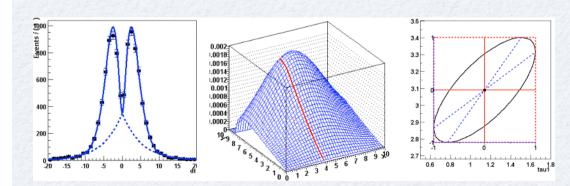
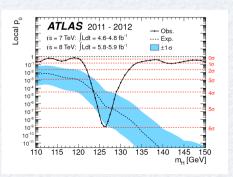
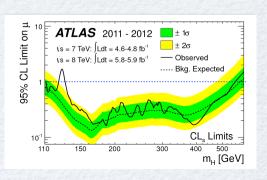
# Statistical Software Tools RooFit/RooStats

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Terascale Statistics School 2015







### Introduction

- We will cover only RooFit/RooStats
- Statistical tools for:
  - point estimation: determine the best estimate of a parameter
  - estimation of confidence (credible) intervals
    - lower/upper limits or multi-dimensional contours
  - hypothesis tests:
    - evaluation of p-value for one or multiple hypotheses (discovery significance)
- Model description and sharing of results
  - analysis combination

### Outline

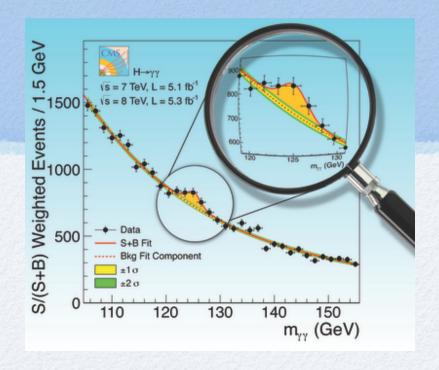
#### • Today:

- Introduction to Fitting in ROOT
- Model building and parameter estimation in RooFit
- Exercises

#### Tomorrow

- Introduction to RooStats
- Interval estimation tools (Likelihood/Bayesian)
- Hypothesis tests
- Frequentist interval/limit calculation (CLs)
- Exercises
- Thursday
  - Tutorial on building model with the HistFactory

# Introduction to Fitting in ROOT

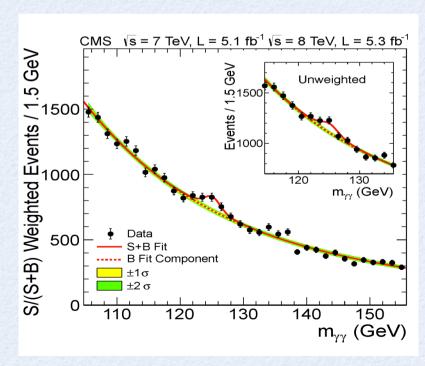


### Outline

- Introduction to Fitting:
  - fitting methods in ROOT
  - how to fit a histogram in ROOT,
  - how to retrieve the fit result.
- Building fit functions in ROOT.
- Interface to Minimization.
- Common Fitting problems.
- Using the ROOT Fit GUI (Fit Panel).

# What is Fitting?

- Estimate parameters of an hypothetical distribution from the observed data distribution
  - $y = f(x \mid \theta)$  is the fit model function
- Find the best estimate of the parameters  $\theta$  assuming f (x |  $\theta$ )



#### Example

Higgs  $\rightarrow \gamma \gamma$  spectrum We can fit for:

- the expected number of Higgs events
- the Higgs mass

# Least Square (x2) Fit

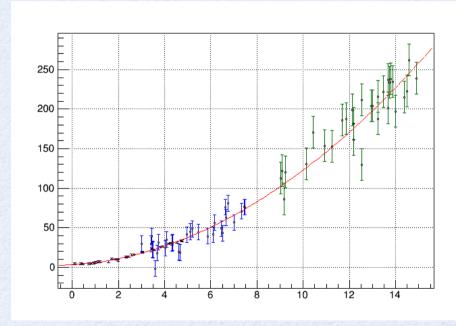
- Minimizes the deviations between the observed y and the predicted function values:
- Least square fit ( $\chi^2$ ): minimize square deviation

#### weighted by the errors

- observed errors (Neyman  $\chi^2$ )
  - $\sigma_i = \sqrt{N_i}$  for the histograms
- expected errors (Pearson  $\chi^2$ )

• 
$$\sigma_i = \sqrt{f(X_i, \theta)}$$

$$\chi^2 = \sum_{i} \frac{(Y_i - f(X_i, \theta))^2}{\sigma_i^2}$$



#### Maximum Likelihood Fit

- The parameters are estimated by finding the maximum of the likelihood function (or minimum of the negative log-likelihood function).
  - Likelihood:

$$L(x|\theta) = \prod_{i} P(x_i|\theta)$$

Find best value θ,
 the maximum of

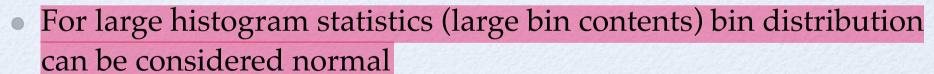
$$logL = \sum_{i} \log(f(x_i, \theta))$$

- The least-square fit and the maximum likelihood fit are equivalent when the distribution of observed events in each bin is normal.
  - $f(x \mid \theta)$  is gaussian

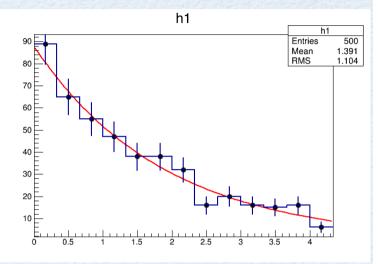
# ML Fit of an Histogram

- The Likelihood for a histogram is obtained by assuming a Poisson distribution in every bin:
  - Poisson(n<sub>i</sub> | V<sub>i</sub>)
    - **n**<sub>i</sub> is the observed bin content.
    - V<sub>i</sub> is the expected bin content,

 $V_i = f(x_i | \theta)$ , where  $x_i$  is the bin center, assuming a linear function within the bin. Otherwise it is obtained from the integral of the function in the bin.

