

Drought forecasting exercise

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Dataset

- ▶ Exercise developed by Chris Wikle and Dan Pagendam (2019).
- ▶ The data consists of:
 - ▶ monthly 33×84 grids (2 degree \times 2 degree) of sea surface temperature (SST) anomaly (2772 pixels).
 - ▶ monthly rainfall anomaly in mm for the Murray Darling Basin (MDB).
- ▶ Obtained from two sources:
 - ▶ <http://www.bom.gov.au/climate/change/>
 - ▶ <http://iridl.ldeo.columbia.edu/>
- ▶ We will use a type of recurrent NN(LSTM) model to obtain 3-month-out forecasts of rainfall anomaly using SST grids as a predictor.

Required packages

We will be using some functions and the images from Dan's github directory, <https://github.com/dpagendam/deepLearningRshort>

```
#remotes::install_github("dpagendam/deepLearningRshort")
```

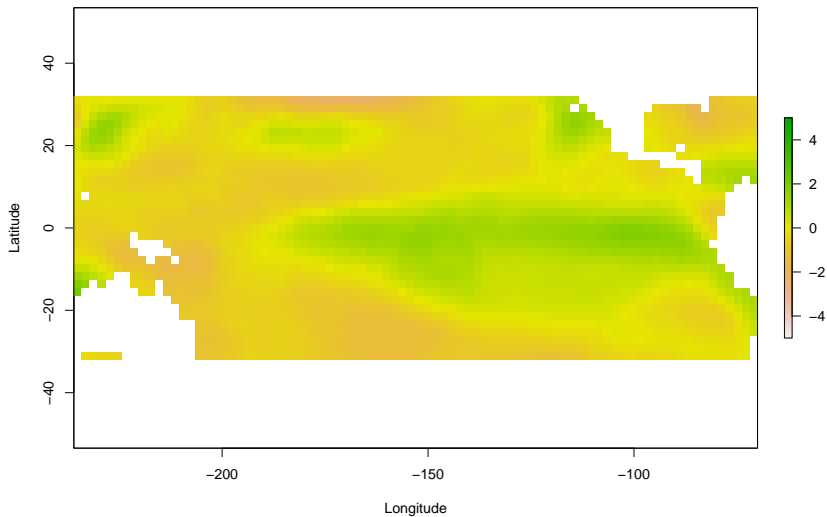
```
library(keras)  
library(raster)
```

```
## Loading required package: sp
```

```
library(deepLearningRshort)  
data(drought)
```

Visualise SST

Sea Surface Temperature Anomaly (1/1900)



Strategy

- ▶ We could apply a CNN layer recurrently to extract both sequential and spatial information from the SST grids, but this will require lots of processing power and parameters
- ▶ Instead, we treat the SST as a multivariate time series and use regular RNNs. However, we have 2772 locations, so we first reduce the dimensionality using EOFs (PCA)

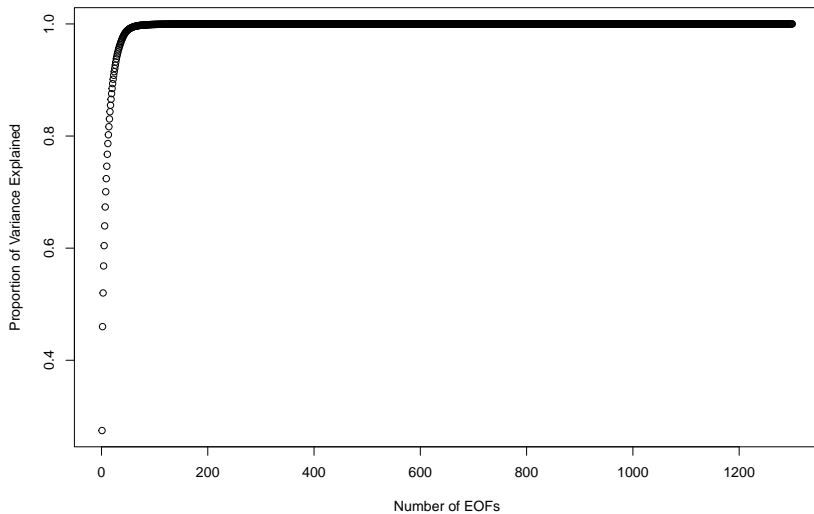
Data manipulation

```
batchSize <- 32
forecastMonthsAhead <- 3
timestepsPerSample <- 24
trainingInds <- 1:1300
validationInds <- 1301:1434
# We consider only 1434 months
```

