	889 0
140 0	390 0	640 0	890 0
141 0	391 0	641 0	891 0
142 0.0867509	392 0	642 0	892 0
143 0	393 0	643 0	893 0
144 0	394 0	644 0	894 0
145 0	395 0	645 0	895 0
146 0	396 0	646 0	896 0
147 0	397 0	647 0	897 0
148 0	398 0	648 0	898 0
149 0	399 0.0276439	649 0	899 0
150 0	400 0	650 0	900 0
151 0	401 0	651 0	901 0
152 0	402 0.0078615	652 0.012927	902 0
153 0	403 0	653 0	903 0
154 0	404 0	654 0	904 0
155 0	405 0	655 0	905 0
156 0	406 0	656 0.0775996	906 0
157 0	407 0	657 0.00957026	907 0
158 0	408 0.0436595	658 0	908 0
159 0	409 0	659 0	909 0
160 0	410 0	660 0	910 0
161 0	411 0	661 0	911 0
162 0	412 0	662 0	912 0
163 0	413 0	663 0	913 0
164 0	414 0	664 0	914 0
165 0	415 0	665 0	915 0
166 0	416 0	666 0	916 0
167 0	417 0	667 0	917 0
168 0	418 0	668 0	918 0
169 0	419 0	669 0	919 0
170 0	420 0	670 0	920 0
171 0	421 0	671 0.0133647	921 0
172 0	422 0	672 0	922 0
173 0	423 0	673 0	923 0
174 0.0732797	424 0	674 0	924 0
175 0	425 0	675 0	925 0
176 0	426 0	676 0	926 0
177 0	427 0	677 0	927 0
178 0	428 0	678 0	928 0
	429 0		929 0
179 0		679 0	
180 0	430 0	680 0	930 0
181 0	431 0	681 0	931 0
182 0	432 0	682 0	932 0.0396808
183 0	433 0	683 0	933 0

184 0	434 0	684 0	934 0
185 0	435 0	685 0	935 0
186 0	436 0	686 0	936 0
187 0	437 0	687 0	937 0
188 0.00476878	438 0	688 0	938 0
189 0	439 0	689 0	939 0
190 0.00345133	440 0	690 0	940 0
191 0	441 0	691 0	941 0
192 0	442 0	692 0	942 0
193 0	443 0	693 0	943 0
194 0	444 0	694 0	944 0
195 0	445 0	695 0	945 0
196 0	446 0	696 0	946 0
197 0	447 0	697 0	947 0
198 0	448 0	698 0	948 0
199 0	449 0	699 0	949 0
200 0	450 0	700 0	950 0
201 0	451 0	701 0	951 0
202 0	452 0	702 0	952 0.000771399
203 0	453 0	703 0	953 0
204 0	454 0	704 0	954 0
205 0	455 0	705 0	955 0
206 0	456 0	706 0.00867424	956 0
207 0	457 0	707 0	957 0.0429957
208 0	458 0	708 0	958 0
209 0	459 0	709 0	959 0
210 0	460 0	710 0	960 0
211 0	461 0	711 0	961 0.00962893
212 0	462 0	712 0	962 0
213 0	463 0.0335068	713 0	963 0
214 0	464 0	714 0	964 0
215 0	465 0	715 0.00258128	965 0
216 0.00463581	466 0	716 0	966 0
217 0	467 0	717 0	967 0
218 0	468 0	718 0	968 0
219 0	469 0	719 0	969 0
220 0	470 0	720 0.0145561	970 0
221 0	471 0	721 0	971 0
222 0	472 0	722 0	972 0
223 0	473 0	723 0	973 0
224 0	474 0	724 0	974 0
225 0	475 0	725 0	975 0
226 0	476 0	726 0	976 0
227 0.0548817	477 0	727 0	977 0
228 0	478 0	728 0	978 0
229 0	479 0	729 0.0207381	979 0
230 0	480 0	730 0	980 0
231 0	481 0.0501023	731 0	981 0
232 0	482 0	732 0	982 0
233 0.0107433	483 0	732 0	983 0
234 0	484 0	734 0.0149577	984 0
235 0	485 0	735 0	985 0
236 0	486 0	736 0	986 0
237 0	487 0	737 0	987 0.0101584
238 0	488 0	738 0	988 0
2J0 V	400 V	ש סכו	300 V

239	0	489	0	739	0	989	0
240	0	490	0	740	0	990	0
241	0	491	0	741	0	991	0
242	0	492	0	742	0	992	0
243	0	493	0	743	0	993	0
244	0	494	0	744	0	994	0
245	0	495	0.00293064	745	0	995	0
246	0	496	0	746	0	996	0
247	0	497	0	747	0	997	0
248	0	498	0	748	0	998	0
249	0	499	0	749	0	999	0
250	0	500	0.0173691	750	0	1000	0
;							

These values of alpha were output into an ASCII file and MATLAB was used to test the SVM output. The code used and the results are as follows:

