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# Advanced Artificial Intelligence

## Lab 08

# Outline

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- More introduction to ensemble learning
- Exercise

# Random Forests

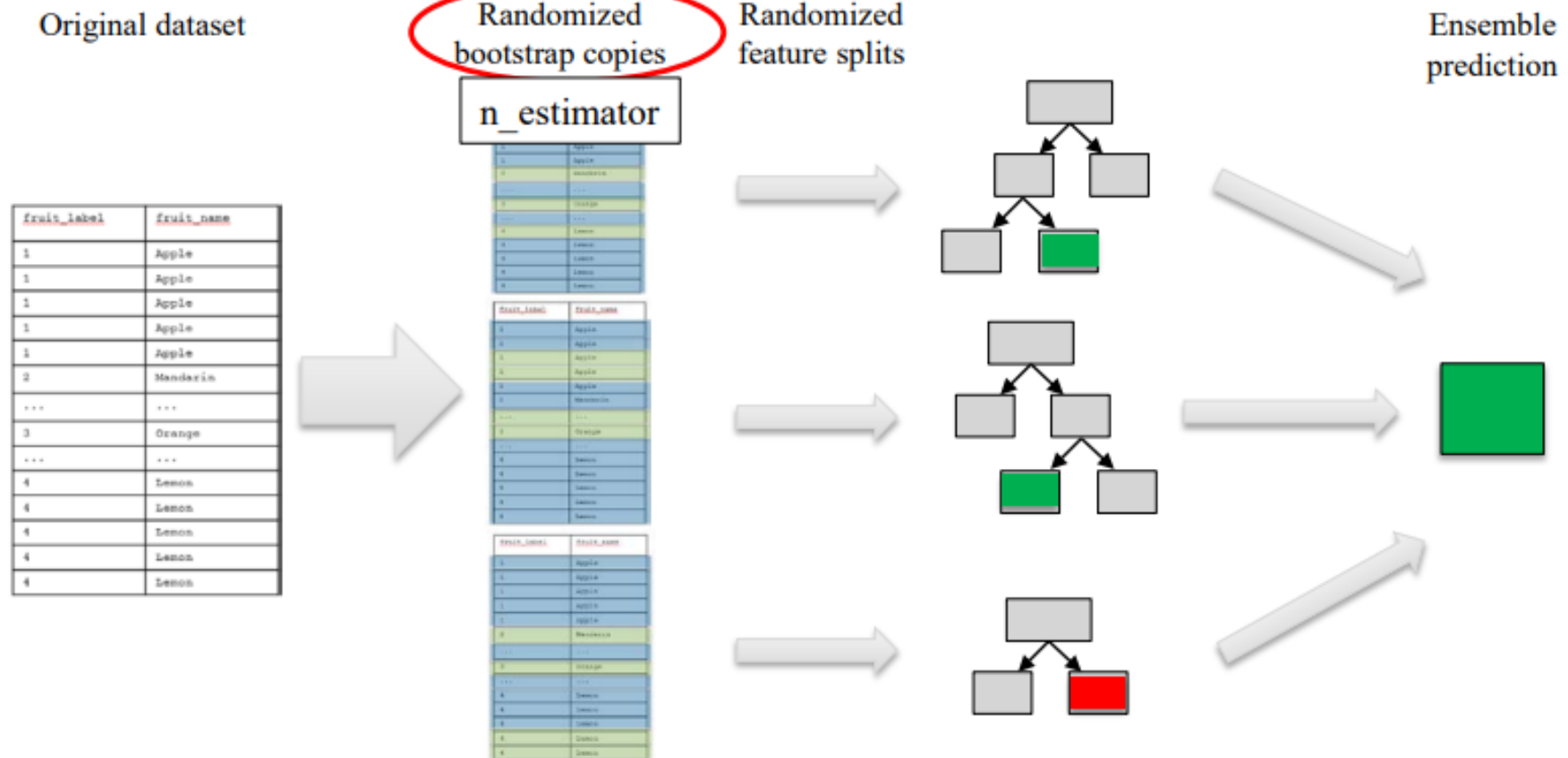
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## Random Forests

