

Homework 5 chapter 7

chapter - 7 Homework - 5 [8, 9, 55, 56]

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- Q8] The first book is already in position, so no work is required. Second book should be moved upward by distance, force to its weight. The force & displacement are in same direction. 3rd book need to move at 2d by same force and this is applied to all the seven books

$$W = mgd + 2mgd + 3mgd + 4mgd + 5mgd + 6mgd + 7mgd \\ = 28mgd = 28(1.8 \text{ kg})(9.8 \text{ m/s}^2)(0.040 \text{ m}) = \boxed{2.0 \times 10^1 \text{ J}}$$

- Q9] box acceleration is constant so,

$$d = x - x_0 = v_0 t + \frac{1}{2} a t^2 \\ = 0 + \frac{1}{2} (2.0 \text{ m/s}^2) (7.0 \text{ s})^2 \\ = 49 \text{ m}$$

So work done to move crate is found using

$$W = Fd \cos 0^\circ = mad = (6.0 \text{ kg})(2.0 \text{ m/s}^2)(49 \text{ m}) \\ = \boxed{580 \text{ J}}$$

- Q55] ball on the glove's force and glove on the ball's force are opposite so using Newton's third law.

$$\text{Work on the ball} = (K_2 - K_1)_{\text{ball}}$$

$$= \frac{1}{2} m v_2^2 - \frac{1}{2} m v_1^2$$

$$= 0 - \frac{1}{2} (0.145 \text{ kg})(32 \text{ m/s}^2) = \boxed{-74.24 \text{ J}}$$

and therefore $\text{for } W_{\text{on glove}} = 74.24 \text{ J}$

But $W_{\text{on glove}} = F_{\text{on glove}} d \cos 0^\circ$, because the force on the glove is in the same direction.

$$74.24 \text{ J} = F_{\text{on glove}} (0.25 \text{ m}) \rightarrow F_{\text{on glove}} = \frac{74.24 \text{ J}}{0.25} \\ = \boxed{3.0 \times 10^2 \text{ N}} \text{ direction of original velocity of the ball.}$$

[Q56] The force exerted by the bow on the arrow is in the same direction as the arrow.

$W = Fd \cos 0^\circ = Fd = (105 \text{ N})(0.75 \text{ m}) = 78.75 \text{ J}$. But that work changes the kinetic energy of the arrow

$$Fd = W = K_2 - K_1 = \frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2 \Rightarrow v_2 = \sqrt{\frac{2Fd}{m} + v_1^2} \\ = \sqrt{\frac{2(78.75 \text{ J})}{0.085 \text{ kg}} + 0} = \boxed{43 \text{ m/s}}$$

Homework 5 Chapter 8

chapter-8 Homework-5 [3, 8, 15, 20, 29, 32, 70, 73]

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Q3] Spring is going to stretch. Force by the spring is equal to the weight of the mass.

$$mg = k(\Delta x) \rightarrow \Delta x = \frac{mg}{k} = \frac{(2.5 \text{ kg})(9.80 \text{ m/s}^2)}{63 \text{ N/m}} = \boxed{0.39 \text{ m}}$$

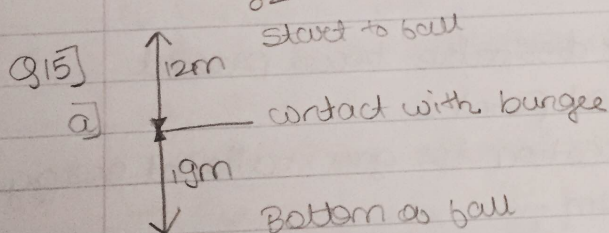
Thus the rulers reading will be $39 \text{ cm} + 15 \text{ cm} = \boxed{54 \text{ cm}}$

Q8] Force, $f_x = \frac{-\partial U}{\partial x} = -(6x + 2yz)$

$$f_y = \frac{\partial U}{\partial y} = -(2x + 8yz)$$

$$f_z = \frac{-\partial U}{\partial z} = -4yz^2$$

$$\vec{F} = \hat{i}(-6x - 2yz) + \hat{j}(-2x - 8yz) + \hat{k}(-4yz^2)$$



y = distance from the 0 gravitational potential energy
 x = amount of bungee cord "stretch" from its unstretched length

Sub1 = jumper at start

Sub2 = jumper at lowest

($x=0$) we have $v_1=0$, $y_1=31\text{m}$, $x_1=0$, $v_2=0$
 $y_2=0$, and $x_2=19\text{m}$

by conservation of energy

$$E_1 = E_2 \rightarrow \frac{1}{2}mv_1^2 + mgy_1 + \frac{1}{2}kx_1^2 = \frac{1}{2}mv_2^2 + mgy_2 + \frac{1}{2}kx_2^2 \rightarrow mgy_1 = \frac{1}{2}kx_2^2 \rightarrow$$

$$k = \frac{2mgy_1}{x_2^2} = \frac{2(55\text{kg})(9.80\text{m/s}^2)(31\text{m})}{(19\text{m})^2}$$