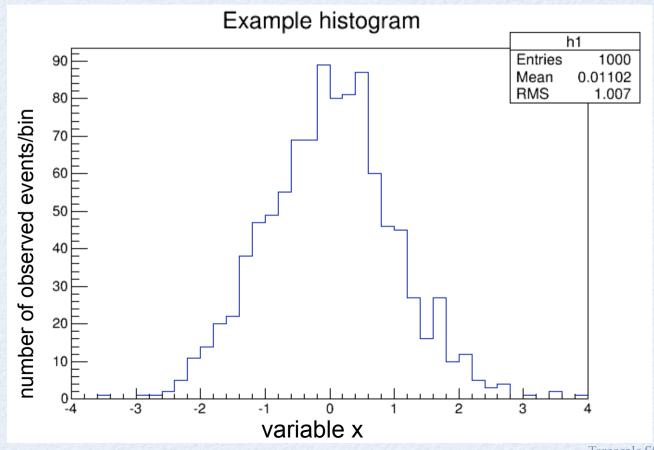


- equivalent to least square fit
- For low histogram statistics the ML method is the correct one!



# Simple Gaussian Fitting

- Suppose we have this histogram
  - we want to estimate the mean and sigma of the underlying gaussian distribution.



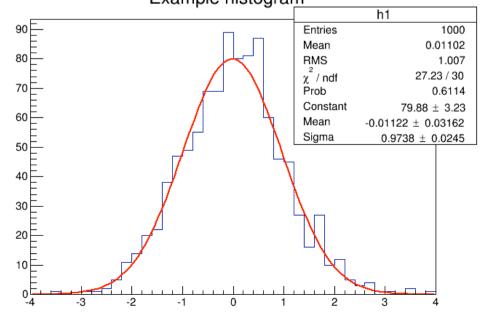
10

# Fitting Histogram

```
root [] TF1 * f1 = new TF1("f1", "gaus");
root [] f1->SetParameters(1,0,1);
root [] h1->Fit(f1);
FCN=27.2252 FROM MIGRAD
                        STATUS=CONVERGED
                                           60 CALLS
                                                           61 TOTAL
                  EDM=1.12393e-07
                                  STRATEGY= 1
                                                 ERROR MATRIX ACCURATE
 EXT PARAMETER
                                           STEP
                                                      FIRST
 NO.
       NAME
               VALUE
                              ERROR
                                           SIZE
                                                    DERIVATIVE
     Constant
               7.98760e+01
                            3.22882e+00
                                         6.64363e-03 -1.55477e-05
     Mean
               -1.12183e-02
                           3.16223e-02
                                        8.18642e-05 -1.49026e-02
                                                               Example histogram
  3 Sigma
                9.73840e-01
                            2.44738e-02
                                        1.692
```

For displaying the fit parameters:

gStyle=>SetOptFit(1111);



# Creating the Fit Function

- To create a parametric function object (a TF1):
  - we can use the available functions in ROOT library

```
TF1 * f1 = new TF1("f1","[0]*TMath::Gaus(x,[1],[2])");
```

- and also use it to write formula expressions
  - [0],[1],[2] indicate the parameters
- we can also use pre-defined functions

```
TF1 * f1 = new TF1("f1", "gaus");
```

- using pre-defined functions we have the parameter name automatically set to meaningful values.
- initial parameter values are estimated whenever possible.
- pre-defined functions avalaible:
  - gaus, expo, landau, pol0,1..,10, chebyshev

#### **Building More Complex Functions**

- Sometimes better to write directly the functions in C/C++
  - but in this case object cannot be fully stored to disk
- Using a general free function with parameters:

```
double function(double *x, double *p){
    return p[0]*TMath::Gaus(x[0],p[0],p[1]);
}
TF1 * f1 = new TF1("f1",function,xmin,xmax,npar);
```

any C++ object implementing double operator() (double \*x, double \*p)

```
struct Function {
   double operator()(double *x, double *p){
      return p[0]*TMath::Gaus(x[0],p[0],p[1]);}
};
Function func;
TF1 * f1 = new TF1("f1",&func,xmin,xmax,npar,"Function");
```

e.g using a lambda function (with Cling and C++-11)

```
auto f1 = new TF1("f1",[](double *x, double *p){return p[0]*x[0];},0,10,1);
```

# Retrieving The Fit Result

- The main results from the fit are stored in the fit function, which is attached to the histogram; it can be saved in a file (except for C/C++ functions were only points are saved).
- The fit function can be retrieved using its name:

```
TF1 * fitFunc = h1->GetFunction("f1");
```

The parameter values/error using indices (or their names):

```
fitFunc->GetParameter(par_index);
fitFunc->GetParError(par_index);
```

• It is also possible to access the TFitResult class which has all information about the fit, if we use the fit option "S":

```
TFitResultPtr r = h1->Fit(f1,"S");
r->Print();
TMatrixDSym C = r->GetCorrelationMatrix();
```

C++ Note: the TFitResult class is accessed by using operator-> of TFitResultPtr

# Some Fitting Options

• Fitting in a Range

```
h1->Fit("gaus","","",-1.5,1.5);
```

• Quite / Verbose: option "Q" / "V".

h1->Fit("gaus","V");

- Likelihood fit for histograms
  - option "L" for count histograms;

```
h1->Fit("gaus","L");
```

option "WL" in case of weighted counts.

```
h1->Fit("gaus","LW");
```

- Default is chi-square with observed errors (and skipping empty bins)
  - option "P" for Pearson chi-square (expected errors) with empty bins

```
h1->Fit("gaus","P");
```

Use integral function of the function in bin

```
h1->Fit("gaus","L I");
```

Compute MINOS errors : option "E"

```
h1->Fit("gaus","L E");
```

All fitting options documented in reference guide or User Guide (Fitting Histogram chapter)

#### Note on Binned Likelihood Fit

• Log-Likelihood is computed using Baker-Cousins procedure (Likelihood  $\chi^2$ )

$$\chi_{\lambda}^{2}(\theta) = -2 \ln \lambda(\theta) = 2 \sum_{i} [\mu_{i}(\theta) - n_{i} + n_{i} \ln(n_{i}/\mu_{i}(\theta))]$$