- **An ensemble of trees, not just one tree.**
- **Widely used, very good results on many problems.**
- **`sklearn.ensemble` module:**
  - *Classification: `RandomForestClassifier`*
  - *Regression: `RandomForestRegressor`*
- **One decision tree → Prone to overfitting.**
- **Many decision trees → More stable, better generalization**
- **Ensemble of trees should be diverse: introduce random variation into tree-building.**

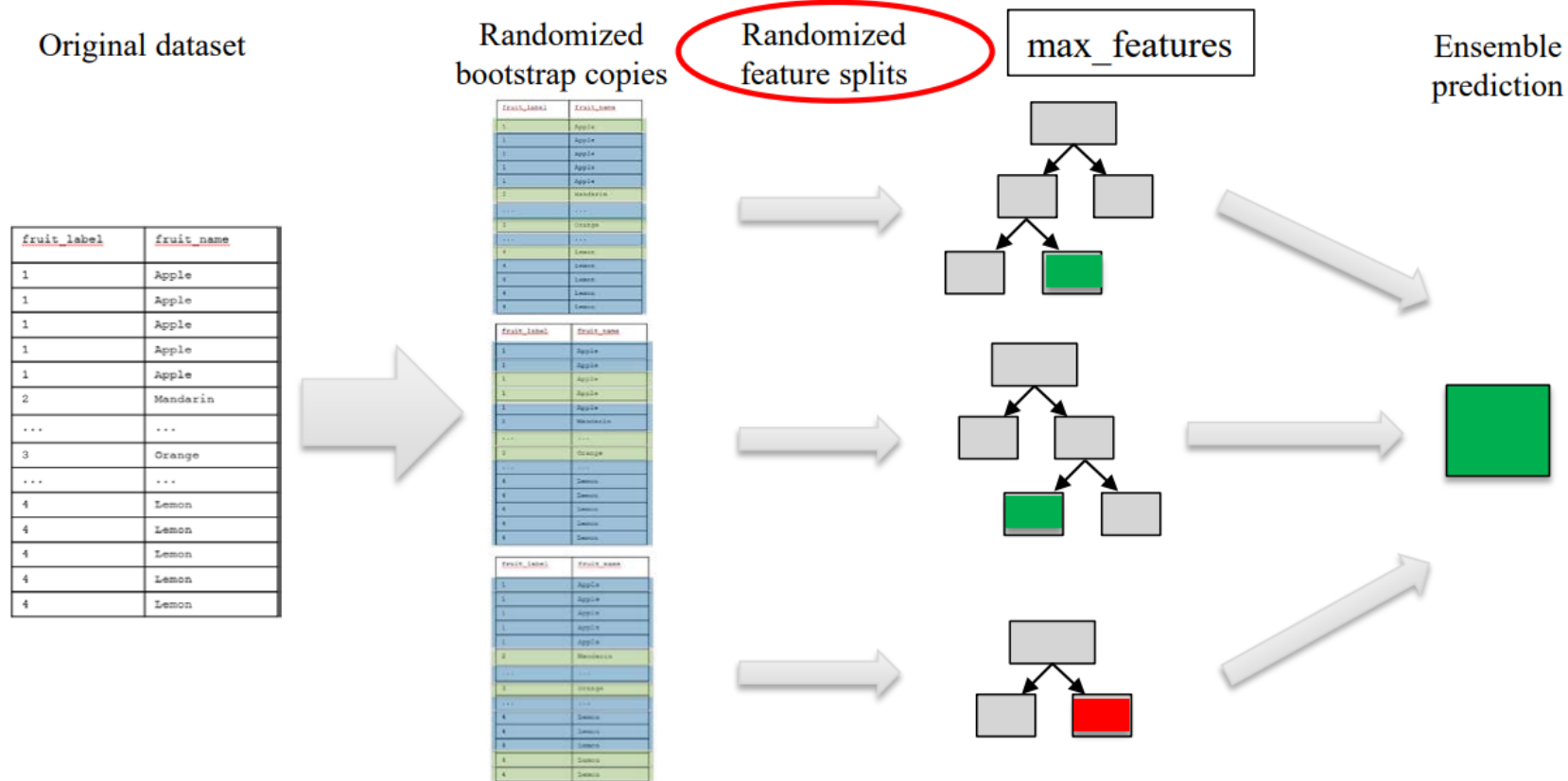
# Random Forests

## Random Forest Process



# Random Forests

## Random Forest Process



# Random Forests

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## Random Forest `max_features` Parameter