$$= 93\text{N/m}$$

b] Newton's second law for the force on the jumper

$$F_{\text{net}} = F_{\text{rod}} - mg$$

$$= kx_2 - mg = ma \rightarrow a = \frac{kx_2}{m} - g$$

$$= \frac{(92.57\text{N/m})(19\text{m})}{(55\text{kg})} - 9.80\text{m/s}^2$$

$$= 22.2\text{m/s}^2$$

Q20] As there are no dissipative forces present

Sub 1 = coaster at point 1

height at 0 = location for gravitational energy

$v_1=0$ and $y_1=32\text{m}$

$$\text{Point 2} = \frac{1}{2}mv_1^2 + mgy_1 = \frac{1}{2}mv_2^2 + mgy_2$$

$$y_2=0 \rightarrow mgy_1 = \frac{1}{2}mv_2^2 \rightarrow v_2 = \sqrt{2gy_1}$$

$$= \sqrt{2(9.80\text{m/s}^2)(32\text{m})} = 25\text{m/s}$$

$$\text{Point 3} = \frac{1}{2}mv_1^2 + mgy_1 = \frac{1}{2}mv_3^2 + mgy_3$$

$$y_3=26\text{m} \rightarrow mgy_1 = \frac{1}{2}mv_3^2 + mgy_3 \rightarrow$$

$$v_3 = \sqrt{2g(y_1 - y_3)} = \sqrt{2(9.80\text{m/s}^2)(6\text{m})} = 11\text{m/s}$$

$$\text{Point 4} \rightarrow \frac{1}{2}mv_1^2 + mgy_1 = \frac{1}{2}mv_4^2 + mgy_4$$

$$y_4 = 14\text{m} \rightarrow mgy_1 = \frac{1}{2}mv_4^2 + mgy_4 \rightarrow$$

$$v_4 = \sqrt{2g(y_1 - y_4)} = \sqrt{2(9.80\text{m/s}^2)(18\text{m})} = \boxed{19\text{m/s}}$$

29] Kinetic energy is transformed to thermal energy

$$E_{\text{initial}} = E_{\text{final}} \rightarrow \frac{1}{2}mV^2 = E_{\text{thermal}}$$

$$= \frac{1}{2}(2)(56,000\text{kg}) \left[(95\text{km/h}) \left(\frac{(1\text{m/s})}{(3.6\text{km/h})} \right) \right]^2 = \boxed{3.9 \times 10^7\text{J}}$$

32] a] Sub 1 = ball as it is dropped

Sub 2 = ball reaches the ground

$$v_1 = 0, y_1 = 14.0\text{m}, y_2 = 0 \text{ solve for } v_2$$

$$E_1 = E_2 \rightarrow \frac{1}{2}mv_1^2 + mgy_1 = \frac{1}{2}mv_2^2 + mgy_2$$

$$mgy_1 = \frac{1}{2}mv_2^2 \rightarrow v_2 = \sqrt{2gy_1} = \sqrt{2(9.80\text{m/s}^2)(14.0\text{m})}$$

$$= \boxed{16.6\text{m/s}}$$

b] energy = $F_{\text{fr}}d$

d which is the frictional force that will be 14.0m

$$v_2 = 8.00\text{m/s}$$

$$\frac{1}{2}mv_1^2 + mgy_1 = \frac{1}{2}mv_2^2 + mgy_2 + F_{\text{fr}}d \rightarrow mgy_1 = \frac{1}{2}mv_2^2 + F_{\text{fr}}d$$

$$\rightarrow F_{\text{fr}} = m \left(g \frac{y_1}{d} - \frac{v_2^2}{2d} \right) = (0.145\text{kg}) \left(\frac{9.80\text{m/s}^2 - \frac{(8.00\text{m/s})^2}{2(14.0\text{m})}}{2(14.0\text{m})} \right)$$

$$= \boxed{1.09\text{N, upwards}}$$

70] The power is the work done per unit time.

$$P = \frac{W}{t} = \frac{mgh}{t} = \frac{(21.0 \text{ kg})(9.80 \text{ m/s}^2)(3.50 \text{ m})}{60 \text{ sec}}$$

$$= 12.0 \text{ W}$$

73] net rate of work done is the power, $P = Fv = m a v$

$$\text{velocity, } v = \frac{dx}{dt} = 15.0 t^2 - 16.0 t - 44$$

$$a = \frac{dv}{dt} = 30.0 t - 16.0$$

$$a) P = m a v = (0.28 \text{ kg})([30.0(2.0) - 16.0] \text{ m/s}^2)$$

$$[15.0(2.0)^2 - 16.0(2.0) - 44] \text{ m/s} = -197.1 \text{ W}$$

$$= -2.0 \times 10^2 \text{ W}$$

$$b) P = m a v = (0.28 \text{ kg})([30.0(4.0) - 16.0] \text{ m/s}^2)$$

$$[15.0(4.0)^2 - 16.0(4.0) - 44] \text{ m/s} = 384 \text{ W}$$

Work done is changed by kinetic energy

$$v(0) = -44 \text{ m/s} \quad v(2.0) = 15.0(2.0)^2 - 16.0(2.0) - 44$$

$$= -16 \text{ m/s} \quad \text{and } v(4.0) = 15.0(4.0)^2 - 16.0(4.0) - 44$$

$$= 13 \text{ m/s}$$

$$c) P_{\text{avg}} = \frac{\Delta K}{\Delta t} = \frac{\frac{1}{2} m (v_f^2 - v_i^2)}{\Delta t} = \frac{\frac{1}{2} (0.28 \text{ kg}) [(-16 \text{ m/s})^2 - (-44 \text{ m/s})^2]}{2.0 \text{ s}}$$

$$= -120 \text{ W}$$

$$d) P_{\text{avg}} = \frac{\Delta K}{\Delta t} = \frac{\frac{1}{2} m (v_f^2 - v_i^2)}{\Delta t} = \frac{\frac{1}{2} (0.28 \text{ kg}) [(13 \text{ m/s})^2 - (-16 \text{ m/s})^2]}{2.0 \text{ s}}$$

$$= 120 \text{ W}$$