

Homework - chapter 32 [5, 15, 23, 29, 37, 41, 45, 49, 55, 61]  
 Jay Patel  
 classical Physics - 2 (220)  
 OL02 - Professor U.

Q5]  $\phi + (90^\circ - \theta_1) + (90^\circ - \theta_2) = 180^\circ \rightarrow \phi = \theta_1 + \theta_2$   
 Do the same for triangle ABO  
 $\alpha + 2\theta_1 + 2\theta_2 = 180^\circ \rightarrow \alpha = 180^\circ - 2(\theta_1 + \theta_2) = 180^\circ - 2\phi$   
 At point O  
 $\beta = 180^\circ - \alpha = 180^\circ - (180^\circ - 2\phi) = \boxed{2\phi}$

Q15]  $m = \frac{-d_i}{d_o} \rightarrow d_i = -md_o$

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \rightarrow f = \frac{d_o d_i}{d_o + d_i} = \frac{d_o (-md_o)}{d_o - md_o} = \frac{md_o}{m-1}$$

$$= \frac{4(2.00\text{cm})}{4-1} = 2.677\text{cm}$$

$$r = 2f = 2(2.667\text{cm}) = \boxed{5.3\text{cm}}$$

As the focal length is positive, mirror is concave

Q23]  $m = \frac{-d_i}{d_o} \rightarrow d_i = -md_o$

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \rightarrow f = \frac{d_o d_i}{d_o + d_i} = \frac{d_o (-md_o)}{d_o - md_o} = \frac{md_o}{m-1}$$

$$\frac{(0.55)(3.2\text{m})}{0.55-1} = \boxed{-3.9\text{m}}$$

Q29] a]  $m = \frac{-d_i}{d_o} \rightarrow d_i = -md_o$

$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i} \rightarrow \frac{1}{f} = \frac{1}{d_o} + \frac{1}{-md_o}$$

$$= \frac{1}{d_o} \left( 1 - \frac{1}{m} \right) \rightarrow \boxed{d_o = f \left( 1 - \frac{1}{m} \right)}$$

$$b) \left( 1 - \frac{1}{m} \right) \leq 0 \rightarrow 1 \leq \frac{1}{m} \rightarrow \boxed{0 \leq m \leq 1}$$

$$37) d = ct = (3.00 \times 10^8 \text{ m/s}) (10^{-8} \text{ s}) = \boxed{3 \text{ m}}$$

$$41) n_1 \sin \theta_1 = n_2 \sin \theta_2 \rightarrow \theta_1 = \sin^{-1} \left( \frac{n_2 \sin \theta_2}{n_1} \right) \\ = \sin^{-1} \left( \frac{1.00 \sin 56.0^\circ}{1.33} \right) = \boxed{38.6^\circ}$$

$$45) \tan \theta_1 = \frac{l_1}{h_1} = \frac{2.5 \text{ m}}{1.3 \text{ m}} = 1.9231 \rightarrow \theta_1 = 62.526^\circ$$

from air into water

$$n_{\text{air}} \sin \theta_1 = n_{\text{water}} \sin \theta_2;$$

$$(1.00) \sin 62.526^\circ = (1.33) \sin \theta_2 \rightarrow \theta_2 = 41.842^\circ$$

horizontal distance

$$l = l_1 + l_2 = l_1 + h_2 \tan \theta_2$$

$$= 2.5 \text{ m} + (2.1 \text{ m}) \tan 41.842^\circ = 4.38 \text{ m} \approx \boxed{4.4 \text{ m}}$$

$$43) n_1 \sin \theta_1 = \sin \theta_r \rightarrow \theta_r = \sin^{-1} (1.52 \sin 30^\circ) = 49.46^\circ$$

$$\left( \phi = 2(\theta_r - 30^\circ) = 2(49.46^\circ - 30^\circ) = \boxed{38.9^\circ} \right)$$

using Snell's law

By symmetry, the angle  $\phi$  is twice the angle of the refracted beam from the vertical

55) Using Snell's law

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \rightarrow (1.000) \sin 60^\circ = (n) \sin \theta_2$$

$$\theta_2 = \sin^{-1} \left( \frac{\sin 60^\circ}{n} \right)$$

$$61] \tan \theta_1 = \frac{l}{h} = \frac{(7.6 \text{ cm})}{(8.0 \text{ cm})} = 0.95 \rightarrow \theta_1 = 43.53^\circ$$

$$n_{\text{liquid}} \sin \theta_1 = n_{\text{air}} \sin \theta_2 \rightarrow n_{\text{liquid}} \sin \theta_{1, \text{max}} = (1.00) \sin 90^\circ \rightarrow \sin \theta_{1, \text{max}} = \frac{1}{n_{\text{liquid}}}$$

$$\text{So, } \sin \theta_1 \geq \sin \theta_{1, \text{max}} = \frac{1}{n_{\text{liquid}}} \rightarrow \sin 6.887 \geq \frac{1}{n_{\text{liquid}}}$$

$$\rightarrow \boxed{n_{\text{liquid}} \geq 1.5}$$



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Homework - chapter 33 [5, 15, 21, 27, 37, 45, 55, 65]