- Learning is quite sensitive to `max_features`.
- Setting `max_features = 1` leads to forests with diverse, more complex trees.
- Setting `max_features = <close to number of features>` will lead to similar forests with simpler trees.

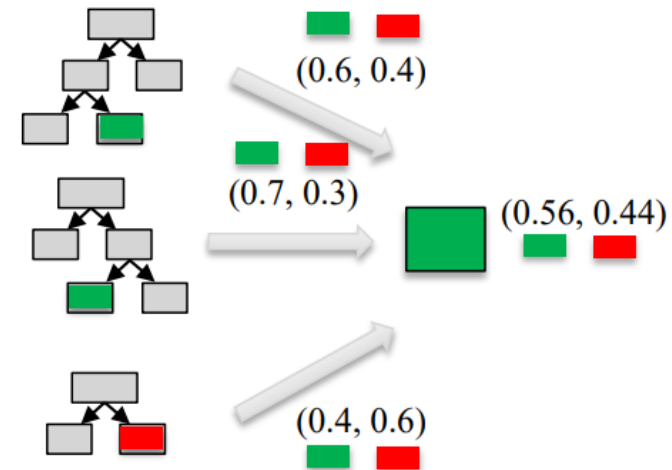
# Random Forests

## Prediction Using Random Forests

1. Make a prediction for every tree in the forest.

2. Combine individual predictions

- *Regression: mean of individual tree predictions.*
- *Classification:*
  - *Each tree gives probability for each class.*
  - *Probabilities averaged across trees.*
  - *Predict the class with highest probability.*



