# Wheat Yield exercise

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2023-11-14

#### Dataset

- Exercise developed by Chris Wikle and Dan Pagendam (2019).
- Dataset created by Dan Pagendam and Josh Bowden at CSIRO.
- The data consists of simulated wheat yields from a farm in Dalby, Queensland using the model APSIMX.
- ▶ The dataset was created from 10,000 simulations of wheat growth under randomly generated meteorological conditions and management (planting and fertiliser application).

#### **Predictors**

- ► The predictors are:
  - summary statistics for the amount of rainfall in each of 52 weeks in the year.
  - degree days in each of the 52 weeks in the year.
  - cumulative evaporation in each of the 52 weeks of the year.
  - the "thermal time" of the wheat at each of the 52 weeks in the year.
  - the amount of Nitrogen fertiliser applied at planting.
  - the amount of Nitrogen fertiliser applied as top-up.
  - the day of year that the crop was planted.
  - the planting density of seed.

# Response

- ▶ There are four response variables:
  - wheat grain yield.
  - grain size.
  - grain protein content.
  - wheat total weight.

#### Load dataset

```
#For those using Colab run: install.packages("keras")
load("../Data/Wheat.Rdata")
```

- ► The dataset contains both training and validation data, with response denoted by *Y* and predictors denoted by **X**
- ► The training and validation sets were determined by randomly allocating approximately 10% of the simulations to the validation set and the remaining 90% to the training set.

```
dim(trainData_X)
## [1] 8993 212
dim(validationData_X)
```

```
## [1] 1007 212
```

#### Data normalisation

▶ We first scale the input data to improve the numerical stability of training

rescaleCols <- function(rowX, colMins, colMaxs)</pre>

```
{
  r <- (rowX - colMins)/(colMaxs - colMins)
  r[is.nan(r)] \leftarrow 0
  return(r)
colMinsX <- apply(trainData_X, 2, min)</pre>
colMaxsX <- apply(trainData_X, 2, max)</pre>
trainData_X_scaled <- t(apply(trainData_X, 1,</pre>
        rescaleCols, colMinsX, colMaxsX))
validationData X scaled <- t(apply(validationData X, 1,
        rescaleCols, colMinsX, colMaxsX))
```

## Response

We focus on modelling a single output response Y: Wheat total weight

We will begin by 'predicting' Y given X, i.e., we estimate the expectation  $\mathbb{E}[Y|X]$ 

# Building a Keras prediction model

- ► We will build a feed-forward neural network with densely-connected layers and ReLU activations
- Begin by defining the input layer:

# Hidden layers

► The model will have three hidden layers, each with 64 nodes

```
hidden.lay<- input.lay %>%
  layer_dense(units = 64, activation = "relu") %>%
layer_dense(units = 64, activation = "relu") %>%
layer_dense(units = 64, activation = "relu")
```

► The output layer has a single unit; we estimate one value, i.e., the expectation, for each input vector

```
output.lay <- hidden.lay %>% layer_dense(units = 1)
```

### Define a Keras model

Model definition and summary

```
model <- keras_model(
  inputs = c(input.lay),
  outputs = c(output.lay)
)
summary(model)</pre>
```

# Model compiltation

- We now compile the model with a loss function and an optimiser
- ► Here we use the MSE loss, which targets the mean of the response Y. If we wanted to target the median, we could use MAE instead
- ▶ We will use the RMSProp optimisation algorithm

```
model %>% compile(
  loss = "mse",
  optimizer = optimizer_rmsprop(learning_rate = 0.0001)
)
```

## Fitting the model

## Epoch 1/30

- ▶ We are now ready to fit the model.
- ▶ We define the training data, but also out-of-sample validation data that we can use to check how well the model generalises.
- ▶ When training the neural network, we use batches of data (32 samples here) to estimate the gradient of the loss function w.r.t the parameters.
- ▶ We also need to specify the number of epochs.
- ▶ Because we chose a small learning rate, we'll probably need to use more epochs to find the optimal fit.

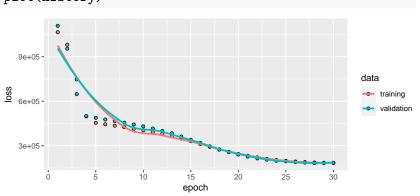
```
history <- model %>% fit(
  x = trainData_X_scaled, y = trainData_Y,
  epochs = 30, batch_size = 32,
  validation_data = list(
    validationData_X_scaled, validationData_Y)
)
```

## 282/282 - 1s - loss: 1065520.7500 - val\_loss: 1108410.3

# Fitting the model

Check for overfitting

plot(history)

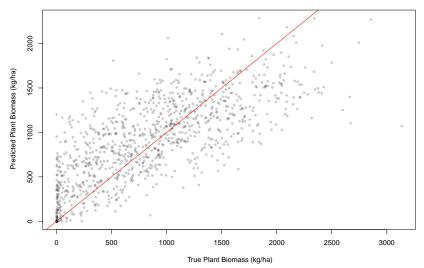


#### **Predictions**

Check predictions

### **Predictions**

## 32/32 - 0s - 111ms/epoch - 3ms/step



## **Improvements**

- We just trained a model using the build in "mse" loss function. This minimises mean squared error and so is analogous to linear regression where we assumed the error to be homoscedastic.
- ► Instead, let's fit a log-normal regression model with varying scale parameter, i.e., a heteroscedastic model
- Do say by minimising the negative log-likelihood, i.e., MLE
- Not implemented as standard in Keras -> We're going to create a custom loss function that is equal to the negative of the log-likelihood under the assumption that our predicted wheat yields can be modelled as having a log-normal distribution.