Jay Patel  
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Q5] a)  $\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \rightarrow d_i = \frac{d_o f}{d_o - f} = \frac{(10.0\text{m})(0.105\text{m})}{10.0\text{m} - 0.105\text{m}}$   
 $= 0.106\text{m} = \boxed{106\text{mm}}$

Same general calculation b)  $d_i = \frac{d_o f}{d_o - f} = \frac{(3.0\text{m})(0.105\text{m})}{3.0\text{m} - 0.105\text{m}} = 0.109\text{m} = \boxed{109\text{mm}}$

Same general calculation c)  $d_i = \frac{d_o f}{d_o - f} = \frac{(1.0\text{m})(0.105\text{m})}{1.0\text{m} - 0.105\text{m}} = 0.117\text{m} = \boxed{117\text{mm}}$

Small to max d)  $\frac{1}{d_{\min}} + \frac{1}{d_{\max}} = \frac{1}{f} \rightarrow d_{\min} = \frac{d_{\max} f}{d_{\max} - f}$

$= \frac{(132\text{mm})(105\text{mm})}{132\text{mm} - 105\text{mm}} = 53\text{mm} = \boxed{0.53\text{m}}$

Q15] a)  $\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \rightarrow d_i = \frac{d_o f}{d_o - f}$ ;  $m = \frac{d_i}{d_o} = \frac{-f}{d_o - f}$

$d_o > f$ , image distance is positive, producing a real image which gives an inverted image

b)  $d_o < f$ , image is negative, producing a virtual image, which gives upright image

c)  $d_i = \frac{(-f)f}{-f - f} = \frac{f}{2}$   $m = \frac{-d_i}{d_o} = \frac{f}{-f - f} = \frac{1}{2}$

limit of large negative object distance

$d_i = \frac{(-\infty)f}{(-\infty - f)} = f$   $m = \frac{-d_i}{d_o} = \frac{f}{-\infty - f} = 0$

$-d_o > f$ , the image is real & upright with  $\frac{1}{2}f < d_i < f$  &  $0 < m < 1/2$ .

$$d) \quad d_i = \frac{(o)f}{o-f} = 0 \quad m = \frac{-d_i}{d_o} = \frac{-f}{o-f} = 1$$

$0 < -d_o < f$ , the image is real & upright with  $0 < d_i < \frac{1}{2}f$  &  $\frac{1}{2} < m < 1$

$$2i) \quad \frac{1}{d_{o1}} + \frac{1}{d_{i1}} = \frac{1}{f_1} \rightarrow d_{i1} = \frac{d_{o1}f_1}{d_{o1}-f_1} = \frac{(35.0\text{cm})(25.0\text{cm})}{(35.0\text{cm})-(25.0\text{cm})} = 87.5\text{cm}$$

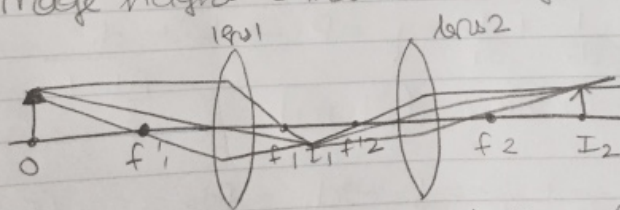
The image is object for the second lens, because it is beyond the second lens

$$d_{o2} = 16.5\text{cm} - 87.5\text{cm} = -71.0\text{cm}$$

$$\frac{1}{d_{o2}} + \frac{1}{d_{i2}} = \frac{1}{f_2} \rightarrow d_{i2} = \frac{d_{o2}f_2}{d_{o2}-f_2} = \frac{(-71.0\text{cm})(25.0\text{cm})}{(-71.0\text{cm})-(25.0\text{cm})} = 18.5\text{cm} \text{ beyond second lens}$$

$$m = m_1 m_2 = \left( \frac{-d_{i1}}{d_{o1}} \right) \left( \frac{-d_{i2}}{d_{o2}} \right) = \frac{d_{i1} d_{i2}}{d_{o1} d_{o2}} = \frac{(87.5\text{cm})(18.5\text{cm})}{(35.0\text{cm})(-71.0\text{cm})} = -0.651 \times (\text{inverted})$$