Test.m : MATLAB code to Test SVM-3.mod output

```
clear all; clc;
ans = dlmread('Train Set Matlab.txt');
Train Set = ans(:,3:end);
ans = dlmread('Test Set Matlab.txt');
Test Set = ans(:,3:end);
op = dlmread('output.txt');
sv = [];
for (i = 1:length(op))
if(op(i,2)>0)
sv = [sv; op(i,1)];
end
sv alpha = op(sv, 2);
sv y = op(sv,3);
support vectors = [sv,sv alpha,sv y];
%Forming the kernel
Kernel = Train Set*Train Set';
%Calculating b for each of the vectors to check if all are equal
for(i = 1:length(support vectors))
    summation = 0;
    for(j = 1:length(Train Set))
        summation = summation+op(j,2)*op(j,3)*Kernel(j,support vectors(i,1));
    end
    b = summation - support_vectors(i,3);
    B(i) = b;
end
%Testing if alpha obtained is correct
```

```
for(i = 1:length(Test Set))
    sum = 0;
    for (j = 1:length(support vectors))
        sum = sum +
(support vectors(j,3)*support vectors(j,2)*(Train Set(support vectors(j,1),:)
*Test Set(i,:)'));
    end
    sum = sum - b;
    if(sum >= 0)
       y_result(i) = 1;
    else
        y_result(i) = -1;
    end
end
y result=y result';
hits = 0;
misses = 0;
for (i = 1:length(y result))
    if(y_result(i) == op(i,3))
        hits = hits+1;
    else
        misses = misses+1;
    end
end
display ('The Value of b for various support vectors:');
display ('Checking the Obtained values of Y for accuracy and errors:')
hits
misses
Accuracy Percent = hits/10
Error Percent = misses/10
```

The output obtained is as follows:

The Value of b for various support vectors:

B =

Columns 1 through 10

 $\hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1009 } \hbox{-0.1009 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008}$

Columns 11 through 20

Columns 21 through 30

 $\hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1009 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1009 } \hbox{-0.1009 } \hbox{-0.1009 } \hbox{-0.1009 } \hbox{-0.1009}$

Columns 31 through 40

 $\hbox{-0.1008} \hskip 0.5cm \hbox{-0.1008} \hskip 0.5cm \hbox{-0.1008}$

Columns 41 through 50

Columns 51 through 60

 $\hbox{-0.1008} \hskip 0.5cm \hbox{-0.1008} \hskip 0.5cm \hbox{-0.1008}$

Columns 61 through 70

```
 \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1009 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008 } \hbox{-0.1008}
```

Checking the Obtained Values for Accuracy:

hits =

985

misses =

15

Accuracy_Percent =

98.5000

Error_Percent =

Dual Soft-Margin SVM Using Radial Basis Kernel:

The training was implemented in AMPL with the following code:

SVM-4.mod

```
reset;
param n := 785;
param D := 1000;
param C := 1000;
param gama := 0.05;
set POINTS := {2..n};
set INPUT_POINTS := {1..n};
set DATASET := {1..D};
param x{DATASET,INPUT_POINTS};
param y{DATASET};
data 3and6_Train_set.txt;
#Initializing KERNEL Function: Radial-basis function machine with K[i,j] = e^{-(-i)}
g*(x[j]-x[i])^2
param K{i in DATASET, j in DATASET} := exp (-gama*(sum{t in POINTS}) (x[i,t]-
x[j,t])^2));
#Initializing Y[i]
for {i in DATASET} {
```

```
if x[i,1] = 3 then {let y[i] := 1} else{ let y[i] := -1};

var alpha{DATASET} >= 0, <= C; #

maximize DUALSVM : (sum {i in DATASET} alpha[i]) - 0.5*(sum {i in DATASET, j in DATASET} alpha[i]*x[i]*y[j]*K[i,j]);

s.t. CONDITION : sum {i in DATASET} alpha[i]*y[i] = 0;

option solver snopt;
solve;</pre>
```

The output generated by modeling SVM using radial basis function is as follows:

SVM-4.mod: Output

```
ampl: model SVM-4.mod;
SNOPT 7.2-8: Optimal solution found.
586 iterations, objective 87.76935479
ampl: display alpha;
alpha [*] :=
   1 0
                   251 0.543351
                                      501 0
                                                         751 0.337143
   2 0
                   252 0.552183
                                      502 0
                                                         752 0.280072
   3 0
                   253 0.0225839
                                      503 0
                                                         753 0.369248
   4 0.0828238
                   254 0
                                      504 0
                                                         754 0.457481
                   255 0
                                      505 0.132391
                                                         755 0.201131
   5 0.405296
   6 0
                   256 0
                                      506 0
                                                         756 0.0359257
  7 0
                   257 0.0870987
                                                         757 0.213857
                                      507 0.118811
   8 0.330414
                   258 0.0457662
                                      508 0
                                                         758 0
  9 0
                   259 0.374511
                                                         759 0
                                      509 0
  10 0
                   260 0.0751795
                                      510 0
                                                         760 0.032983
 11 0
                   261 0.224942
                                      511 0
                                                         761 0
                   262 0.32666
                                      512 0.199674
                                                         762 0
 12 0
 13 0
                                      513 0.370024
                                                         763 0.107191
                   263 0
 14 0
                   264 0.0243264
                                      514 0.590751
                                                         764 0
 15 0.216766
                   265 0
                                      515 0
                                                         765 0
                   266 0.408875
                                                         766 0.228641
 16 0.47841
                                      516 0
 17 0.201054
                   267 0
                                      517 0.239417
                                                         767 0.147964
 18 0.408476
                   268 0.306282
                                      518 0
                                                         768 0
                                                         769 0.686097
  19 0.628396
                   269 0.471984
                                      519 0.162162
  20 0
                   270 0.238273
                                      520 0
                                                         770 0
                                                         771 0.0948227
 21 0.877585
                   271 0
                                      521 0
  22 0.345111
                   272 0
                                      522 0
                                                         772 0
                   273 0
                                      523 0
                                                         773 0.642589
  23 0
  24 0
                   274 0.0582172
                                      524 0
                                                         774 0.241383
 25 0
                   275 0.216708
                                      525 0.83491
                                                         775 0.185831
 26 0
                   276 0.518567
                                      526 0.867771
                                                         776 0
 27 0
                   277 0.0973474
                                      527 0.21089
                                                         777 0
                                                         778 0
  28 0.182475
                   278 0.209095
                                      528 0.271342
                                      529 0.363801
  29 0.261304
                   279 0.608632
                                                         779 0
```

