
Improvements in the high-energy lepton propagator PROPOSAL

Jean-Marco Alameddine

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E5b

Introduction

- **PROPOSAL:** Tool to propagate charged leptons
→ MC simulations, multivariate statistics
- **Requirements:** Accuracy, performance
- **Processes:** Energy losses, scattering, decays
- Possibility to use **different parametrizations** → Study **systematic uncertainties**
- C++ library with Python bindings

Propagation

$$\frac{d\sigma}{dv} \quad \underbrace{\longrightarrow}_{?} \quad \text{energy losses}$$

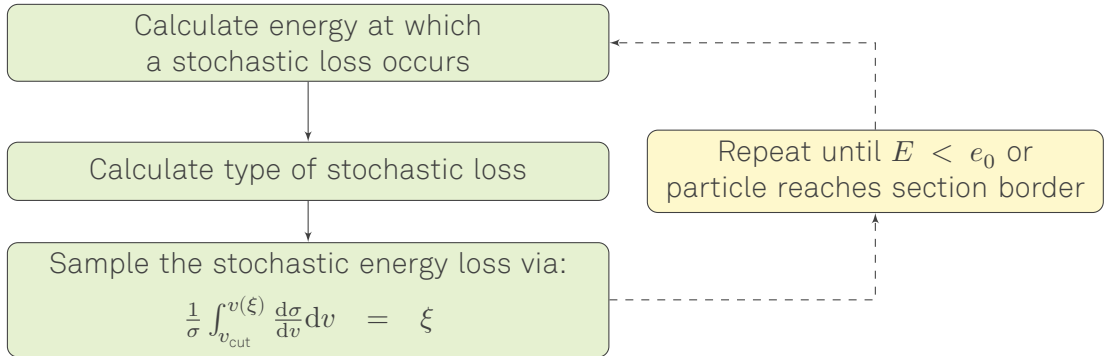
Propagation

$v < v_{\text{cut}}$
continuous losses

$v > v_{\text{cut}}$
stochastic losses

with $v_{\text{cut}} = \min [e_{\text{cut}}/E, v'_{\text{cut}}]$

Propagation

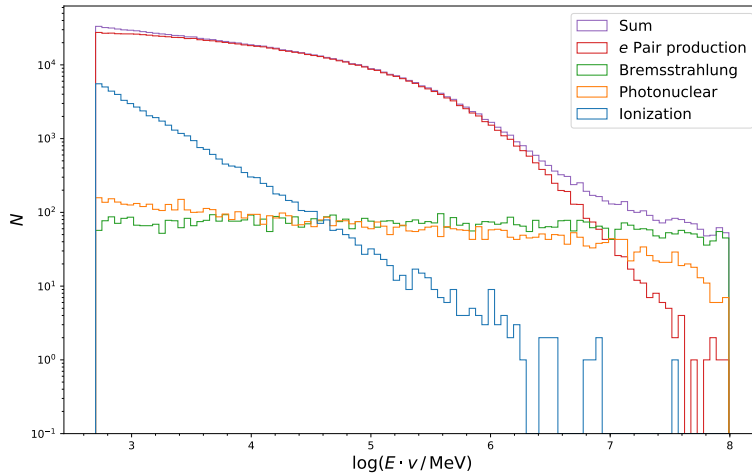


Standard interactions:

- e pair production
- Bremsstrahlung
- Photonuclear
- Ionization

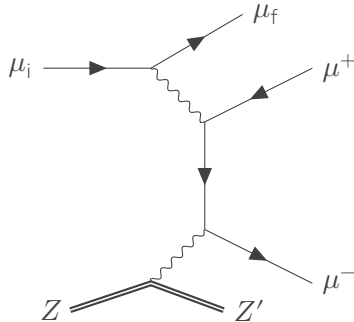
Rare interactions:

- μ pair production
- Weak interaction
- Negligible contribution to overall energy loss
- Observable, interesting signature



Propagation of 10^4 muons with energy 10^8 MeV through 100 m of standard rock.

Direct Production of Muon Pairs



With the energy fraction transferred to the muon pair:

$$v = \frac{(\epsilon_+ + \epsilon_-)}{E}$$

With the asymmetry parameter:

$$\rho = \frac{(\epsilon_+ - \epsilon_-)}{(\epsilon_+ + \epsilon_-)}$$

E : Initial energy of the incoming muon μ_i
 ϵ_{\pm} : Energy of the produced (anti)muon