- ▶ We will project the 2772 pixels onto 100 EOFs.

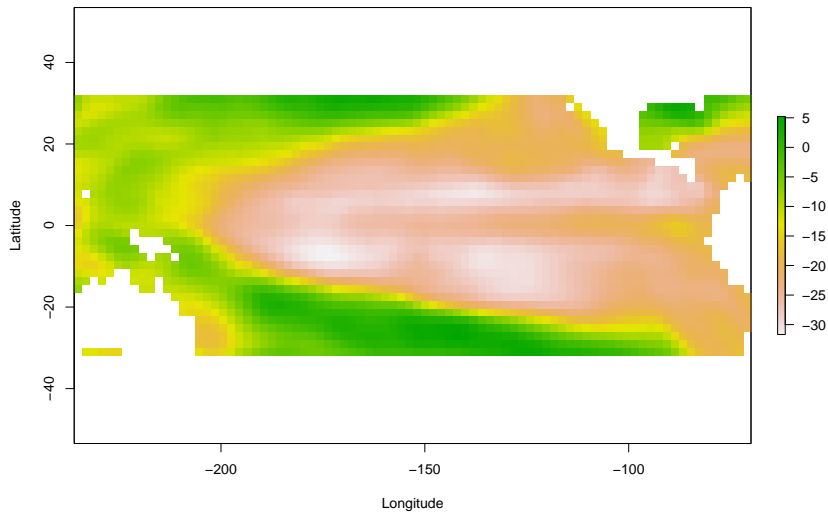
```
numComponents <- 100
EOFList <- rasterToEOFs(anomalyRasterList[trainingInds],
  numComponents = numComponents, plot = FALSE)
v.train <- EOFList[["rasterEOFs"]][["v.dim.red"]]
```

