## **Diffraction Grating**

Lab: 06

Jaden Moore

Diffraction Grating Lab: 06

## 1 Introduction

In this lab, we measure the distance between the slits on a diffraction grating glass slide by analyzing the diffraction pattern projected onto a screen and compare it to the theoretical value. We then experimentally measure the distance between bright spots and the central bright maxima and compare it to the theoretical values.

## 2 The Spacing for a Diffraction Grating

Consider the experiment provided by Physlet® Physics Exploration 38.2: Diffraction Grating. The location of the intensity maxima on a screen created by any diffraction grating is calculated such that

$$dsin(\theta) = m\lambda_{light} \tag{1}$$

Where d is the distance between adjacent slits. We set the experiment up such that the distance between slits is  $d_{theory} = 3663 \,\mathrm{nm}$ . That is, there are 273 slits per millimeter. Thus, we can experimentally calculate the distance between slits such that

$$d = \frac{m\lambda_{light}}{sin(\theta)} \tag{2}$$

Where m = 1,2. Below we put into a table the experimental data gathered from different wavelengths of light.

| Table 1: Diffraction Pattern Data |                |                       |                     |                     |                |  |  |  |
|-----------------------------------|----------------|-----------------------|---------------------|---------------------|----------------|--|--|--|
| $\lambda \text{ [nm]}$            | $\theta_1$ [°] | $\theta_2 \ [^\circ]$ | $d_1 [\mathrm{nm}]$ | $d_2 [\mathrm{nm}]$ | $d_{avg}$ [nm] |  |  |  |
| 589                               | 9.2            | 18.8                  | 3683.99             | 3655.37             | 3669.68        |  |  |  |
| 505                               | 8.0            | 16.0                  | 3628.58             | 3664.24             | 3646.405       |  |  |  |
| 470                               | 7.3            | 15.0                  | 3649.19             | 3631.88             | 3640.54        |  |  |  |

Thus, we can calculate  $d_{exp}$  by taking the average of the  $d_{avg}$  values for each wavelength in Table 1. That is,

$$d_{exp} = \frac{3669.68 + 3646.41 + 3640.54}{3} = 3652.21 \,\text{nm} \tag{3}$$

We can then calculate the percent error between the theoretical distance  $d_{theory}$  and the experimental value such that

$$\% \text{ error} = \left(\frac{d_{exp} - d_{theory}}{d_{theory}}\right) 100 = \left(\frac{3652.21nm - 3663nm}{3663nm}\right) 100 = 0.295\%$$
 (4)

## 3 Measuring the Location of the Diffraction Maxima

From the experiment, we can calculate the distance between the central bright maxima and any other diffraction maxima that corresponds to the mth bright fringe. If we let x be the distance from the middle grating to the central bright maximum, we can calculate the distance such that

$$y_m = x tan(\theta_m) \tag{5}$$

Using the previous case of yellow light where  $\lambda = 589 \,\mathrm{nm}$ , and taking the distance between the grating and the screen  $x = 500 \,\mathrm{cm}$ . We can compare the theoretical distances  $y_m$  to the experimental distances. Below we into a table the locations of the diffraction maxima for yellow light.

| Table 1: Diffraction Pattern Data |    |                       |                     |                  |          |  |  |  |
|-----------------------------------|----|-----------------------|---------------------|------------------|----------|--|--|--|
| x [cm]                            | m  | $\theta_m \ [^\circ]$ | $y_{m-theory}$ [cm] | $y_{m-exp}$ [cm] | % error  |  |  |  |
| 500                               | 2  | 9.2                   | 82.774              | 3655.37          | 3669.68  |  |  |  |
| 500                               | 1  | 18.8                  | 3628.58             | 3664.24          | 3646.405 |  |  |  |
| 500                               | -1 | 9.4                   | 3649.19             | 3631.88          | 3640.54  |  |  |  |
| 500                               | -2 | 18.8                  | 3649.19             | 3631.88          | 3640.54  |  |  |  |