Mathe Nachhilfe

Analytische Geometrie - Einführung

Analytische Geometrie - Einführung

Ein neues Koordinatensystem

Punkte ablesen Punkte eintragen

Vektoren

Ortsvektoren Vektoren durch zwei Punkte

Länge eines Vektors

2D

3D

Analytische Geometrie - Einführung

Ein neues Koordinatensystem Punkte ablesen Punkte eintragen

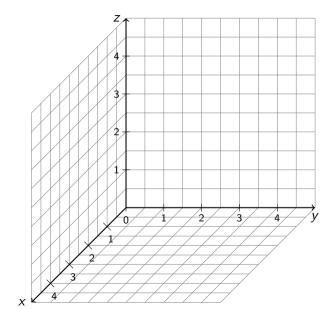
Vektoren

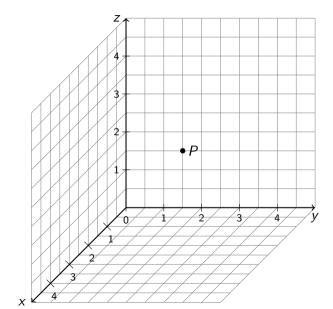
Ortsvektoren Vektoren durch zwei Punkte

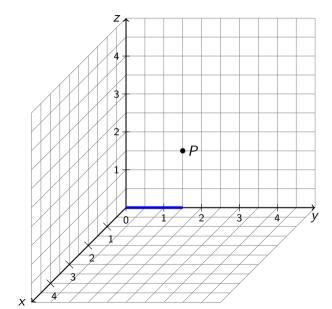
Länge eines Vektors

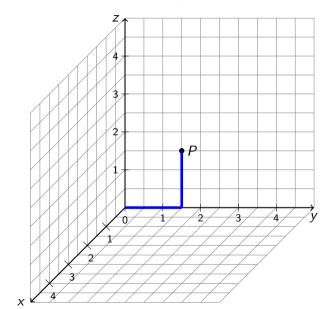
2[

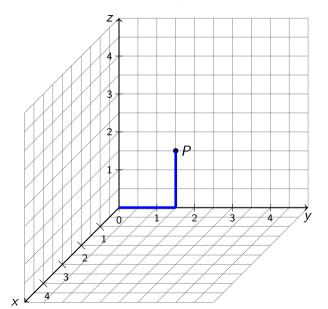