Plot EOFs



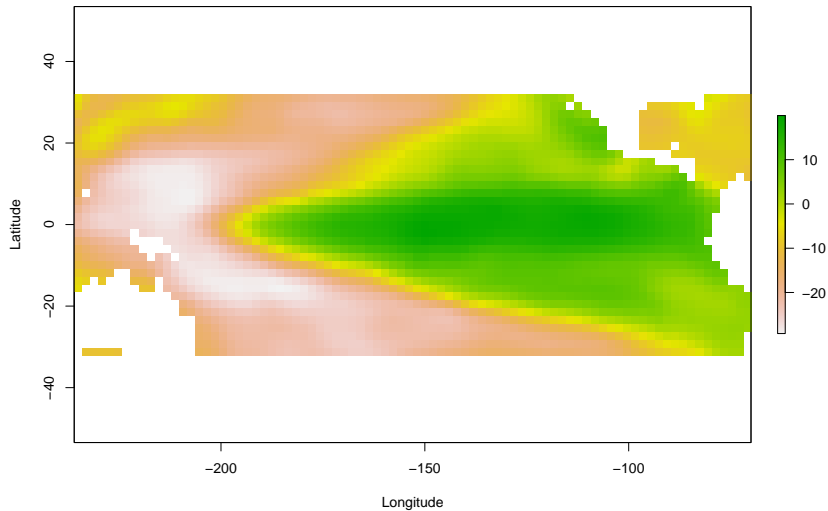
Plot EOFs

1st EOF



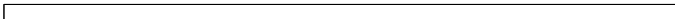
Plot EOFs

2nd EOF



Plot EOFs

100th EOF

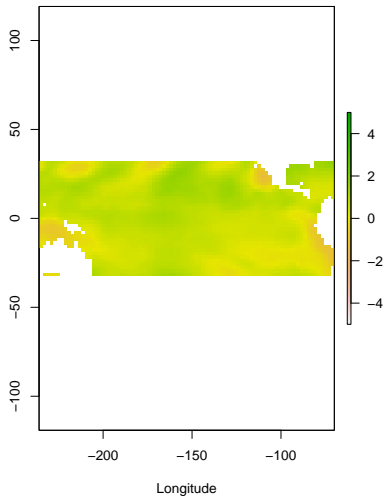
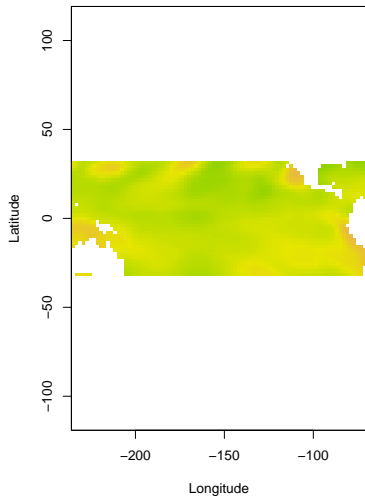


Reconstructing SST

```
validationSample <- 1434
X <- EOFList$rasterEOFs$EOFs
r1 <- anomalyRasterList[[validationSample]]
validPixels <- EOFList[["raster.validPixels"]]
Y <- getValues(r1)
Y <- Y[validPixels]
lm1 <- lm(Y~X)
intercept <- coefficients(lm1)[1]
alpha <- coefficients(lm1)[1]
beta <- coefficients(lm1)[2:(numComponents + 1)]
r2 <- alpha + EOFsToRaster(X, matrix(beta, nrow = 1),
  c(33, 84), validPixels)[[1]]
extent(r2) <- extent(r1)
```

Reconstructing SST

Original

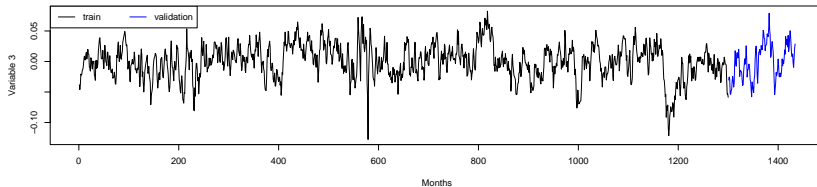
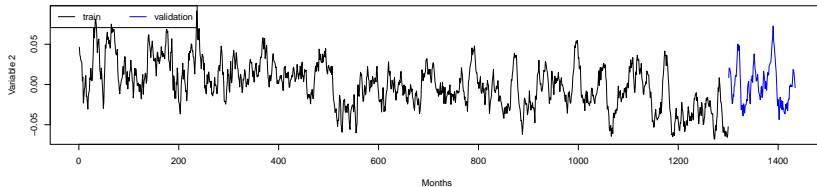
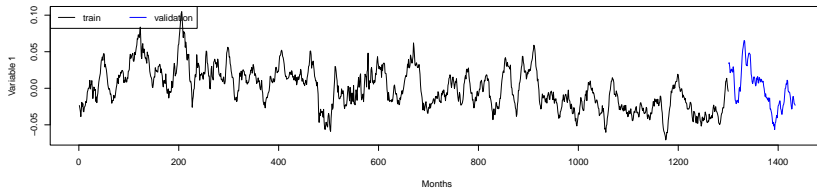


Dimension reduction for validation data

- ▶ Here we project the validation data SST anomaly grids onto the same EOFs generated from the training data. · You can think of `v.validation` as a multivariate time series of coefficients that we can use to reconstruct SST anomaly from the EOFs.

```
v.validation <- proj.raster.EOFs(  
  anomalyRasterList[validationInds],  
  EOFList[["rasterEOFs"]][["EOFs"]],  
  EOFList[["raster.validPixels"]])
```

