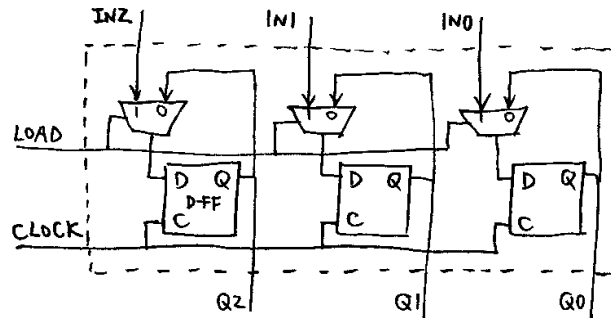


## CPRE 281 – Solutions to Practice Questions for Exam #3

1.



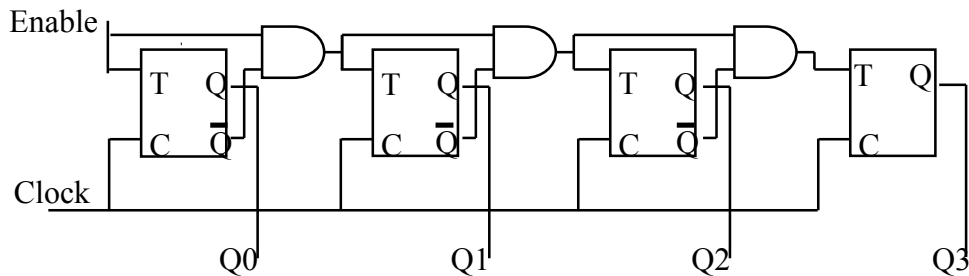
2. Bit  $Q_i$  is toggled when  $Q_{i-1}=0, \dots, Q_0=0$  and  $ENABLE=1$ . Therefore,

$$T_0 = ENABLE$$

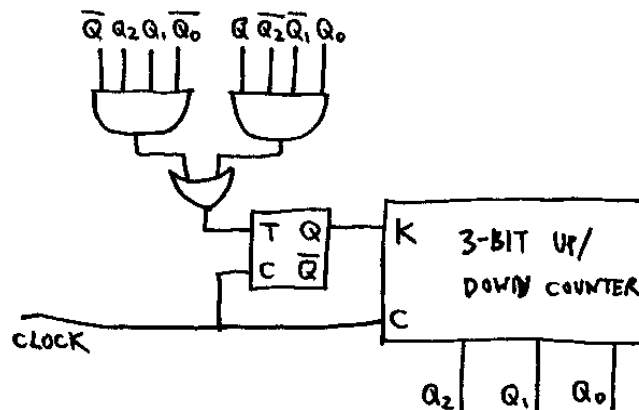
$$T_1 = Q_0' \cdot ENABLE$$

$$T_2 = Q_1' \cdot Q_0' \cdot ENABLE$$

$$T_3 = Q_2' \cdot Q_1' \cdot Q_0' \cdot ENABLE$$

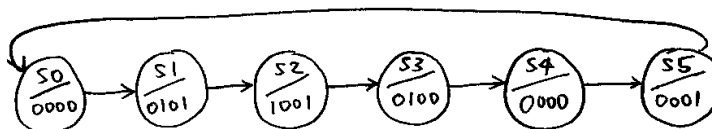


3.



We use the T flip-flop to store the direction of the counting. Notice that we need to change the input of the T flip-flop when  $Q = 0$  and  $Q_2 Q_1 Q_0 = 110$  or  $Q = 1$  and  $Q_2 Q_1 Q_0 = 001$ . In other words,  $T = Q' Q_2 Q_1 Q_0' + Q Q_2' Q_1' Q_0$ . Then the input to K will be toggled and the counting direction will change when  $Q_2 Q_1 Q_0 = 111$  or  $000$ .

4.



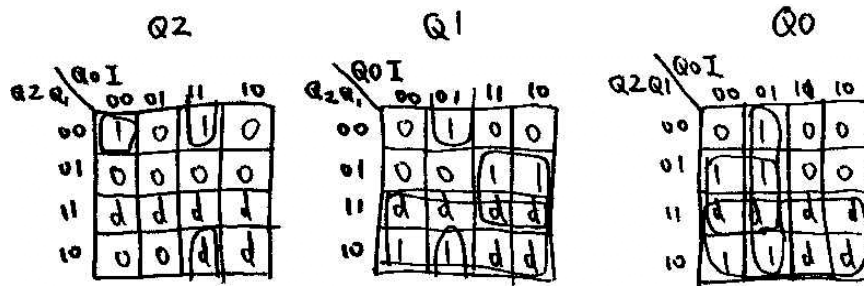
At least 3 bits.