3D

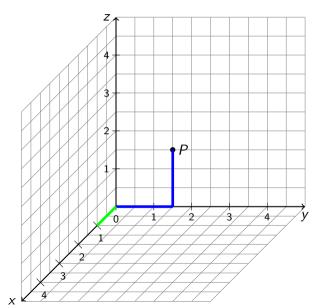


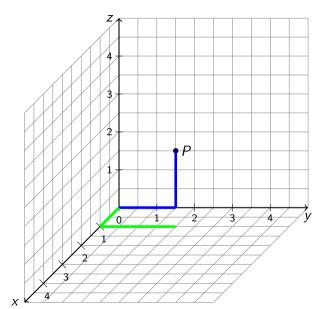


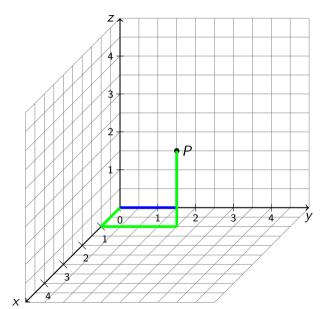


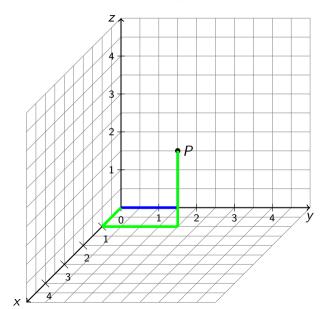


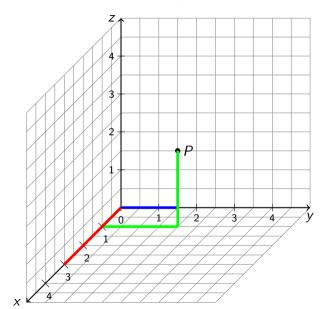


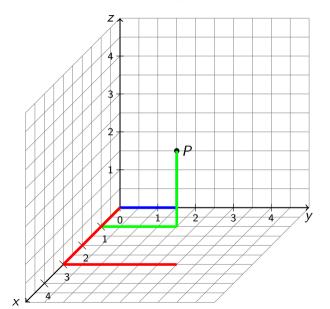


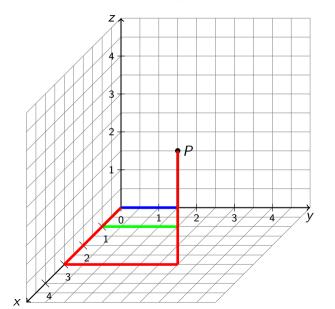


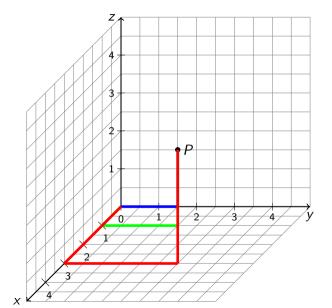




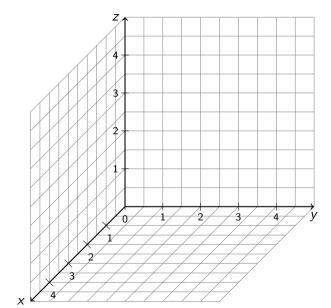


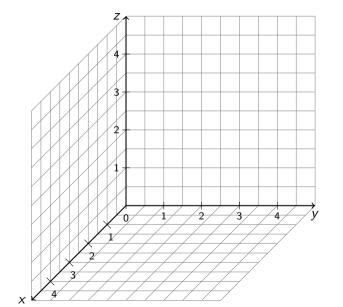


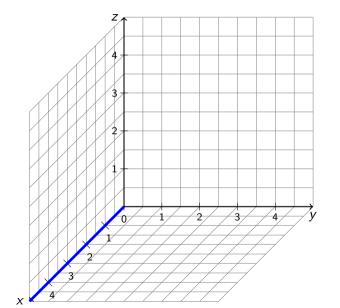


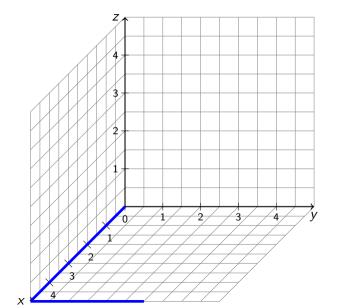


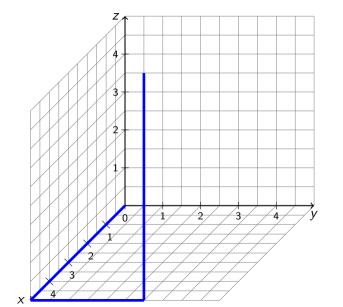
P(0, 1.5, 1.5) P(1, 2, 2) P(3, 3, 3)