# Boosting

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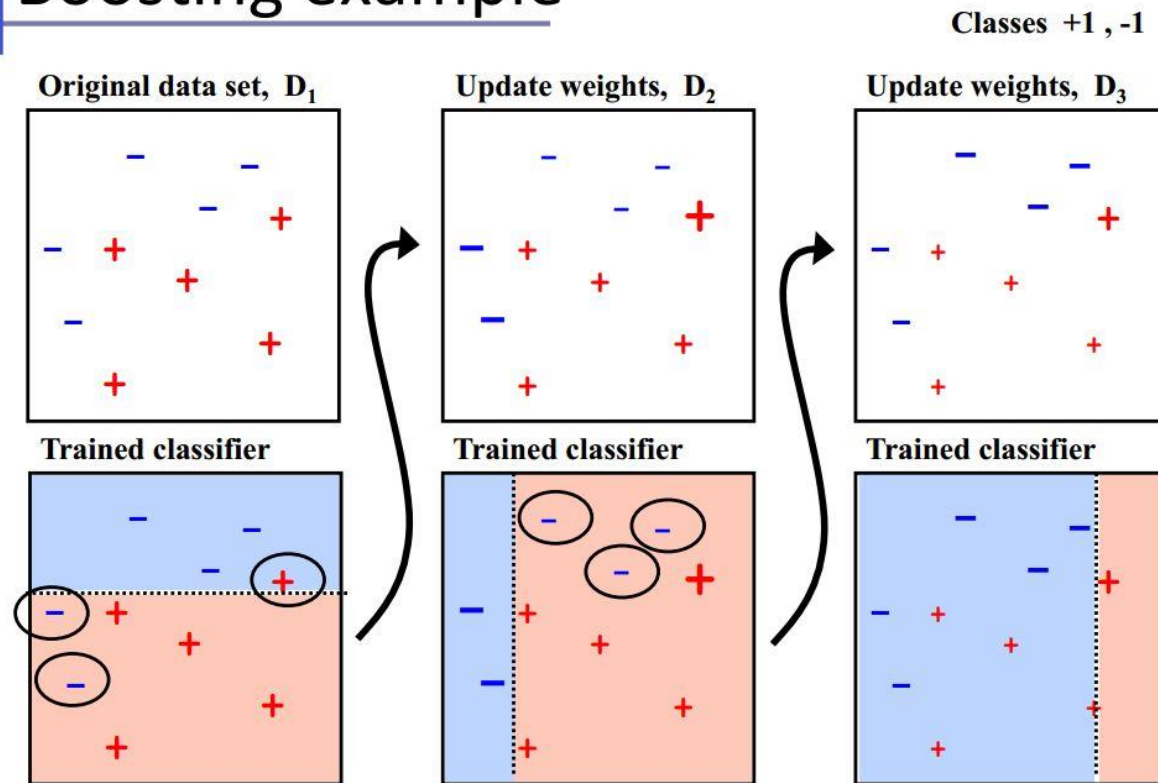
- **Pseudo-code**

- 1: **Input** the original data set  $\mathcal{D}$
- 2: **Input** the number of bootstrap samples  $k$
- 3: Number of training samples  $N = |\mathcal{D}|$
- 4: Initialise the weights for samples  $\mathbf{w} \leftarrow (\frac{1}{N}, \frac{1}{N}, \dots, \frac{1}{N})$
- 5: **for**  $i = 1$  to  $k$  **do**
- 6:   Create a bootstrap sample  $\mathcal{D}_i$  of size  $N$  from  $\mathcal{D}$  according to  $\mathbf{w}$
- 7:   Train a base model on  $\mathcal{D}_i$
- 8:   **Increase** the weights of **incorrectly** classified examples
- 9:   **Reduce** the weights of **correctly** classified examples
- 10:   Normalise  $\mathbf{w}$
- 11: **end for**
- 12: Aggregating the trained base classifiers and use it as final ensemble model



# Boosting Example

## Boosting example

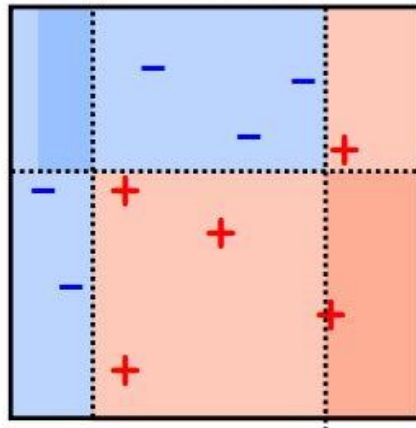


# Boosting example

Weight each classifier and combine them:

$$.33 * \begin{array}{|c|} \hline \text{blue} \\ \hline \text{red} \\ \hline \end{array} + .57 * \begin{array}{|c|} \hline \text{blue} \\ \hline \text{red} \\ \hline \end{array} + .42 * \begin{array}{|c|} \hline \text{blue} \\ \hline \text{red} \\ \hline \end{array} \geq 0$$

