

## **CptS 223 Homework #4 - Graphs**

Please complete the homework problems on the following page using a separate piece of paper. Note that this is an individual assignment and all work must be your own. Be sure to show your work when appropriate.

1. [13] Define these terms as they relate to graph and graph algorithms:  
Use mathematical terms where appropriate.

Graph  $G = (V, E)$  consists of a set of edges,  $E$ .

Vertex is a node in the graph.

Edge is a line or path that connects two or one node.

Undirected Graph Each Edge does not have front and back and can be traversed in either direction.

Directed Graph Each edge has a front and a back and a direction.

Path is a sequence of vertices.

Loop is a path that leads a node to itself  $(v, v)$ .

Cycle is a directed graph of at least length 1 such that  $w_1 = w_n$  (you get back to the start  $w$ ).

Acyclic Graph does not have cycles.

Connected There is a path from every vertex to every other vertex.

Sparse Number of vertices is larger than number of edges.

Weight value that a path has which can be "Cost".



2. [4] Under what circumstances would we want to use an adjacency matrix instead of an adjacency list to store our graph?

If we want to know the weights of each data path and want to find out the shortest path rather than just list of data

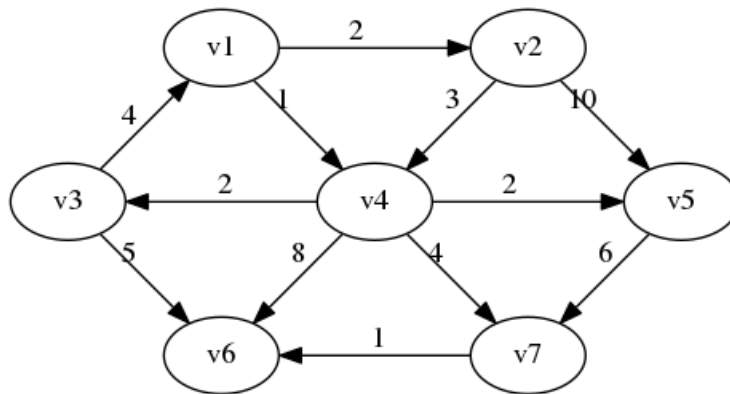
3. [6] Name three problems or situations where a graph would be a good data structure to use:

Making Navigation

Building the infrastructure road of town

Making flight map for every airport connected

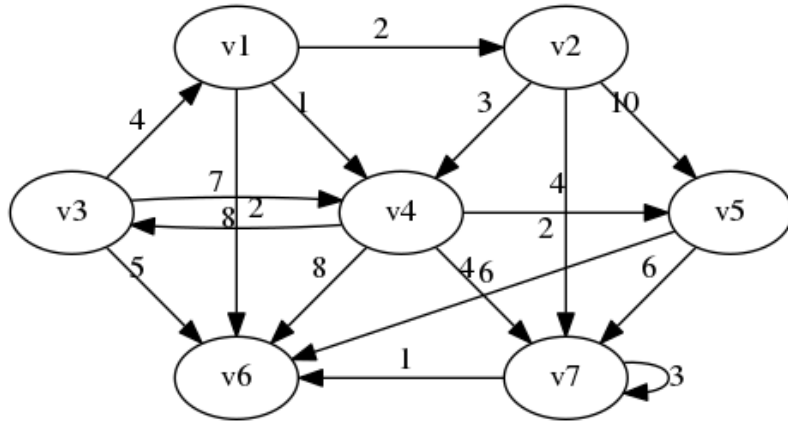
4. [4] What kind of graph is this?



weight

Directed connected graphs with

5. [4] Identify the loop in this graph:



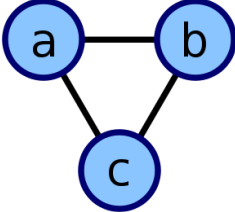
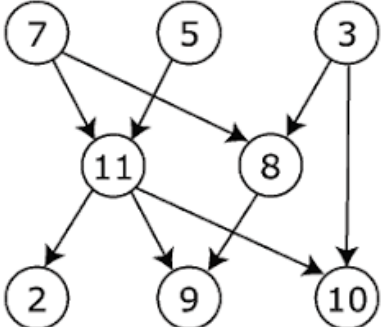
V7 has loop with weight 3