- $-2\ln\lambda(\theta)$  is an equivalent chi-square
- Its value at the minimum can be used for checking the fit quality
  - avoiding problems with bins with low content
- ROOT computes  $-\ln\lambda(\theta)$ 
  - retrieve it using TFitResult::MinFcnValue()

#### Parameter Errors

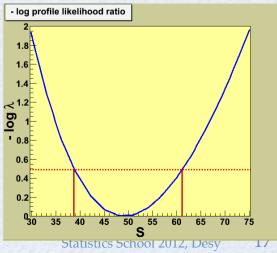
- Errors returned by the fit are computed from the second derivatives of the likelihood function
  - Asymptotically the parameter estimates are normally distributed. The estimated correlation matrix is then:

$$\mathbf{\hat{V}}(\boldsymbol{\hat{\theta}}) = \left[ \left( -\frac{\partial^2 \ln L(\mathbf{x}; \boldsymbol{\theta})}{\partial^2 \boldsymbol{\theta}} \right)_{\boldsymbol{\theta} = \boldsymbol{\hat{\theta}}} \right]^{-1} = \mathbf{H}^{-1}$$

• A better approximation to estimate the confidence level in the parameter is to use directly the log-likelihood function and look at the difference from the minimum.

- Method of Minuit/Minos (Fit option "E")
  - obtain a confidence interval which is in general not symmetric around the best parameter estimate

```
TFitResultPtr r = h1->Fit(f1,"E S");
r->LowerError(par_number);
r->UpperError(par_number);
```



#### Minimization

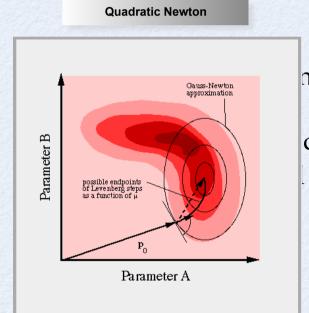
- The fit is done by minimizing the least-square or likelihood function.
- A direct solution exists only in case of linear fitting
  - it is done automatically in such cases (e.g fitting polynomials).
- Otherwise an iterative algorithm is used:
  - Minuit is the minimization algorithm used by default
    - ROOT provides two implementations: Minuit and Minuit2
    - other algorithms exists: Fumili, or minimizers based on GSL, genetic and simulated annealing algorithms
  - To change the minimizer:

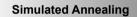
```
ROOT::Math::MinimizerOptions::SetDefaultMinimizer("Minuit2");
```

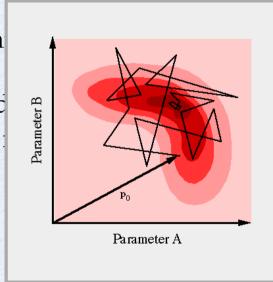
 Other commands are also available to control the minimization:

```
ROOT::Math::MinimizerOptions::SetDefaultTolerance(1.E-6);
```

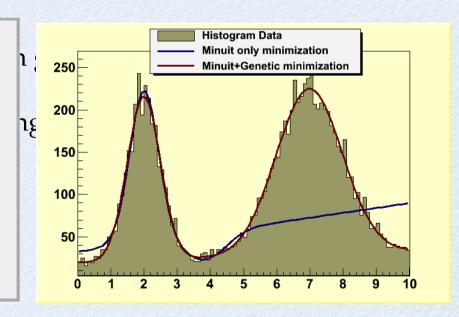
# Minimization Techniques







#### Example: Fitting 2 peaks in a spectrum



#### **Function Minimization**

- Common interface class (ROOT::Math::Minimizer)
- Existing implementations available as plug-ins:
  - Minuit (based on class TMinuit, direct translation from Fortran code)
    - with Migrad, Simplex, Minimize algorithms
  - Minuit2 (new C++ implementation with OO design)
    - with Migrad, Simplex, Minimize and Fumili2
  - Fumili (only for least-square or log-likelihood minimizations)
  - **GSLMultiMin**: conjugate gradient minimization algorithm from GSL (Fletcher-Reeves, BFGS)
  - GSLMultiFit: Levenberg-Marquardt (for minimizing least square functions) from GSL
  - Linear for least square functions (direct solution, non-iterative method)
  - **GSLSimAn**: Simulated Annealing from GSL
  - Genetic: based on a genetic algorithm implemented in TMVA
- All these are available for ROOT fitting and in RooFit/RooStats
- Possible to combine them (e.g. use Minuit and Genetic)
- Easy to extend and add new implementations
  - e.g. minimizer based on NagC exists in the development branch (see <a href="here">here</a>)

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20

#### Comments on Minimization

- Sometimes fit converges to a wrong solution
  - Often is the case of a local minimum which is not the global one.
    - This is often solved with better initial parameter values. A minimizer like Minuit is able to find only the local best minimum using the function gradient.
    - Otherwise one needs to use a genetic or simulated annealing minimizer (but it can be quite inefficient, e.g. many function calls).
- Sometimes fit does not converge

```
Warning in <Fit>: Abnormal termination of minimization.
```

- can happen because the Hessian matrix is not positive defined
  - e.g. there are no minimum in that region →wrong initial parameters;
- numerical precision problems in the function evaluation
  - need to check and re-think on how to implement better the fit model function;
- highly correlated parameters in the fit. In case of 100% correlation the point solution becomes a line (or an hyper-surface) in parameter space. The minimization problem is no longer well defined.

```
PARAMETER CORRELATION COEFFICIENTS

NO. GLOBAL 1 2

1 0.99835 1.000 0.998
2 0.99835 0.998 1.000

Signs of trouble...
```