27) a) We see the image is real & upright. We estimate that it is 30 cm beyond the second lens, & that the final image height is half the original object height



$$b) \quad \frac{1}{d_{o1}} + \frac{1}{d_{i1}} = \frac{1}{f_1} \rightarrow d_{i1} = \frac{d_{o1}f_1}{d_{o1}-f_1} = \frac{(36\text{cm})(13\text{cm})}{(36\text{cm})-(13\text{cm})} = 20.35\text{cm}$$

$$\begin{array}{r} 56.00 \\ -20.35 \\ \hline 35.65 \end{array}$$

for second lens,

$$d_{o2} = 56\text{cm} - 20.35\text{cm} = 35.65\text{cm}$$

image from second lens,

$$\frac{1}{d_{o2}} + \frac{1}{d_{i2}} = \frac{1}{f_2} \rightarrow d_{i2} = \frac{d_{o2} f_2}{d_{o2} - f_2} = \frac{(35.65\text{cm})(16\text{cm})}{(35.65\text{cm}) - (16\text{cm})}$$

$$= \boxed{29.25\text{cm}} \text{ beyond the second lens}$$

Total two lenses

$$m = m_1 m_2 = \left( \frac{-d_{i1}}{d_{o1}} \right) \left( \frac{-d_{i2}}{d_{o2}} \right) = \frac{(20.35\text{cm})(29.25\text{cm})}{(36\text{cm})(35.65\text{cm})}$$

$$= \boxed{0.46\times}$$

$$37] f\text{-stop}_2 = \frac{f}{D} = \frac{(70\text{mm})}{(1.0\text{mm})} = \frac{f}{70}$$

$$+1 (f\text{-stop}_1)^{-2} = f_2 (f\text{-stop}_2)^{-2} \Rightarrow f_2 = +1 \left( \frac{f\text{-stop}_2}{f\text{-stop}_1} \right)^2$$

$$= \frac{1}{2505} \left( \frac{70}{11} \right)^2 = 0.165 \approx \boxed{\frac{1}{6}}$$

$$45] a) p = \frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{\infty} + \frac{1}{(-0.78\text{m})} = -1.2820 \approx \boxed{1.30}$$

$$b) \frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} = p \rightarrow d_o = \frac{d_i}{p d_i - 1} = \frac{(0.25)}{(-1.2820)(0.25) - 1}$$

$$= 0.37\text{m} \approx \boxed{37\text{cm}}$$

$$55] a) \frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \rightarrow d_i = \frac{f d_o}{d_o - f} = \frac{(6.00\text{cm})(5.85\text{cm})}{(5.85\text{cm}) - (6.00\text{cm})}$$

$$= \boxed{-234\text{cm}}$$

$$b) m = \frac{N}{f} = \frac{25.0\text{cm}}{6.00\text{cm}} = \boxed{4.17\times}$$



65] The focal length of the objective is just half the radius of the curvature. So for the magnification,

$$m = \frac{-f_o}{f_e} = \frac{-\frac{1}{2}r}{f_o} = \frac{3.2m}{0.028m} = -114x$$

$$\approx \boxed{-110x}$$

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Homework - Chapter 34 [1, 5, 15, 25, 35]

Jay Patel

Classical Physics - 2 (220)

OL02 - Professor U.

$$Q1] \sin \theta_2 = \frac{vt}{AB} = \frac{-vt}{\frac{vt}{\sin \theta_1}} = \sin \theta_1 \rightarrow \boxed{\theta_2 = \theta_1}$$

$$Q5] d \sin \theta = m\lambda \rightarrow d \frac{x}{l} = m\lambda \rightarrow x = \frac{\lambda m l}{d}$$

$$x_1 = \frac{\lambda_1 m l}{d}, \quad x_2 = \frac{\lambda_2 m l}{d} \rightarrow$$

$$\Delta x = x_2 - x_1 = \frac{(\lambda_2 - \lambda_1) m l}{d} = \frac{[(720 - 660) \times 10^{-9} \text{m}]}{(2)(1.0 \text{m})}$$

$$= 1.76 \times 10^{-4} \text{m} \approx \boxed{0.2 \text{mm}} \quad (6.8 \times 10^{-4} \text{m})$$

