

# Airfoil Performance Estimation Project Report

## 1. Introduction

This project provides a simple Python-based tool for estimating the aerodynamic performance of airfoils, specifically focusing on the lift coefficient ( $C_L$ ) and the moment coefficient about the quarter-chord ( $C_{M,c/4}$ ). The estimations are based on the fundamental principles of **Thin Airfoil Theory**, a foundational concept in aerodynamics. Designed for intermediate-level coders, the tool features a user-friendly interactive interface for selecting various airfoil types and inputting flight parameters.

## 2. Theoretical Basis: Thin Airfoil Theory

Thin Airfoil Theory is a simplified analytical method used to predict the aerodynamic characteristics of airfoils, particularly at small angles of attack. It makes several key assumptions to simplify the complex equations of fluid dynamics:

- **Thin Airfoil Assumption:** The airfoil is assumed to be infinitesimally thin, represented by its camber line.
- **Inviscid Flow:** The fluid is assumed to be ideal, meaning there are no viscous effects (friction).
- **Incompressible Flow:** The fluid density is assumed to be constant.
- **Small Perturbations:** The flow disturbances caused by the airfoil are small.

Under these assumptions, Thin Airfoil Theory provides elegant analytical solutions for the lift and moment characteristics.

### Key Formulas Used:

- **Lift Coefficient ( $C_L$ ):**  
The lift coefficient is given by:  
$$C_L = 2\pi(\alpha - \alpha_{L=0})$$

Where:

- $\alpha$  is the angle of attack (in radians).
- $\alpha_{L=0}$  is the zero-lift angle of attack (the angle of attack at which  $C_L=0$ ).
- **Moment Coefficient about the Quarter-Chord ( $C_{M,c/4}$ ):**  
Thin Airfoil Theory predicts that the moment coefficient about the quarter-chord point is independent of the angle of attack.
  - For Symmetric Airfoils:  
$$C_{M,c/4} = 0$$

This is because symmetric airfoils have no inherent pitching moment.

- For Cambered Airfoils (Parabolic Camber Approximation):  
For a parabolic camber line defined by  $z_c(x) = 4hx(1-x)$ , where  $h$  is the maximum camber as a fraction of the chord:  
 $\alpha_L = 0 = -2h$  (in radians)  $CM, c/4 = \pi h$

### 3. Project Features

The Python code implements the following functionalities:

- **Lift and Moment Estimation:** Calculates the LIFT\_COEFFICIENT (CL) and MOMENT\_COEFFICIENT\_C4 (CM,c/4).
- **Zero-Lift Angle of Attack Calculation:** Determines ZERO\_LIFT\_ANGLE\_OF\_ATTACK\_DEG ( $\alpha_L = 0$ ).
- **Airfoil Type Selection:** Users can choose from:
  - **Symmetric Airfoil:** Assumes a flat camber line.
  - **Cambered Airfoil (Generic Parabolic):** Allows the user to input a MAX\_CAMBER\_FRACTION directly.
  - **NACA 4-Digit Series (Approximate):** The user inputs a 4-digit NACA number (e.g., 2412). The code extracts the maximum camber percentage from the first digit and uses it to approximate the airfoil's camber as a parabolic shape for the Thin Airfoil Theory calculations.
- **Interactive User Interface:** A command-line menu guides the user through the selection process and input of the ANGLE\_OF\_ATTACK\_DEG.
- **Robust Input Handling:** Includes error handling for invalid numerical or string inputs, prompting the user to re-enter valid data.
- **Clear Output:** Presents the estimated CL, CM,c/4, and  $\alpha_L = 0$  in a formatted manner.

### 4. Key Variables and Functions

#### Functions:

- ESTIMATE\_AIRFOIL\_PERFORMANCE(AIRFOIL\_TYPE, ANGLE\_OF\_ATTACK\_DEG, MAX\_CAMBER\_FRACTION): The core function for calculating aerodynamic coefficients.
- RUN\_AIRFOIL\_ESTIMATOR(): Manages the user interaction, menu, and input validation.

#### Key Variables:

- AIRFOIL\_TYPE: String ('symmetric' or 'cambered') indicating the chosen airfoil

type.

- **ANGLE\_OF\_ATTACK\_DEG:** User-input angle of attack in degrees.
- **MAX\_CAMBER\_FRACTION:** Maximum camber of the airfoil as a fraction of the chord. This is either 0 for symmetric, user-defined for generic cambered, or derived from NACA 4-digit input.
- **LIFT\_COEFFICIENT:** The calculated lift coefficient ( $C_L$ ).
- **MOMENT\_COEFFICIENT\_C4:** The calculated moment coefficient about the quarter-chord ( $C_{M,c/4}$ ).
- **ZERO\_LIFT\_ANGLE\_OF\_ATTACK\_DEG:** The calculated zero-lift angle of attack in degrees ( $\alpha_{L=0}$ ).

## 5. Limitations of the Project

It is crucial to understand the limitations inherent in using Thin Airfoil Theory and the approximations made in this project:

- **Inherent Limitations of Thin Airfoil Theory:**
  - **No Drag Calculation:** The theory does not account for drag, as it assumes inviscid flow.
  - **Accuracy at Small Angles:** It is accurate only for small angles of attack (typically up to  $10^\circ$ – $15^\circ$ ).
  - **No Stall Prediction:** It cannot predict the onset of stall or post-stall behavior.
  - **Incompressible Flow Only:** Not suitable for high-speed (compressible) flows.
  - **Idealized Flow:** Does not account for real-world effects like boundary layers, flow separation, or turbulence.
- **Project-Specific Approximations:**
  - **NACA 4-Digit Approximation:** For NACA 4-digit airfoils, the code uses a simplified parabolic camber line based *only* on the maximum camber percentage. Real NACA 4-digit airfoils have a more complex, piecewise parabolic camber distribution, which is not fully captured by this simplification. This means the results for NACA airfoils are approximate, especially for  $\alpha_{L=0}$  and  $C_{M,c/4}$ .
  - **Limited Airfoil Types:** The project only supports symmetric, generic parabolic camber, and a simplified NACA 4-digit representation. More complex airfoil series (e.g., NACA 5-digit, 6-series) have different camber line equations that are not implemented.