30	0	280	0.792564	530	0.251013	780	0.442396
	0.360436	281	0.441873		0.737655	781	0.518337
32	0.135854	282	0.186943	532	0.128686	782	-
33			0.74986	533	0.824847		0.339046
34	0	284	0.372235	534	0.202837		0.219045
35	0.287394	285			0.0472703	785	0.142218
36	0.644072	286	0.367373	536	0.286145	786	0
	0.55737		0.471695		0.448244	787	-
	0.308258		0.358583		0.0693457		0.172081
	0.294114	289			0.840551		0.028594
	0.078198		0.102332	540			0.925056
	0.212997	291			0.0795548		0.216666
	0.0854596	292		542	-	792	
	0.130041		0.133415		0.192297		0.109358
	0.274695		0.28297	544			0.847948
	0.21158	295		545			0.0361688
46	-	296			0.655395		0.314659
47	-		0.156736	547	•		0.183063
	0.344381		0.0308611	548			0.228765
49			0.457095		0.848482		0.200963
50			0.248695	550		800	
	0.22524	301			0.740587		0.245673
52		302			0.259241	802	
53		303			0.288728	803	
	0.342471		0.790683		0.379145	804	
55		305			0.434649		0.290694
	0.180932		0.340151		0.287973		0.340423
	0.0882733	307			0.137395	807	
58		308	-	558			0.0399604
60	0.375524		0.23116	559	-	809	
	-	310			0.380854		0.721054
	0.351001	311 312			0.439529	811	
	0.231709 0.285059		0.0868251		0.0598512 0.0164353	813	0.0866122
	0.40009		0.110039	564		814	
	0.12916		0.870975		0.445614		0.322403
	0.33083		0.194509		0.504626		0.179806
	0.295639		0.360498		0.00837891		0.368898
	0.334848		0.838357	568		818	
69			0.0392401		0.475034	819	
70			0.274721	570			0.749432
	0.0637517	321		571			0.201765
	0.0416463	322		572			0.349142
	0.447982		0.845298		0.0659888		0.629163
74		324			0.176023	824	
	0.167598	325			0.460648		0.74666
	0.805018	326			0.780718	826	
	0.540831		0.214742	577		827	
	0.0311393	328		578			0.441648
	0.298303	329		579		829	
80		330			0.0453264	830	
81		331			0.220442		0.159324
	0.551498	332			0.189497		0.215277
	0.512809		0.28534		0.117051	833	
84	0.262398	334	0.066426	584	0.126489	834	0

05 0 04 40 7 2 2	225 0 220520	505.0	005 0 0000444
	335 0.229698	585 0	835 0.0320411
86 0	336 0.0362476	586 0.230969	836 0
87 0.399659	337 0.0708338	587 0	837 0.0447912
88 0	338 0	588 0	838 0
89 0.440365	339 0.319621	589 0.254582	839 0.214206
90 0.120963	340 0.532614	590 0	840 0.551333
91 0	341 0.232232	591 0.125605	841 0
92 0.134512	342 0	592 0.166988	842 0
	343 0.566005	593 0.75457	
94 0	344 0.482786		
	345 0.189914	595 0	845 0
	346 0.294848	596 0.113495	846 0.0789927
97 0	347 0.235104	597 0.007323	847 0
98 0	348 0.640147	598 0	848 0.0596351
99 0	349 0.156822	599 0	849 0
100 0	350 0.232071	600 0.961795	850 0.111799
101 0.165129	351 0	601 0	851 0.0603805
102 0	352 0.520474	602 0	852 0
103 0.38556	353 0.286468	603 0	853 0.432873
104 0	354 0.1187	604 0	854 0
105 0	355 0.142851	605 0	855 0.206037
		606 0.0168101	
106 0	356 0.172139		
107 0.480342	357 0	607 0	857 0.158492
108 0.32527	358 0.422909	608 0.341193	858 0
109 0	359 0	609 0	859 0.557548
110 0	360 0	610 0	860 0.134514
111 0	361 0.0905198	611 0.370238	861 0
112 0.188753	362 0.0702003	612 0	862 0.961126
113 0	363 0.0588756	613 0.232234	863 0
114 0.47325	364 0	614 0	864 0
115 0	365 0	615 0	865 0
116 0.400533	366 0.139395	616 0	866 0
117 0	367 0.344569	617 0.277526	867 0
	368 0	618 0	868 0.0756281
118 0.16512			
119 0.0644397	369 0	619 0.192505	869 0
120 0	370 0.183175	620 0.699973	870 0
121 0	371 0.0983092	621 0	871 0
122 0	372 0.173783	622 0.413688	872 0.188764
123 0.0419663	373 0.136237	623 0.281191	873 0
124 0.0138942	374 0.0815875	624 0	874 0.385433
125 0.634891	375 0	625 0.0587905	875 0
126 0.373056	376 0.0257261	626 0	876 0.759982
127 0.161799	377 0.319832	627 0.0129422	877 0
128 0.128518	378 0.310127	628 0.213121	878 0.88244
129 0	379 0.122282	629 0	879 0.0976339
130 0	380 0.147725	630 0.0976889	880 0.360442
131 0.542203	381 0.386029		
		631 0.167735	881 0.967868
132 0.251535	382 0	632 0.599425	882 0
133 0.108042	383 0.15892	633 0	883 0.0321553
134 0	384 0	634 0.0634269	884 0
135 0	385 0.335797	635 0	885 0
136 0.0693474	386 0.313676	636 0	886 0.0522611
137 0.273596	387 0.332336	637 0	887 0
138 0.136228	388 0.30649	638 0.676907	888 0
139 0	389 0.415413	639 0.0137484	889 0.70052