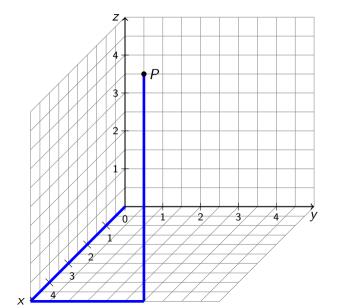


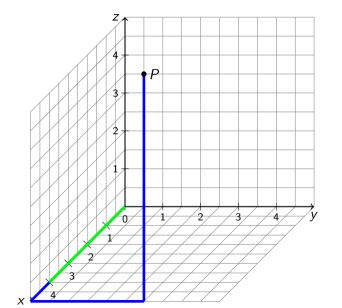


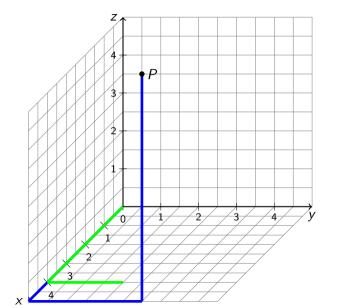


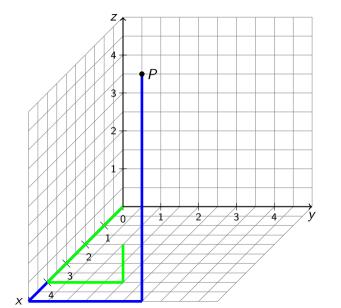


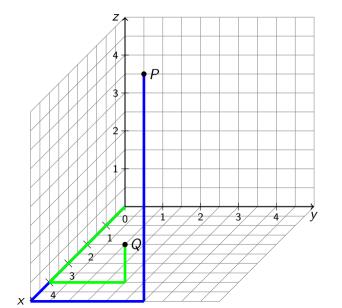


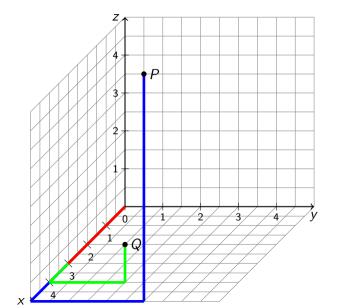


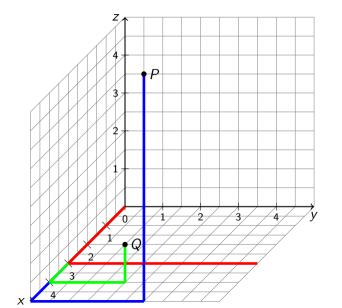


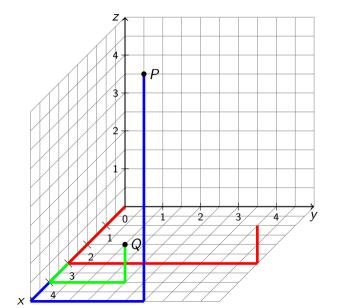


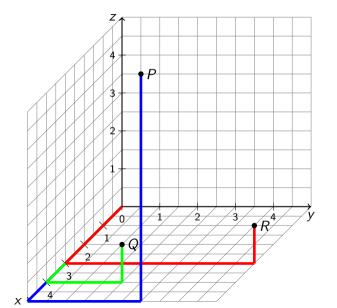


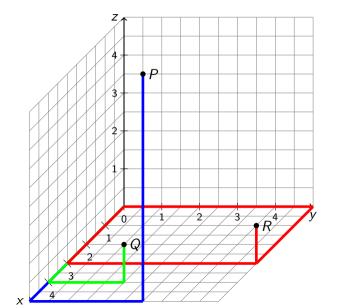


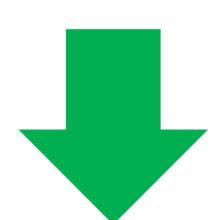




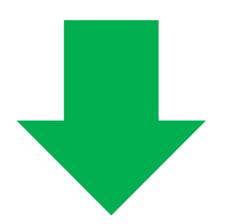








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Analytische Geometrie - Einführung

Ein neues Koordinatensystem Punkte ablesen Punkte eintragen

Vektoren

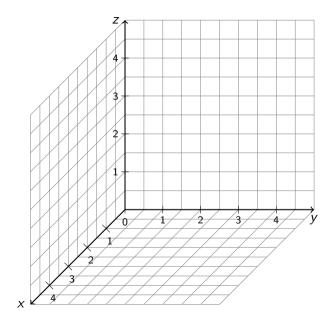
Ortsvektoren Vektoren durch zwei Punkte

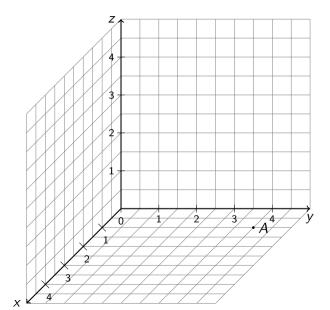
Länge eines Vektors

20

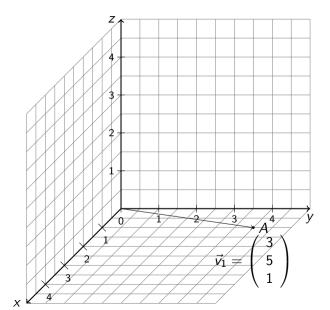
3E

Vektoren - Ortsvektoren

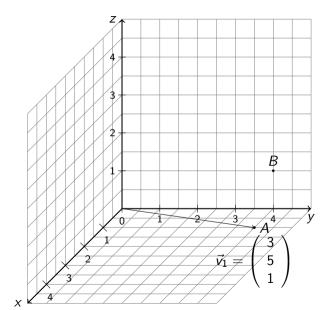




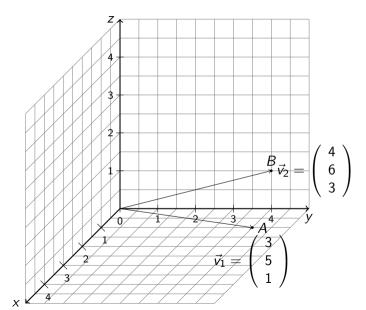
A = (3, 5, 1)



