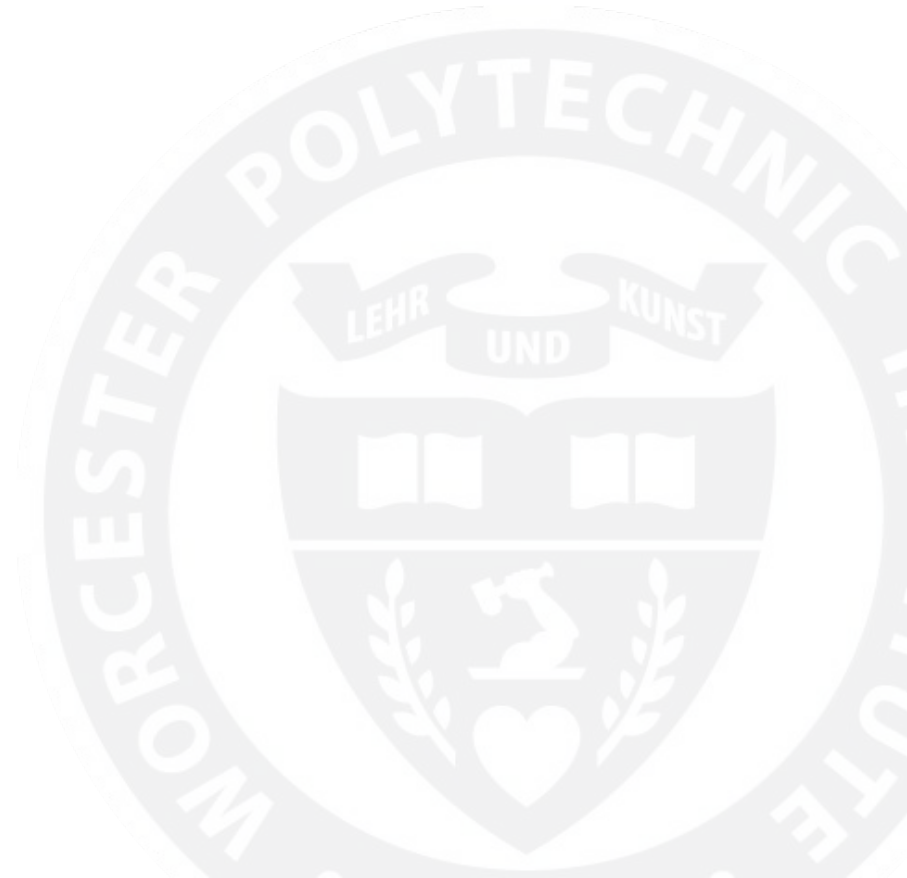


# WPI

## **CS534 Spring 2019 Project Part II**

### **--Sudoku**

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# Introduction

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What is Sudoku?

Sudoku is a logic-based, combinatorial number-placement puzzle. The objective is to fill a  $9 \times 9$  grid with digits so that each column, each row, and each of the nine  $3 \times 3$  subgrids that compose the grid contain all of the digits from 1 to 9. The puzzle setter provides a partially completed grid, which for a well-posed puzzle has a single solution.

# Introduction

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What we do?

We implement a program that could solve classic 9\*9 sudoku problem. Beside that, we expand our program and make it compatible with all  $n*n$  sudoku problem.

# Detailed description

Variables: [0,0] [1,0] [2,3].....

Values: 0,1,2,3,...,dimension (dimension=9/16/25/...)