140 0	390 0.155605	640 0	890 0.193852
141 0	391 0.196735	641 0.492787	891 0.744535
142 0.634695	392 0	642 0.240658	892 0.128258
143 0.239357	393 0	643 0	893 0.413743
144 0.317891	394 0.590104	644 0.144862	894 0.0130363
145 0	395 0	645 0	895 0.205412
146 0	396 0.297974	646 0	896 0
147 0	397 0.256953	647 0	897 0
148 0.114831	398 0.0411328	648 0.414478	898 0.298437
149 0.110283	399 0.221826	649 0.423224	899 0.0834039
150 0.0909535	400 0	650 0.125797	900 0.354265
151 0.280392	401 0.135707	651 0	901 0.659423
152 0.30674	402 0.655971	652 0.338216	902 0.421396
153 0	403 0.051864	653 0	903 0.203881
154 0.185151	404 0	654 0	904 0
155 0.0549533	405 0	655 0	905 0
156 0.157467	406 0.162899	656 0.976392	906 0
157 0.241392	407 0.427351	657 0.920446	907 0.618651
158 0.200834	408 0.85125	658 0	908 0.156333
159 0.0667085	409 0.144152	659 0.192165	909 0
160 0	410 0.269275	660 0	910 0.18158
161 0.0511314	411 0.378316	661 0	911 0.122995
162 0.561656	412 0	662 0	912 0.431925
163 0.199165	413 0	663 0	913 0.390937
164 0.340151	414 0	664 0.282096	914 0
165 0	415 0	665 0	915 0.21761
166 0	416 0.0514366	666 0.0434762	916 0.0569363
167 0.281415	417 0.396392	667 0	917 0
168 0.171968	418 0	668 0	918 0.0430681
169 0.428484	419 0	669 0.298469	919 0
170 0	420 0	670 0	920 0.264985
171 0.39594	421 0.734734	671 0.208168	921 0
172 0	422 0	672 0.0217915	922 0.00578642
173 0.467471	423 0	673 0	923 0.328487
174 0.980161	424 0	674 0.597	924 0
175 0.232221	425 0.49511	675 0.147863	925 0.0119021
176 0.116414	426 0	676 0	926 0.174702
177 0.0154371	427 0.0290984	677 0	927 0
178 0.0811916	428 0.11759	678 0.528817	928 0
179 0	429 0	679 0	929 0.216071
180 0	430 0.4557	680 0	930 0.00879106
181 0.206413	431 0.308859	681 0.204401	931 0.111661
182 0.163111	432 0.331245	682 0	932 1.20092
183 0.360286	433 0	683 0	933 0
184 0	434 0.363471	684 0.572546	934 0
185 0	435 0.73493	685 0.418385	935 0.441016
186 0.02999	436 0.0702142	686 0	936 0
187 0.298306	437 0.363687	687 0.539342	937 0
188 0.509719	438 0.343231	688 0	938 0
189 0	439 0.146292	689 0.443328	939 0.0755847
190 0.475834	440 0.0295736	690 0.100322	940 0.160823
191 0	441 0.367307	691 0	941 0
192 0	442 0	692 0	942 0
193 0.119643	443 0.412691	693 0.732499	943 0
194 0	444 0	694 0.22996	944 0.499266
134 U		UJ4 U.ZZJJO	J44 U.477200

