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# Improvements in the high-energy lepton propagator PROPOSAL

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E5b

## Introduction

- **PROPOSAL:** Tool to propagate charged leptons
  - MC simulations, multivariate statistics
- **Requirements:** Accuracy, performance
- **Processes:** Energy losses, scattering, decays
- Possibility to use **different parametrizations**
  - Study **systematic uncertainties**
- C++ library with Python bindings



<https://github.com/tudo-astroparticlephysics/PROPOSAL>

## Propagation

$$\frac{d\sigma}{dv} \quad \underbrace{\longrightarrow}_{?} \quad \text{energy losses}$$

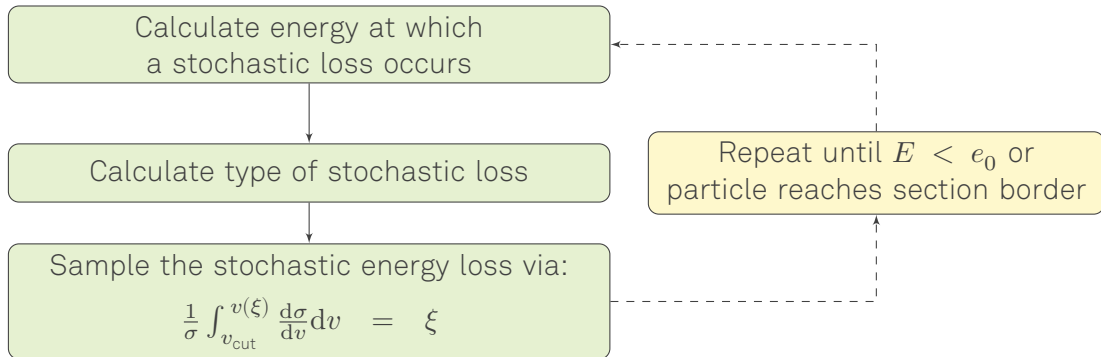
## Propagation

$v < v_{\text{cut}}$   
continuous losses

$v > v_{\text{cut}}$   
stochastic losses

with  $v_{\text{cut}} = \min [e_{\text{cut}}/E, v'_{\text{cut}}]$

## Propagation

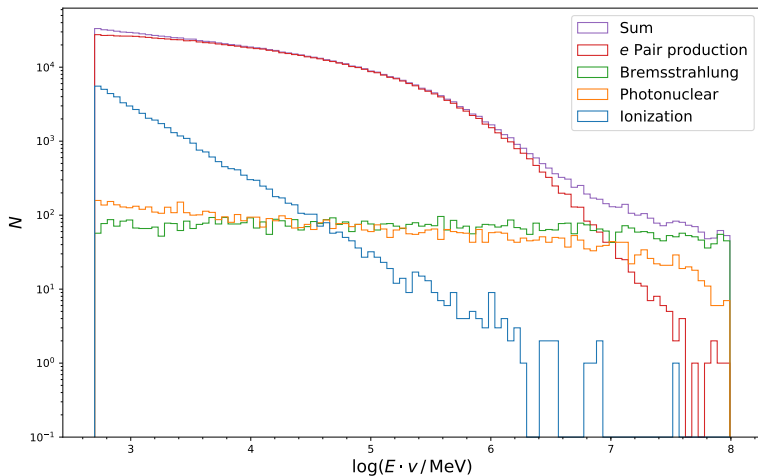


### Standard interactions:

- $e$  pair production
- Bremsstrahlung
- Photonuclear
- Ionization

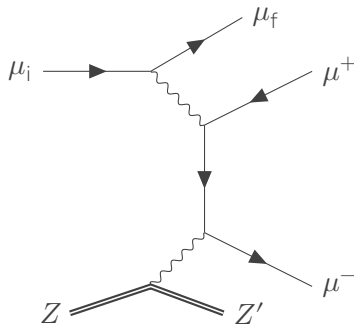
### Rare interactions:

- $\mu$  pair production
- Weak interaction
- Negligible contribution to overall energy loss
- Observable, interesting signature



Propagation of  $10^4$  muons with energy  $10^8$  MeV through 100 m of standard rock.

## Direct Production of Muon Pairs



Energy fraction transferred to the muon pair:

$$v = \frac{(\epsilon_+ + \epsilon_-)}{E}$$

Asymmetry parameter:

$$\rho = \frac{(\epsilon_+ - \epsilon_-)}{(\epsilon_+ + \epsilon_-)}$$

$E$ : Initial energy of the incoming muon  $\mu_i$

$\epsilon_{\pm}$ : Energy of the produced (anti)muon



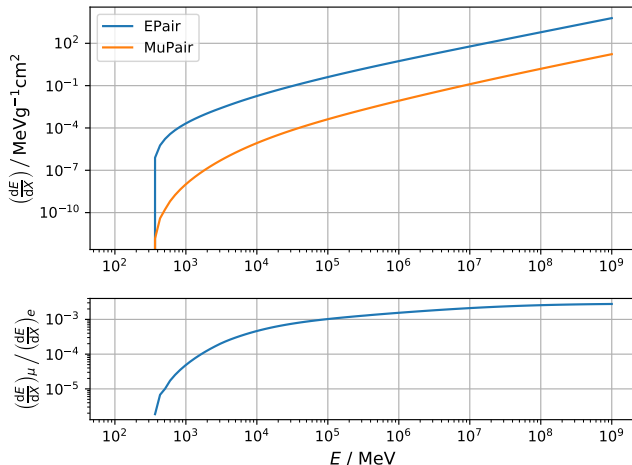
Continuous energy loss per  
distance

$$-\left\langle \frac{dE}{dx} \right\rangle = E \frac{N_A}{A} \int_{v_{\min}}^{v_{\text{cut}}} v \frac{d\sigma}{dv} dv$$