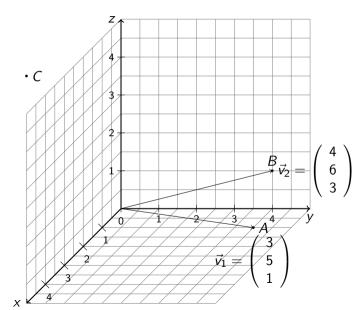
A = (3, 5, 1)



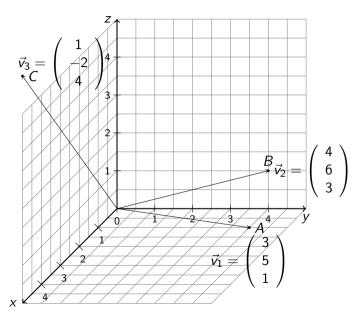
A = (3,5,1)B = (4,6,3)



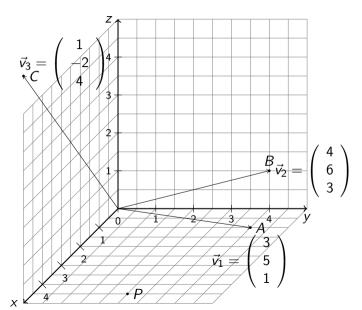
A = (3,5,1)B = (4,6,3)



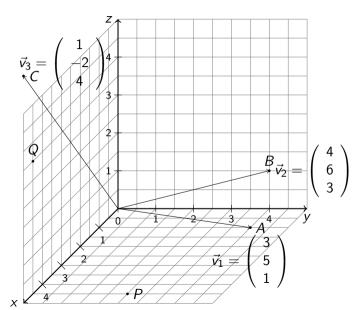
A = (3,5,1) B = (4,6,3)C = (1,-2,4)



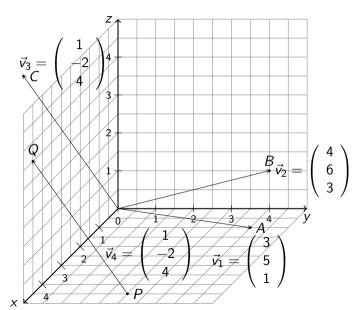
A = (3,5,1) B = (4,6,3)C = (1,-2,4)



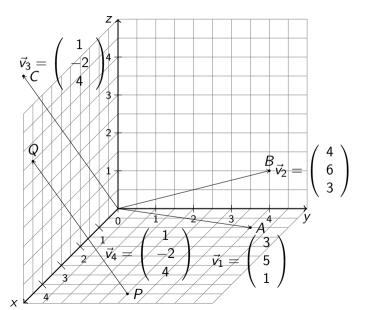
A = (3,5,1) B = (4,6,3) C = (1,-2,4)P = (3.5,2,-0.5)



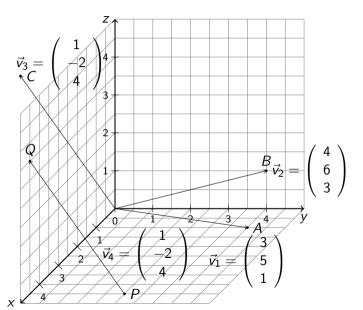
A = (3,5,1) B = (4,6,3) C = (1,-2,4) P = (3.5,2,-0.5) Q = (4.5,0,3.5)



A = (3,5,1) B = (4,6,3) C = (1,-2,4) P = (3.5,2,-0.5) Q = (4.5,0,3.5)

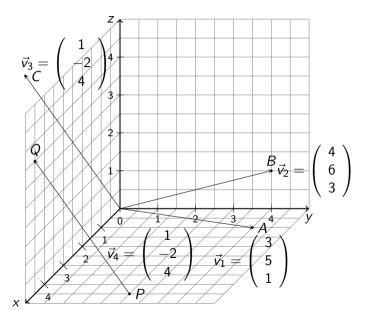


A = (3, 5, 1)B = (4, 6, 3)C = (1, -2, 4)P = (3.5, 2, -0.5)Q = (4.5, 0, 3.5) $\vec{v}_1 = \vec{OA}$



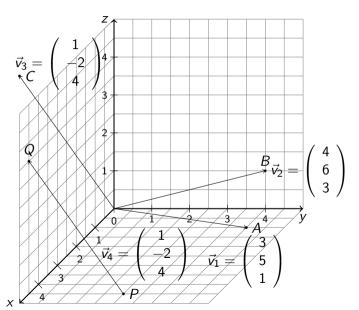
A = (3,5,1) B = (4,6,3) C = (1,-2,4) P = (3.5,2,-0.5) Q = (4.5,0,3.5)