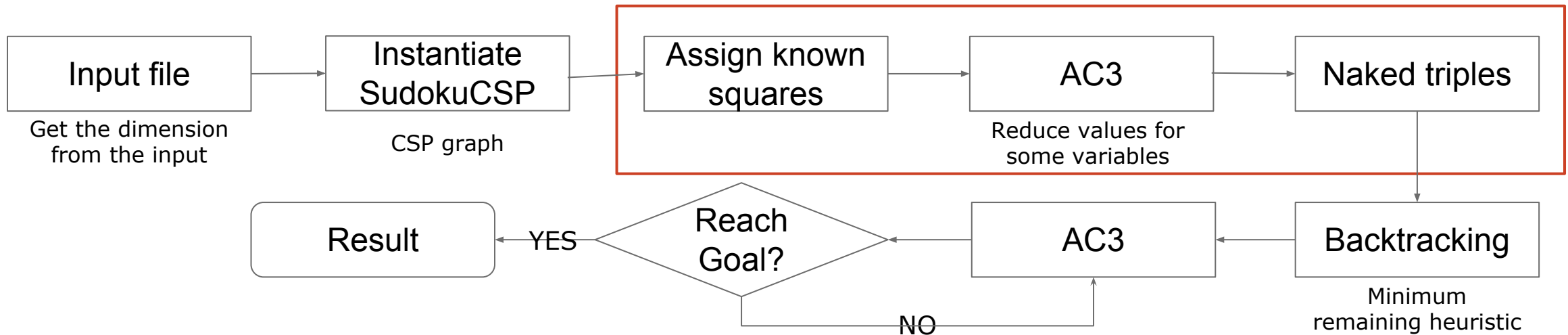
Constraints: Alldiff (row), Alldiff(collum), Alldiff(3\*3 / 4\*4 / 5\*5 /...)

				7			8	
	1		8	4				
			3		5		4	
5		9			8		3	6
				6		4		
		8	7	3				
			4	8				
3		6				9		
	7			2	3			

12		6	2			14		3		8		16			1
		10		16			2		1		9		3		
	4		5	1	8	3		6		14				9	10
1			7					6	12		16		14		11
	5			10	13		7		12		1		9	14	
9		11	12		3			15		10	14		1		
	10			11		9			4				8		3
6		4	15		16		12		8		3	7		11	
	7		1	2	14			9		3		10	16		15
3		12			6	1			15		13			2	
		9		4	5		16			7		1	12		14
	8	2		13		12		1		4	16		11	5	
10			9		4		11	2				5			8
5	2		6		1		15		9	13	11			10	
		7		5		16		10			15		6		
14			4		10		9		16			11	13		2

# Implementation

- Class `csp(variable, domain, neighbours, constraints)`
  - Extends class of part 1



- Naked triples
  - In any unit (row, column or box), find three squares that each have a domain that contains the same three numbers or a subset of those numbers



# Test Result

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9\*9

Directly solved by AC-3

```
Goal reached! One of solution(num of assign: 81):  
  
-----+-----+-----  
4 8 3 | 9 2 1 | 6 5 7  
9 6 7 | 3 4 5 | 8 2 1  
2 5 1 | 8 7 6 | 4 9 3  
-----+-----+-----  
5 4 8 | 1 3 2 | 9 7 6  
7 2 9 | 5 6 4 | 1 3 8  
1 3 6 | 7 9 8 | 2 4 5  
-----+-----+-----  
3 7 2 | 6 8 9 | 5 1 4  
8 1 4 | 2 5 3 | 7 6 9  
6 9 5 | 4 1 7 | 3 8 2  
-----+-----+-----  
  
AC3 directly reach Goal!
```

```
0 0 3 0 2 0 6 0 0  
9 0 0 3 0 5 0 0 1  
0 0 1 8 0 6 4 0 0  
0 0 8 1 0 2 9 0 0  
7 0 0 0 0 0 0 0 8  
0 0 6 7 0 8 2 0 0  
0 0 2 6 0 9 5 0 0  
8 0 0 2 0 3 0 0 9  
0 0 5 0 1 0 3 0 0
```

# Test Result

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9\*9

No result

0	0	5	3	0	0	0	0	0
8	0	0	0	0	0	0	2	0
0	7	0	0	1	0	0	5	0
4	5	0	0	0	5	3	0	0
9	1	0	0	7	0	0	0	6
2	0	3	2	0	0	0	8	0
0	6	0	5	0	0	0	0	9
0	0	4	0	0	0	0	3	0
0	0	0	0	0	9	7	0	0

