Integration Problem Set

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Techniques:

- 1. Definite Integrals
- 2. Indefinite Integrals
- 3. Improper Integrals
- 4. U-Substitution
- 5. Integration by Parts
- 6. Partial Fractions
- 7. Improper Integrals
- 8. Reduction Formulas

Instructions

Solve the following integrals using appropriate techniques. Clearly state the method used and show all steps in your solution.

Problem Set

1.

$$\int x \sin(x^2) \, dx$$

2.

$$\int \frac{x}{\sqrt{x^2 + 4}} \, dx$$

3.

$$\int (2x+1)e^{x^2+x} \, dx$$

4.

$$\int \frac{x}{1+x^2} \, dx$$

5.

$$\int_0^{\frac{\pi}{2}} \cos^2(x) \, dx$$

6.

$$\int_{1}^{4} \frac{1}{x+2} dx$$

7.

 $\int_0^1 e^{x^2} dx$

8.

 $\int_{-1}^{1} x^3 \cos(x) \, dx$

9.

 $\int x \sin(x^2) \, dx$

10.

 $\int \frac{x}{\sqrt{x^2 + 4}} \, dx$

11.

 $\int (2x+1)e^{x^2+x} \, dx$

12.

 $\int \frac{x}{1+x^2} \, dx$

13.

 $\int xe^x \, dx$

14.

 $\int x \ln(x) \, dx$

15.

 $\int x^2 e^x \, dx$

16.

 $\int \arctan(x) \, dx$

17.

 $\int \frac{2x+3}{(x-1)(x+2)} \, dx$

18.

 $\int \frac{x+1}{x^2-x-6} \, dx$

19.

 $\int \frac{3x^2 + 5x + 2}{(x-1)(x+1)(x+3)} \, dx$

20.

 $\int \frac{4x+1}{x^2+x-2} \, dx$

21.

 $\int_{1}^{\infty} \frac{1}{x^2} \, dx$

22.

 $\int_{0}^{\infty} e^{-x} dx$

23.

24.

24.

25.

26.

28.

27.

29.

30.

31.

32.

33.

34.

35.

36.

37.

 $\int_0^1 \frac{1}{\sqrt{1-x^2}} \, dx$

 $\int_{-\infty}^{0} e^x \, dx$

 $\int x^n e^x \, dx$

 $\int \cos^n(x) \, dx$

 $\int x^n e^{-x} \, dx$

 $\int x^n \ln(x) \, dx$

 $\int_{1}^{\infty} \frac{1}{x^3} \, dx$

 $\int_0^\infty e^{-x} \cos(x) \, dx$

 $\int_0^1 \frac{1}{\sqrt{1-x^2}} \, dx$

 $\int_{-\infty}^{0} e^{x} dx$

 $\int_0^\infty \frac{\sin x}{x} \, dx$

 $\int_0^1 \frac{x-1}{\ln x} \, dx$

 $\int_{-\infty}^{\infty} \frac{\cos x}{x^2 + 2} \, dx$

 $\int_0^1 \frac{\sin \ln x}{\ln x} \, dx$

 $\int \frac{1}{\left(1+x\right)^2} \, dx$