



**PARUL UNIVERSITY**  
**FACULTY OF ENGINEERING AND TECHNOLOGY**  
**DEPARTMENT OF APPLIED SCIENCE AND HUMANITIES**  
**4<sup>th</sup> SEMESTER B. TECH PROGRAMME**  
**PROBABILITY, STATISTICS AND NUMERICAL METHODS (303191251)**  
**ACADEMIC YEAR 2024-25**

## Tutorial: Finite Differences and Interpolation

1	Write forward difference table if <table><tr><td>x:</td><td>10</td><td>20</td><td>30</td><td>40</td></tr><tr><td>y:</td><td>1.1</td><td>2.0</td><td>4.4</td><td>7.9</td></tr></table>	x:	10	20	30	40	y:	1.1	2.0	4.4	7.9				
x:	10	20	30	40											
y:	1.1	2.0	4.4	7.9											
2	With the usual notations, show that (i) $\nabla = 1 - e^{-hD}$ (ii) $(1 + \Delta)(1 - \nabla) = 1$														
3	Given $\sin 45^\circ = 0.7071$ , $\sin 50^\circ = 0.7660$ , $\sin 55^\circ = 0.8192$ , $\sin 60^\circ = 0.8660$ . Find $\sin 52^\circ$ using Newton's forward formula.														
4	Find $f(22)$ from the following data using Newton's backward formula <table><tr><td>X</td><td>20</td><td>25</td><td>30</td><td>35</td><td>40</td><td>45</td></tr><tr><td>f(x)</td><td>354</td><td>332</td><td>291</td><td>260</td><td>231</td><td>204</td></tr></table>	X	20	25	30	35	40	45	f(x)	354	332	291	260	231	204
X	20	25	30	35	40	45									
f(x)	354	332	291	260	231	204									
5	Construct Newton's forward interpolation polynomial for the following data : <table><tr><td>X</td><td>4</td><td>6</td><td>8</td><td>10</td></tr><tr><td>Y</td><td>1</td><td>3</td><td>8</td><td>16</td></tr></table> Hence evaluate y for x=5.	X	4	6	8	10	Y	1	3	8	16				
X	4	6	8	10											
Y	1	3	8	16											
6	Use Gauss's forward formula to evaluate $y_{30}$ , given that $y_{21}=18.4708$ , $y_{25}=17.8144$ , $y_{29}=17.1070$ , $y_{33}=16.3432$ and $y_{37}=15.5154$ .														
7	Using Gauss backward difference formula, find $y(8)$ from the following table: <table><tr><td>x</td><td>0</td><td>5</td><td>10</td><td>15</td><td>20</td><td>25</td></tr><tr><td>y</td><td>7</td><td>11</td><td>14</td><td>18</td><td>24</td><td>32</td></tr></table>	x	0	5	10	15	20	25	y	7	11	14	18	24	32
x	0	5	10	15	20	25									
y	7	11	14	18	24	32									
8	Find the polynomial $f(x)$ by using Lagrange's formula and hence find $f(3)$ for x:            0        1        2        5 f(x):        2        3        12       147														
9	Use Lagrange's formula to find the form of $f(x)$ , given x:            0            2            3            6 f(x):        648        704        729        792														
10	Using Newton's divided difference formula, evaluate $f(8)$ and $f(15)$ given: x:            4            5            7            10          11          13 f(x):        48          100        294        900        1210       2028														