NO such assignment is possible

# Test Result

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9\*9

1	0	0	5	3	0	0	0	0	0
2	8	0	0	0	0	0	0	2	0
3	0	7	0	0	1	0	0	5	0
4	4	0	0	0	0	5	3	0	0
5	0	1	0	0	7	0	0	0	6
6	0	0	3	2	0	0	0	8	0
7	0	6	0	5	0	0	0	0	9
8	0	0	4	0	0	0	0	3	0
9	0	0	0	0	0	9	7	0	0

6	4	5	3	9	2	8	7	1
8	3	1	6	5	7	9	2	4
2	7	9	8	1	4	6	5	3
4	2	6	1	8	5	3	9	7
5	1	8	9	7	3	2	4	6
7	9	3	2	4	6	1	8	5
3	6	7	5	2	8	4	1	9
9	8	4	7	6	1	5	3	2
1	5	2	4	3	9	7	6	8



# Test Result

16\*16

12		6	2			14		3		8		16			1
		10		16			2		1		9		3		
	4		5	1	8	3		6		14				9	10
1			7				6	12		16		14			11
	5			10	13		7		12		1		9	14	
9		11	12		3			15		10	14		1		
	10			11		9			4				8		3
6		4	15		16		12		8		3	7		11	
	7		1	2	14			9		3		10	16		15
3		12			6	1			15		13			2	
		9		4	5		16			7		1	12		14
	8	2		13		12		1		4	16		11	5	
10			9		4		11	2				5			8
5	2		6		1		15		9	13	11			10	
		7		5		16		10			15		6		
14			4		10		9		16			11	13		2

12	9	6	2	7	11	14	4	3	13	8	10	16	5	15	1
11	14	10	8	16	12	5	2	7	1	15	9	4	3	6	13
16	4	15	5	1	8	3	13	6	11	14	2	12	7	9	10
1	3	13	7	15	9	10	6	12	5	16	4	14	2	8	11
-----+-----+-----+-----															
2	5	8	3	10	13	4	7	16	12	11	1	15	9	14	6
9	13	11	12	6	3	8	5	15	7	10	14	2	1	4	16
7	10	14	16	11	15	9	1	5	4	2	6	13	8	12	3
6	1	4	15	14	16	2	12	13	8	9	3	7	10	11	5
-----+-----+-----+-----															
4	7	5	1	2	14	11	8	9	6	3	12	10	16	13	15
3	16	12	11	9	6	1	10	14	15	5	13	8	4	2	7
13	6	9	10	4	5	15	16	11	2	7	8	1	12	3	14
15	8	2	14	13	7	12	3	1	10	4	16	6	11	5	9
-----+-----+-----+-----															
10	12	1	9	3	4	13	11	2	14	6	7	5	15	16	8
5	2	16	6	8	1	7	15	4	9	13	11	3	14	10	12
8	11	7	13	5	2	16	14	10	3	12	15	9	6	1	4
14	15	3	4	12	10	6	9	8	16	1	5	11	13	7	2
-----+-----+-----+-----															

# Conclusion

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- Good expansibility
  - Theoretically support all  $n * n$  sudoku problem
- Good efficiency when solve classical sudoku
  - When solving  $9*9$  and  $16*16$  sudoku problem, our program has a good efficiency.
- Low efficiency when solve complicated sudoku problem
  - When solving  $25*25$  sudoku, our program spend a lot of time and space.

The background features a large, faint, circular watermark of the Worcester Polytechnic Institute seal. The seal contains the text "WORCESTER POLYTECHNIC INSTITUTE" around the perimeter and "1865" at the bottom. In the center is a shield with an open book and a figure.

**Thank you!**

**Questions**



# WPI

## Backup Slides

