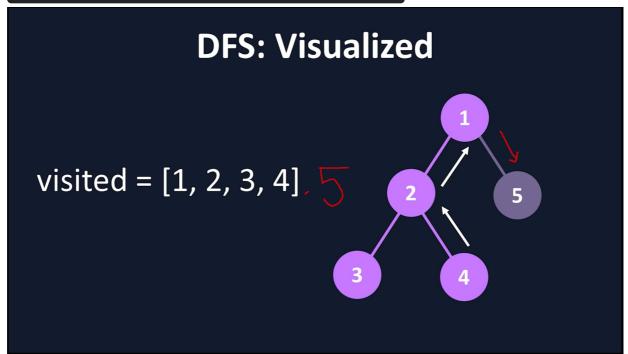
# Overview of important Algorithms

- Searching
  - Binary Search
  - Depth First Search for trees and graphs
    - start from the top of a tree and go as deep as possible along the same branch
    - once you are at the bottom then go to nearest unvisited node usually a sibling of the deepest node
      - this process is called Backtracking
    - used to solve a maze
    - O(number of nodes + number of branches)



- Breadth First Search for trees and graphs
  - you don't go to deepest point like DFS
  - instead you make sure that the sibling node has been visited
  - once you are on a node look at its children and add them to a queue and then you visit the node in the queue and add them to visited array and remove them from sibling queue
  - if the node in the queues has more children then add them to queue when marking it visited
  - used in chess
  - O(number of nodes + number of branches)
- Sorting

- Insertion Sort
  - compares the nth element with (n+1)th element and swaps them if nth element is larger
  - best case O(n) if everything is already sorted
  - worst case 0(n^2) when nothing is sorted beforehand

#### Merge Sort

- divide and conquer and conquer by divide and conquer and so on
- recursion
- splits array in half till we have pairs of 2
- then all pairs of 2 are sorted and then 2 pairs of 2 are merged and sorted till the array is completely merged back again
- best and worst case are same 0(n log n)

#### Quick Sort

- recursive like merge sort so divides and conquers
- we choose a pivot element of the array which is closest to the median of the array elements
- then we split the lists into 2 such that one list has elements less than the pivot element and one where all elements are greater than the pivot element
- we repeat the same on these 2 lists
- we move the pivot element to the end of the list
- we place 2 pointers one on the 0th index and the 2nd on the 2nd last element and compare the two if the 0th one is larger we swap
- deep doing it till the 2 pointers meet
- when they meet replace that element with the last one
- we know have 2 lists like we wanted and we can do the same thing on them individually
- best case 0(n log n)
- worst case 0(n^2)
- still can be 2 to 3 times faster than merge sort by reducing the chances of worst case
- needs less memory O(log n) than merge sort O(n)

### Greedy Algorithm

- It makes the best possible decision at every local step
- when not to be greedy
  - not meant for efficiency

- when to be greedy
  - when you don't want to find the most efficient way out of millions of permutations then greedy might be a good enough solution
  - when optimal solution not possible and brute force is not acceptable become greedy

## Recursion

- a recursive function should have a terminating condition also called as a base condition
  - the values in the scope of the function can be used before(ascending) or after(descending) the termination condition and recursive call

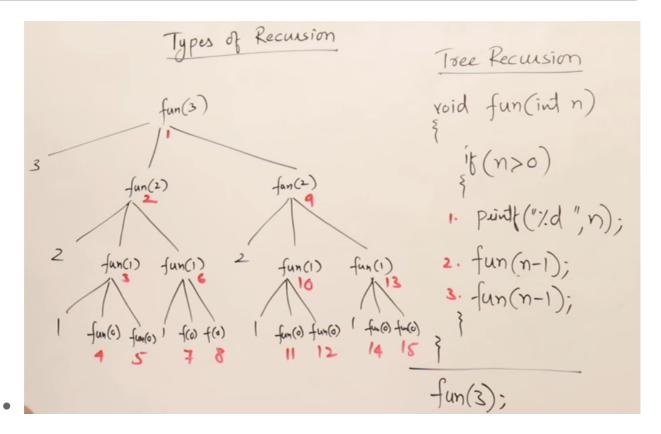
```
#include <iostream>
using namespace std;
void head(int n)
{
    if (n > 0)
    {
        head(n - 1);
        cout << n << " ";
    }
}
void tail(int n)
{
    if (n > 0)
        cout << n << " ";
        tail(n - 1);
    }
}
int main()
{
    head(10);
    cout << endl;</pre>
    tail(10);
```

```
return 0;
}
// 1 2 3 4 5 6 7 8 9 10
// 10 9 8 7 6 5 4 3 2 1
```

