Data Structures Chapter 5: Heap and Priority Queue

- 1. Heap & Priority Queue
- 2. Heapsort
- 3. Heap & PQ Coding



자기 아들을 아끼지 아니하시고 우리 모든 사람을 위하여 내주신 이가 어찌 그 아들과 함께 모든 것을 우리에게 주시지 아니하겠느냐 (로마서 8:32)

우리가 알거니와 하나님을 사랑하는 자 곧 그의 뜻대로 부르심을 입은 자들에게는 모든 것이 합력하여 선을 이루느니라 (로마서 8:28)

Heap ADT - heap.h

- Heap ADT: A one based and one dimensional array is used to simplify parent and child calculations.
- heap.h

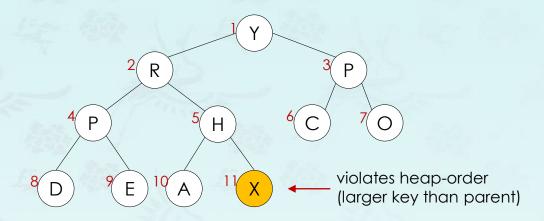
```
struct Heap {
 int *nodes;  // an array of nodes
 int capacity; // array size of node or key, item
 int N;
        // the number of nodes in the heap
 bool (*comp)(Heap*, int, int);
 Heap(int capa = 2) {
   capacity = capa;
   nodes = new int[capacity];
   N = 0;
   comp = nullptr;
 };
 ~Heap() {};
using heap = Heap*;
```

Heap ADT - heap.h

```
void clear(heap hp);
                                  // deallocate heap
int size(heap hp);
                                  // return nodes in heap currently
int level(int n);
                                  // return level based on num of nodes
int capacity(heap hp);
                                  // return its capacity (array size)
int reserve(heap hp, int capa); // reserve the array size (= capacity)
int full(heap hp);
                               // return true/false
int empty(heap hp);
                               // return true/false
void grow(heap hp, int key);
                              // add a new key
void trim(heap hp);
                                  // delete a queue
int heapify(heap hp);
                               // convert a complete BT into a heap
// helper functions to support grow/trim functions
int less(heap hp, int i, int j);  // used in max heap
int more(heap hp, int i, int j);  // used in min heap
void swim(heap hp, int k);  // bubble up
void sink(heap hp, int k);  // tickle down
// helper functions to check heap invariant
int heapOrdered(heap hp);  // is heap[1..N] a heap?
```

- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

This is a maxheap example.



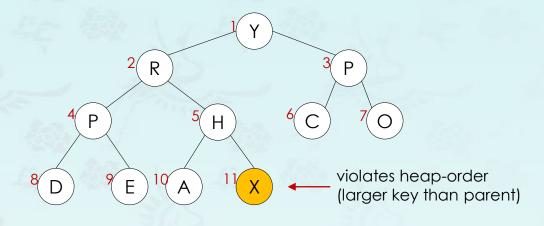
swim up or sink down?

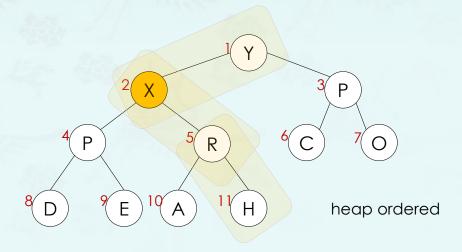
- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

```
bool less (heap h, int p, int c) {
    return h->nodes[p] < h->nodes[c];
}
```

```
void swap (heap h, int p, int c) {
   int item = h->nodes[p];
   h->nodes[p] = h->nodes[c];
   h->nodes[c] = item;
} // Inside this swap(), we may use swap() in c++
```

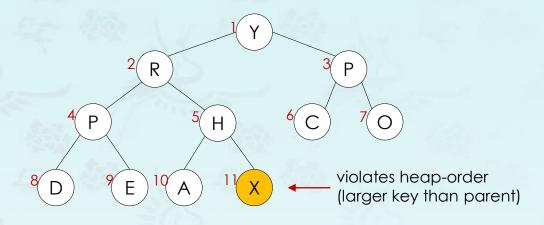
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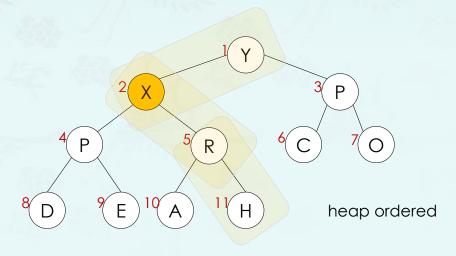




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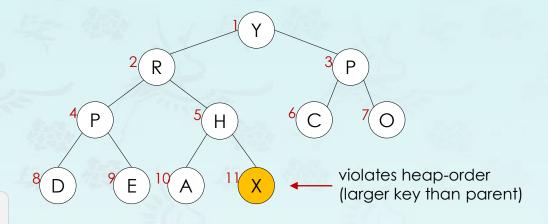


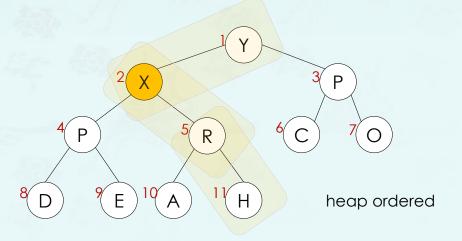


- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

```
not reached at root , parent is less than its child(k)  
    while (k > 1 \&\& less(h, k / 2, k))  
    swap(h, k / 2, k); swap parent(k/2)  
        k = k / 2; and its child(k)  
    }  
    move up one level
```

This is a maxheap example.

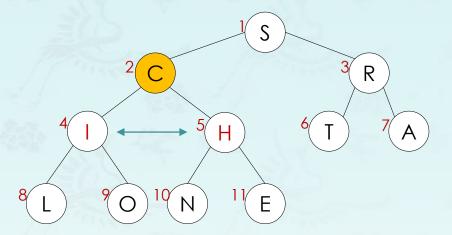




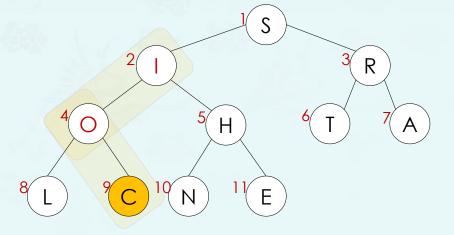
Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child (of two)
 - Repeat until heap order restored.

Top-down reheapify (sink)



swim up or sink down?



Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:

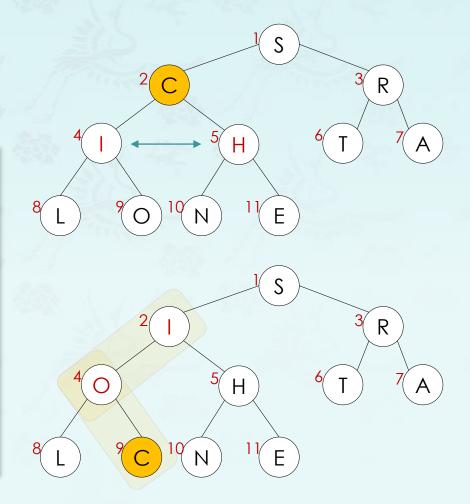
Why not smaller child?

- Swap key in parent with key in larger child (of two)
- Repeat until heap order restored.

```
void sink(heap h, int k)
{
    while (k's child not reached the last)
    {
        find the larger child of k, let it be j. (j = 5)

        if k's key is not less than j's key, break;
        swap k and j since k's key > j's key
        set k to the next node which is j.
    }
}
```

Top-down reheapify (sink)



Demotion in a heap: sink

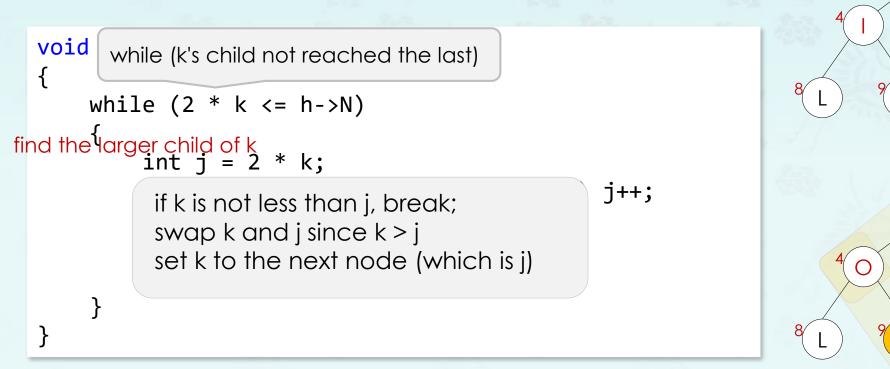
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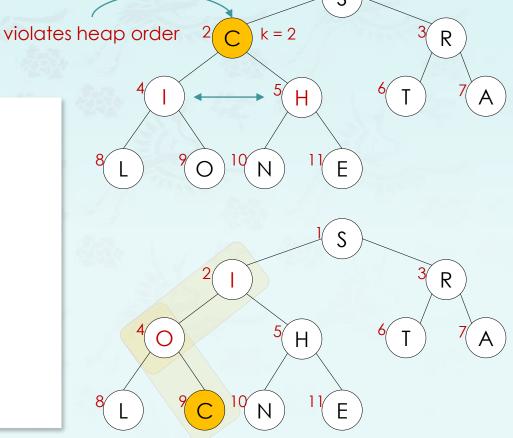
Why not smaller child?

Top-down reheapify (sink)

Swap key in parent with key in larger child (of two)

Repeat until heap order restored.