 $ec{v}_1 = ec{OA} \ ec{v}_2 = ec{OB} \$



A = (3,5,1) B = (4,6,3) C = (1,-2,4) P = (3.5,2,-0.5) Q = (4.5,0,3.5)

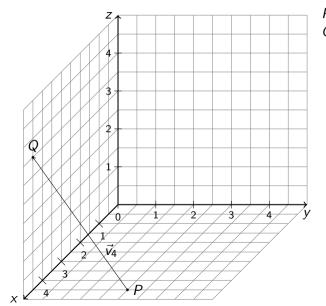
 $ec{v}_1 = ec{OA} \ ec{v}_2 = ec{OB} \ ec{v}_3 = ec{OC}$



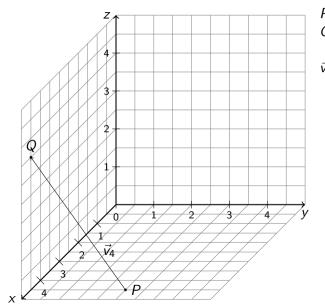
A = (3,5,1) B = (4,6,3) C = (1,-2,4) P = (3.5,2,-0.5) Q = (4.5,0,3.5)

 $ec{v}_1 = ec{OA} \ ec{v}_2 = ec{OB} \ ec{v}_3 = ec{OC}$

 $\vec{v}_4 = \vec{PQ} = \vec{v}_3$

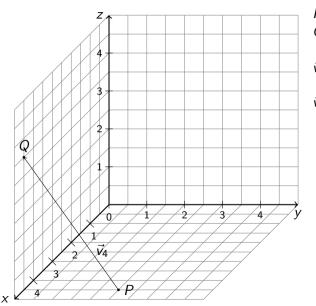


P = (3.5, 2, -0.5)Q = (4.5, 0, 3.5)



P = (3.5, 2, -0.5)Q = (4.5, 0, 3.5)

 $\vec{v}_4 = \vec{PQ} = \vec{OQ} - \vec{OP}$

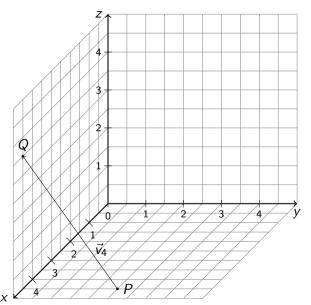


$$P = (3.5, 2, -0.5)$$

$$Q = (4.5, 0, 3.5)$$

$$\vec{v}_4 = \vec{PQ} = \vec{OQ} - \vec{OQ}$$

$$ec{v_4} = ec{PQ} = ec{OQ} - ec{OP}$$
 $ec{v_4} = \left(egin{array}{c} x_q - x_p \ y_q - y_p \ z_q - z_p \end{array}
ight)$

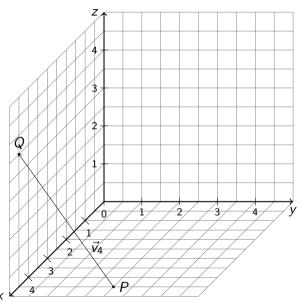


$$P = (3.5, 2, -0.5)$$

 $Q = (4.5, 0, 3.5)$

$$ec{v_4} = ec{PQ} = ec{OQ} - ec{OP}$$
 $ec{v_4} = \left(egin{array}{c} x_q - x_p \ y_q - y_p \ z_q - z_p \end{array}
ight)$
 $ec{v_4} = \left(egin{array}{c} 4.5 - 3.5 \ 0 - 2 \ 3.5 - (-0.5) \end{array}
ight)$

$$\vec{c}_4 = \begin{pmatrix}
4.5 - 3.5 \\
0 - 2 \\
3.5 - (-0.5)
\end{pmatrix}$$



$$P = (3.5, 2, -0.5)$$

 $Q = (4.5, 0, 3.5)$

$$\vec{v}_4 = \vec{PQ} = \vec{OQ} - \vec{OQ}$$

$$\vec{v}_4 = \begin{pmatrix} x_q - x_p \\ y_q - y_p \\ z_q - z_p \end{pmatrix}$$

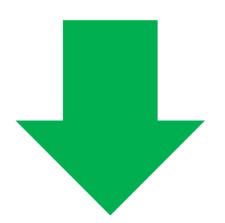
$$\vec{v}_{4} = \vec{PQ} = \vec{OQ} - \vec{OP}$$