Dimension reduction for validation data



Data wrangling

- ▶ All predictors combined together

```
v.combined <- rbind(v.train, v.validation)
```

- ▶ and normalised

```
v.scaling.train <- scaleCols.pos(  
  v.combined[trainingInds, ])  
v.train.scaled <- v.scaling.train[["X.scaled"]]  
v.scaling.validation <- scaleCols.pos(  
  v.combined[validationInds, ],  
    colMaxsX = v.scaling.train[["colMaxsX"]],  
    colMinsX = v.scaling.train[["colMinsX"]])  
v.validation.scaled <- v.scaling.validation[["X.scaled"]]  
  
v.scaled <- rbind(v.train.scaled, v.validation.scaled)
```

Formatting data for an RNN

```
numDims <- ncol(v.scaled)
tensorData <- tensorfyData.rnn(v.scaled,
                                forecastMonthsAhead,
                                timestepsPerSample, indicesX = 1:numDims,
                                indicesY = 1:numComponents,
                                indicesTrain = trainingInds,
                                indicesTest = validationInds)
str(tensorData)
```

```
## List of 8
```

```
## $ X.train.rnn      : num [1:1273, 1:24, 1:100] 0.268 0.248
## $ Y.train.rnn      : num [1:1273, 1:100] 0.396 0.323 0.363
## $ X.test.rnn       : num [1:107, 1:24, 1:100] 0.597 0.602
## $ Y.test.rnn       : num [1:107, 1:100] 0.58 0.654 0.7 0.7
## $ x.train.tsInds: int [1:1273] 24 25 26 27 28 29 30 31
## $ x.test.tsInds  : int [1:107] 1324 1325 1326 1327 1328
## $ y.train.tsInds: int [1:1273] 27 28 29 30 31 32 33 34
## $ y.test.tsInds  : int [1:107] 1327 1328 1329 1330 1331
```

Response data

```
Y.train.inds <- tensorData$y.train.tsInds  
Y.valid.inds <- tensorData$y.test.tsInds  
Y.train.rnn_MDB <- rainfallAnomaly[Y.train.inds, 3]  
Y.valid.rnn_MDB <- rainfallAnomaly[Y.valid.inds, 3]
```

- ▶ We will also normalise the response, but this is only because we will fit a Gaussian model

```
Y.train.min <- min(Y.train.rnn_MDB)  
Y.train.max <- max(Y.train.rnn_MDB)  
  
Y.rnn.train <- (Y.train.rnn_MDB - Y.train.min)/  
               (Y.train.max - Y.train.min)  
Y.rnn.valid <- (Y.valid.rnn_MDB - Y.train.min)/  
               (Y.train.max - Y.train.min)
```


RNN tensors

We finally get

```
X.rnn.train <- tensorData[["X.train.rnn"]]
```

```
X.rnn.valid <- tensorData[["X.test.rnn"]]
```

```
dim(X.rnn.train)
```

```
## [1] 1273    24   100
```

```
length(Y.rnn.train)
```

```
## [1] 1273
```

Custom loss

```
Gaussian_logLikelihood <- function(y_true, y_pred)
{
  K <- backend()
  # Extract the first and second columns of predictions
  mu <- (y_pred[,1])
  sigma <- K$exp(y_pred[,2])

  #Extract first column of y_true to ensure same dimension
  y <- y_true[,1]

  ll <- -0.5*((mu - y)/(sigma))^2 - K$log(sigma)
  ll <- ll -0.5*K$log(2*pi)

  return( -(K$sum(ll)))
}
```

Building an LSTM Model

```
library(keras)
input.lay <- layer_input(shape = dim(X.rnn.train)[-1],
                        name = 'input_layer')

model <- input.lay %>%
  layer_lstm(units = 128,
            input_shape = c(timestepsPerSample, numDims),
            return_sequences = FALSE) %>%
  layer_dense(units = 128, activation = "relu")
output.lay <- model %>% layer_dense(units = 2)
```