6. [4] How many vertices and edges are in this graph:

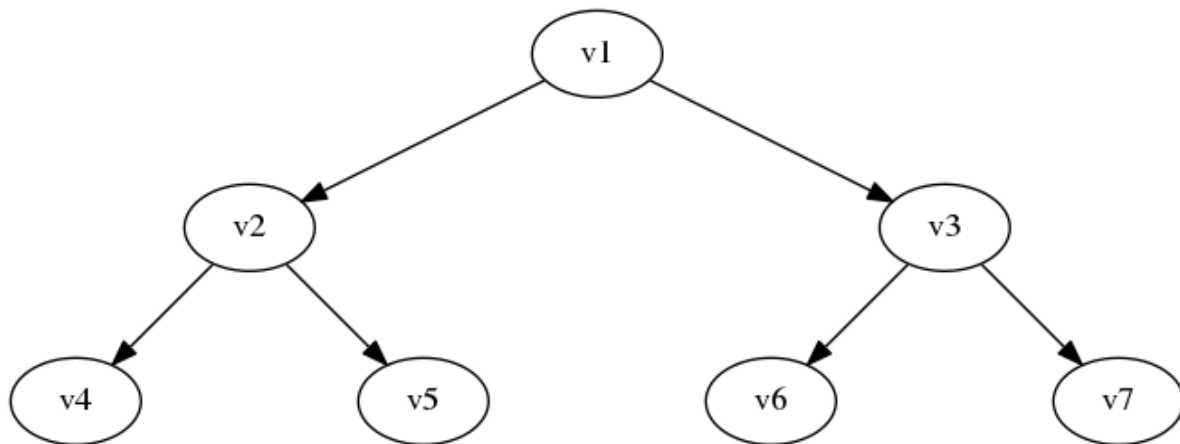
	<p>Vertices <u>  7  </u></p> <p>Edges <u>  17  </u></p>
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7. [6] Are these cyclic or acyclic graphs?

	<p>Cyclic?</p> <p>(Yes)</p>
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	Cyclic?  No
	Cyclic?  Yes

8. [5] A tree is a particular kind of graph. What kind of graph is that?



Directed acyclic graph

9. [4] What is the difference between a breadth-first search and a depth first search?

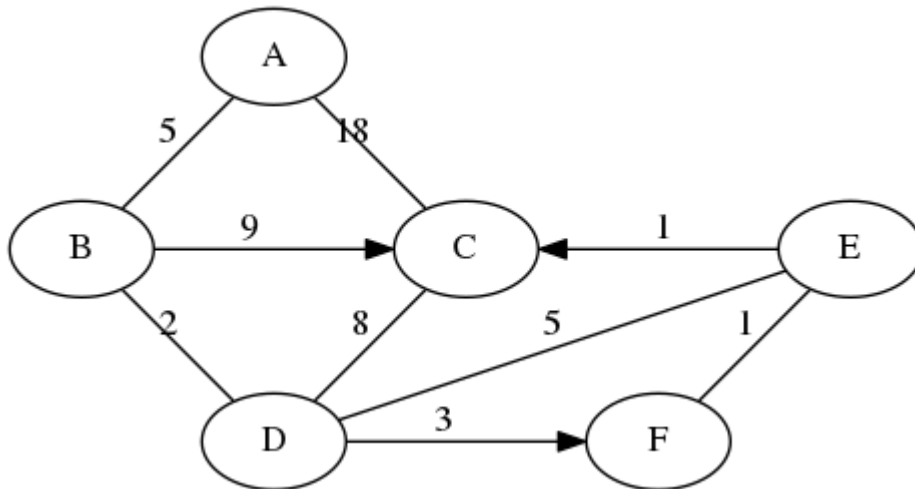
The breadth first search examine the network in layers starting from a root node.