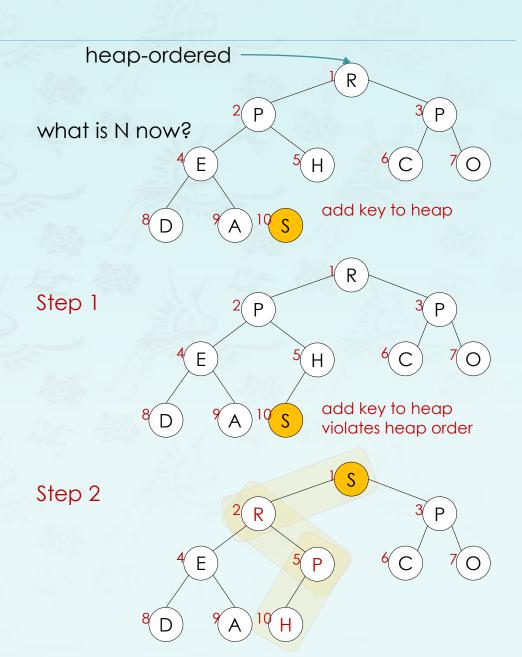


Insert in a heap

- Insert: Add node at end, then swim it up.
 - Cost: At most 1 + log N compares.

```
void insert(heap h, int key)
{
    h->nodes[++h->N] = key;
}
```

```
struct Heap {
  int *nodes;
  int capacity;
  int N;
};
using heap = *Heap;
```



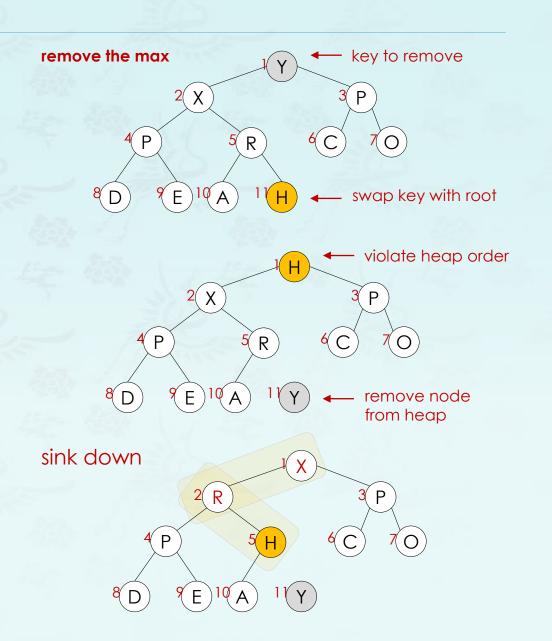
Delete in a heap

Delete the root (max or min) in a heap:

- Delete root: Swap root with node at end, then sink it down.
- Cost: At most 2 log N compares.

```
void delete(heap h)
{
   swap(h, 1, h->N--);
}
```

```
void swim(heap h, int k)
void sink(heap h, int k)
bool less(heap h, int p, int c)
void swap(heap h, int p, int c)
```



Heap ADT

```
void clear(heap hp);
                                      // deallocate heap
int size(heap hp);
                                      // return nodes in heap currently
int level(int n);
                                      // return level based on num of nodes
int capacity(heap hp);
                                      // return its capacity (array size)
int reserve(heap hp, int capa);
                              // reserve the array size (= capacity)
int full(heap hp);
                                      // return true/false
int empty(heap hp);
                                      // return true/false
void grow(heap hp, int key);
                                      // add a new key
void trim(heap hp);
                                      // delete a queue
int heapify(heap hp);
                                      // convert a complete BT into a heap
// helper functions to support grow/trim functions
int less(heap hp, int i, int j);  // used in max heap
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void swim(heap hp, int k);  // bubble up
void sink(heap hp, int k);  // tickle down
// helper functions to check heap invariant
int heapOrdered(heap hp);
                        // is it heap-ordered?
```

Data Structures Chapter 5: Heap and Priority Queue

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```
// return the number of items in heap
int size(heap hp) {
    return hp->N;
// Is this heap empty?
int empty(heap hp) {
    return (hp->N == 0) ? true : false;
// Is this heap full?
int full(heap hp) {
    return (hp->N == hp->capacity - 1) ? true : false;
```

```
int less(heap hp, int i, int j) {
    return hp->nodes[i] < hp->nodes[j];
void swap(heap hp, int i, int j) {
    int t = hp->nodes[i];
    hp->nodes[i] = hp->nodes[j];
    hp->nodes[j] = t;
void swim(heap hp, int k) {
void sink(heap hp, int k) {
```

```
void grow(heap hp, int key) {
   cout << "YOUR CODE HERE\n";
   // add key @ ++heap->N
   // swim up @ heap->N
}
```

```
void trim(heap hp) {
   if (empty(hp)) return;

cout << "YOUR CODE HERE\n";
}</pre>
```

newCBT()	with a given array, instantiate a new complete binary tree its result is neither maxheap nor minheap.
<pre>heapify() heapsort() heapprint()</pre>	<pre>make a complete binary tree into a max/minheap use max/min-heap to sort elements in heap build a binary tree from heap/CBT for display purpose only</pre>

newCBT() - convert an int array to CBT

```
// instantiates a CBT with given data and its size.
heap newCBT(int *a, int n) {
   int capa = ?

   heap p = new Heap{ capa };

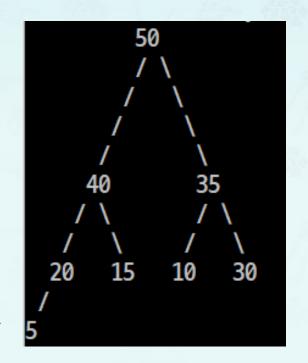
   p->N = n;
   for (int i = 0; i < n; i++)
        p->nodes[i + 1] = a[i];
   return p;
}
```

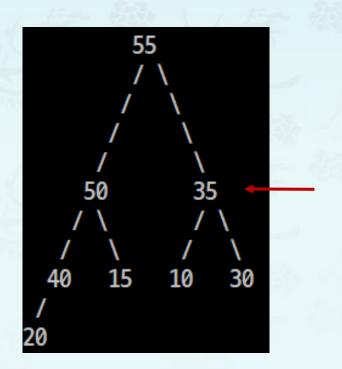
```
struct Heap {
  int *nodes;
  int capacity;
  int N;
  bool (*comp)(Heap*, int, int);
  Heap(int capa = 2) {
    capacity = capa;
    nodes = new int[capacity];
    N = 0;
    comp = nullptr;
  ~Heap() {};
using heap = Heap*;
```

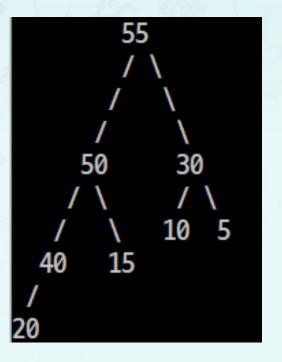
Priority Queue

For example:

- If you **change 5 to 55**, it will go up to the root and 20 is placed at the bottom.
- If you **change 35 to 5**, 30 will go up where 35 is, then 5 goes down to the right corner.







grow() - inserts a new key to the max-heap or min-heap.

grow(heap p, int key)

- 1. if full(p), invoke **reserve()** to double the size of nodes[]. Use p->capacity * 2.
- 2. add the key to nodes[]. The index of nodes[] must be ++p->N.
- 3. swim up to maintain heap invariant.

```
void grow(heap p, int key) {
  if (full(p))
    ...
  p->nodes ...
  swim...
  return;
}
```

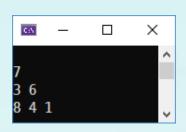
growN()

- 1. Find the max key(max) in heap or CBT.
- 2. Set a function pointer to the function to insert a node.
- 3. Allocate a Key type array such as keys to store random keys.
- 4. Invoke randomN() function to generate keys in the range [(max + 1)..(max + count)]
- 5. Invoke the function to insert keys in keys[], but one key at a time.
- 6. Print the heap if DEBUG is defined whenever a node is inserted.
- 7. Don't forget freeing the array of keys you allocated in Step 3.

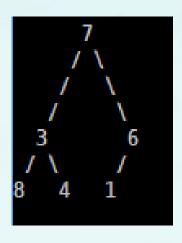
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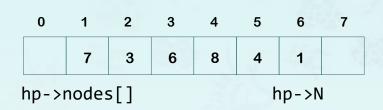
Heapprint(): build a tree from CBT - heapprint.cpp

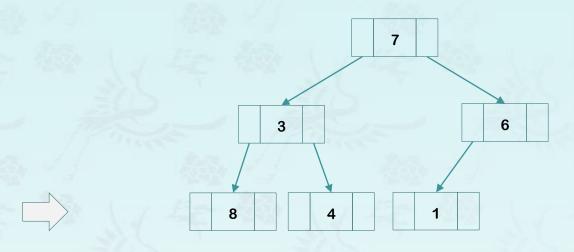




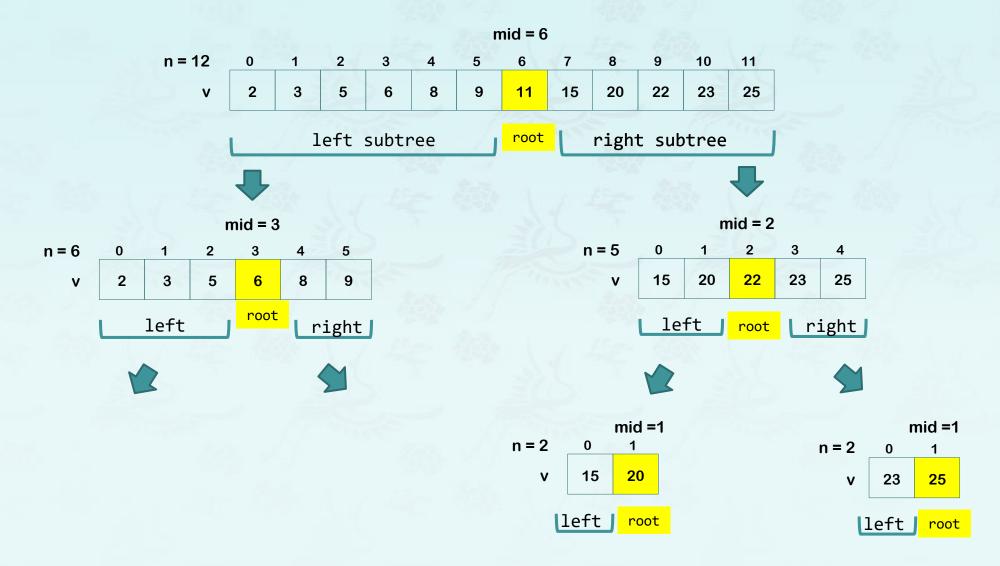