Using small angle approximation, since  $x \ll l$

$$Q15] d \sin \theta = m\lambda n \rightarrow d \frac{x}{l} = m\lambda n \rightarrow x = \frac{\lambda m l}{d}$$

$$x_1 = \frac{\lambda m l}{d}, \quad x_2 = \frac{\lambda(m+1)l}{d} \rightarrow$$

$$\Delta x = x_2 - x_1 = \frac{\lambda n(m+1)l}{d} - \frac{\lambda m l}{d} = \frac{\lambda n l}{d}$$

$$\frac{(470 \times 10^{-9} \text{m})(0.500 \text{m})}{(1.33)(6.00 \times 10^{-5} \text{m})} = \boxed{2.94 \times 10^{-3} \text{m}}$$

$$Q25] a] \phi_{\text{net}} = \phi_2 - \phi_1 = \left[ \left( \frac{2t}{\lambda_{\text{min}}} \right) 2\pi \right] - \pi$$

$$= \pi \rightarrow + = \frac{1}{2} \lambda_{\text{film}} = \frac{\lambda}{2n} = \frac{480 \text{nm}}{2(1.33)} = \boxed{180 \text{nm}}$$



$$b) \phi_{net} = \phi_2 - \phi_1 = \left[ \left( \frac{2t}{\lambda_{film}} \right) 2\pi \right] - \pi = 3\pi \rightarrow$$

$$t = \lambda_{film} = \frac{\lambda}{n} = \frac{480nm}{(1.33)} = \boxed{361nm}$$

$$\phi_{net} = \phi_2 - \phi_1 = \left[ \left( \frac{2t}{\lambda_{film}} \right) 2\pi \right] - \pi = 3\pi \rightarrow$$

$$t = \lambda_{film} = \frac{\lambda}{n} = \frac{3}{2} \frac{480nm}{(1.33)} = \boxed{541nm}$$

c) If the thickness is less than one wavelength, there would be change in path length, & so the two reflected waves would have a phase difference of about  $\phi_1 = \pi$ .

$$35) \frac{r_{air}}{r_{liquid}} = \frac{\sqrt{m\lambda R}}{\sqrt{m(2/n)R}} = \sqrt{n} \rightarrow n = \left( \frac{r_{air}}{r_{liquid}} \right)^2$$

$$= \left( \frac{2.92cm}{2.54cm} \right)^2 = \boxed{1.32}$$

Note : I wrote 45 instead of 43, but I have also written 43

at the very end of chapter 35 homework, so please ignore number 45.

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Homework - chapter 35 [3, 11, 25, 35, 45, 51, 59]

Jay Patel  
Classical Physics - 2 (220)  
OL02 - Professor U.

Q3]  $D \sin \theta = m \lambda \rightarrow \theta = \sin^{-1} \left( \frac{m \lambda}{D} \right)$

$$\theta_1 = \sin^{-1} \left( \frac{1 \times 580 \times 10^{-9} \text{ m}}{3.8 \times 10^{-6} \text{ m}} \right) = 8.678^\circ$$

$$\theta_2 = \sin^{-1} \left( \frac{2 \times 580 \times 10^{-9} \text{ m}}{3.8 \times 10^{-6} \text{ m}} \right) = 17.771^\circ$$

$$\theta = \frac{\theta_1 + \theta_2}{2} = \frac{8.678^\circ + 17.774^\circ}{2} = 13.23^\circ$$

$$y = l \tan \theta = (10.0 \text{ m}) \tan (13.23^\circ) = \boxed{2.35 \text{ m}}$$

Q11] a]  $\sin \theta_1 = \frac{\lambda}{D} \rightarrow \theta_1 = \sin^{-1} \frac{\lambda}{D} = \sin^{-1} \frac{780 \times 10^{-9} \text{ m}}{1.5 \times 10^{-6} \text{ m}}$

$$= 31.35^\circ$$

$$\Delta \theta = 2\theta_1 = 2(31.3^\circ) = \boxed{63^\circ}$$

b]  $\sin \theta_1 = \frac{\lambda}{D} \rightarrow \theta_1 = \sin^{-1} \frac{\lambda}{D} = \sin^{-1} \frac{780 \times 10^{-9} \text{ m}}{3.0 \times 10^{-6} \text{ m}}$

$$= \boxed{15.07^\circ}$$

$$\Delta \theta = 2\theta_1 = 2(15.07^\circ) = \boxed{30^\circ}$$

Q25]  $\theta = 1.22 \frac{\lambda}{D}$ ,  $l = r\theta = 1.22 \frac{r \lambda}{D} = 1.22$

$$\frac{(16 \text{ ly}) \left( \frac{9.46 \times 10^{15} \text{ m}}{1 \text{ ly}} \right) (550 \times 10^{-9} \text{ m})}{(0.66 \text{ m})} = \boxed{1.5 \times 10^{11} \text{ m}}$$