5. (a)

State	State Assignment
S0	000
S1	001
S2	010
S3	011
S4	100

Current State Q2 Q1 Q0	Input X	Next State Q2 Q1 Q0
000	0	100
000	1	011
001	0	000
001	1	100
010	0	001
010	1	001
011	0	010
011	1	010
100	0	011
100	1	011
101	0	ddd
101	1	ddd
110	0	ddd
110	1	ddd
111	0	ddd
111	1	ddd

(b)



$$\text{Next } Q2 = Q2' Q1' Q0' X' + Q1' Q0 X$$

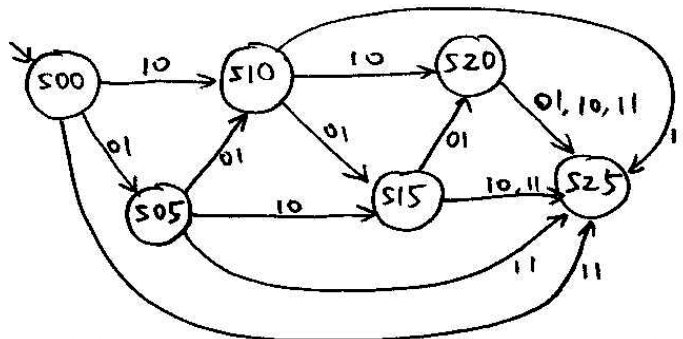
$$\text{Next } Q1 = Q2 + Q1 Q0 + Q1' Q0' X$$

$$\text{Next } Q0 = Q2 + Q1 Q0' + Q0' X$$

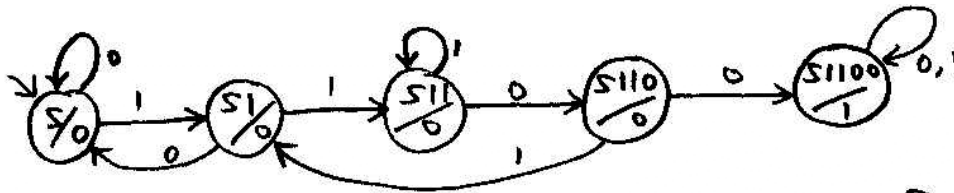
6. S1 (The sequence is S0 S3 S2 S1 S0 S4 S3 S2 S1.)

7. The machine is a Moore machine with the following outputs:

State	Outputs
S00	0000 0000
S05	0000 0101
S10	0001 0000
S15	0001 0101
S20	0010 0000
S25	0010 0101



8.



State table:

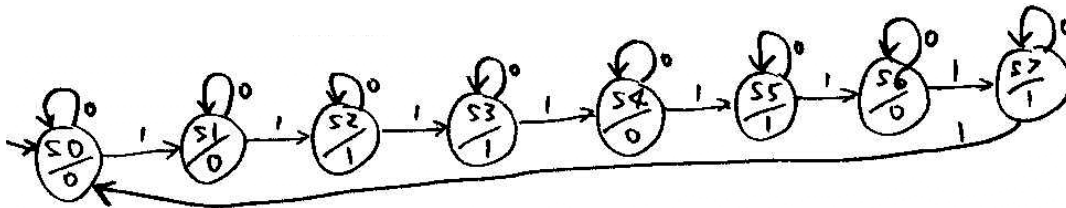
Present state	Next state		Output z
	w=0	w=1	
S	S	S1	0
S1	S	S11	0
S11	S110	S11	0
S110	S1100	S1	0
S1100	S1100	S1100	1

State-assigned table:

Present state y2 y1 y0	Next state			Output z
	w=0 Y2 Y1 Y0	w=1 Y2 Y1 Y0		
000	000	001		0
001	000	010		0
010	011	010		0
011	100	001		0
100	100	100		1
101	ddd	ddd		d
110	ddd	ddd		d
111	ddd	ddd		d

Expressions for Y2, Y1, Y0 and z can be derived. Then the circuit diagram can be drawn. They are skipped here.