```
// print a heap using treeprint() -
// build a tree to call treeprint()
void heapprint(heap p, int mode) {
  if (empty(p)) return;
  if (size(p) \% 2 == 0) {
    cout << "\t[Tree built using recursion]\n";</pre>
    root = buildBT(p->nodes, 1, size(p)); // using recursion
  else {
    cout << "\t[Tree built using iteration]\n";</pre>
    root = buildBT(p);
                                             // using iteration
  ... treeprint(root);
  clear(root);
```





Building AVL tree from BST in O(n) - Review



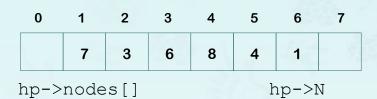
Building AVL tree from BST in O(n) - Review

```
// rebuilds an AVL tree with a list of keys sorted.
// v - an array of keys sorted, n - the array size

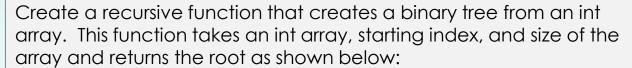
tree buildAVL(int* v, int n) {
  if (n <= 0) return nullptr;

int mid = n / 2;
  ...
  return root;
}</pre>
```

```
tree reconstruct(tree root) {
  if (root == nullptr) return nullptr;
  if (size(root) > 10) { // recycling method
   vector<tree> v; // get nodes sorted
   root = buildAVL(...);
                      // recreation method
  else {
   vector<int> v;  // get keys sorted
   root = buildAVL(...);
  return root;
```

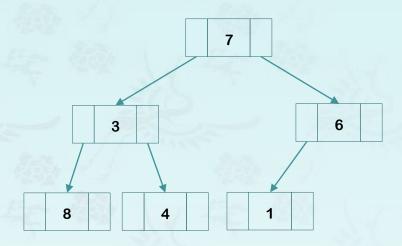


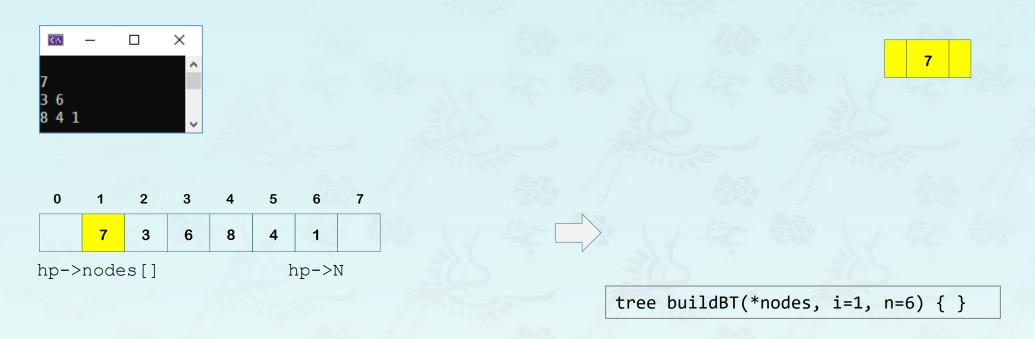




tree buildBT(int *nodes, int i, int n) {

- 1. If i > n, return nulltptr terminate condition
- 2. Create the tree (root) node with nodes[i]).
 - A. Invoke buildBT() for all its left children (or **i** * **2**). Set its return to the left child of the root.
 - B. Invoke buildBT() for all its right children (or **i** * **2** + **1**). Set its return to the right child of the root.
- 3. return root

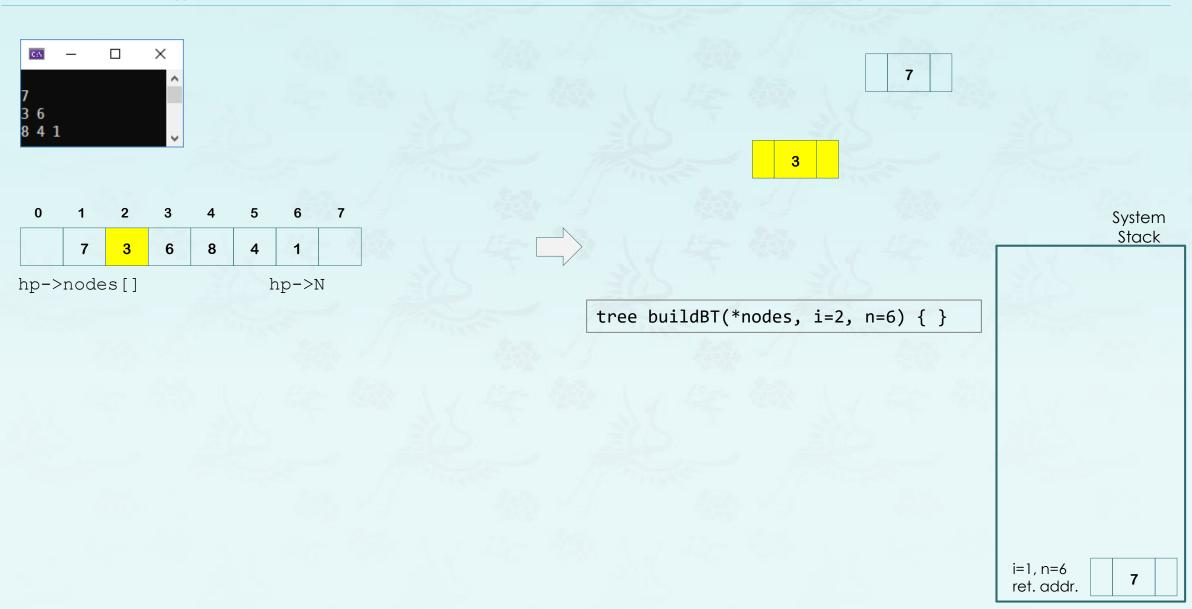


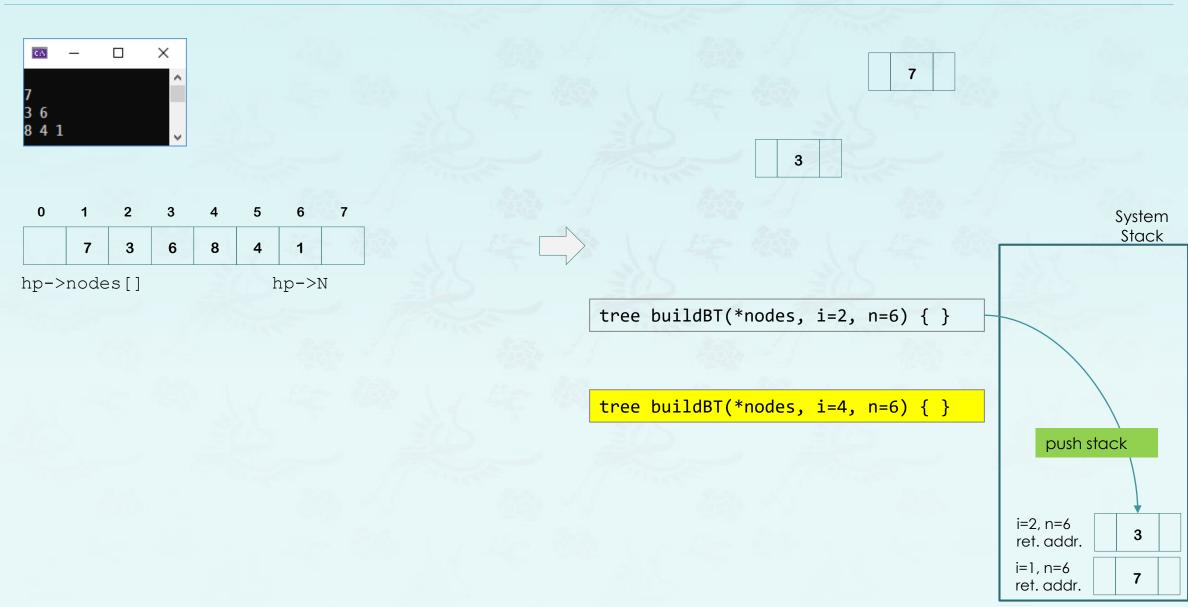