195			0.327447		0.894006	945	
196	0	446	0.425299	696	-	946	
197	0.518999	447	0.0912591	697	0	947	0
198	0	448	0.195418	698	-	948	-
199	0	449	0		0.13648	949	0.501789
	0.572819	450	0	700			0.080078
201	0.186225	451		701		951	0
202	0	452	0.582448	702	0.211928	952	0.177317
	0.359171		0.132159	703		953	
204	0.569268	454	0.286281	704	0.276625	954	0
205	0.258718	455	0.069628	705	-	955	-
206	0	456	0	706	0.186289	956	0.0343649
207	0.154279	457	0.279299	707	0.0453639	957	0.35326
208	0	458	0.0246735	708	0.0923635	958	0
209	0.0548216	459	0.377721	709	0.377031	959	0
210	0	460	0	710	0.057472	960	0.623813
211	0	461	0	711	0.168894	961	0.265106
212	0	462	0.303348	712	0.231532	962	0
213	-	463	0.70188	713	0.258557	963	0
214	0.146342	464	0.167952	714	0	964	0.503417
215	0	465	0	715	0.336567	965	0
216	0.375863	466	0	716	0	966	0
217	0	467	0.0145906	717	0.134234	967	0.0970009
218	0	468	0	718	0	968	0
219	0.345899	469	0	719	0.0293412	969	0.578538
220	0	470	0	720	1.12497	970	0.378364
221	0	471	0	721	0	971	0.478624
222	0	472	0.638816	722	0.0537692	972	0
223	0.0801721	473	0	723	0	973	0.136918
224	0.189696	474	0	724	0	974	0.45531
225	0.313312	475	0	725	0	975	0.350487
226	0.153588	476	0.158179	726	0.0147402	976	0.284055
227	0.652083	477	0.0962412	727	0	977	0.365105
228	0	478	0.189305	728	0	978	0.3715
229	0.264539	479	0	729	1.1739	979	0
230	0.482231	480	0.596667	730	0	980	0.196374
231	0.15863	481	0.450151	731	0	981	0.305205
232	0.339995	482	0	732	0	982	0.0325256
233	0.720511	483	0.240785	733	0	983	0.230625
234	0	484	0.247176	734	0.397895	984	0
235	0	485	0.322611	735	0	985	0
236	0	486	0.28826	736	0.0727223	986	0.380838
237	0.0258435	487	0.497746	737	0.258928	987	0.828729
238	0.387668	488	0.39768	738	0.793016	988	0
239	0	489	0.158332	739	0	989	0.295836
240	0.0333182	490	0	740	0.180385	990	0.254667
241	0	491	0.0786052	741	0	991	0.272515
242	0.347115	492	0.393665	742	0.396433	992	0.751416
243	0.588083	493	0	743	0.376752	993	0.205435
244	0.0538069	494	0	744	0	994	0
245	0	495	0.395627	745	0	995	0.163205
246	0.00697644	496	0.0807348	746	0	996	0.236692
247	0		0.0474954	747	0.417673	997	0
248	0	498	0.22097	748	0.300632	998	0.50451
249	0.195517	499	0.173559	749	0	999	0.426533

```
250 0 500 0.654088 750 0 1000 0.15504;
ampl:
```

The SVM output was tested using MATLAB with the code below:

Test3.m

```
clear all; clc;
ans = dlmread('Train Set Matlab.txt');
Train Set = ans(:,3:end);
ans = dlmread('Test Set Matlab.txt');
Test Set = ans(:,3:end);
op = dlmread('output.txt');
sv = [];
for (i = 1:length(op))
if(op(i,2)>0)
sv = [sv; op(i,1)];
end
end
sv alpha = op(sv,2);
sv y = op(sv,3);
support_vectors = [sv,sv_alpha,sv y];
%Forming the kernel
Kernel = zeros(length(Train Set));
gama = 0.05;
for(i = 1:length(Train Set))
    xi = Train Set(i,:);
    for (j = 1:length(Train Set))
        xj = Train Set(j,:);
        k = \exp(-gama*norm(xi-xj,2)^2);
        Kernel(i,j) = k;
    end
end
%Calculating b for each of the vectors to check if all are equal
for(i = 1:length(support vectors))
    summation = 0;
    for(j = 1:length(Train Set))
        summation = summation+op(j,2)*op(j,3)*Kernel(j,support vectors(i,1));
    b = summation - support vectors(i,3);
    B(i) = b;
end
%Testing if alpha obtained is correct
for(i = 1:length(Test Set))
    sum = 0;
    for (j = 1:length(support vectors))
```

```
sum = sum +
(support vectors(j,3)*support vectors(j,2)*(Train Set(support vectors(j,1),:)
*Test Set(i,:)'));
    end
    sum = sum - b;
    if(sum >= 0)
        y_result(i) = 1;
    else
        y_result(i) = -1;
    end
end
y_result=y_result';
hits = 0;
misses = 0;
for (i = 1:length(y result))
    if(y result(i) == op(i,3))
        hits = hits+1;
    else
        misses = misses+1;
    end
end
display ('The Value of b for various support vectors:');
display ('Checking the Obtained values of Y from Test data to verify accuracy
and errors')
hits
misses
Accuracy Percent = hits/10
Error Percent = misses/10
```

The Test output was as follows:

Test4.m : Output for Testing SVM-4.mod

The Value of b for various support vectors:

B =

Columns 1 through 10

```
-0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573
```

Columns 11 through 20

-0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -

Columns 21 through 30

-0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -

Columns 31 through 40

-0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -

Columns 41 through 50

Columns 51 through 60

-0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -

...

Columns 571 through 580

-0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -0.1573 -

Column 581

-0.1573

```
Checking the Obtained values of Y from Test data to verify accuracy and errors

hits =
976
misses =
24

Accuracy_Percent =
97.6000

Error_Percent =
2.4000

>>
```

Dual-soft Margin SVM with Radial Basis Kernel to differentiate Even from Odd

The training code for this question was implemented in AMPL as follows:

SVM-5.mod

```
reset;
param n := 785;
param D := 1000;
param C := 1000;
param gama := 0.05;
set POINTS := {2..n};
set INPUT_POINTS := {1..n};
set DATASET := {1..D};
param x{DATASET,INPUT_POINTS};
param y{DATASET};
data Train_Set_Full.txt;
#Initializing KERNEL Function: Radial-basis function machine with K[i,j] = e^{-t}
g*(x[j]-x[i])^2
param K{i in DATASET, j in DATASET} := exp (-gama*(sum{t in POINTS} (x[i,t]-
x[j,t])^2);
#Initializing Y[i]
for {i in DATASET} {
```

```
#Determining if the digit is ODD(=1) or EVEN(=-1)
if ((x[i,1] mod 2) = 1) then {let y[i] := 1} else{ let y[i] := -1};

var alpha{DATASET} >= 0, <= C; #

maximize DUALSVM : (sum {i in DATASET} alpha[i]) - 0.5*(sum {i in DATASET, j in DATASET} alpha[i]*alpha[j]*y[i]*y[j]*K[i,j]);

s.t. CONDITION : sum {i in DATASET} alpha[i]*y[i] = 0;

option solver snopt;
solve;</pre>
```