### Custom loss functions

- ► See "keras\_build.rmd" for help writing custom loss functions
- ▶ All custom loss functions have the same broad structure

```
custom_loss=function(y_true,y_pred){
  K <- backend()
  #Code here
}</pre>
```

### Custom loss functions

#### Important notes:

- when writing your code, you need to remember that y\_true and y\_pred are tensors.
- y\_true and y\_pred don't necessarrily have to have the same dimension.
- the first dimension of both the input tensors is equal to the batch size.
- there is very little documentation on how to write custom loss functions.
- try to use the Keras backend functions as much as possible and avoid using R functions (they may not work).
- ▶ if a Keras function has the "axis" argument, it is asking you which dimension you want to "apply" the function to.

### Custom loss functions

```
negLL logNormal <- function(y true, y pred)</pre>
{
 K <- backend()</pre>
# Extract the first and second columns of predictions
  mu <- (y pred[,1])
  sigma <- K$exp(y_pred[,2])</pre>
# Extract first column of y_true to ensure same dimensions
 y <- y_true[,1]
  # Use mu and sigma as parameters
  # describing log-normal distributions
  logLike \leftarrow -1*(K$log(y) + K$log(sigma)) -
    0.5*K$log(2*pi) - (K$log(y) - mu)^2/(2*(sigma)^2)
  return( -(K$sum(logLike)))
```

# Building a custom model

- ▶ Based on the custom loss function we just created, our model requires two outputs:
  - one for mu (location parameter of the log-normal).
  - one for sigma (scale parameter of the log-normal).
- ► Let's use 3 hidden layers, with 64 nodes per layer and stick with the rectified linear unit (ReLU) activation function.
- ▶ Notice, that we now have two nodes / units in the output layer of the network.

# Compiling

- ▶ We will use the same optimiser as previously
- but must specify the custom loss function

```
model2 <- keras_model(
    inputs = c(input.lay),
    outputs = c(output.lay2)
)
model2 %>% compile(
  loss = negLL_logNormal,
  optimizer = optimizer_rmsprop(learning_rate = 0.0001)
)
```

# Fitting the model

- We're also going to introduce a callback into our training procedure.
- ► This will reduce the learning rate when we stop seeing a reduction in the validation loss.
- A smaller learning rate means smaller changes to the parameters, so we can think of this as fine-tuning our parameters with more and more epochs.
- Other callbacks include checkpoints and early-stopping

# Fitting the model history <- model2 %>% fit( x = trainData\_X\_scaled, y = trainData\_Y, epochs = 50, batch\_size = 32, validation data = list( validationData X scaled, validationData Y), callbacks = callback ## Epoch 1/50 ## 282/282 - 1s - loss: 338.7747 - val\_loss: 269.2893 - lr ## Epoch 2/50 ## 282/282 - 0s - loss: 264.7363 - val\_loss: 262.3626 - lr ## Epoch 3/50 ## 282/282 - 0s - loss: 260.9782 - val\_loss: 258.1455 - lr ## Epoch 4/50 ## 282/282 - 0s - loss: 256.5180 - val loss: 252.7120 - lr

## 282/282 - 0s - loss: 251.7740 - val loss: 247.1667 - lr

## Epoch 5/50

## Emach 6/EA

#### **Predictions**

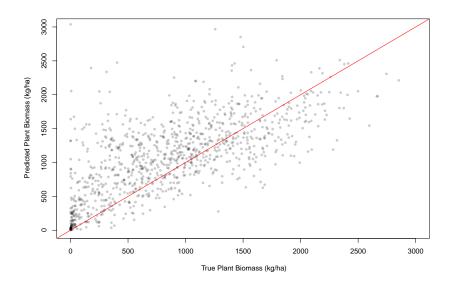
The model outputs two quantities for each input vector

yhat <- predict(model2, validationData X scaled)</pre>

- ► These are the mu and log(sigma) parameters for a log-normal predictive density.
- We can compare the mean of the log-normal to the true yield.

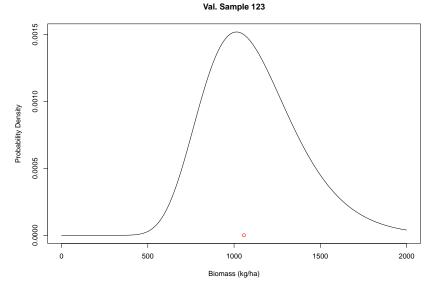
```
## 32/32 - 0s - 68ms/epoch - 2ms/step
mu <- yhat[, 1]
sigma <- exp(yhat[, 2])
pred_mean <- exp(mu + 0.5*sigma^2)</pre>
```

# **Predictions**



### Predicted densities

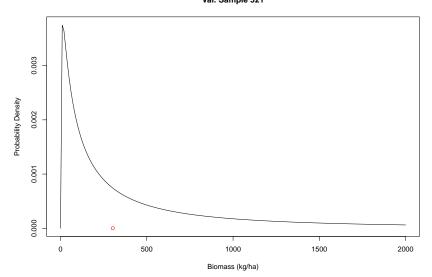
▶ We can also look at the predicted density for specific samples



### Predicted densities

► We can also look at the predicted density for specific samples

Val. Sample 321



#### Extensions

- ► How do your results change if you include more nodes in the hidden layers?
- How do your results change if you make the network deeper?
- ► Try including some form of regularisation (e.g. Dropout or L1 regularisation) in the hidden layers to help prevent overfitting.
- ► There's some extra details in keras\_build.html, including how to save/load models (can be difficult with custom loss functions), multi input/output models, homogeneous model parameters