### Mitigating fit stability problems

- When using a polynomial parametrization:
  - $a_0+a_1x+a_2x^2+a_3x^3$  nearly always results in strong correlations between the coefficients.
    - problems in fit stability and inability to find the right solution at high order
- This can be solved using a better polynomial parametrization:
  - e.g. Chebychev polynomials

$$T_0(x) = 1$$

$$T_1(x) = x$$

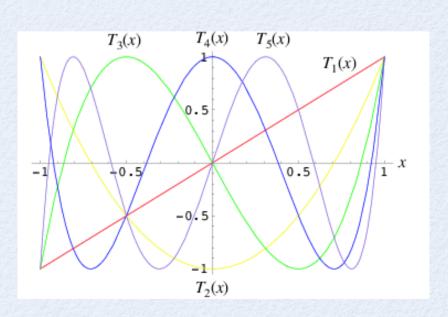
$$T_2(x) = 2x^2 - 1$$

$$T_3(x) = 4x^3 - 3x$$

$$T_4(x) = 8x^4 - 8x^2 + 1$$

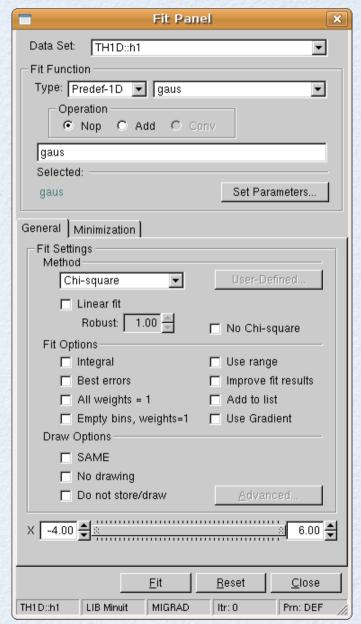
$$T_5(x) = 16x^5 - 20x^3 + 5x$$

$$T_6(x) = 32x^6 - 48x^4 + 18x^2 - 1$$



### The Fit Panel

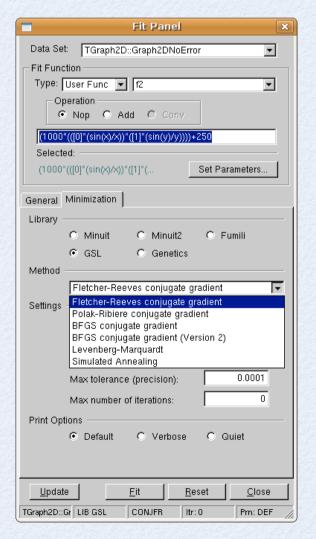
- The fitting in ROOT using the FitPanel GUI
  - GUI for fitting all ROOT data objects (histogram, graphs, trees)
- Using the GUI we can:
  - select data object to fit
  - choose (or create) fit model function
  - set initial parameters
  - choose:
    - fit method (likelihood, chi2)
    - fit options (e.g Minos errors)
    - drawing options
  - change the fit range



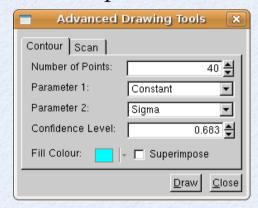
## Fit Panel (2)

The Fit Panel provides also extra functionality:

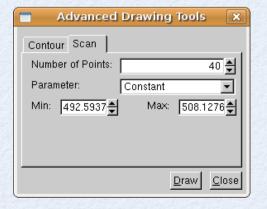
Control the minimization



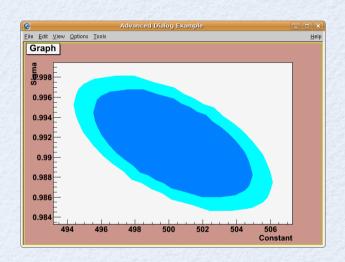
Contour plot

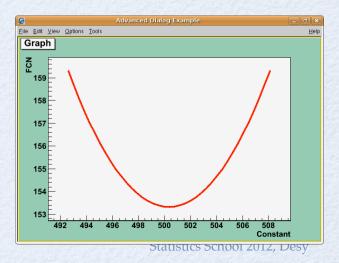


Scan plot of minimization function

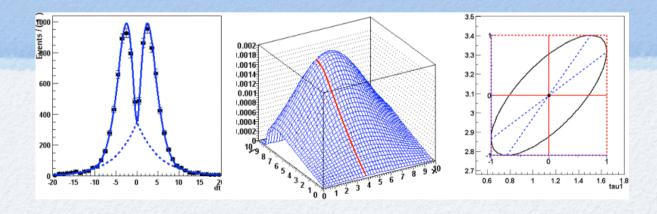


Advanced drawing tools





# RooFit



### Outline

- Introduction to RooFit
  - Basic functionality
  - Model building using the workspace
  - Composite models

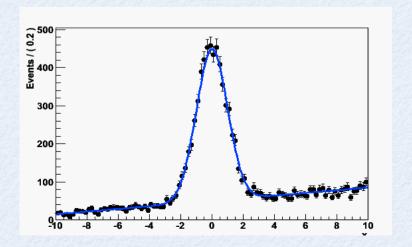
Material based on slides from W. Verkerke (author of RooFit)

26

- Exercises on RooFit:
  - building and fitting model

#### RooFit

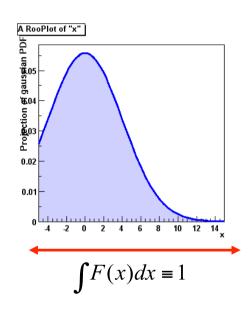
- Toolkit for data modeling
  - developed by W. Verkerke and D. Kirkby
- model distribution of observable x in terms of parameters p
  - probability density function (pdf): P(x;p)
- pdf are normalized over allowed range of observables
   x with respect to the parameters p

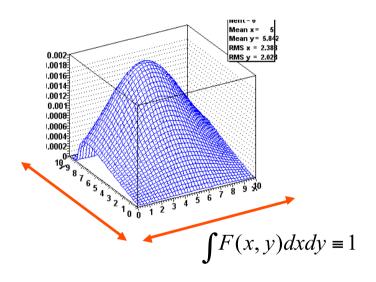


#### Mathematic - Probability density functions

- Probability Density Functions describe probabilities, thus
  - All values most be >0
  - The total probability must be 1 for each p, i.e.
  - Can have any number of dimensions

$$\int_{\vec{x}_{\min}}^{\vec{x}_{\max}} g(\vec{x}, \vec{p}) d\vec{x} = 1$$





- Note distinction in role between parameters (p) and observables (x)
  - Observables are measured quantities
  - Parameters are degrees of freedom in your model

