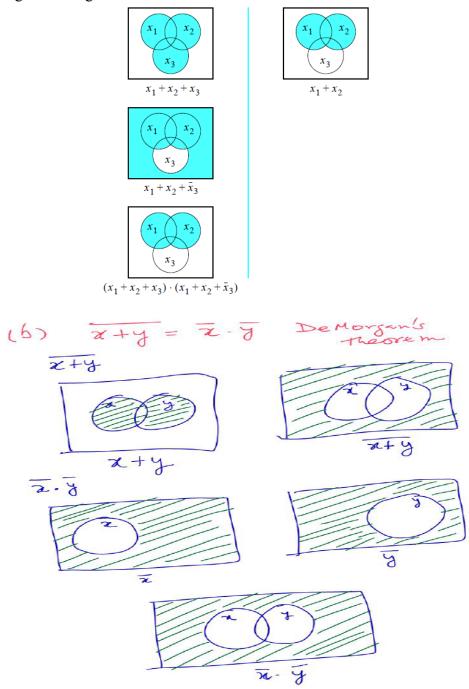
ELECTRICAL AND COMPUTER ENGINEERING IOWA STATE UNIVERSITY

Initial Stuff and Basics Assigned Date: Second Week Due Date: First class of 3rd week

P1. Proof using Venn diagrams:



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P2. (a) The answer is:

LHS

$$(x_1+x_2+x_3) \cdot (x_1+x_2+x_3) = x_1x_1+x_1x_2+x_1x_3+x_2x_1+x_2x_2+x_2x_3+x_3x_1+x_3x_2+x_3x_3$$

Using the Boolean algebra properties in the book section 2.5 page 34 and 35 we can simplify the last equation as follow:

$$x1x1=x1$$
, $x2x2=x2$, $x1x2+x2x1+x1x2+x1x2+x1x2$, $x3x3'=0$,

Then the equation will be reduced to: x1+x2+x1x2+x2x3+x2x3+x1x3+x1x3

P3. Here, we will substitute the value of x1, x2 and x3 in the following equation to validate that LHS=RHS

$$(x_1 + x_3)(\overline{x}_1 + \overline{x}_2 + \overline{x}_3)(\overline{x}_1 + x_2) = (x_1 + x_2)(x_2 + x_3)(\overline{x}_1 + \overline{x}_3)$$

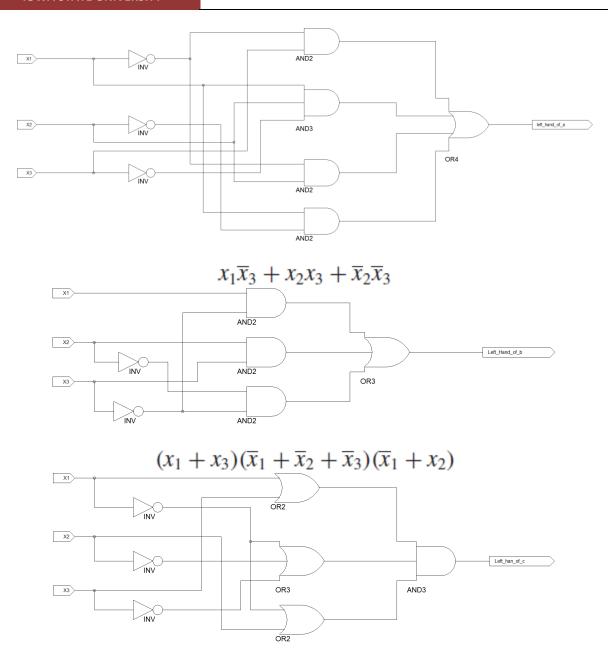
X1	X2	Х3	Left Hand	Right Hand	Valid?
0	0	0	0*1*1=0	0*0*1=0	Υ
0	0	1	1*1*1=1	0*1*1=0	N
0	1	0	0*1*1=0	1*1*1=1	N
0	1	1	1*1*1=1	1*1*1=1	Υ
1	0	0	1*1*0=0	1*0*1=0	Υ
1	0	1	1*1*0=0	1*1*0=0	Υ
1	1	0	1*1*1=1	1*1*1=1	Υ
1	1	1	1*0*1=0	1*1*0=0	Υ

P4. Please see the three figures below:

$$\overline{x}_1x_3 + x_1x_2\overline{x}_3 + \overline{x}_1x_2 + x_1\overline{x}_2$$