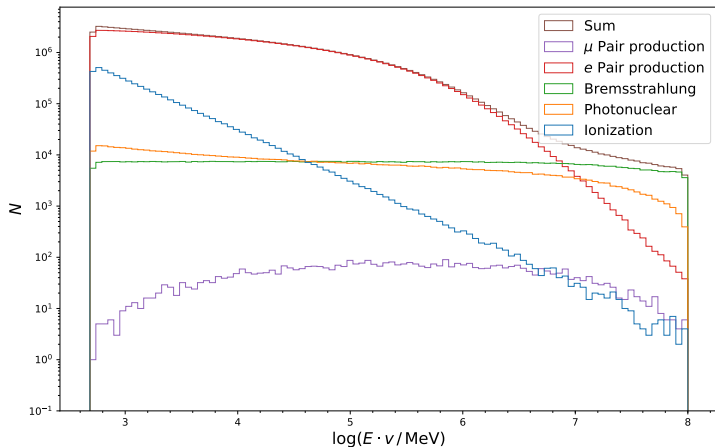
with

$$v_{\min} = \frac{2m_{\mu}}{E},$$

$$v_{\max} = 1 - \frac{m_{\mu}}{E}.$$

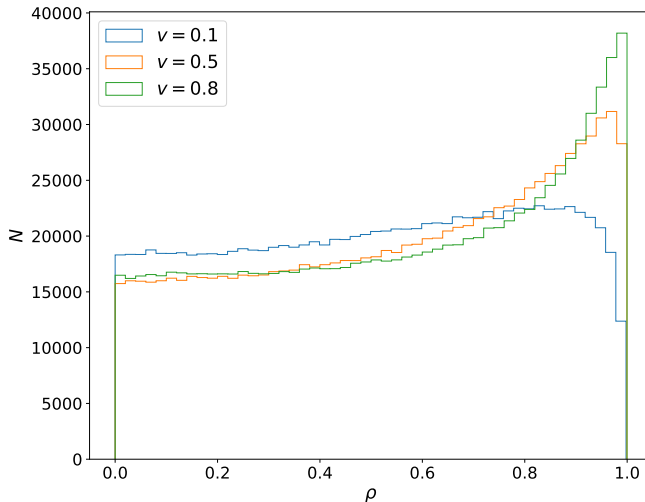


Comparison of  $e$ -pair and  $\mu$ -pair production, only  
continuous losses (i.e.  $v_{\text{cut}} = v_{\max}$ ).



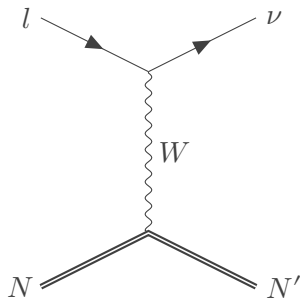
process	$N / N_{\text{ges}}$	$E / E_{\text{ges}}$
e pairp.	0,94	0,94
Ioniz.	$4 \cdot 10^{-2}$	$5 \cdot 10^{-2}$
Brems.	$1 \cdot 10^{-2}$	$7 \cdot 10^{-3}$
Photon.	$8 \cdot 10^{-3}$	$6 \cdot 10^{-3}$
$\mu$ pairp.	$6 \cdot 10^{-5}$	$5 \cdot 10^{-5}$

Stochastic losses, standard rock,  $10^6$  muons with  $E = 10^8$  MeV,  $e_{\text{cut}} = 500$  MeV,  $v_{\text{cut}} = 5 \cdot 10^{-2}$ .



Sampling of  $\rho$  for muons with  $E = 1 \cdot 10^6$  MeV and different  $v$  in standard rock.

## Weak interaction



- Highly suppressed process
- Similarities with "lollipop" signature in  $\tau$ -events
- Crossing symmetry<sup>3</sup>:

$$d\sigma(\mu Z \rightarrow \nu_\mu Z) = \frac{1}{2} d\sigma(\nu_\mu Z \rightarrow \mu Z)$$

<sup>3</sup>Sandrock, Alexander: Higher-order corrections to the energy loss cross sections of high-energy muons, 2018, pp. 38-40

## Future: Physical improvements in PROPOSAL

- Improvement of electron propagation
- Propagation of high-energy photons
- Deflection of particles in magnetic fields
- Propagation through media with non-homogenous density



[https://github.com/tudo-  
astroparticlephysics/PROPOSAL](https://github.com/tudo-astroparticlephysics/PROPOSAL)



<https://arxiv.org/abs/1809.07740>

PROPOSAL may be modified and distributed under terms of a modified LGPL license.  
More information on our GitHub page.