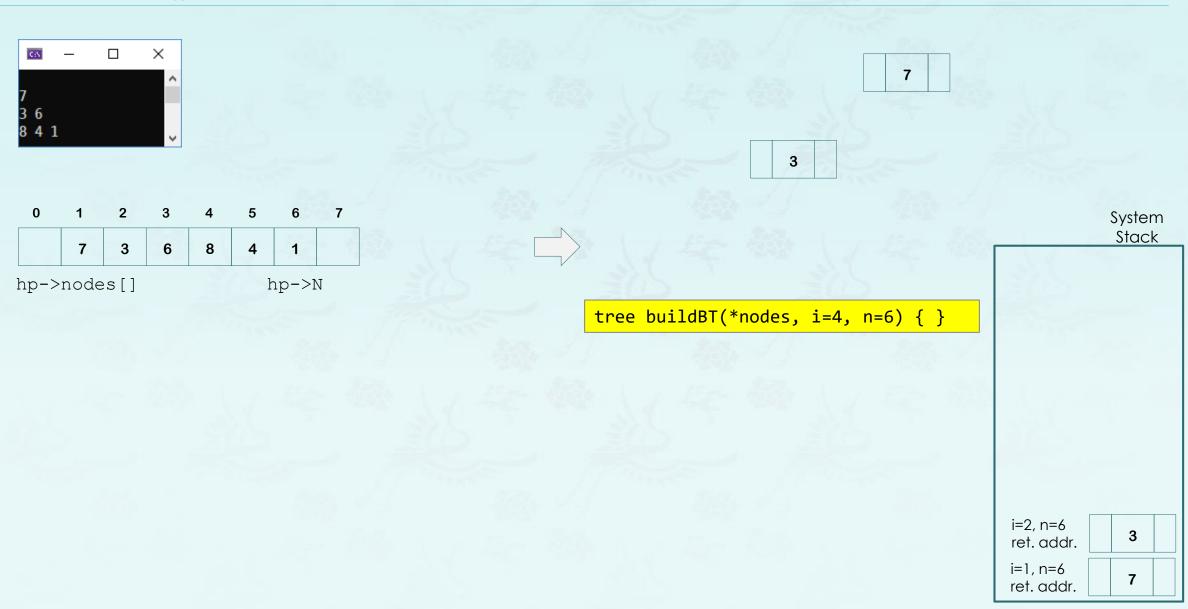


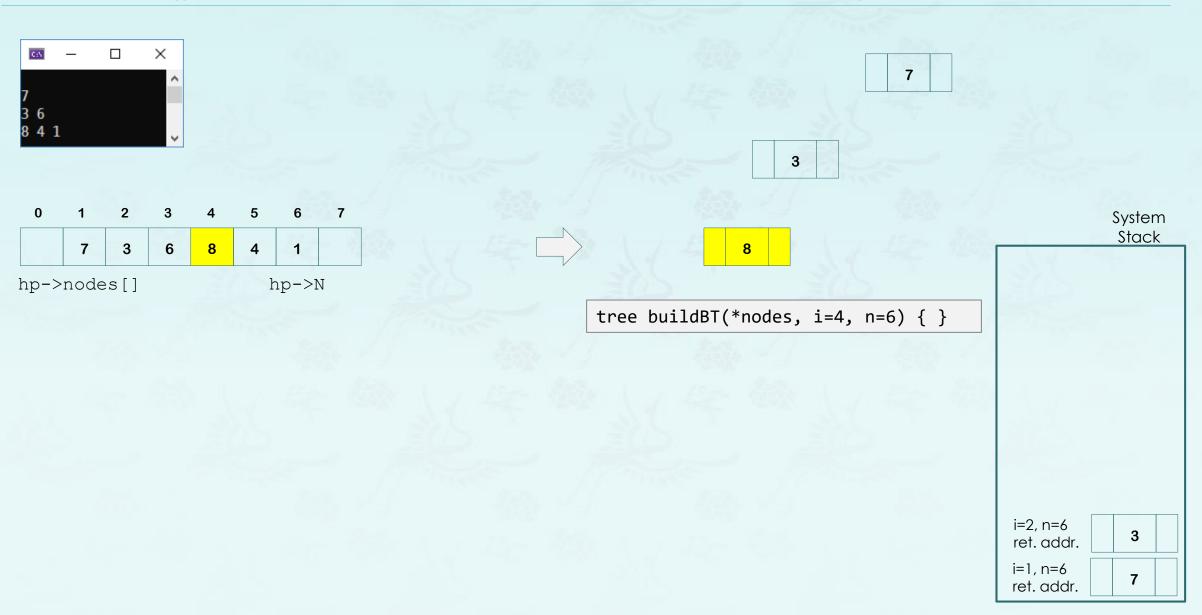
ret. addr.

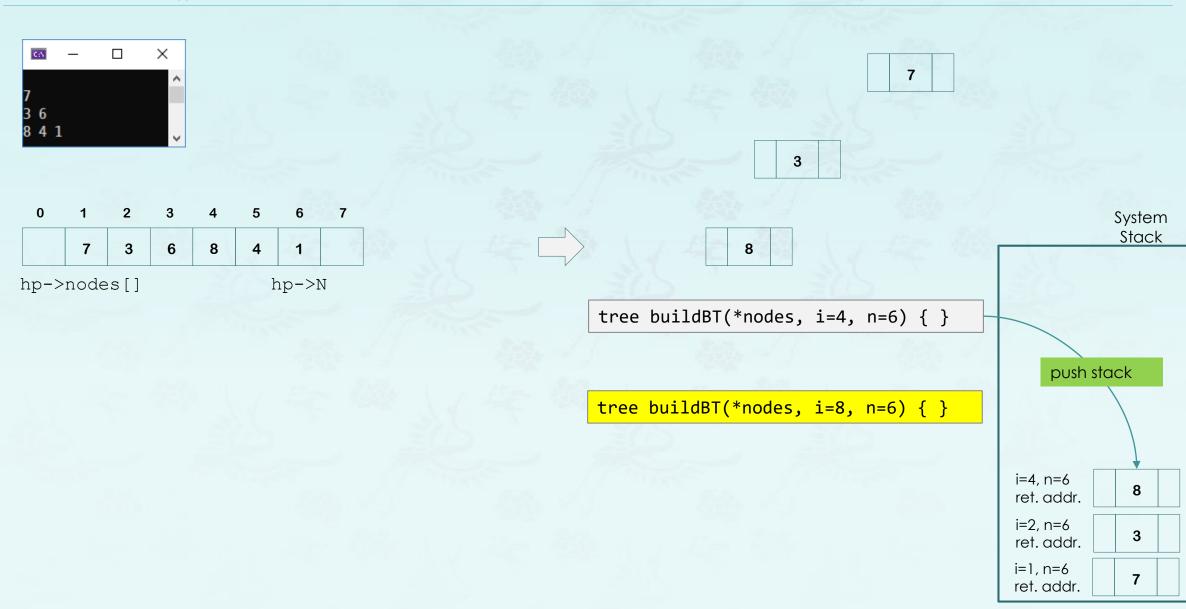


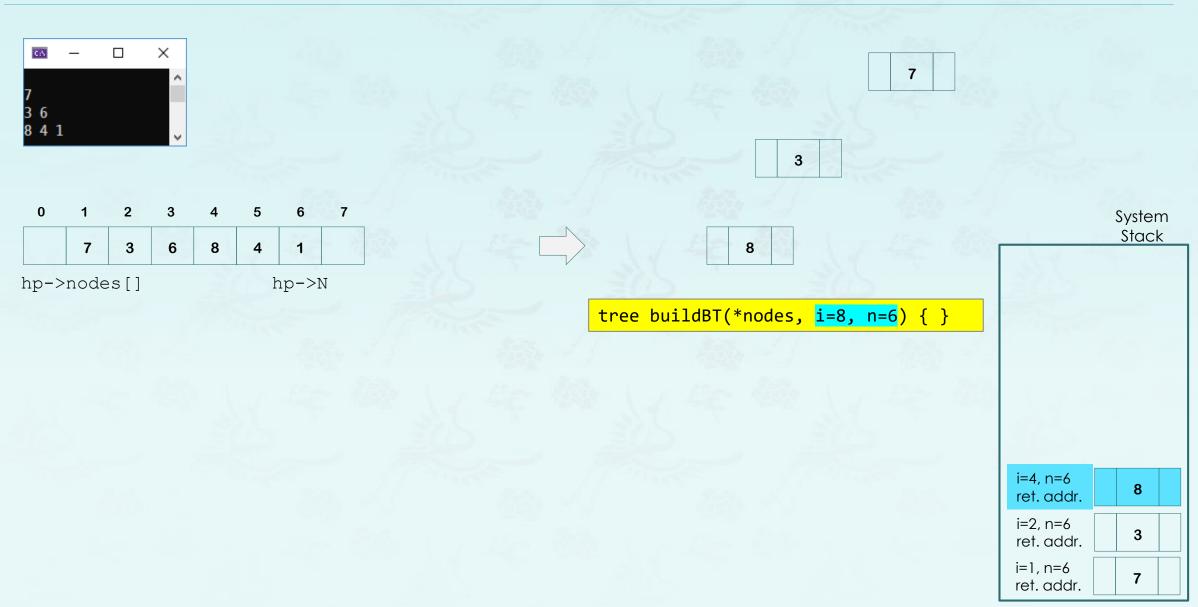


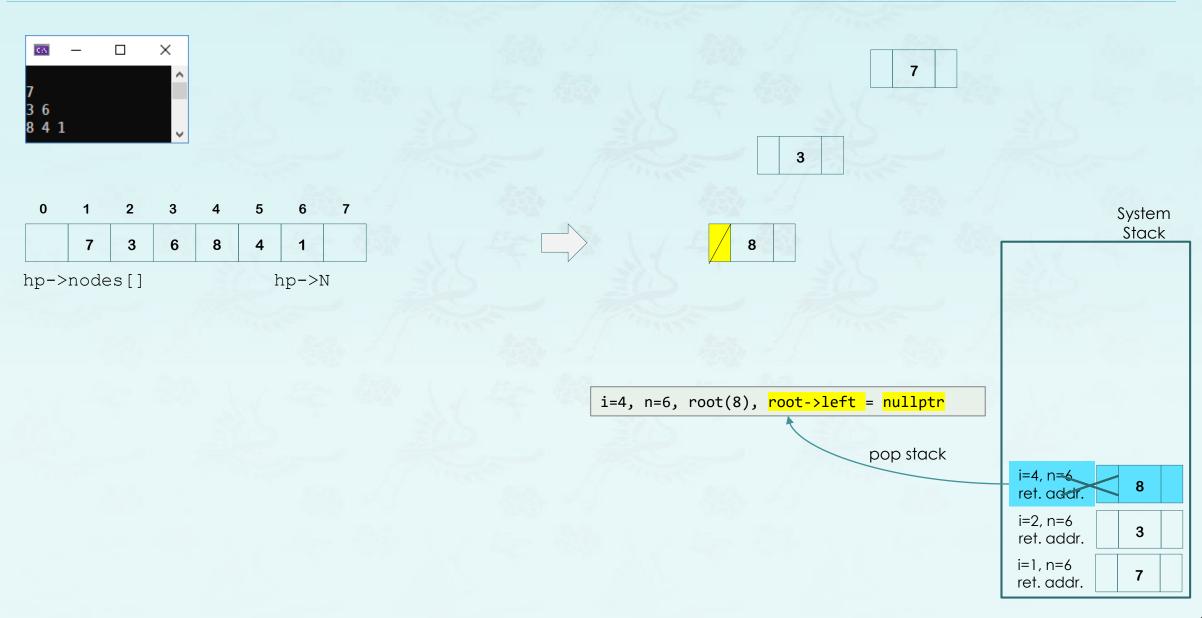


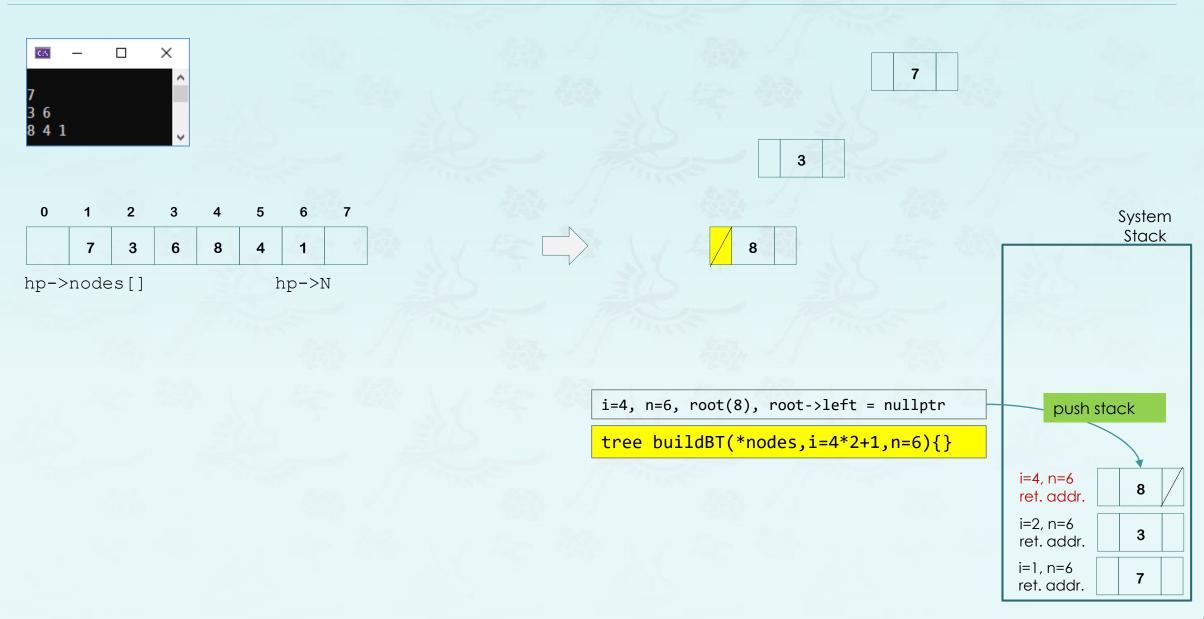


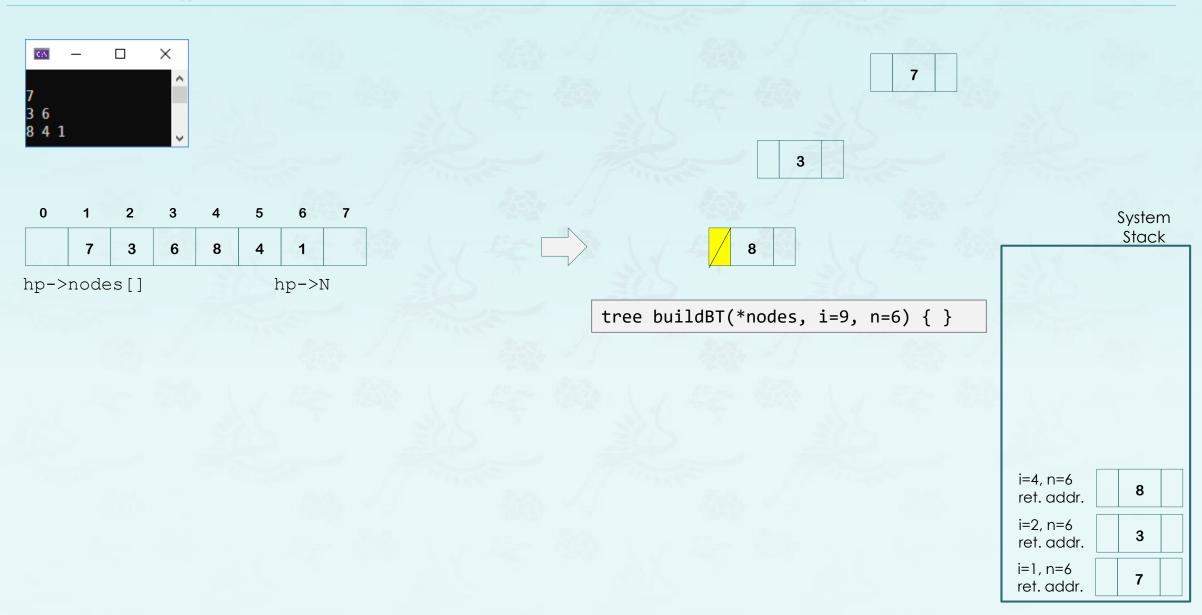


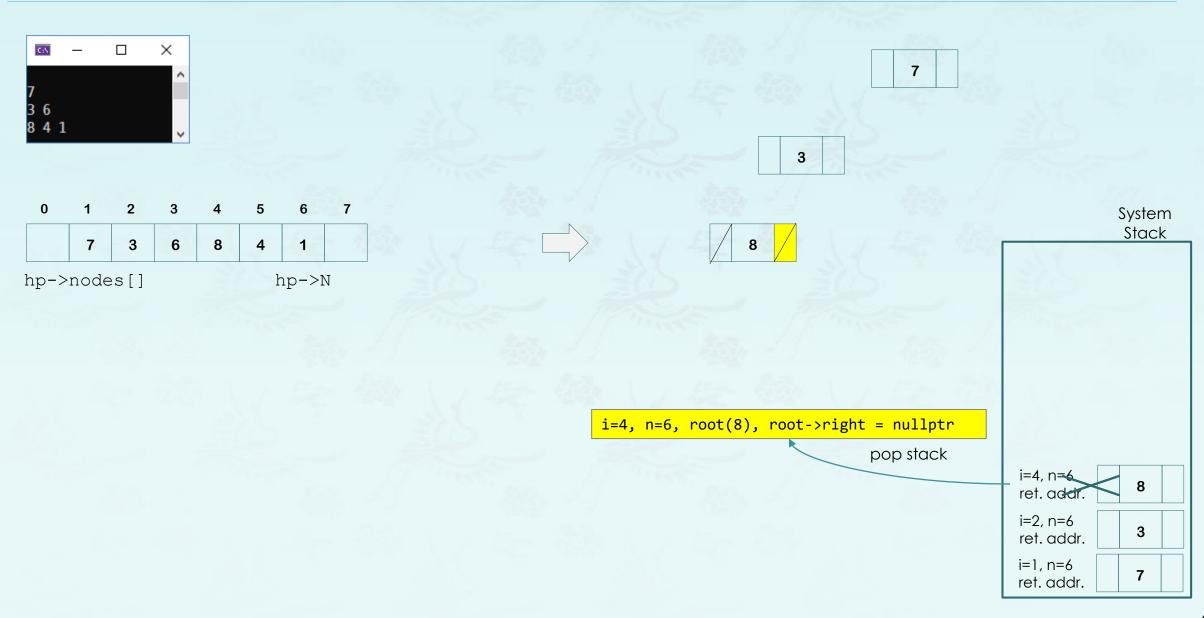


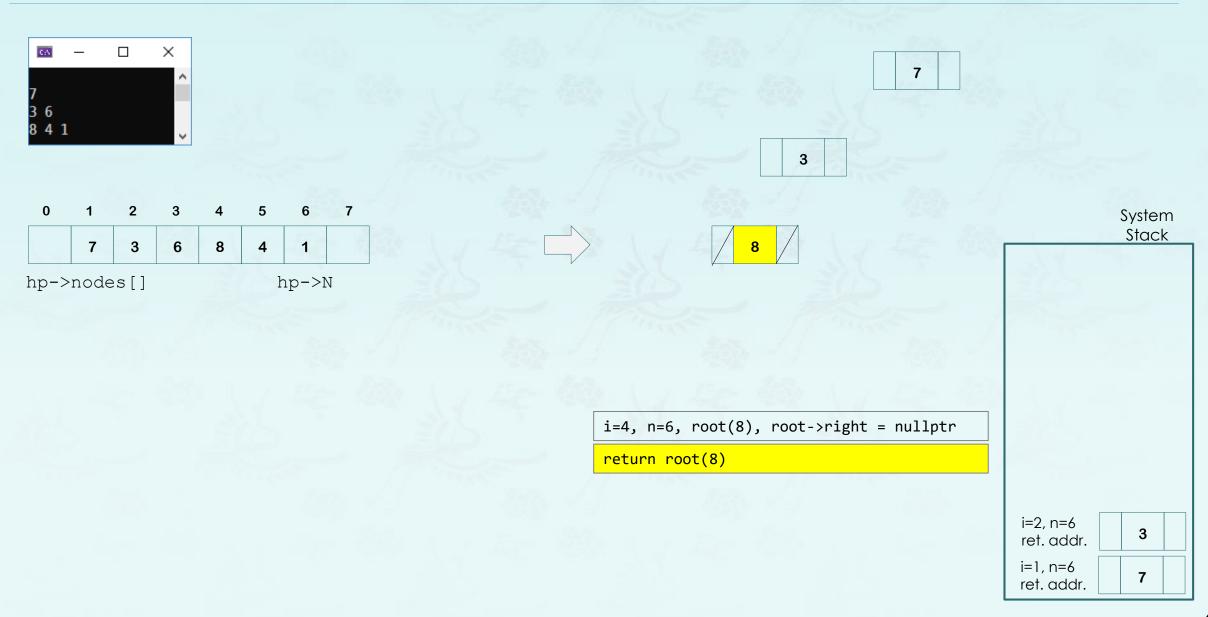


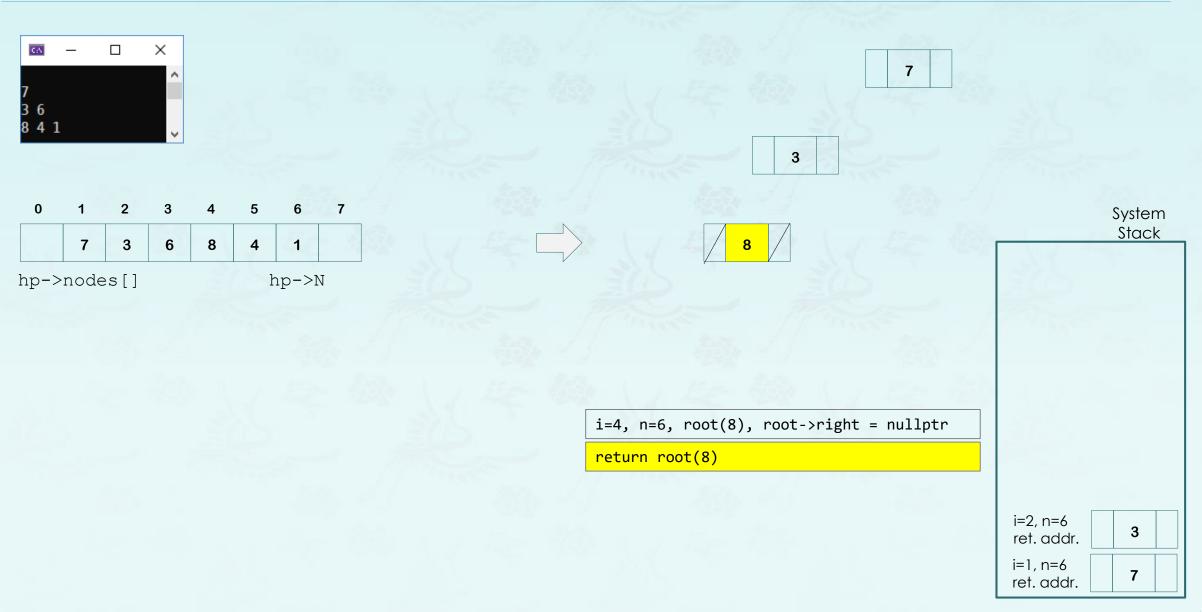


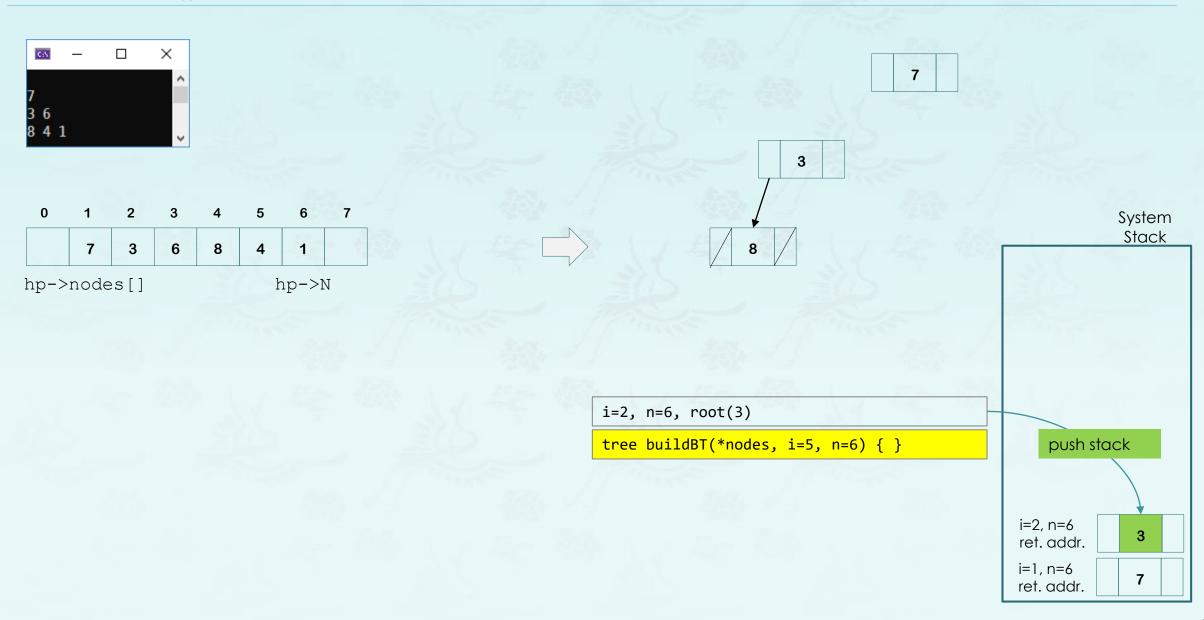


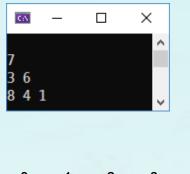


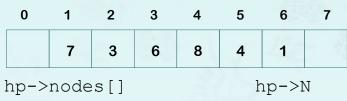


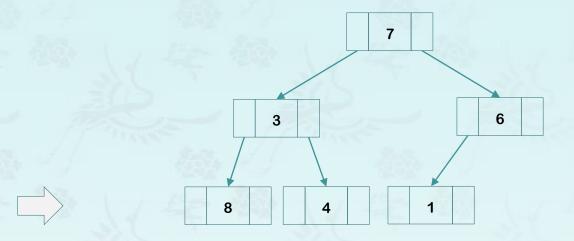




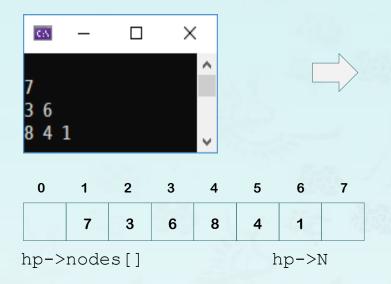


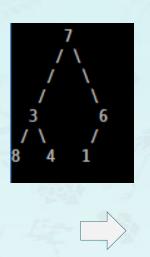


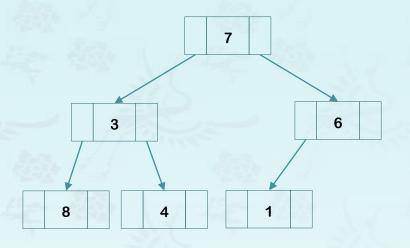


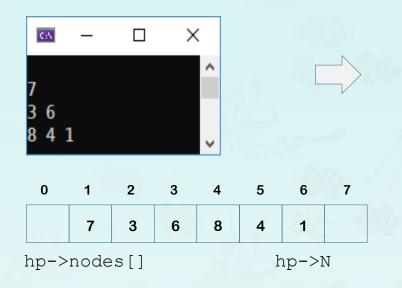


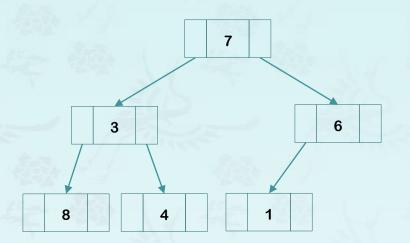




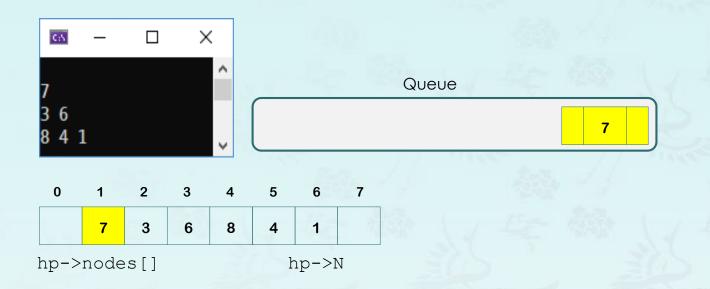




