Homework 8 Com S 331, Spring 2017

Due date: Wednesday, March 29, 2017

Please submit the homework via BlackBoard before the class that day.

Note: All submissions should be **typed** and in .pdf or .doc(x) format. However, state diagrams can be drawn with hand and presented in the final manuscript as images. We recommend to use Latex for typing homeworks. You **do not** need to formally prove the correctness of your constructions unless a question specifically asks to do so. However, in most cases you need to present a reasonable justification of correctness.

Total points available: 85

- 0. Read pages 130–146 of Section 2.4 in the class-book (Sipser, 3rd edition).
- 1. **(25 points)** Prove that if a grammar is *ambiguous*, then it is **not** deterministic. Use the definition of deterministic CFGs via *forced handles* (see Definition 2.47 in the class-book).
- 2. (60 points) Use the DK-test to determine whether the following grammars are deterministic or not:
 - (a) (20 points)

$$\begin{split} R &\to S \,|\, T \\ S &\to aSb \,|\, ab \\ T &\to aTbb \,|\, abb \end{split}$$

(b) (20 points)

$$S \to T \dashv \mid \dashv \\ T \to aTb \, | \, ab$$

(c) (20 points)

$$S \to T \dashv \\ T \to TaTb \,|\, TbTa \,|\, \varepsilon$$

Present diagrams of the respective DFAs DK (see Examples 2.53 and 2.55 in the class-book), and justify your conclusions.