The values of support vectors obtained were as follows:

SVM-5.mod: Output

```
ampl: model SVM-5.mod;
SNOPT 7.2-8: Optimal solution found.
561 iterations, objective 24727290.29
alpha [*] :=
   1
                         335
                                    0
                                                  669
                                                        88742.9
   2
            1.08293
                         336
                                    0
                                                  670
                                                             0
   3
           12,4707
                         337
                                                             0
                                    0
                                                  671
                                                             0
   4
           12.4005
                         338
                                    0
                                                  672
   5
            0
                         339
                                    0
                                                  673
                                                             0
   6
           11.1521
                         340
                                    0
                                                  674
                                                             0
   7
            0
                         341
                                    0
                                                  675
                                                             0
   8
                         342 241127
                                                  676
                                                             0
            0
   9
            2.89783
                         343
                                    0
                                                  677
                                                             0
  10
           10.63
                         344
                                    0
                                                  678
                                                             0
                                                             0
  11
                         345
                                    0
                                                  679
            0
  12
           15.3639
                         346
                                    0
                                                  680
                                                             0
  13
            0
                         347
                                    0
                                                  681
                                                             0
  14
            0
                         348
                                    0
                                                  682
                                                             0
  15
                         349
                                    0
                                                  683
                                                             0
            0
  16
            0
                         350
                                    0
                                                  684
                                                             0
  17
                         351
                                    0
                                                  685
                                                             0
                              849474
                                                             0
  18
            0.122802
                         352
                                                  686
  19
                                                             0
           11.3511
                         353
                                    0
                                                  687
                                                             0
  20
                                    0
            0
                         354
                                                  688
  21
            2.87149
                         355
                                    0
                                                  689
                                                             0
  22
                         356
                                                  690
                                                             0
                                    0
  23
                         357
                                    0
                                                  691
                                                             0
  24
            3.19399
                         358
                                                  692
                                                             0
                                    0
  25
            3.49242
                         359
                               506467
                                                  693
                                                             0
  26
            7.68065
                         360
                                                  694
                                                             0
                                    0
  27
                         361
                                                  695
                                                             0
            9.23025
                                    0
  28
            4.85517
                         362
                                                  696
                                                             0
                                    0
```

29	7.93756	363	0	697	0
30	12.2203	364	0	698	0
31	3.62271	365	0	699	0
32	0	366	0	700	0
33	4.45621	367	0	701	0
34	0	368	0	702	0
35	9.52635	369	0	703	0
36	5.50384	370	0	704	0
37	0	371	Ø	705	ø
38	2.62178	372	86252	706	ø
39	0	373	0	707	0
40	0	374	0	707	0
41	0	375	0	709	0
42	-		-		_
	0	376	0	710	3289.84
43	0	377	0	711	7072.44
44	1.28197	378	0	712	0
45	0	379	0	713	0
46	11.3503	380	113591	714	0
47	7.10089	381	742664	715	0
48	9.47784	382	0	716	0
49	4.83504	383	828412	717	0
50	5.01973	384	0	718	0
51	0	385	1513.04	719	14460.2
52	8.0308	386	0	720	70178.7
53	0	387	0	721	23319.3
54	0	388	0	722	0
55	0	389	1546.87	723	0
56	5.35372	390	446411	724	0
57	0	391	0	725	0
58	0	392	0	726	0
59	0	393	0	727	ø
60	0	394	0	728	0
61	0	395	0	729	0
62	0	396	0	730	13100.3
63	0	397	320425	730 731	46817.9
64	3.46969	398	0	731	46617.9
65	0	399	0	733	0
66	10.5403	400	0	734	50398
67	0	401	25347.9	735	0
68	0	402	929760	736	0
69	0	403	0	737	0
70	0	_	2719010	738	0
71	0	405	0	739	12744.6
72	0	406	63616.7	740	0
73	5.98871	407	0	741	0
74	1.69913	408	245296	742	0
75	13.4808	409	0	743	0
76	5.52811	410	0	744	0
77	5.29266	411	0	745	0
78	2.70554	412	0	746	0
79	16.5686	413	0	747	0
80	15.0955	414	0	748	0
81	2.94544	415	Ø	749	0
82	8.62111	416	Ø	750	0
83	11.0779	417	767566	751	27623.1
	,,,,	71/	, 0, 500	, , , ,	_,