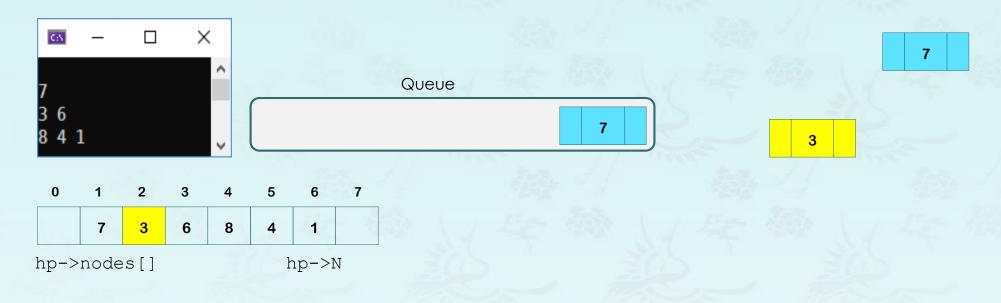




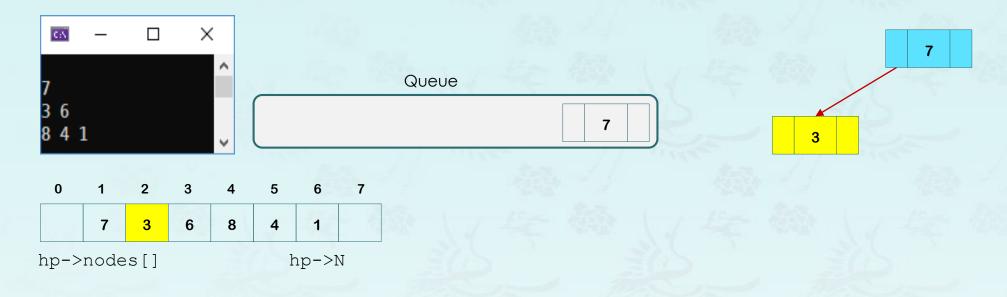
- 1. Create the **tree (root) node** with the first key from CBT (or **nodes[1]**).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeue) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



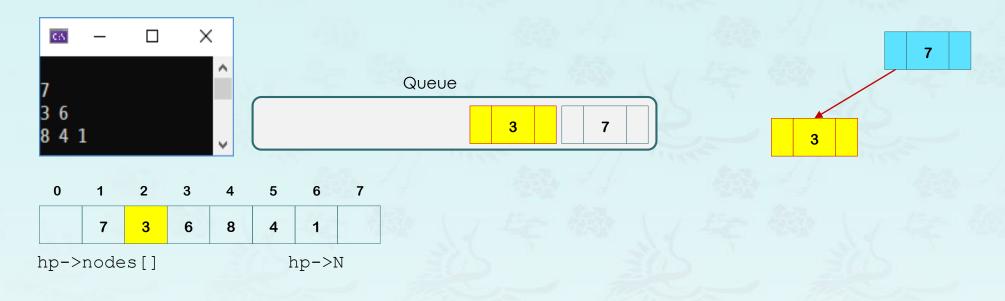
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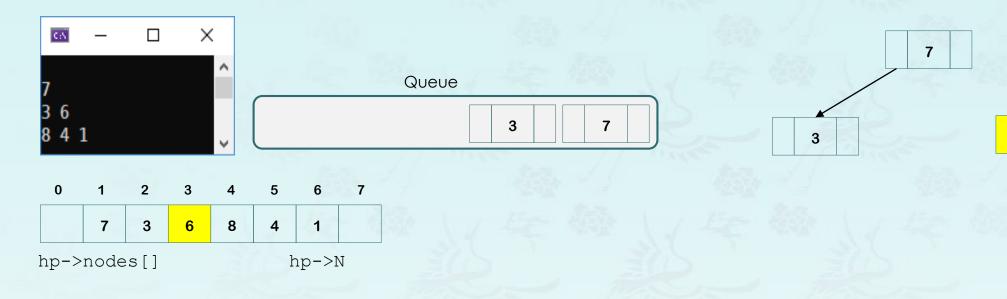
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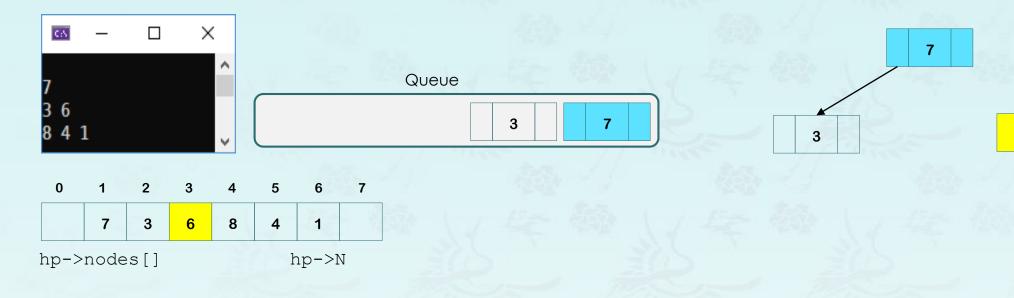
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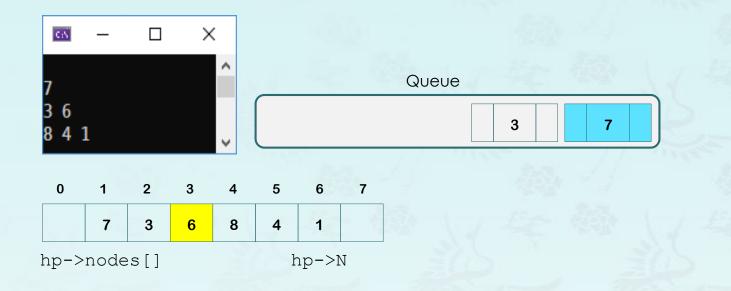
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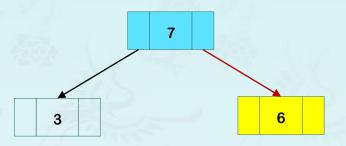


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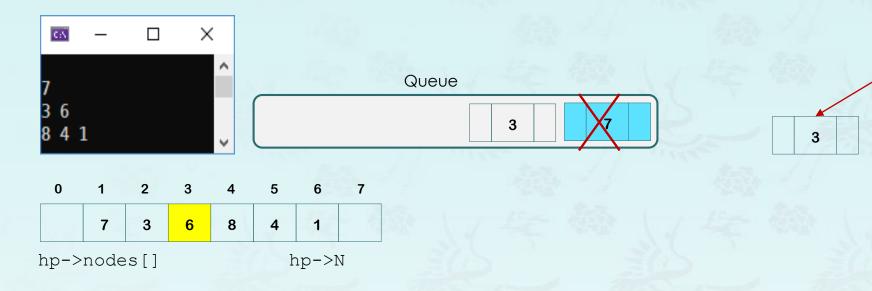


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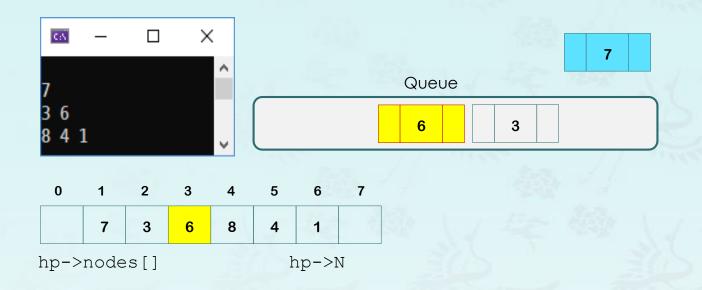