# Why RooFit?

- ROOT function framework can handle complicated functions
  - but require writing large amount of code
- Normalization of p.d.f. not always trivial
  - RooFit does it automatically
- In complex fit, computation performance important
  - need to optimize code for acceptable performance
  - built-in optimization available in RooFit
    - evaluation only when needed
- Simultaneous fit to different data samples
- Provide full description of model for further use

#### RooFit

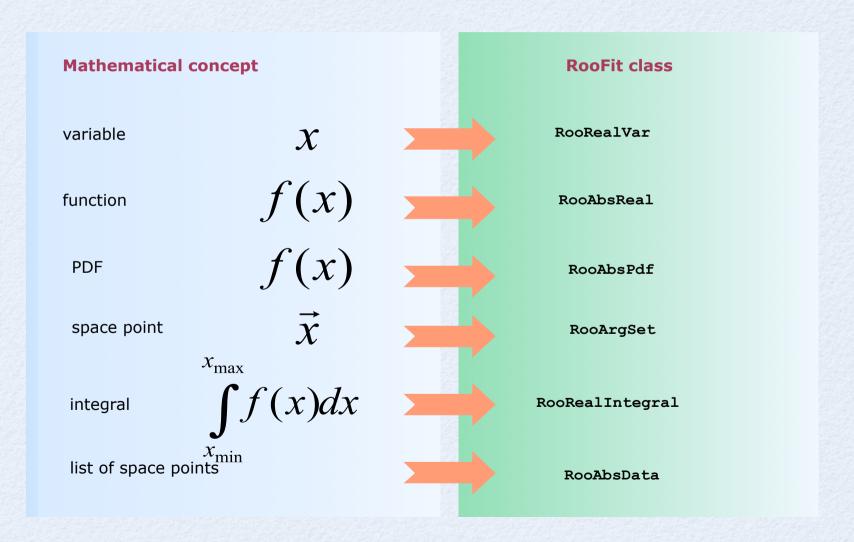
- RooFit provides functionality for building the pdf's
  - complex model building from standard components
  - composition with addition product and convolution
- All models provide the functionality for
  - maximum likelihood fitting
  - toy MC generator
  - visualization

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30

# RooFit Modeling

Mathematical concepts are represented as C++ objects



# RooFit Modeling

Gaus(x,m,s)Example: Gaussian pdf RooGaussian q RooRealVar x RooRealVar s RooRealVar m RooRealVar x("x","x",2,-10,10) RooRealVar s("s","s",3) ; RooFit code: RooRealVar m("m","m",0) ;

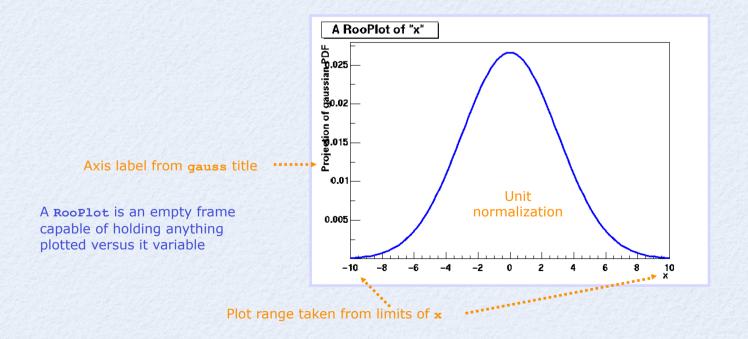
> Represent relations between variables and functions as client/server links between objects

RooGaussian q("q","q",x,m,s)

# RooFit Functionality

pdf visualization

```
RooPlot * xframe = x->frame();
pdf->plotOn(xframe);
xframe->Draw();
```



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33

# RooFit Functionality

Toy MC generation from any pdf

Generate 10000 events from Gaussian p.d.f and show distribution

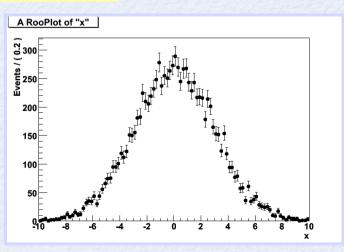
```
RooDataSet * data = pdf->generate(*x,10000);
```

data visualization

```
RooPlot * xframe = x->frame();
data->plotOn(xframe);
xframe->Draw();
```

Note that dataset is *unbinned* (vector of data points, x, values)

Binning into histogram is performed in data->plotOn() call



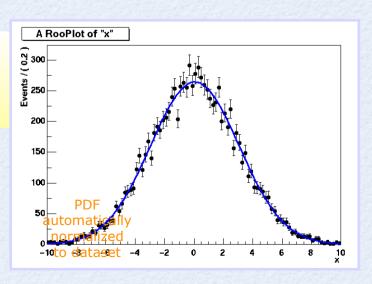
# RooFit Functionality

- Fit of model to data
  - e.g. unbinned maximum likelihood fit

```
pdf = pdf->fitTo(data);
```

data and pdf visualization after fit

```
RooPlot * xframe = x->frame();
data->plotOn(xframe);
pdf->plotOn(xframe);
xframe->Draw();
```



35

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### RooFit Workspace

- RooWorkspace class: container for all objected created:
  - full model configuration
    - PDF and parameter/observables descriptions
    - uncertainty/shape of nuisance parameters
  - (multiple) data sets
- Maintain a complete description of all the model
  - possibility to save entire model in a ROOT file
  - all information is available for further analysis
- Combination of results joining workspaces in a single one
  - common format for combining and sharing physics results

```
RooWorkspace workspace("w");
workspace.import(*data);
workspace.import(*pdf);
workspace.writeToFile("myWorkspace.root")
```

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36

# RooFit Factory

```
RooRealVar x("x","x",2,-10,10)
RooRealVar s("s","s",3);
RooRealVar m("m","m",0);
RooGaussian g("g","g",x,m,s)
```

The workspace provides a factory method to autogenerates objects from a math-like language (the p.d.f is made with 1 line of code instead of 4)

```
RooWorkspace w;
w.factory("Gaussian::g(x[2,-10,10],m[0],s[3])")
```

