

NAME

MATH 227 DIFFERENTIAL EQUATIONS
Part I

Final Exam

6 Problems- 16 2/3 points each

Show all work for full credit!

- 1** An airplane takes off on a runway that is 3 kilometers long. The plane starts off with an initial velocity of 15 meters/sec and moves with constant acceleration for 50 seconds and then lifts off at the end of the runway. How fast was the plane traveling (in meters/sec) on lift off? Model and solve using differential equations. Show all differential equations and all work.

- 2** Solve using the method of undetermined coefficients:

$$y'' - 3y' - y = e^{4x} \cos 2x$$

- 3** Use the Laplace transform and partial fractions (show all steps) to solve the differential equation with initial conditions:

$$y'' + 2y' + 10y = 10$$

$$y(0) = 0, y'(0) = 1$$

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- 4 Use the Frobenius method to solve: $xy'' - 2y' + y = 0$. Find index r and recurrence relation. Compute the first 5 terms $(a_0 - a_4)$ using the recurrence relation for each solution and index r .

$$X'(t) = \begin{bmatrix} -7 & 0 & 0 & 0 \\ 8 & -3 & 4 & 0 \\ 1 & 0 & -5 & 0 \\ 2 & 1 & 4 & -1 \end{bmatrix} X(t)$$

5. Find the eigenvalues and eigenvectors for the above system of equations.

6. Apply the Runge-Kutta method to approximate the solution on the interval $[0,1]$ with step size $h=0.25$ Construct a table showing five-decimal-place values of the approximate solution for $y'=\sinh(x)+1$, $y(0)=1$.