84	11.2127	418	0	752	0
85	13.4749	419	0	753	0
86	0	420	0	754	18158.7
87	9.95221	421	0	755	0
88	4.49409	422	360497	756	0
89	8.59351	423	388907	757	0
90	3.33396	424	0	758	0
91	0	425	0	759	0
92	0	426	454085	760	0
93	9.7331	427	0	761	145935
94	8.61736	428	0	762	0
95	0	429	0	763	0
96	0	430	1140240	764	0
97	0	431	424519	765	0
98	0	432	0	766	0
99	0	433	0	767	0
100	0	434	0	768	0
101	0	435	0	769	69627.8
102	0	436	0	770	0
103	0		2216500	771	0
104	48.4622	438	0	772	0
105	0	439	923847	773	0
106	0	440	0	774	0
107	60.3446	441	0	775	1080.76
108	0	442	412533	776	0
109	0	443	0	777	Ø
110	0	444	288965	778	Ø
111	13.1709	445	0	779	80628.2
112	0	446	943522	780	0
113	0	447		781	0
114	0	448	0	782	19186.8
115	0	449	873599	783	0
116	0	450	0	784	0
117	0	451	660128	785	Ø
118	11.8408		1905280	786	0
119	0	453	0	787	0
120	ø	454	0	788	0
121	ø	455	0	789	ø
122	ø	456	0	790	ø
123	ø	457	0	791	0
124	128.046	458	660918	792	0
125	0	459	0	793	0
126	3.58183	460	0	794	Ø
127	17.083	461	0	795	0
128	0	462	0	796	5102.45
129	ø		1056710	797	0
130	22.5777	464	0	798	0
131	0	465	0	799	23135.1
132	0	466	0	800	0
133	149.27	467	0	801	0
134	0	467	252660	802	0
135	65.7512	469	144278	803	0
136	05.7512	470	429030	804	0
137		470	429030	805	0
	0 27 7326				
138	27.7326	472	0	806	1980.62

	•				_
139	0	473	92188.4	807	0
140	40.0632	474	0	808	1535.1
141	68.1525	475	0	809	0
142	0	476	0	810	302.788
143	0	477	0	811	2140.55
144	12.637	478	102762	812	0
145	92.7699	479	0	813	0
146	0.547909	480	0	814	5145.71
147	0	481	0	815	0
148	0	482	132123	816	0
149	18.3213	483	426436	817	0
150	0	484	0	818	813.255
151	0	485	0	819	0
152	10.1877	486	765734	820	9050.28
153	89.5913	487	0	821	4494.19
154	0	488	550499	822	0
155	0	489	0	823	0
156	0	490	0	824	0
157	0	491	0	825	0
158	0	492	0	826	0
159	0	493	0	827	0
160	0	494	0	828	0
161	0	495	0	829	3613.49
162	0	496	17609.2	830	0
163	0	497	234910	831	0
164	17.6628	498	0	832	0
165	0	499	0	833	0
166	18.2793	500	0	834	0
167	0	501	0	835	7543.87
168	0	502	21957	836	0
169	0	503	0	837	0
170	0	504	831141	838	5334.28
171	0	505	0	839	3396.68
172	0	506	0	840	0
173	90.5567	507	0	841	261.669
174	11.8555	508	520598	842	48.0613
175	45.9337	509	0	843	0
176	74.2487	510	0	844	ø
177	0	511	53181.9	845	0
178	111.89	512	0	846	0
179	0	513	0	847	0
180	97.8517	514	0	848	0
181	0	515	0	849	1616.49
182	0	516	0	850	0
183	291.636	517	395556	851	0
184	0	518	0	852	0
185	0	519	0	853	0
186	0	520	0	854	0
187	287.309	521	0	855	0
188	0	522	0	856	0
189	202.8	523	0	857	0
190	0	524	0	858	0
191	48.5509	525	0	859	883.665
192	0	526	1136210	860	1913.46
193	0	527	0	861	0
_			-	-	

194	0	528	560640	862	0
195	0	529	0	863	0
196	0	530	0	864	0
197	0	531	0	865	0
198	0	532	264583	866	0
199	0	533	0	867	1028.18
200	0	534	0	868	0
201	88000.6	535	0	869	ø
202	33453.9	536	382690	870	0
203	0	537	0	871	0
204	0		474714	872	0
	192591	538			
205		539	0	873	0
206	0	540	0	874	0
207	0	541	840365	875	0
208	0	542	0	876	0
209	0	543	0	877	0
210	0	544	0	878	0
211	182490		1522070	879	0
212	0	546	0	880	0
213	0	547	0	881	0
214	0	548	0	882	5015.49
215	187803	549	0	883	0
216	0	550	0	884	2825.64
217	0	551	77074	885	0
218	78823.8	552	0	886	0
219	0	553	586503	887	0
220	0	554	0	888	0
221	0	555	0	889	1463.59
222	0	556	0	890	0
223	0	557	229362	891	0
224	0	558	990283	892	0
225	0	559	0	893	0
226	0	560	252641	894	0
227	0	561	232041	895	0
228	108941	562	_	896	0
229		563	0	897	467.28
	0		0		
230	0	564	0	898	0
231	0	565	0	899	0
232	0	566	0	900	2326.96
233	0	567	0	901	0
234	0	568	0	902	22.1341
235	0		1507420	903	135.602
236	0	570	773561	904	144.881
237	0	571	0	905	82.3009
238	0	572	676212	906	0.930635
239	0	573	0	907	0
240	0	574	0	908	10.875
241	20478.5	575	38404.8	909	2.11469
242	0	576	0	910	0
243	0	577	0	911	0
244	0	578	797614	912	0
245	94811.9	579	0	913	0
246	0	580	0	914	0
247	0	581	118456	915	63.0542
248	0	582	0	916	0
•	_		_		-