Combined classifier



1-node decision trees  
"decision stumps"  
*very simple classifiers*

# Boosting: GBDT

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```
1 from sklearn.ensemble import GradientBoostingClassifier
2 from sklearn.model_selection import GridSearchCV
3
4 rfc = GradientBoostingClassifier(learning_rate=1.0)
5 para = {'n_estimators': [88, 99, 100, 111, 122, 133], 'max_depth': [7, 8, 9, 10, 13, 14]}
6 gscv = GridSearchCV(rfc, param_grid=para, cv=2)
7 gscv.fit(X_train, y_train)
8 predict = gscv.predict(X_test)
9 score = gscv.score(X_test, y_test)
10 # print(predict)
11 print(score)
12 print(gscv.best_params_)
13
```

0.8977777777777778

{'max\_depth': 7, 'n\_estimators': 99}

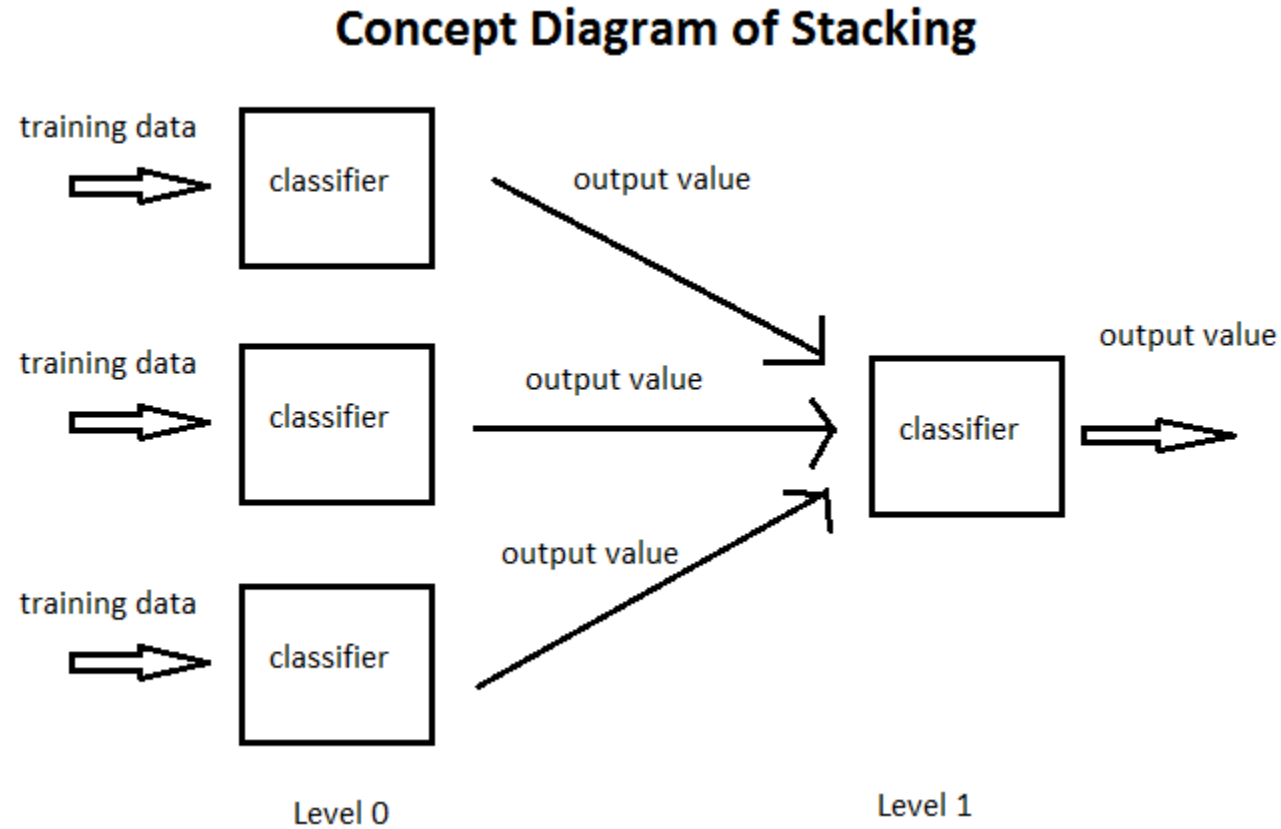
# Stacking Algorithm

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Algorithm	Stacking
1:	Input: training data $D = \{x_i, y_i\}_{i=1}^m$
2:	Output: ensemble classifier $H$
3:	<i>Step 1: learn base-level classifiers</i>
4:	<b>for</b> $t = 1$ to $T$ <b>do</b>
5:	learn $h_t$ based on $D$
6:	<b>end for</b>
7:	<i>Step 2: construct new data set of predictions</i>
8:	<b>for</b> $i = 1$ to $m$ <b>do</b>
9:	$D_h = \{x'_i, y_i\}$ , where $x'_i = \{h_1(x_i), \dots, h_T(x_i)\}$
10:	<b>end for</b>
11:	<i>Step 3: learn a meta-classifier</i>
12:	learn $H$ based on $D_h$
13:	return $H$

# Stacking Example

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# Stacking Ensemble

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```
1 from sklearn.ensemble import RandomForestClassifier
2 from sklearn.ensemble import AdaBoostClassifier
3 from sklearn.linear_model import LogisticRegression
4 from sklearn.ensemble import StackingClassifier
5 X, y = load_iris(return_X_y=True)
6 estimators = [
7     ('rf', RandomForestClassifier(n_estimators=122, max_depth=8, random_state=0)),
8     ('ada', AdaBoostClassifier(n_estimators = 88, random_state=0)),
9     ('lr', LogisticRegression(random_state=1)),
10    ('knn', KNeighborsClassifier(n_neighbors=4))
11 ]
12 )
13 ]
14 clf = StackingClassifier(
15     estimators=estimators, final_estimator=LogisticRegression()
16 )
17
18 clf.fit(X_train, y_train).score(X_test, y_test)
```