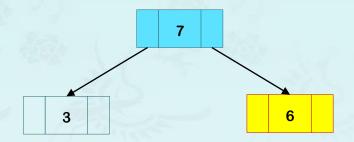


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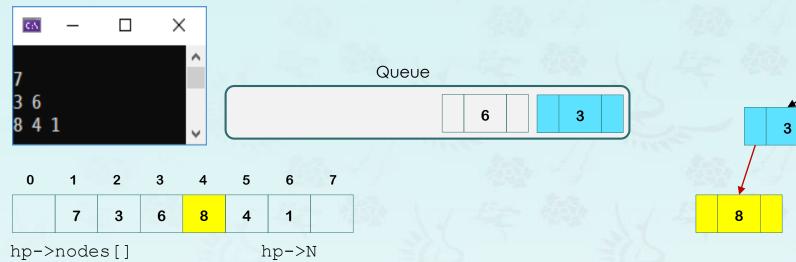
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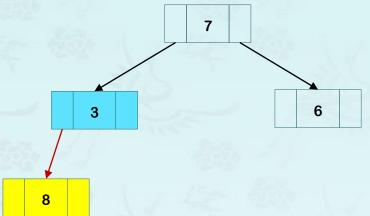


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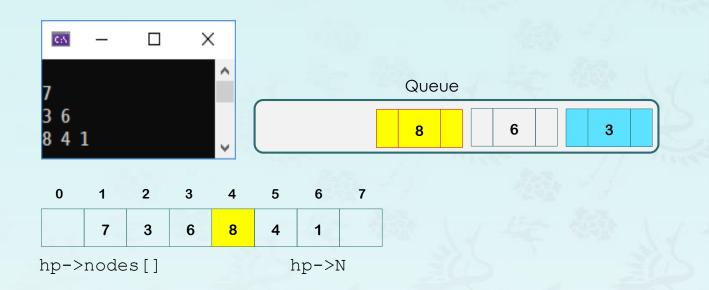


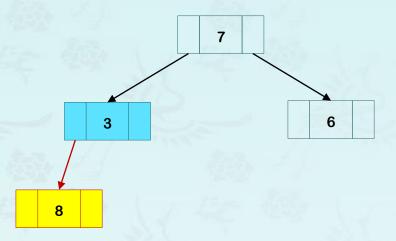
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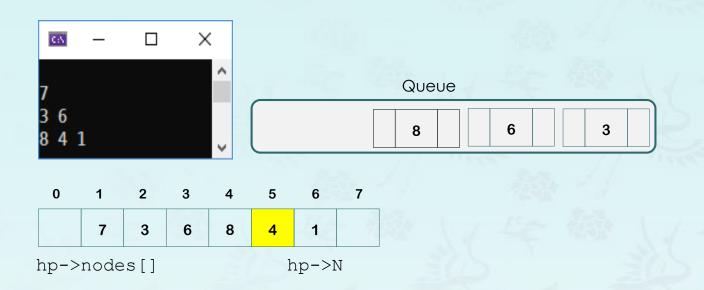


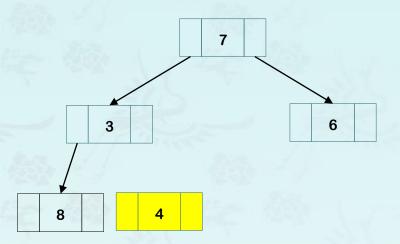
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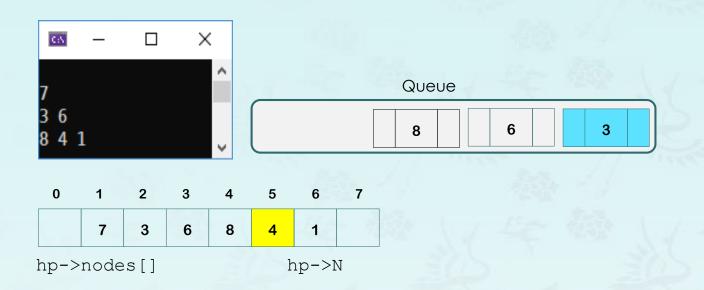


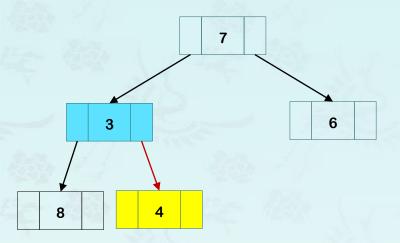
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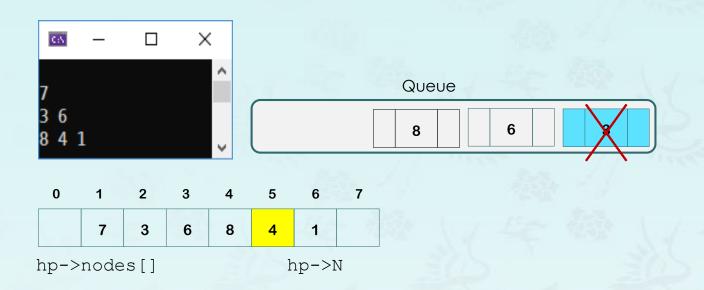


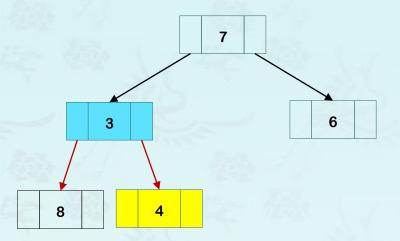
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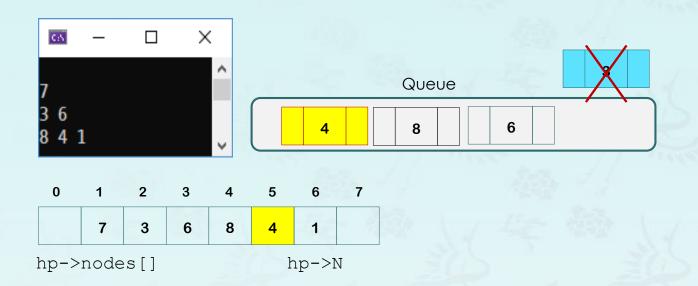