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$$\vec{v}_{4} = \begin{pmatrix} 4.5 - 3.5 \\ 0 - 2 \\ 3.5 - (-0.5) \end{pmatrix} = \begin{pmatrix} 1 \\ -2 \\ 4 \end{pmatrix}$$



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Ein neues Koordinatensystem

Punkte ablesen

Punkte eintragen

Vektoren

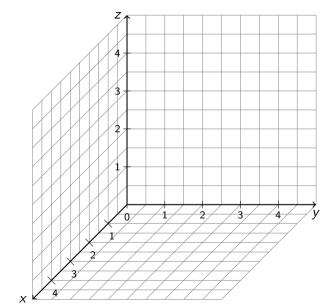
Ortsvektoren

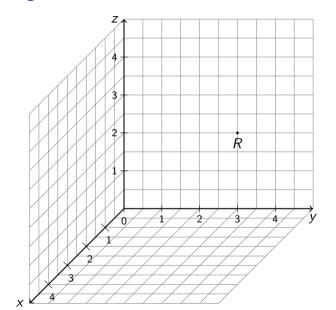
Vektoren durch zwei Punkte

Länge eines Vektors

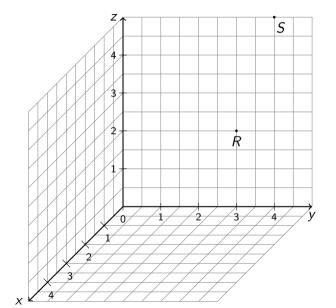
2D

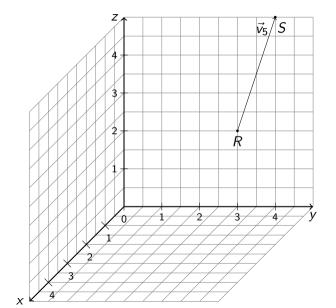
3D

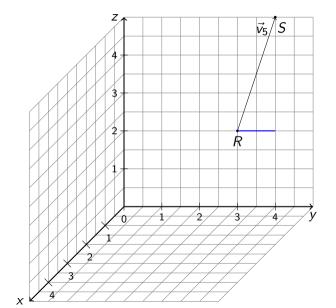


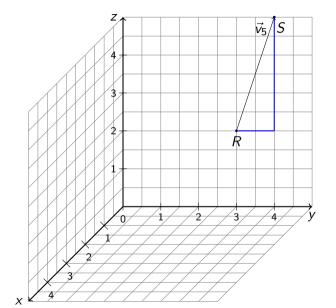


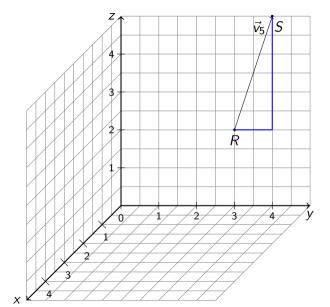
R = (3, 2)





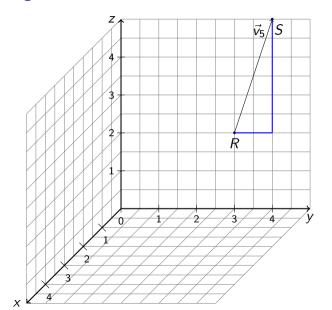






$$R = (3, 2)$$

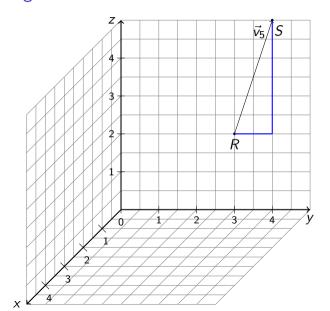
 $S = (4, 5)$
 $\vec{v}_5 = \begin{pmatrix} 4 - 3 \\ 5 - 2 \end{pmatrix}$



$$R = (3,2)$$

$$S = (4,5)$$

$$\vec{v}_5 = \begin{pmatrix} 4-3\\5-2 \end{pmatrix} = \begin{pmatrix} 1\\3 \end{pmatrix}$$