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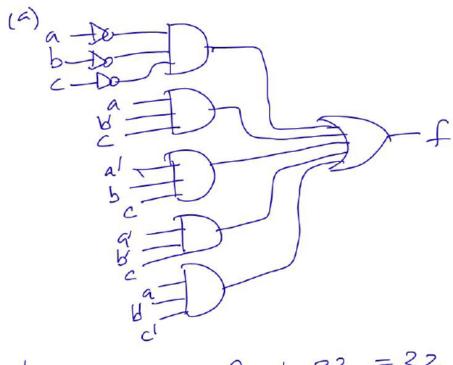
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P5. (a) The diagram is shown below

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(c)
$$f = \frac{ab'c' + ab'c}{+ ab'c'} + \frac{ab'c'}{+ ab'c'} + \frac{ab'c'}{+ ab'c'} + \frac{ab'c'}{+ a'bc} + \frac{ab'c'}{+ a$$

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P6. a) The Truth table:

Х	у	Z	w	f
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

- b) SOP: f= x'.y'.z'.w + x'.y'.z.w' + x'.y.z'.w' + x.y'.z'.w' + x'.y.z.w + x.y'.z.w + x.y.z'.w + x.y.z.w'
- c) SOP in shorthand: $f=\sum m(1,2,4,7,8,11,13,14)$
- d) SOP: $f' = \sum m(0,3,5,6,9,10,12,15)$
- e) POS: f = (x+y+z+w'). (x+y+z'+w). (x+y'+z+w). (x'+y+z+w). (x+y'+z'+w'). (x'+y+z'+w'). (x'+y+z+w'). (x'+y'+z+w'). (x'+y'+z'+w').
- f) $f = \Pi M(0,3,5,6,9,10,12,15)$
- g) $f' = \Pi M(1,2,4,7,8,11,13,14)$
- P7. Starting with the canonical product-of-sums for f can derive:

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$$f = (x_{1} + x_{2} + x_{3})(x_{1} + x_{2} + \overline{x}_{3})(x_{1} + \overline{x}_{2} + x_{3})(x_{1} + \overline{x}_{2} + \overline{x}_{3}) \cdot (\overline{x}_{1} + x_{2} + x_{3})(\overline{x}_{1} + x_{2} + x_{3})(\overline{x}_{1} + x_{2} + x_{3})$$

$$= ((x_{1} + x_{2} + x_{3})(x_{1} + x_{2} + \overline{x}_{3}))((x_{1} + \overline{x}_{2} + x_{3})(x_{1} + \overline{x}_{2} + \overline{x}_{3})) \cdot ((\overline{x}_{1} + x_{2} + x_{3})(\overline{x}_{1} + x_{2} + x_{3}))$$

$$= (x_{1} + x_{2} + x_{3}\overline{x}_{3})(x_{1} + \overline{x}_{2} + x_{3}\overline{x}_{3}) \cdot (\overline{x}_{1} + x_{2} + x_{3}\overline{x}_{3}) \cdot (\overline{x}_{1} + x_{2} + x_{3}\overline{x}_{3})(\overline{x}_{1} + \overline{x}_{2}x_{2} + x_{3})$$

$$= (x_{1} + x_{2})(x_{1} + \overline{x}_{2})(\overline{x}_{1} + x_{2})(\overline{x}_{1} + x_{3})$$

$$= (x_{1} + x_{2}\overline{x}_{2})(\overline{x}_{1} + x_{2}x_{3})$$

$$= x_{1}(\overline{x}_{1} + x_{2}x_{3})$$

$$= x_{1}(\overline{x}_{1} + x_{2}x_{3})$$

$$= x_{1}x_{2}x_{3}$$

P8. Derivation of the minimum sum-of-products expression:

$$f = x_1 \overline{x}_2 \overline{x}_3 + x_1 x_2 x_4 + x_1 \overline{x}_2 x_3 \overline{x}_4$$

$$= x_1 \overline{x}_2 \overline{x}_3 (\overline{x}_4 + x_4) + x_1 x_2 x_4 + x_1 \overline{x}_2 x_3 \overline{x}_4$$

$$= x_1 \overline{x}_2 \overline{x}_3 \overline{x}_4 + x_1 \overline{x}_2 \overline{x}_3 x_4 + x_1 x_2 x_4 + x_1 \overline{x}_2 x_3 \overline{x}_4$$

$$= x_1 \overline{x}_2 \overline{x}_3 + x_1 \overline{x}_2 (\overline{x}_3 + x_3) \overline{x}_4 + x_1 x_2 x_4$$

$$= x_1 \overline{x}_2 \overline{x}_3 + x_1 \overline{x}_2 \overline{x}_4 + x_1 x_2 x_4$$