

- A strategy profile is an assignment of strategies for each player
- A pure strategy is discrete: either north or south for example
- A mixed Nash equilibrium is the best outcome for both players when they're using mixed strategies (where the strategy is a probability of going north or south rather than a discrete north or south choice).
- A simplex is when each component adds to 1, e.g.  $x + y = 1 \leftarrow 2$  strategy game.
- $\sigma$  is a mixed profile
- $x = f(x)$  is a fixpoint
- Brouwer fixpoint theorem
- Kakutani fixpoint theorem
- Every  $n$ -player game has at least one Nash equilibrium.
- Sperner's Lemma:
  - Pick an arbitrary set of  $n - 1$  colors (let's say red and blue)
  - Count red-blue edges after slicing simplex along cutlines
  - Count exterior edges (call it  $a$ )
  - Count interior edges twice (call it  $b$ )
  - Total count is  $a + 2b$