9.



10. (a) Step 1:  $B \leftarrow e^x$  //  $A = x, B = e^x$   
 Step 2:  $A \leftarrow A * B$  //  $A = x * e^x, B = e^x$   
 Step 3:  $B \leftarrow A + B$  //  $A = x * e^x, B = x * e^x + e^x$

(b)

Step	ALE	BLE	e0	e1	e2	e3	e4
0	0	1	0	0	1	0	0
1	1	0	0	0	0	0	1
2	0	1	0	0	0	1	0

11.

Step	LD1	LD2	M1	M2	OpCode	enable0	enable1
(1)	1	0	d	d	dd	0	1
(2)	0	1	d	d	dd	0	1
(3)	1	0	0	1	00	1	0
(4)	0	1	0	1	01	1	0
(5)	1	0	0	1	01	1	0

Step	A after step	B after step
(1)	3	????
(2)	3	5
(3)	8	5
(4)	8	3
(5)	5	3

12. (a)

Operation	LD1	LD2	M1	M2	OpCode	enable0	enable1
i)	1	0	d	d	d	0	1
ii)	0	1	d	d	d	0	1
iii)	1	0	0	1	0	1	0
iv)	0	1	0	1	0	1	0
v)	1	0	0	1	0	1	0

(b)

Operation	Register A	Register B
i)	0101	????
ii)	0101	1100
iii)	1001	1100
iv)	1001	0101
v)	1100	0101

(c) This way is better for the following reasons:

- 1) There is no overflow problem if XOR is used.
- 2) XOR is faster and less expensive than ADD and SUB.

13. The state table is given below.

Curr. State	CC	W	INDATA	LDA	LDB	OP	FOUND	Next State
S0	xx	0	1110	1	0	d	0	S1
S1	xx	0	0100	0	1	d	0	S2
S2	01	1	dddd	1	0	0	0	S2
S2	00	1	dddd	1	0	0	0	S2
S2	10	d	dddd	0	0	d	1	S2

14. Note that  $1\text{MHz} = 10^6\text{Hz}$ .

(a) Clock period =  $1/(1000 \cdot 10^6\text{Hz}) = 1\text{ nsec}$ .

Clock period  $\geq$  FF set-up time + Next state compute time + FF propagation delay

So Next state compute time  $\leq 1 - 0.15 - 0.25 = 0.6\text{ nsec}$

(b) Clock period =  $1/(1333 \cdot 10^6\text{Hz}) = 0.75\text{ nsec}$ .

Clock period  $\geq$  FF set-up time + Next state compute time + FF propagation delay

So Next state compute time  $\leq 0.75 - 0.15 - 0.25 = 0.35\text{ nsec}$

15. (a)

A1	A0	B1	B0	R1	R0	E
0	0	0	0	d	d	1
0	0	0	1	0	0	0
0	0	1	0	0	0	0
0	0	1	1	0	0	0
0	1	0	0	d	d	1
0	1	0	1	0	1	0
0	1	1	0	0	0	0
0	1	1	1	0	0	0
1	0	0	0	d	d	1
1	0	0	1	1	0	0
1	0	1	0	0	1	0
1	0	1	1	0	0	0
1	1	0	0	d	d	1
1	1	0	1	1	1	0
1	1	1	0	0	1	0
1	1	1	1	0	1	0

(b)

*Handwritten Karnaugh map for R1:*

	B1 \ B0	00	01	11	10
A1 \ A0	00	d	0	0	0
	01	d	0	0	0
	11	d	1	0	0
	10	d	1	0	0

*Handwritten label:* R1

*Handwritten Karnaugh map for R0:*

	B1 \ B0	00	01	11	10
A1 \ A0	00	d	0	0	0
	01	d	1	0	0
	11	d	1	1	1
	10	d	0	0	1

*Handwritten label:* R0

*Handwritten Karnaugh map for E:*

	B1 \ B0	00	01	11	10
A1 \ A0	00	1	0	0	0
	01	1	0	0	0
	11	1	0	0	0
	10	1	0	0	0

*Handwritten label:* E

$$R1 = A1 B1'$$

$$R0 = A1 A0 + A1 B0' + A0 B1'$$

$$E = B1' B0'$$

(c)