In the tutorial we will work using the workspace factory to build models

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37

## Using the workspace

- Workspace
  - A generic container class for all RooFit objects of your project
  - Helps to organize analysis projects
- Creating a workspace

```
RooWorkspace w("w") ;
```

- Putting variables and function into a workspace
  - When importing a function or pdf, all its components (variables) are automatically imported too

```
RooRealVar x("x","x",-10,10) ;
RooRealVar mean("mean","mean",5) ;
RooRealVar sigma("sigma","sigma",3) ;
RooGaussian f("f","f",x,mean,sigma) ;

// imports f,x,mean and sigma
w.import(f) ;
```

## Using the workspace

Looking into a workspace

```
w.Print();

variables
-----
(mean, sigma, x)

p.d.f.s
-----
RooGaussian::f[ x=x mean=mean sigma=sigma ] = 0.249352
```

Getting variables and functions out of a workspace

```
// Variety of accessors available
RooRealVar * x = w.var("x");
RooAbsPdf * f = w.pdf("f");
```

Writing workspace and contents to file

```
w.writeToFile("wspace.root") ;
```

## Factory syntax

• Rule #1 – Create a variable

• Rule #2 – Create a function or pdf object

```
ClassName::Objectname(arg1,[arg2],...)
```

- Leading 'Roo' in class name can be omitted
- Arguments are names of objects that already exist in the workspace
- Named objects must be of correct type, if not factory issues error
- Set and List arguments can be constructed with brackets {}

### Factory syntax

- Rule #3 Each creation expression returns the name of the object created
  - Allows to create input arguments to functions 'in place' rather than in advance

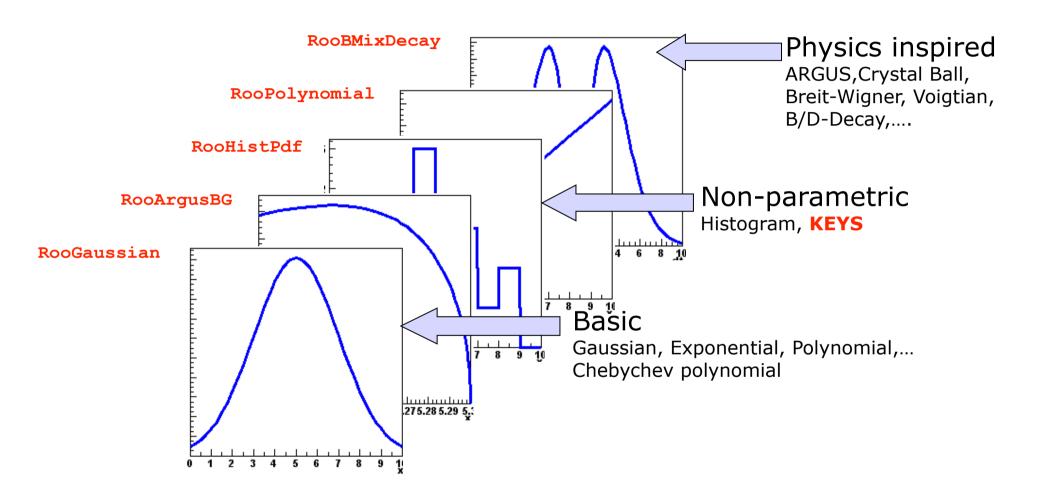
- Miscellaneous points
  - You can always use numeric literals where values or functions are expected
  - It is not required to give component objects a name, e.g.

```
Gaussian::g(x[-10,10],0,3)
```

```
SUM::model(0.5*Gaussian(x[-10,10],0,3),Uniform(x));
```

#### Model building – (Re)using standard components

RooFit provides a collection of compiled standard PDF classes



Easy to extend the library: each p.d.f. is a separate C++ class

42

## Model building – (Re)using standard components

List of most frequently used pdfs and their factory spec

```
Gaussian
                      Gaussian::q(x,mean,sigma)
Breit-WignerBreitWigner::bw(x,mean,gamma)
Landau
                        Landau::1(x,mean,sigma)
Exponential
                  Exponential::e(x,alpha)
Polynomial
                   Polynomial::p(x,{a0,a1,a2})
Chebychev
                     Chebychev::p(x, \{a0, a1, a2\})
Kernel Estimation
                     KeysPdf::k(x,dataSet)
Poisson
                       Poisson::p(x,mu)
Voigtian
                     Voigtian::v(x,mean,gamma,sigma)
(=BW\otimes G)
```

## Factory syntax – using expressions

Customized p.d.f from interpreted expressions

```
w.factory("EXPR::mypdf('sqrt(a*x)+b',x,a,b)");
```

Customized class, compiled and linked on the fly

```
w.factory("CEXPR::mypdf('sqrt(a*x)+b',x,a,b)") ;
```

re-parametrization of variables (making functions)

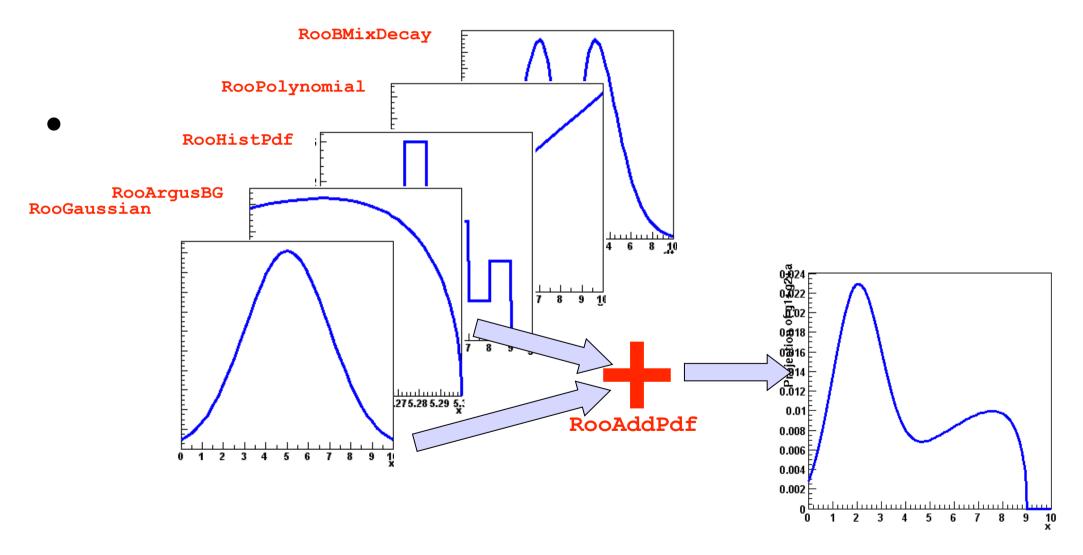
```
w.factory("expr::w('(1-D)/2',D[0,1])");
```

- note using expr (builds a function, a RooAbsReal)
- instead of EXPR (builds a pdf, a RooAbsPdf)

This usage of upper vs lower case applies also for other factory commands (SUM, PROD,....)