However the Depth-First search just start with any vertex V then recursively process all vertices adjacent to V

10. [10] Dijkstra's Algorithm. Use Dijkstra's Algorithm to determine the shortest path starting at A. Note that edges without heads are bi-directional. To save time,

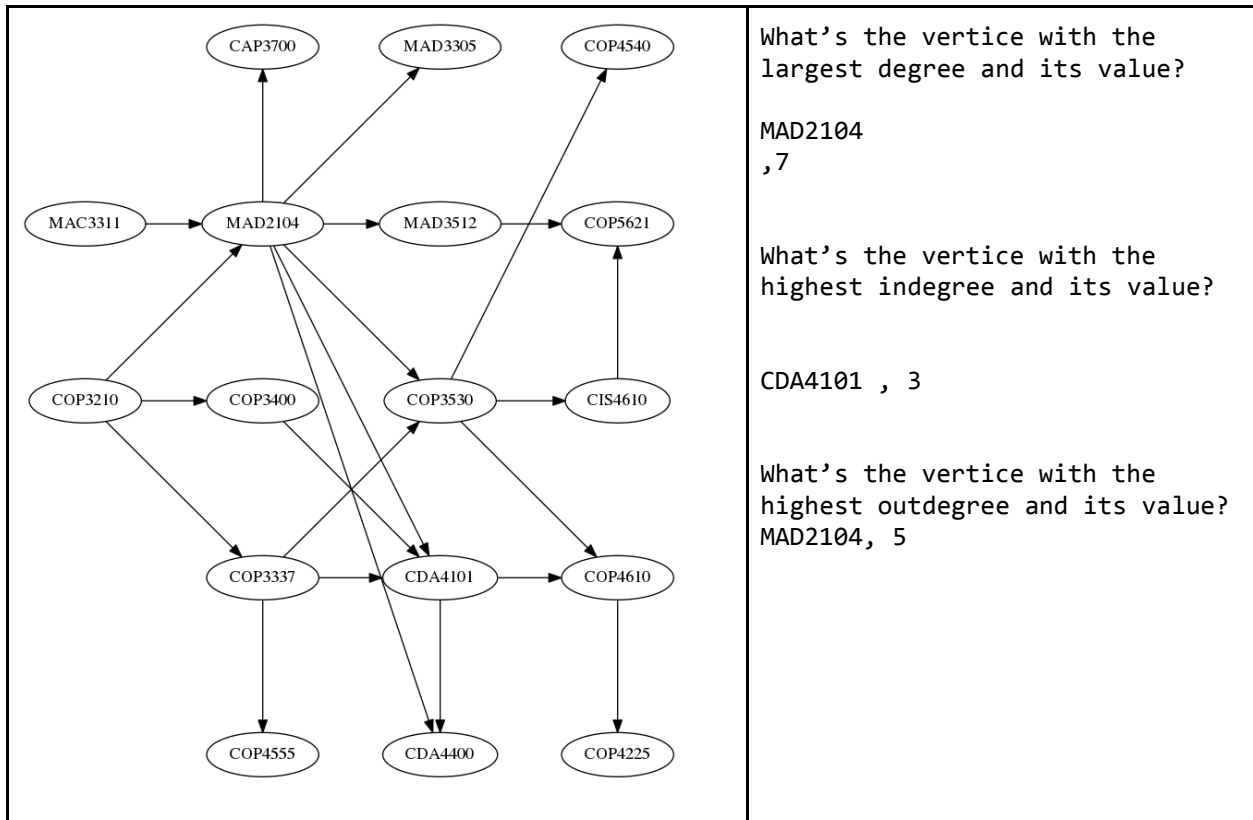
you do not have to add items to the "priority queue" column after it has been discovered (listed in the "distance" column). Use the table below to show your work.

What's the shortest route (by weight) from A to C? \_\_\_\_\_A-B-D-F-E-C\_\_\_\_\_



Node: Distance	Priority Queue
0	A
5	B
7	D
10	F
11	E
12	C

11. [10] Topo sort. Show the final output of running Topo Sort on this graph:



Topo sort output:

MAC3311 COP 3210

MAD2104 COP3400 COP3337 CAP3700 COP4555

MAD3512 COP3530 CDA4400 MAD 3305 CDA4101

COP4540 COP5621 CIS4610 COP4610 COP4255