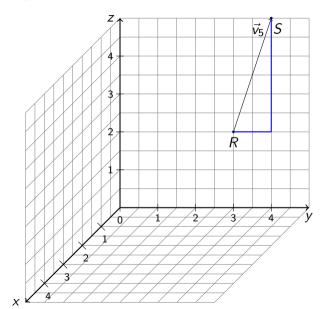


$$R = (3,2)$$

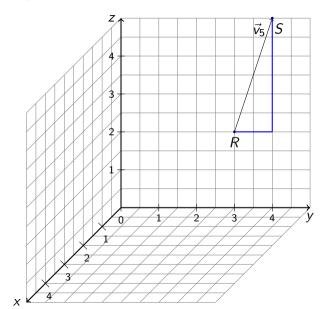
$$S = (4,5)$$

$$\vec{v}_5 = \begin{pmatrix} 4-3\\5-2 \end{pmatrix} = \begin{pmatrix} 1\\3 \end{pmatrix}$$

$$|\vec{v}_5| = \sqrt{x^2 + y^2}$$



$$R = (3,2)
S = (4,5)
\vec{v}_5 = \begin{pmatrix} 4-3 \\ 5-2 \end{pmatrix} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}
|\vec{v}_5| = \sqrt{x^2 + y^2}
|\vec{v}_5| = \sqrt{1^2 + 3^2}$$



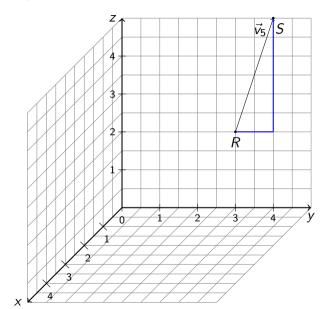
$$R = (3,2)$$

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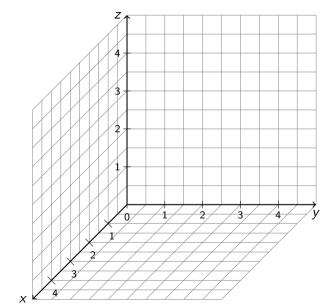
$$\vec{v}_5 = \begin{pmatrix} 4-3 \\ 5-2 \end{pmatrix} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$$

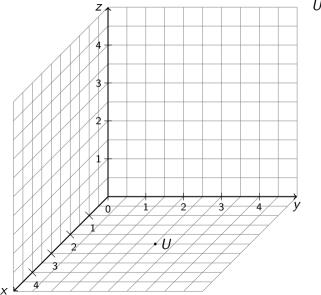
$$|\vec{v}_5| = \sqrt{x^2 + y^2}$$

$$|\vec{v}_5| = \sqrt{1^2 + 3^2} = \sqrt{10}$$

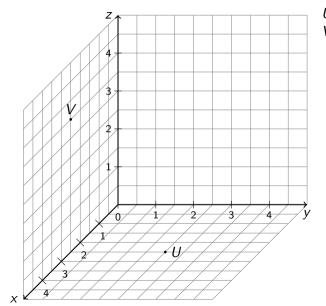


$$R = (3,2)
S = (4,5)
\vec{v}_5 = \begin{pmatrix} 4-3 \\ 5-2 \end{pmatrix} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}
|\vec{v}_5| = \sqrt{x^2 + y^2}
|\vec{v}_5| = \sqrt{1^2 + 3^2} = \sqrt{10}
|\vec{v}_5| \approx 3.1623$$

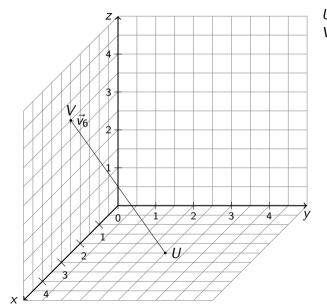




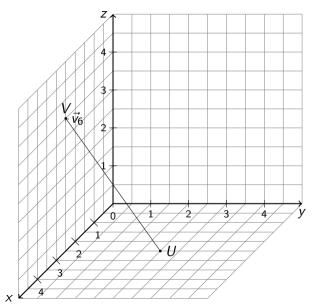
U = (1.5, 2, -0.5)



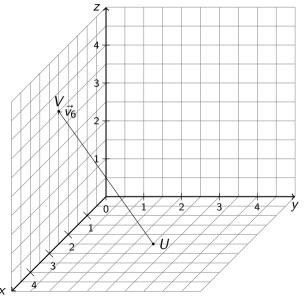
U = (1.5, 2, -0.5)V = (2.5, 0, 3.5)