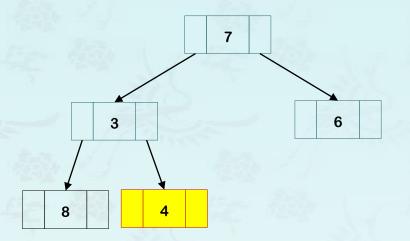
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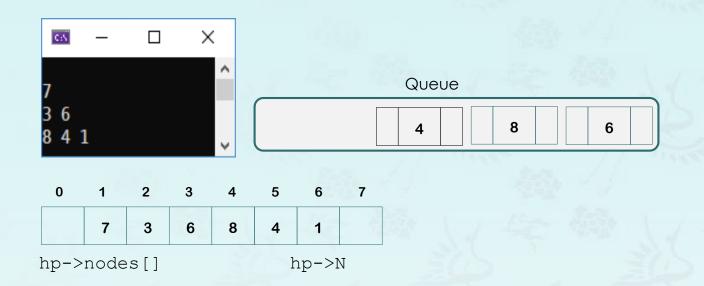


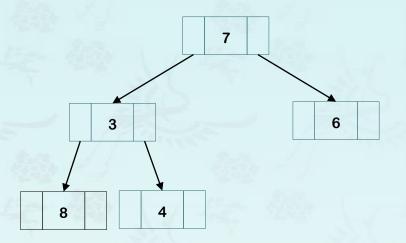
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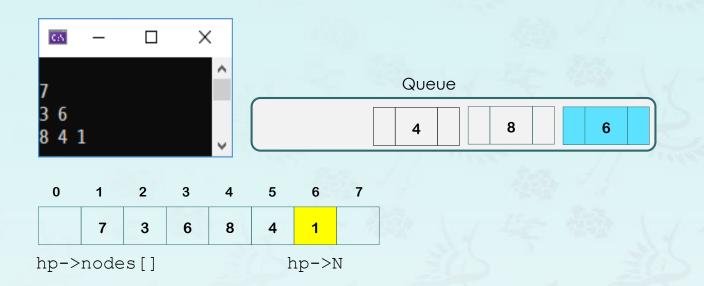


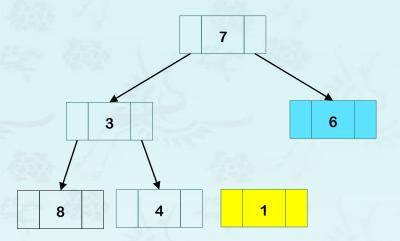
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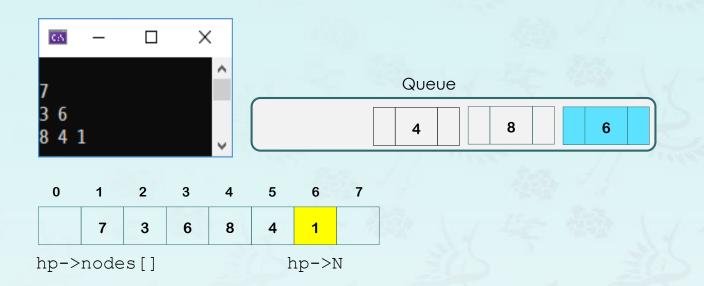


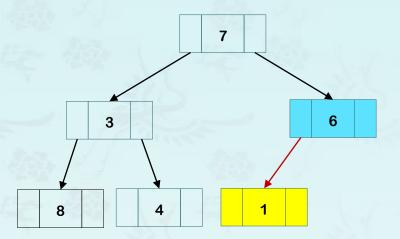
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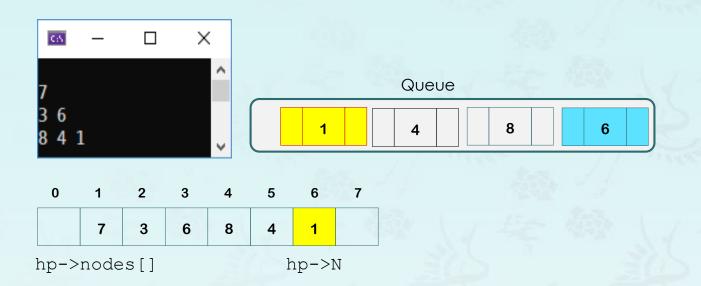


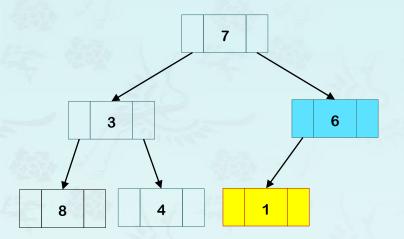
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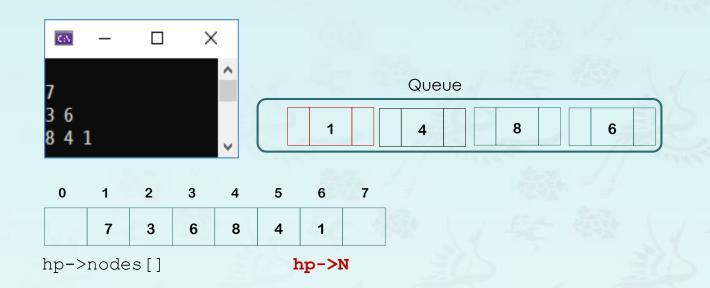


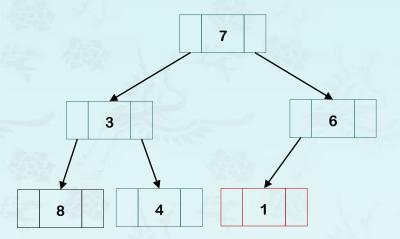
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Data Structures Chapter 5: Heap and Priority Queue

- 1. Heap & Priority Queue
- 2. Heapsort
- 3. Heap & PQ Coding