$$35] d \sin \theta = m \lambda \Rightarrow d = \frac{m \lambda_1}{\sin \theta_1} \Rightarrow$$

$$\lambda_2 = \frac{m_1 \sin \theta_2}{m_2 \sin \theta_1} \quad \lambda_1 = \frac{2 \sin 20.6^\circ}{1 \sin 53.2^\circ} (632.8 \text{ nm})$$

$$= \boxed{556 \text{ nm}}$$

$$45] a] \Delta l = \Delta l_1 + \Delta l_2 = d(\sin \phi + \sin \theta) = \pm m \lambda,$$

$$m = 0, 1, 2, \dots$$

Diffraction occurs at angle for which the incident light conserves interference.

b] The  $\pm$  allows for the incident angle & the diffracted angle to have +ve and -ve values.

$$c] \theta = \sin^{-1} \left( -\sin \phi \pm \frac{m \lambda}{d} \right) = \sin^{-1} \left( -\sin 15^\circ \pm \frac{550 \times 10^{-9} \text{ m}}{0.01 \text{ m}/5000} \right)$$

$$= \boxed{0.93^\circ \text{ \& \; } -32^\circ}$$

$$51] m \lambda = 2d \sin \phi \rightarrow \lambda = 2d \sin \phi_1; 2\lambda = 2d \sin \phi_2;$$

$$3\lambda = 2d \sin \phi_3$$

For each equation, all we can find is the ratio

$$\frac{\lambda}{d} = 2 \sin \phi = \frac{2}{3} \sin \phi_3 \quad \boxed{\text{NO}} \text{ we cannot determine}$$

the wavelength or the spacing.

$$59] \tan \theta_p = \frac{n_{\text{air}}}{n_{\text{water}}} \rightarrow \theta_p = \tan^{-1} \frac{n_{\text{air}}}{n_{\text{water}}}$$

$$= \tan^{-1} \frac{1.00}{1.33} = \boxed{36.9^\circ}$$

Second case  $\sin \theta_c = \frac{n_{\text{air}}}{n_{\text{water}}} \rightarrow \theta_p = \sin^{-1} \frac{n_{\text{air}}}{n_{\text{water}}}$

$$= \sin^{-1} \frac{1.00}{1.33} = \boxed{48.8^\circ}$$

Third case  $\tan \theta_p = n_{\text{water}} \rightarrow \theta_p = \tan^{-1} n_{\text{water}} =$

$$\tan^{-1} 1.33 = \boxed{53.1^\circ}$$

The two Brewster's angle add to give  $\boxed{90.0^\circ}$

(Q43)  $\tan \theta = \frac{y}{L}$ , where  $y$  is the displacement

$L$  is the distance

$$\sin \theta = \frac{m\lambda}{d}, d = \frac{1}{610 \text{ lines/mm}} \left( \frac{1 \text{ m}}{10^3 \text{ mm}} \right) = (1/6.1 \times 10^5) \text{ m}$$

$$y = L \tan \theta = L \tan \left[ \sin^{-1} \frac{m\lambda}{d} \right]$$

$$l_1 = L \tan \left[ \sin^{-1} \frac{m_{\text{red}} \lambda}{d} \right] - L \tan \left[ \sin^{-1} \frac{m_{\text{violet}} \lambda}{d} \right]$$

$$= (0.32 \text{ m}) \left\{ \tan \left[ \sin^{-1} \frac{(1)(700 \times 10^{-9} \text{ m})}{(1/6.1 \times 10^5) \text{ m}} \right] - \tan \left[ \sin^{-1} \frac{(1)(400 \times 10^{-9} \text{ m})}{(1/6.1 \times 10^5) \text{ m}} \right] \right\} = 0.0706 \text{ m} = \boxed{7 \text{ cm}}$$

$$l_2 = L \tan \left[ \sin^{-1} \frac{m_{\text{red}} \lambda}{d} \right] - L \tan \left[ \sin^{-1} \frac{m_{\text{violet}} \lambda}{d} \right]$$

$$= (0.32 \text{ m}) \left\{ \tan \left[ \sin^{-1} \frac{(2)(700 \times 10^{-9} \text{ m})}{(1/6.1 \times 10^5) \text{ m}} \right] \right.$$

$$\left. - \tan \left[ \sin^{-1} \frac{(2)(400 \times 10^{-9} \text{ m})}{(1/6.1 \times 10^5) \text{ m}} \right] \right\} = 0.3404 \text{ m} = \boxed{35 \text{ cm}}$$

The Second order rainbow is dispersed over a larger distance