#### Model building – (Re)using standard components

- Most realistic models are constructed as the sum of one or more p.d.f.s (e.g. signal and background)
- Facilitated through operator p.d.f RooAddPdf



## Factory syntax: Adding p.d.f.

Additions of PDF (using fractions)

SUM::name(frac1\*PDF1,PDFN)

SUM: :name (frac1\*PDF1, frac2\*PDF2, ..., PDFN)

Note that last PDF does not have an associated fraction

$$F(x) = f \times S(x) + (1 - f)B(x)$$
 ;  $N_{\text{exp}} = N$ 

PDF additions (using expected events instead of fractions)

SUM::name(Nsig\*SigPDF,Nbkg\*BkgPDF)

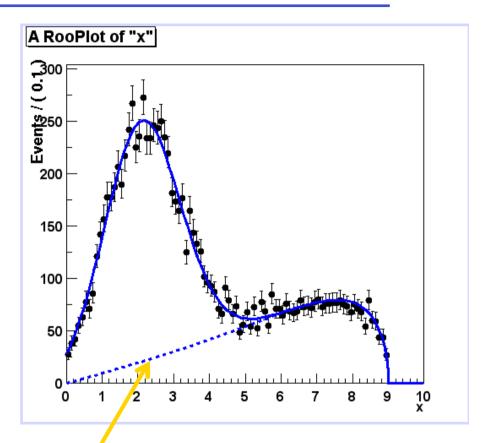
$$F(x) = \frac{N_S}{N_S + N_B} \times S(x) + \frac{N_B}{N_S + N_B} B(x)$$
;  $N_{\text{exp}} = N_S + N_B$ 

- the resulting model will be extended
- the likelihood will contain a Poisson term depending on the total number of expected events (Nsig+Nbkg)

$$L(x \mid p) \rightarrow L(x \mid p) Poisson(N_{obs}, N_{exp})$$

## Component plotting - Introduction

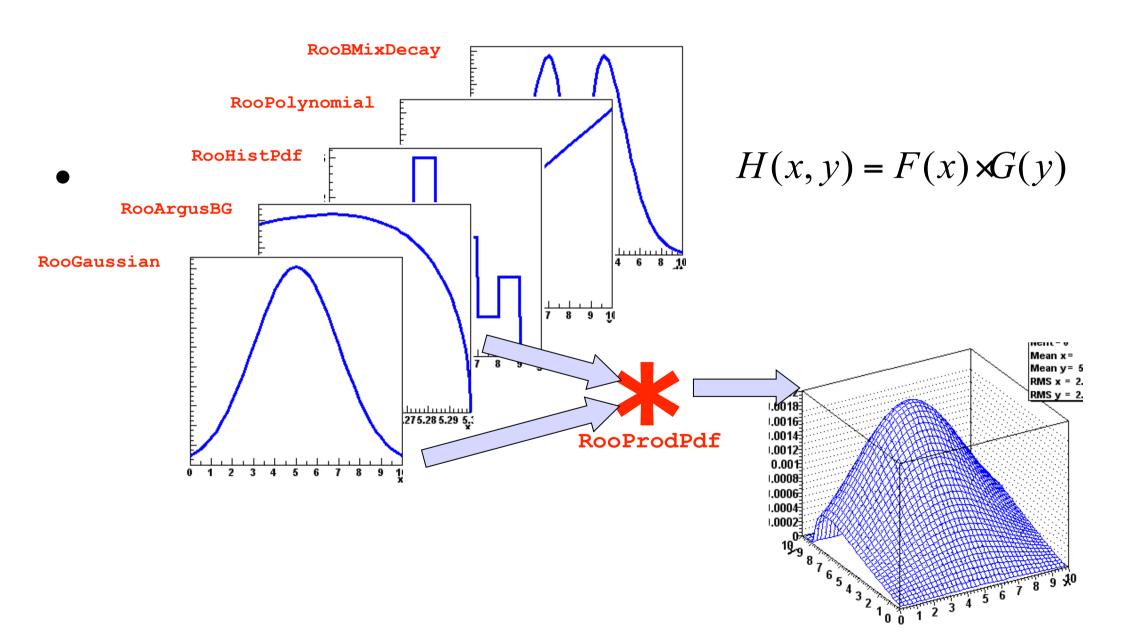
- Plotting, toy event generation and fitting works identically for composite p.d.f.s
  - Several optimizations applied behind the scenes that are specific to composite models (e.g. delegate event generation to components)
- Extra plotting functionality specific to composite pdfs
  - Component plotting



```
// Plot only argus components
w::sum.plotOn(frame, Components("argus"), LineStyle(kDashed));

// Wildcards allowed
w::sum.plotOn(frame, Components("gauss*"), LineStyle(kDashed));
```

## Model building – Products of uncorrelated p.d.f.s



#### Uncorrelated products - Mathematics and constructors

 Mathematical construction of products of uncorrelated p.d.f.s is straightforward

 $H(x,y) = F(x) \times G(y) \qquad H(x^{\{i\}}) = \prod_{i} F^{\{i\}}(x^{\{i\}})$ 

- No explicit normalization required → If input p.d.f.s are unit normalized, product is also unit normalized
- (Partial) integration and toy MC generation automatically uses factorizing properties of product, e.g. is deduced from structure.  $\int H(x,y)dx = G(y)$
- Corresponding factory operator is PROD

```
w.factory("Gaussian::gx(x[-5,5],mx[2],sx[1])") ;
w.factory("Gaussian::gy(y[-5,5],my[-2],sy[3])") ;
w.factory("PROD::gxy(gx,gy)") ;
```