Compile

```
model <- keras_model(  
  inputs = c(input.lay),  
  outputs = c(output.lay)  
)  
model %>% compile(loss = Gaussian_logLikelihood,  
  optimizer = optimizer_rmsprop())
```

Summary

```
summary(model)
```


Checking performance

- ▶ We can calculate the mean and standard deviations of the 3 month out (Gaussian) predictive distributions.
- ▶ Then create 50% and 95% prediction intervals.

```
lstmPredictions <- model %>% predict(X.rnn.valid)

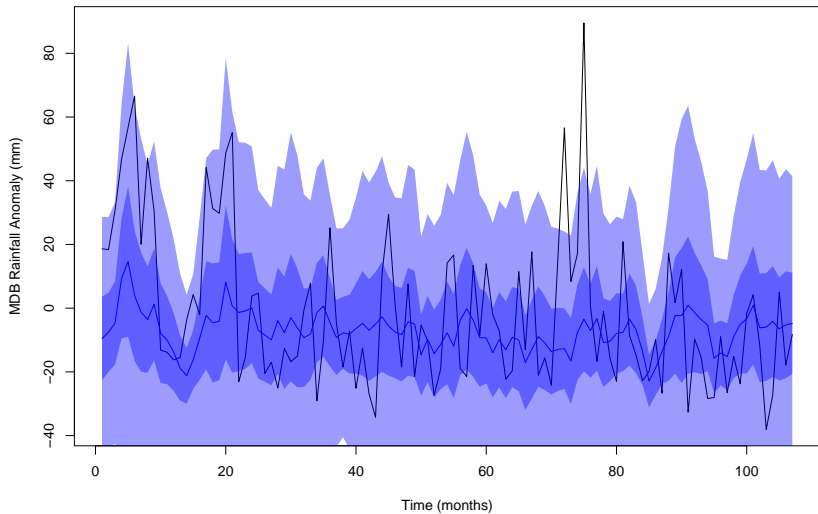
mu <- Y.train.min +
  lstmPredictions[, 1]*(Y.train.max - Y.train.min)
sigma <- exp(lstmPredictions[, 2])*
  (Y.train.max - Y.train.min)
n <- length(mu)
upper95 <- mu + 1.96*sigma
lower95 <- mu - 1.96*sigma
upper50 <- mu + 0.674*sigma
lower50 <- mu - 0.674*sigma
```

Checking performance

Plot the true time series with 3-month-out forecast and 50% and 95% prediction intervals.

```
plot(rainfallAnomaly[Y.validation.indxs, 3], ty = "l",  
     xlab = "Time (months)",  
     ylab = "MDB Rainfall Anomaly (mm)")  
lines(mu, col = "blue")  
polygon(x = c(1:n, rev(1:n), 1),  
        y = c(lower95, rev(upper95), lower95[1]),  
        col = fade("blue", 100), border = NA)  
polygon(x = c(1:n, rev(1:n), 1),  
        y = c(lower50, rev(upper50), lower50[1]),  
        col = fade("blue", 100), border = NA)
```


Checking performance



Checking performance

Calculate what percentage of the time the true rainfall anomaly was within the 50% and 95% prediction intervals.

```
n <- (length(Y.valid.inds))  
coverage50 <- length(  
  which(rainfallAnomaly[Y.valid.inds, 3] > lower50  
    & rainfallAnomaly[Y.valid.inds, 3] < upper50))/n  
coverage95 <- length(  
  which(rainfallAnomaly[Y.valid.inds, 3] > lower95  
    & rainfallAnomaly[Y.valid.inds, 3] < upper95))/n  
print(coverage50)
```

```
## [1] 0.5514019
```

```
print(coverage95)
```

```
## [1] 0.9626168
```

Extensions

- ▶ How does varying the number of units in the LSTM layer affect the predictions?
- ▶ How do the predictions change if you add three dense layers after the LSTM layer (instead of just 1)?
- ▶ How are the predictions if much fewer EOFs are used for prediction?
- ▶ How does fewer EOFs affect the number of parameters in the model?