- use static variables in recursive function if you need a counter and don't want
   the counter to reset on every recursive call
  - static variable will have a single copy for all recursive calls and will not be a local variable of the scope of a recursive function
  - it is like global but more restrictive
- types of recursion
  - tail
    - when the function calls itself in the last line of the function
    - easier to convert recursive logic to iterative
  - head
    - when the function calls itself in the first line of the function
    - harder to convert recursive logic to iterative
  - tree
    - opposite of tree recursion is linear recursion when the recursive function calls itself only one time
    - in tree recursion the recursive function calls itself more than one times

```
#include <iostream>
using namespace std;
void tree(int n)
{
    if (n > 0)
    {
        cout << n << " ";
        tree(n - 1);
        tree(n - 1);
    }
}</pre>
```

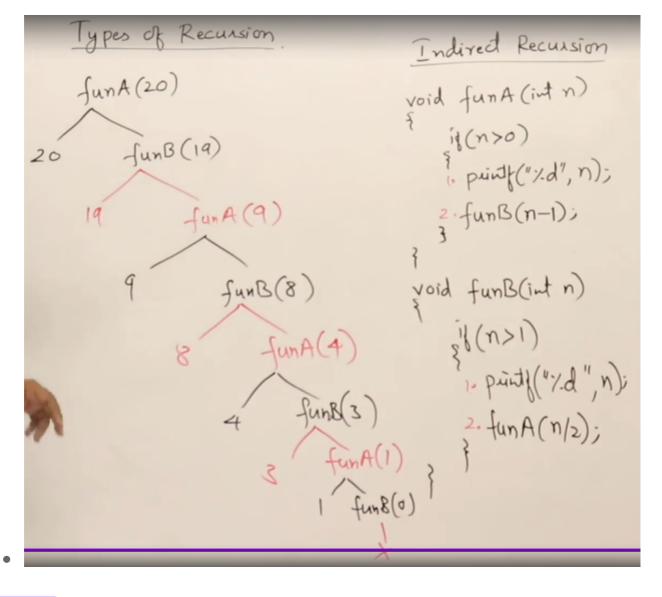
```
int main()
{
    tree(3);
    return 0;
}
// 3 2 1 1 2 1 1
// Time 0(2^n)
// Space 0(n)
```



- indirect
  - when a function A calls B and B calls C and C calls A

```
#include <iostream>
using namespace std;
void funB(int n);

void funA(int n)
{
   if (n > 0)
   {
      cout << n << " ";
      funB(n - 1);
   }
}</pre>
```



• parameter of a recursive call function is the same function

```
#include <iostream>
using namespace std;
int fun(int n)
{
    if (n > 100)
        return n - 10;
    return fun(fun(n + 11));
}
int main()
{
    cout << fun(95); // 91
        return 0;
}</pre>
```

```
Types of Recursion.

\int un(95) = 91 \\
\int un(fun(95+11)) \\
fun(fun(95+11)) \\
fun(fun(107)) \\
fun(fun(107)) \\
fun(fun(107)) \\
fun(fun(108)) \\
fun(fun(108)) \\
fun(fun(108)) \\
fun(fun(109)) \\
fun(fun(109)) \\
fun(fun(109)) \\
fun(fun(109)) \\
fun(fun(100)) \\
f
```

Implementing pow function from cmath using recursion

```
#include <iostream>
using namespace std;
int pow(int k, int p) { return p = 0 ? 1 : pow(k, p - 1) * k; }
int main()
{
    cout << "Enter constant and power: ";</pre>
```

```
int con, pwr;
cin >> con >> pwr;
cout << con << "^" << pwr << " = " << pow(con, pwr);
return 0;
}</pre>
```

- optimization: for  $2^8$  instead of multiplying 2 8 times shouldn't we half and square like  $(2^2)^4 = 4^4$ 
  - this way we can reduce the stack height and increase memory efficiency
  - so if the power is even we half it and then we square the constant
  - else if the power is odd like  $2^9$  we can still do  $2 \times 2^8$  and so on

