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A. Matematika diskrit

1) $f(x) = x^2 - 4$, $g(x) = x + 3$ (A) tentukan $(f \circ g)(x)$, $(g \circ f)(1)$ maka

$$\begin{aligned} = f \circ g(x) &= f(g(x)) = f(x+3) \\ &= (x+3)^2 - 4 \\ &= (x^2 + 6x + 9) - 4 \\ &= x^2 + 6x + 5 \end{aligned}$$

$$\begin{aligned} = g \circ f(1) &= g(f(1)) = g(1^2 - 4) \\ &= g(-3) \\ &= -3 + 3 = 0 \end{aligned}$$

2) $f(x) = x^2 - x - 6$, $g(x) = x^2 + 2$

$$\begin{aligned} = f \circ g(x) &= f(g(x)) = f(x^2 + 2) \\ &= (x^2 + 2)^2 - (x^2 + 2) - 6 \\ &= x^4 + 4x^2 + 4 - x^2 - 2 - 6 \\ &= x^4 + 3x^2 - 4 \end{aligned}$$

$$\begin{aligned} = g \circ f(1) &= g(f(1)) = g(1^2 - 1 - 6) \\ &= g(-6) \\ &= (-6)^2 + 2 \\ &= 36 + 2 = 38 \end{aligned}$$

3) $f(x) = \frac{x-1}{3x+5}$, $g(x) = 2x-6$ | $= g \circ f(1) = g\left(\frac{1-1}{3 \cdot 1 + 5}\right) - 6$

$$\begin{aligned} = f \circ g(x) &= f(2x-6) = \frac{(2x-6)-1}{3(2x-6)+5} = 2\left(\frac{\frac{1-1}{3(1)+5}}{1}\right) - 6 \\ &= \frac{2x-7}{6x-18+5} = \frac{2x-7}{6x-13} = 2\left(\frac{0}{8}\right) - 6 \\ &= 2 \cdot 0 - 6 = -6 \end{aligned}$$

$$4) f(x) = \frac{x-6}{2x+2}, g(x) = \frac{5}{1-2x}$$

$$= f \circ g(x) = f\left(\frac{5}{1-2x}\right) \quad = \quad g \circ f(1) = g\left(\frac{x-6}{2x+2}\right)$$

$$= \frac{\frac{5}{1-2x} - 6}{2\left(\frac{5}{1-2x}\right) + 2}$$

$$= g\left(\frac{1-6}{2(1)+2}\right)$$

$$= g\left(-\frac{5}{4}\right)$$

$$= \frac{5 - 6(1-2x)}{1-2x}$$

$$= \frac{-5}{1-2\left(-\frac{5}{4}\right)}$$

$$\frac{10 + 2(1-2x)}{1-2x}$$

$$= \frac{5-6+12x}{10+2-4x} = \frac{-1+12x}{12-4x}$$

$$= \frac{-5}{1+\frac{10}{4}}$$

$$5) f(x) = \sqrt{x+3}, g(x) = x^2+6x+6$$

$$= f \circ g(x) = \sqrt{g(x)+3}$$

$$= \sqrt{x^2+6x+6+3}$$

$$= \sqrt{x^2+6x+9} = \sqrt{(x+3)^2} = x+3$$

$$= g \circ f(1) = g(f(1)) = g(\sqrt{1+3})$$

$$= g(2) = 2^2 + 6(2) + 6$$

$$= 4 + 12 + 6 = 22$$

$$= \frac{5}{\frac{24}{4}} = \frac{5 \cdot 4}{14} = \frac{20}{14} = \frac{10}{7}$$

$$= \frac{10}{7}$$

$$6) f(x) = \sqrt{x+3}, g(x) = \frac{2x+1}{1-x}$$

$$= f \circ g(x) = f\left(\frac{2x+1}{1-x}\right) = \sqrt{\frac{2x+1}{1-x} + 3} = \sqrt{\frac{2x+1+3(1-x)}{1-x}}$$

$$= g \circ f(1) = g(\sqrt{x+3})$$

$$= g(\sqrt{1+3})$$

$$= g(\sqrt{4})$$

$$= g(2)$$

$$= \frac{2(2)+1}{1-2} = \frac{5}{-1} = -5$$

$$= \sqrt{\frac{2x+1+3-3x}{1-x}}$$

$$= \sqrt{\frac{-x+4}{1-x}}$$

B. Tentukan $F(x-2)$ jika:

1). $F(x) = 3x + 7$

$$= F(x-2) = 3(x-2) + 7 = 3x - 6 + 7 = \underline{\underline{3x + 1}}$$

2). $F(x) = x^2 + x - 12$

$$\begin{aligned} = F(x-2) &= (x-2)^2 + (x-2) - 12 \\ &= x^2 - 4x + 4 + x - 2 - 12 \\ &= x^2 - 3x - 10 \\ &\underline{\underline{\hspace{1cm}}}\end{aligned}$$

C. Tentukan $F(x)$ jika

1). $F(x+3) = 6 - 5x$

$$\begin{aligned} = F(u) &= 6 - 5(u-3) \\ &= 6 - 5u + 15 \\ &= -5u + 21 \end{aligned}$$

$$F(x) = -5x + 21$$

2). $F(2x-7) = 4x-3$

$$= F(u) = 4\left(\frac{u+7}{2}\right) - 3$$

$$= 2(u+7) - 3$$

$$= 2u + 14 - 3$$

$$= 2u + 11$$

$$F(x) = 2x + 11$$

3). $F(2-x) = x^2 - 10$

$$\begin{aligned} = F(u) &= (2-u)^2 - 10 \\ &= 4 - 4u + u^2 - 10 \\ &= u^2 - 4u - 6 \end{aligned}$$

$$F(x) = x^2 - 4x - 6$$