## Introducing correlations through composition

- RooFit pdf building blocks do not require variables as input, just real-valued functions
  - Can substitute any variable with a function expression in parameters and/or observables

$$f(x; p) \Rightarrow f(x, p(y,q)) = f(x, y; q)$$

- Example: Gaussian with shifting mean

```
w.factory("expr::mean('a*y+b',y[-10,10],a[0.7],b[0.3])");
w.factory("Gaussian::g(x[-10,10],mean,sigma[3])");
```

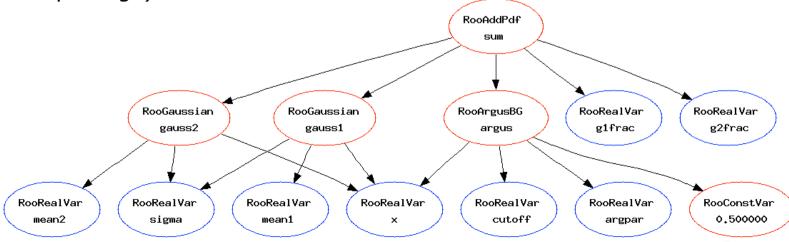
 No assumption made in function on a,b,x,y being observables or parameters, any combination will work

## Operations on specific to composite pdfs

Tree printing mode of workspace reveals component structure –
 w.Print("t")

```
RooAddPdf::sum[ glfrac * gl + g2frac * g2 + [%] * argus ] = 0.0687785
RooGaussian::gl[ x=x mean=mean1 sigma=sigma ] = 0.135335
RooGaussian::g2[ x=x mean=mean2 sigma=sigma ] = 0.011109
RooArgusBG::argus[ m=x m0=k c=9 p=0.5 ] = 0
```

- Can also make input files for GraphViz visualization
  (w.pdf("sum")->graphVizTree("myfile.dot"))
- Graph output on ROOT Canvas in near future (pending ROOT integration of GraphViz package)



## Constructing joint pdfs (RooSimultaneous)

- Operator class SIMUL to construct joint models at the pdf level
  - need a discrete observable (category) to label the channels

```
// Pdfs for channels 'A' and 'B'
w.factory("Gaussian::pdfA(x[-10,10],mean[-10,10],sigma[3])");
w.factory("Uniform::pdfB(x)");

// Create discrete observable to label channels
w.factory("index[A,B]");

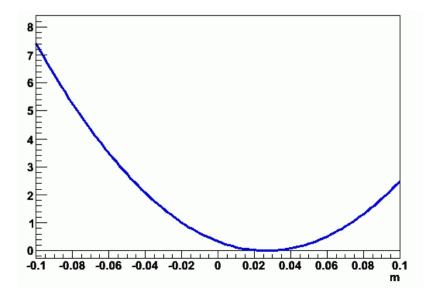
// Create joint pdf (RooSimultaneous)
w.factory("SIMUL::joint(index,A=pdfA,B=pdfB)");
```

- Construct joint datasets
  - contains observables ("x") and category ("index")

## Constructing the likelihood

- So far focus on construction of pdfs, and basic use for fitting and toy event generation
- Can also explicitly construct the likelihood function of and pdf/ data combination
  - Can use (plot, integrate) likelihood like any RooFit function object

```
RooAbsReal* nll = pdf->createNLL(data) ;
RooPlot* frame = parameter->frame() ;
nll->plotOn(frame,ShiftToZero()) ;
```



## Constructing the likelihood

- Example Manual MIMIZATION using MINUIT
  - Result of minimization are immediately propagated to RooFit variable objects (values and errors)

- Also other minimizers (Minuit, GSL etc) supported
- N.B. Different minimizer can also be used from RooAbsPdf::fitTo

```
//fit a pdf to a data set using Minuit2 as minimizer
pdf.fitTo(*data, RooFit::Minimizer("Minuit2","Migrad")) ;
```

## Basics - Importing data

Unbinned data can also be imported from ROOT TTrees

```
// Import unbinned data
RooDataSet data("data","data",x,Import(*myTree));
```

- Imports TTree branch named "x".
- Can be of type Double\_t, Float\_t, Int\_t or UInt\_t.
   All data is converted to Double\_t internally
- Specify a RooArgSet of multiple observables to import multiple observables
- Binned data can be imported from ROOT THX histograms

```
// Import binned data
RooDataHist data("data","data",x,Import(*myTH1)) ;
```

- Imports values, binning definition and SumW2 errors (if defined)
- Specify a RooArgList of observables when importing a TH2/3.

Wouter Verkerke, NIKHEF 55

# RooFit Summary

- Overview of RooFit functionality
  - not everything covered
  - not discussed on how it works internally (optimizations, analytical deduction, etc..)
- Capable to handle complex model
  - scale to models with large number of parameters
  - being used for many analysis at LHC
- Workspace:
  - easy model creation using the factory syntax
  - tool for storing and sharing models (analysis combination)

## RooFit Documentation

- Starting point: <a href="http://root.cern.ch/drupal/content/roofit">http://root.cern.ch/drupal/content/roofit</a>
- Users manual (134 pages ~ 1 year old)
- Quick Start Guide (20 pages, recent)
- Link to 84 tutorial macros (also in \$ROOTSYS/tutorials/roofit)
- More than 200 slides from W. Verkerke documenting all features are available at the French School of Statistics 2008
  - http://indico.in2p3.fr/getFile.py/access?contribId=15&resId=0&materialId=slides&confId=750

L. Moneta Terascale Statistics School 2015

57

## Time For Exercises!

Follow the RooFit exercises at the Twiki page: <a href="https://twiki.cern.ch/twiki/bin/view/RooStats/RooStatsTutorialsMarch2015">https://twiki.cern.ch/twiki/bin/view/RooStats/RooStatsTutorialsMarch2015</a>