249	0	583	0	917	17.855
250	0	584	0	918	0
251	0	585	0	919	0
252	0	586	0	920	0
253	0	587	0	921	87.6325
254	0	588	912701	922	17.3897
255	0	589	0	923	54.7555
256	0		1208000	924	0
257	0	591	0	925	124.724
258	0	592	0	926	0
259	0	593	0	927	0
260	0	594	802802	928	29.0404
261	0	595	0	929	0
262	88427.4	596	0	930	18.4927
263	0	597	0	931	13.155
264	0	598	0	932	0
265	15742.3	599	0	933	0
266	0	600	0	934	0
267	127388	601	0	935	25.0522
268	0	602	28085.		3.14903
269	ø	603	0	937	0.892668
270	ø	604	0	938	91.2667
271	99858.6	605	157184	939	0
272	0	606	207718	940	0
273	ø	607	0	941	0
274	ø	608	0	942	0
275	40235.8	609	0	943	0
276	0	610	0	944	28.2235
277	0	611	0	945	0
278	0	612	0	946	0
279	117616	613	0	947	0
280	0	614	0	948	197.072
281	105510	615	0	949	63.4595
282	69946.1	616	231902	950	03.4393
283	09940.1	617	231302	951	0
284	0	618	0	952	0
285	0	619		953	
286	0	620	0 0	954	0 0
287				955	0
288	0 0	621 622	0 0	956	195.092
	0	623	0	957	0
289 290	0	624	0	958	0
290	0	625	0	959	
291	0	626	0	960	37.6753 0
293	0	627	0	961	14.6176
294	0	628	0	962	0
295	0	629	0	963	0
296	0	630	0	964	0
297	3161.3	631	0	965	0
298	0	632	0	966	16.3822
299	36346.6	633	0	967	67.4438
300	0	634	0	968	0
301	0	635	0	969	0
302	0	636	0	970	0
303	0	637	0	971	0

304	0	638	0	972	0
305	0	639	0	973	27.5051
306	0	640	0	974	0
307	0	641	0	975	0
308	0	642	0	976	22.5344
309	0	643	0	977	0
310	168848	644	0	978	0
311	0	645	0	979	91.329
312	0	646	79434.7	980	2.93459
313	680078	647	101294	981	0
314	0	648	0	982	45.4414
315	874624	649	0	983	0
316	668101	650	0	984	0
317	0	651	0	985	0
318	0	652	0	986	24.462
319	223951	653	0	987	0
320	0	654	0	988	90.6672
321	0	655	0	989	0
322	0	656	0	990	26.871
323	0	657	0	991	0
324	0	658	0	992	1.39968
325	0	659	194386	993	25.3075
326	649942	660	0	994	37.3718
327	0	661	0	995	0
328	0	662	0	996	0
329	0	663	16342.6		5.12634
330	589137	664	0	998	51.089
331	87696.6	665	0	999	0
332	0	666	34641.1	1000	0
333	0	667	12056.7		
334	36235.2	668	0		
;					
ampl:					

The code used for Testing was as follows:

Test5.m

```
clear all; clc;
Train_Set = dlmread('Train_Set_Matlab.txt');
Train_Set = Train_Set(2:end,2:end);
Test_Set = dlmread('Test_Set_Full.txt');
Test_Set = Test_Set(2:end, 2:end);
op = dlmread('output.txt');
sv = [];
nop = [op(:,1:2); op(:,3:4); op(:,5:6); op(:,7:8)];
%op = nop;
for (i = 1:length(op))
if(op(i,2)>0 && op(i,2) < 100)
sv = [sv; op(i,1)];
end
end
sv alpha = op(sv, 2);
sv y = op(sv,3);
```

```
support vectors = [sv,sv alpha,sv y];
%Forming the kernel
Kernel = zeros(length(Train Set)-1);
gama = 0.05;
for(i = 1:length(Train Set))
    xi = Train Set(i,:);
    for (j = 1:length(Train Set))
        xj = Train Set(j,:);
        k = \exp(-gama*norm(xi-xj,2)^2);
        Kernel(i,j) = k;
    end
end
%Calculating b for each of the vectors to check if all are equal
for(i = 1:length(support vectors))
    summation = 0;
    for(j = 1:length(Train Set))
        summation = summation+op(j,2)*op(j,3)*Kernel(j,support vectors(i,1));
    b = summation - support_vectors(i,3);
    B(i) = b;
end
%Testing if alpha obtained is correct
for(i = 1:length(Test Set))
    sum = 0;
    for (j = 1:length(support_vectors))
        sum = sum +
(support vectors (j,3) *support vectors (j,2) * (Train Set (support vectors (j,1),:)
*Test Set(i,:)'));
    end
    sum = sum - b;
    if(sum >= 0)
        y result(i) = 1;
    else
        y_result(i) = -1;
    end
end
y result=y result';
misses = 0;
hits = 0;
for (i = 1:length(y result))
    if(y result(i) - op(i,3) \sim = 0)
        misses = misses+1;
    else
        hits = hits+1;
    end
end
fprintf ('Accuracy Percent: %f \n', hits/10);
fprintf('Error Percent: %f \n', misses/10);
```

SVM-5: Radial Basis	, Even/Odd -	Values of E	B and Test	Accuracy
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B =

Columns 1 through 10

-0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650

Columns 11 through 20

-0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650

Columns 21 through 30

-0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650

Columns 31 through 40

-0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650

Columns 41 through 50

-0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650

Columns 51 through 60

-0.2650 -0.265

Columns 821 through 830

-0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650

Columns 831 through 840

-0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650 -0.2650

Columns 841 through 844

-0.2650 -0.2650 -0.2650

Accuracy Percent: 81.000000

Error Percent: 19.000000