0.9777777777777777

# Weighted Average Probabilities (Soft Voting)

To illustrate this with a simple example, let's assume we have 3 classifiers and a 3-class classification problems where we assign equal weights to all classifiers:  $w_1=1$ ,  $w_2=1$ ,  $w_3=1$ .

The weighted average probabilities for a sample would then be calculated as follows:

<b>classifier</b>	<b>class 1</b>	<b>class 2</b>	<b>class 3</b>
classifier 1	$w_1 * 0.2$	$w_1 * 0.5$	$w_1 * 0.3$
classifier 2	$w_2 * 0.6$	$w_2 * 0.3$	$w_2 * 0.1$
classifier 3	$w_3 * 0.3$	$w_3 * 0.4$	$w_3 * 0.3$
weighted average	0.37	0.4	0.23

# Weighted Average Probabilities (Soft Voting)

```
1 from sklearn.linear_model import LogisticRegression
2 from sklearn.naive_bayes import GaussianNB
3 from sklearn.neighbors import KNeighborsClassifier
4 from sklearn.ensemble import VotingClassifier
5
6 clf1 = LogisticRegression(random_state=1)
7 clf2 = KNeighborsClassifier(n_neighbors=3)
8 clf3 = GaussianNB()
9
10 eclf = VotingClassifier(
11     estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)],
12     voting='soft', weights=[2, 2, 1])
13
14 for clf, label in zip([clf1, clf2, clf3, eclf], ['Logistic Regression', 'Random Forest', 'Naive Bayes', 'Voting Ensemble']):
15     clf.fit(X_train, y_train)
16     score = clf.score(X_test, y_test)
17     print("Accuracy: %0.4f, [%s] " % (score, label))
```

Accuracy: 0.9711, [Logistic Regression]

Accuracy: 0.9667, [Random Forest]

Accuracy: 0.7778, [Naive Bayes]

Accuracy: 0.9756, [Voting Ensemble]



# Exercise

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- To implement the instances of the Section Ensemble methods in Sklearn and try different models as base learners for stacking algorithm in the above example.
- <https://scikit-learn.org/stable/modules/ensemble.html#>