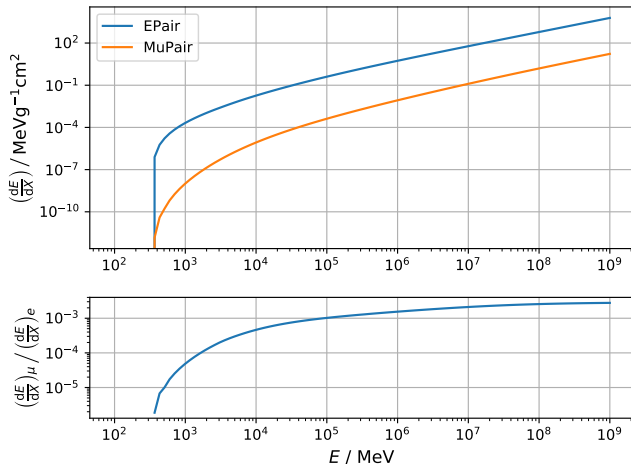
Continuous energy loss per
distance

$$-\left\langle \frac{dE}{dx} \right\rangle = E \frac{N_A}{A} \int_{v_{\min}}^{v_{\text{cut}}} v \frac{d\sigma}{dv} dv$$

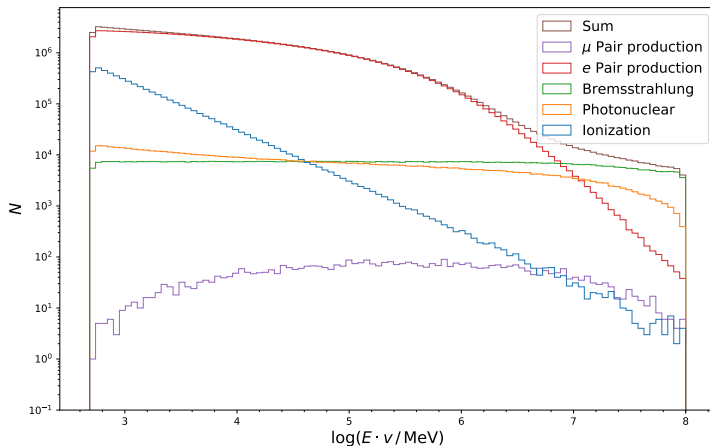
with

$$v_{\min} = \frac{2m_{\mu}}{E},$$

$$v_{\max} = 1 - \frac{m_{\mu}}{E}.$$

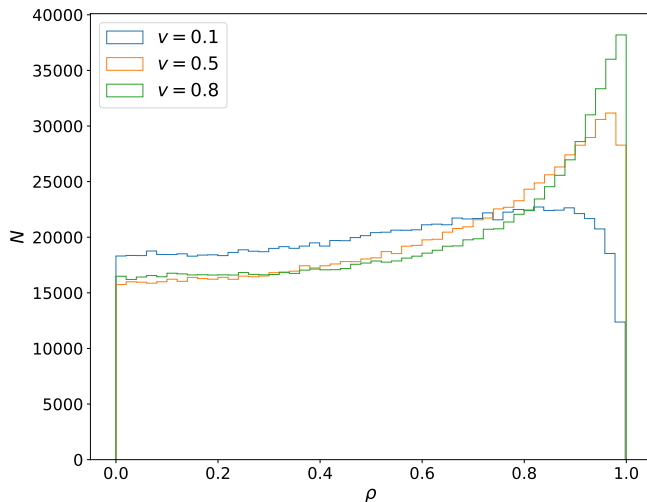


Comparison of e -pair and μ -pair production, only
continuous losses (i.e. $v_{\text{cut}} = v_{\max}$).



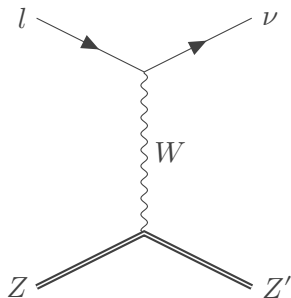
process	N / N_{ges}	E / E_{ges}
e pairp.	0,94	0,94
Ioniz.	$4 \cdot 10^{-2}$	$5 \cdot 10^{-2}$
Brems.	$1 \cdot 10^{-2}$	$7 \cdot 10^{-3}$
Photon.	$8 \cdot 10^{-3}$	$6 \cdot 10^{-3}$
μ pairp.	$6 \cdot 10^{-5}$	$5 \cdot 10^{-5}$

Stochastic losses in standard rock of 10^6 muons with $E = 10^8$ MeV, $e_{\text{cut}} = 500$ MeV, $v_{\text{cut}} = 5 \cdot 10^{-2}$.



Sampling of ρ for muons with $E = 1 \cdot 10^6$ MeV and different v in standard rock.

Weak interaction



- Highly suppressed process
- Similarities with "lollipop" signature in τ -events
- Crossing symmetry³:

$$d\sigma(\mu Z \rightarrow \nu_\mu Z) = \frac{1}{2} d\sigma(\nu_\mu Z \rightarrow \mu Z)$$

³Sandrock, Alexander: Higher-order corrections to the energy loss cross sections of high-energy muons, 2018, pp. 38-40

Future: Physical improvements in PROPOSAL

- Improvement of electron propagation
- Propagation of high-energy photons
- Deflection of particles in magnetic fields
- Propagation through media with non-homogenous density



[https://github.com/tudo-
astroparticlephysics/PROPOSAL](https://github.com/tudo-astroparticlephysics/PROPOSAL)



<https://arxiv.org/abs/1809.07740>

PROPOSAL may be modified and distributed under terms of a modified LGPL license.
More information on our GitHub page.