

MATH 424: Final Homework

Due on Wednesday, December 20, 2017

Kafai 11:10am

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Contents

Q1. Consider the data in q1data.txt. All subjects are asthmatics. For the model with Forced Expiratory Volume (FEV) as the response and Height, Weight, and Age as the predictors,

- Examine a plot of the studentized or jackknife residuals versus the predicted values. Are any regression assumption violations apparent? If so, suggest possible remedies.
- Examine numerical descriptive statistics, histograms, box-and-whisker plots, and normal probability plots of jackknife residuals. Is the normality assumption violated? If so, suggest possible remedies.
- Examine outlier diagnostics, including Cook's distance, leverage statistics, and jackknife residuals, and identify any potential outliers. What course of action, if any, should be taken when outliers are identified?
- Examine variance inflation factors, condition indices (unadjusted and adjusted for the intercept), and variance proportions. Are there any important collinearity problems? If so, suggest possible remedies.

Q2. A random sample of data was collected on residential sales in a large city. The data in q2data.txt shows the selling price (Y, in \$1,000s), area (x1, in hundreds of square feet), number of bedrooms (X2), total number of rooms (X3), house age (X4, in years), and location (Z = 0 for in-town and inner suburbs, Z=1 for outer suburbs). In parts a through c, use variables X1, X2, X3, X4, and Z as the predictor variables.

- Use the all possible regressions procedure to suggest a best model.
- Use the stepwise regression algorithm to suggest a best model.
- Use the backward elimination algorithm to suggest a best model.
- Which of the models selected in a, b, and c seems to be the best model, and why?

Q3. The data listed in q3data.txt relate to a study by Reiter and others concerning the effects of injecting triethyl-tin (TET) into rats once at age 5 days. The animals were injected with 0, 3, or 6 mg per kilogram of body weight. The response was the log of the activity count, log (ac), for 1 hour, recorded at 21 days of age. The rat was left to move about freely in a figure 8 maze. Analysis of other studies with this type of activity count confirms that log counts should yield Gaussian errors if the model is correct.

- Conduct a two-way ANOVA with SEX and DOSAGE as factors.
- Using $\alpha = .05$, report your conclusions based on the ANOVA.
- Which, if any, families of means should be followed up with multiple-comparison tests? What type of comparisons would you recommend?

Q4. The data in q4data.txt is the record of coronary artery disease (ca, 0=no, 1= yes), age, ECG (0, 1, and 2 based on the reading of ST segment depression), and sex (0=male, 1=female). Based on this model

- What is the estimated logistic regression model for the relationship between ca and age, ECG, sex?
- What is a 30-year-old male, ECG=2 predicted probability of having coronary artery disease?
- Estimate the odds ratio comparing a 30-year-old male, ECG=2 to a 31-year-old male, ECG=2. Interpret this estimated odds ratio.
- Find a 95% confidence interval for the population odds ratio being estimated in part (c).