

1. (text) Stacking [10 pts] a stack is LIFO, the leftmost element is the bottom, the right most is the top ex: $[8, 2]$
 bottom \rightarrow top

Operations: start: $[]$ empty

1. push(8) 8 inserted $[8]$
 2. push(2) 2 inserted $[8, 2]$
 3. pop(): 2 is removed $[8]$
 4. push(pop()*2): will remove 8 multiply it by 2 $[8 \cdot 2 = 16] \rightarrow$ then it pushed onto the stack $[] \rightarrow [16]$
 5. push(10) 10 inserted $[16, 10]$
 6. push(pop()/2): will remove 10 from stack then divide it $[10/2 = 5]$ then it's pushed on to the stack $[16] \rightarrow [16, 5]$
- Final Stack: $[16, 5]$ top
bottom

2. (text) Queueing [10 pts] a Queue is FIFO ex: $[8, 2, 4]$
front \rightarrow back

Operation: start $[]$ empty

1. push(4) 4 inserted $[4]$
 2. push(pop()+4): 4 is popped then we add 4 $[4+4=8]$ $[8]$
 3. push(8) 8 inserted $[8, 8]$ original 8
 4. push(pop()/2): 8 is popped then we div by 2 $[8/2=4]$ now we pop 4. $[8, 4]$
 5. pop() 8 is removed $[4]$
 6. pop() 4 is removed $[]$
- Final Queue: $[]$ now empty

3. (text) find in deque [10 points]

algorithm:

left_index = 0 // front of the deque
right_index = n - 1 // start from the back

traverse to find element x from both ends of the deque

deque[left_index] = x, return left_index } increment left_index
 deque[right_index] = x return right_index } decrement right_index } each step

IF element x not found return -1 or null

iterate at most $\frac{n}{2}$ times *

n = len(deque)

for i in range((n+1)/2):
 loop runs half of the input size
 it will find it by searching from
 both ends.

We iterate at most $O(\frac{n}{2}) = O(n)$ - deque allows to traverse from both sides @ the same time. $O(\frac{n}{2})$

7. (text) Algorithm Analysis

• Balanced Brackets.java

Time Complexity: $O(n)$ is Balanced method has a time complexity of $O(n)$, where n is the length of input string S. Function iterates through the string once, for loop has $O(1)$ operations (adding to or removing from the stack for each char. Each char is processed only once \therefore time complexity is $O(n)$

Space Complexity: $O(n)$ in the worst case, where all characters in the input are opening brackets, all n characters are stored in the stack. In the best case the sequence is balanced, the stack never grows more than the original input. But still consider the worst case possibility $\therefore O(n)$ is the space complexity where n is the original input.

REST ON NEXT PG.!!

• DecodeString.java

Time Complexity: $O(n)$ decodeString method has time complexity of $O(n)$, where n is the length of the input string S . Function processes each char once, single pass through the string for loop. Inside the loop we have $O(1)$ atomic operations like push() & pop() from the stack. When a ']' bracket is met, the worst case scenario involves concat a substring multiple times, but since each char is only push() & pop() from the stack a limited # of times we can say $O(n)$.

Space Complexity: $O(n)$ in the worst case bc of stackStr & stackNum stacks will hold substring & #'s for the nested bracket sequences. Also, the ^{mutable string}StringBuilder used for concat/construct the final output can take up to $O(n)$ space. All data structures hold at most n chars in the worst case, \therefore Space complexity is $O(n)$.

• Infix to Postfix.java

Time Complexity: $O(n)$ infixToPostfix method has time complexity of $O(n)$, where n is the length of the input infix expression. Each char in the string is processed once in the for loop, $O(1)$ atomic operations like push() & pop(). Worst case, operation may be popped more than once when a closing ')' or operator sign with lower precedence, but since each element is pushed & popped at most once time complexity $O(n)$.

Space Complexity: $O(n)$ in the worst case the stack may store all operators before they are appended to the result string. The ^{StringBuilder}SB used to store the final postfix expression also takes $O(n)$ space. Both data structures hold at most n characters where n is the input. Overall space complexity is $O(n)$.