- Taylor Series using recursion is a combination of sum till n, power, factorial using recursion
  - to print  $e^x = 1 + x/1 + x^2/2! + x^3/3! + x^4/4! + ...$  till n terms
  - we need to use static variables as 3 variables are involved but we can return only one
    - the program will be less efficient if we don't use power and factorial as static variables as we will have to calculate the complete factorial over and over again
      - if factorial would have been static we just need to multiply a new number with the factorial of the previous number as  $n! = n \times (n-1)!$

• similarly we have to find  $x^n$  every time but if static we can store  $x^n-1$  and multiply x once

```
#include <iostream>
using namespace std;
float e(int x, int n)
{
    if (n = 0)
        return 1;
    static float pwr = 1, fac = 1;
    float res = e(x, n - 1);
    pwr *= x;
    fac *= n;
    return res + pwr / fac;
int main()
    cout << "Enter x and n: ";</pre>
    int x, n;
    cin \gg x \gg n;
    cout << "e^" << x << " till n precision is " << e(x, n);
    return 0;
}
```

- optimizing using Horner's Rule
  - earlier the number of times we were multiplying was  $O(n^2)$  but using Horner's Rule it can be O(1)
  - to print  $e^x = 1 + x/1(1 + x/2(1 + x/3(1 + x/4 + ... till n terms)))$ 
    - we keep taking commons out and this reduces number of multiplications that are needed to be performed
    - we find the value for the innermost bracket lets say (1+  $\times$ /4) here and multiply it with the common multiple  $\times$ /3 and add 1 to it and go on recursively
    - using iteration

```
#include <iostream>
using namespace std;
float e(int x, int n)
{
   int res = 1;
   for (; n > 0; n--)
```

```
res = 1 + x * res / n;
return res;
}
int main()
{
    cout < "Enter x and n: ";
    int x, n;
    cin >> x >> n;
    cout << "e^" << x << " till n precision is " << e(x,
n);
    return 0;
}</pre>
```

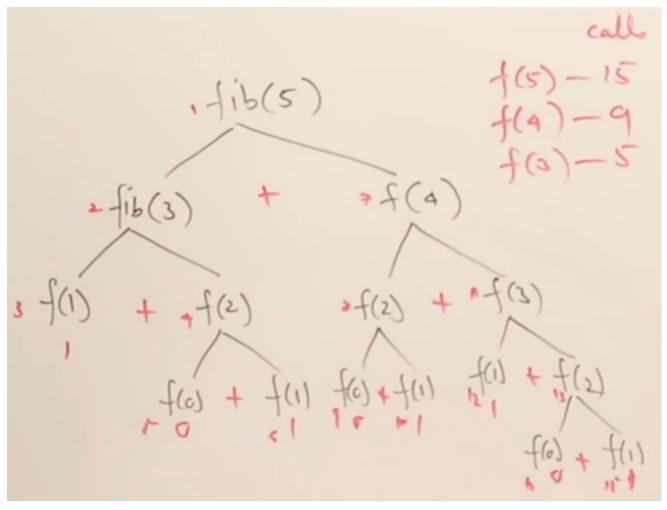
using recursion

```
#include <iostream>
using namespace std;
float e(int x, int n)
{
    static int res = 1;
    if (n = 0)
        return res;
    res = 1 + x * res / n;
    return e(x, n - 1);
int main()
{
    cout << "Enter x and n: ";</pre>
    int x, n;
    cin \gg x \gg n;
    cout << "e^" << x << " till n precision is " << e(x,
n);
    return 0;
}
```

- Fibonacci Series
  - using recursion 0(2<sup>n</sup>)

```
#include <iostream>
using namespace std;
int fibo(int n)
{
```

```
if (n ≤ 1)
    return n;
return fibo(n - 2) + fibo(n - 1); // as the function calls
itself 2 times with n as arg so 0(2^n)
}
```



- here we can see that fib(3) and fib(2) get calculated over and over as the value is not stored
- using iteration 0(n)

```
#include <iostream>
using namespace std;
int fibo(int n)
{
    if (n \le 1)
        return n;
    int t0 = 0, t1 = 1, s;
    for (int i = 2; i \le n; i++)
    {
        s = t0 + t1;
        t0 = t1;
        t1 = s;
    }
}
```

```
return s;
```