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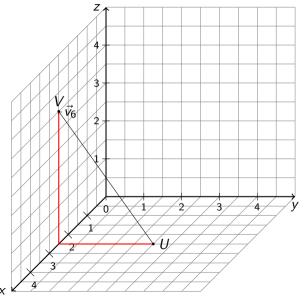
U = (1.5, 2, -0.5) V = (2.5, 0, 3.5) $\vec{v}_6 = \begin{pmatrix} 2.5 - 1.5 \\ 0 - 2 \\ 3.5 - (-0, 5) \end{pmatrix}$



$$U = (1.5, 2, -0.5)$$

$$V = (2.5, 0, 3.5)$$

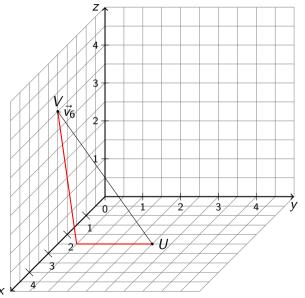
$$\vec{v}_6 = \begin{pmatrix} 2.5 - 1.5 \\ 0 - 2 \\ 3.5 - (-0, 5) \end{pmatrix} = \begin{pmatrix} 1 \\ -2 \\ 4 \end{pmatrix}$$



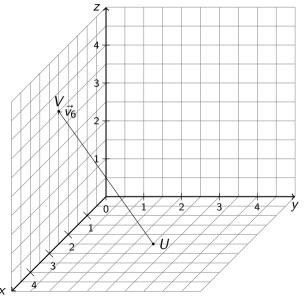
$$U = (1.5, 2, -0.5)$$

$$V = (2.5, 0, 3.5)$$

$$\vec{v_6} = \begin{pmatrix} 2.5 - 1.5 \\ 0 - 2 \\ 3.5 - (-0, 5) \end{pmatrix} = \begin{pmatrix} 1 \\ -2 \\ 4 \end{pmatrix}$$



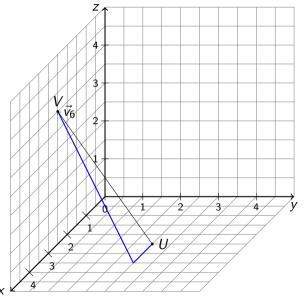
$$U = (1.5, 2, -0.5)$$
 $V = (2.5, 0, 3.5)$
 $\vec{v_6} = \begin{pmatrix} 2.5 - 1.5 \\ 0 - 2 \\ 3.5 - (-0, 5) \end{pmatrix} = \begin{pmatrix} 1 \\ -2 \\ 4 \end{pmatrix}$



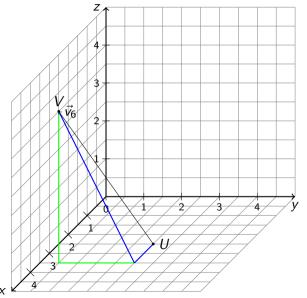
$$U = (1.5, 2, -0.5)$$

$$V = (2.5, 0, 3.5)$$

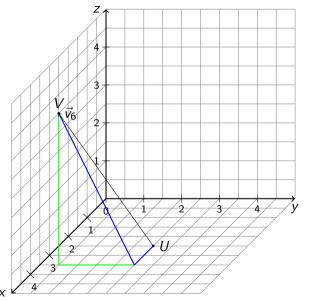
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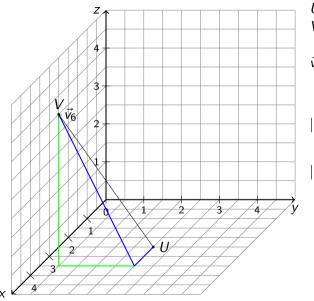


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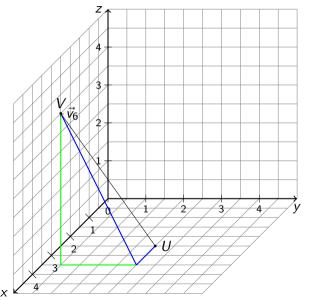
$$|\vec{v}_6| = \sqrt{x^2 + \left| \left(\begin{array}{c} 0 \\ y \\ z \end{array} \right) \right|^2}$$



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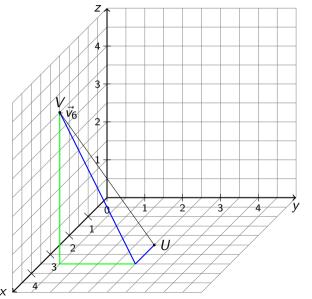
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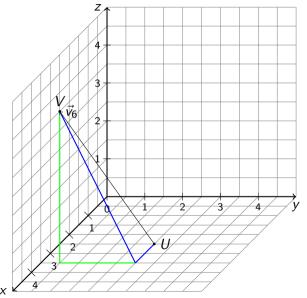
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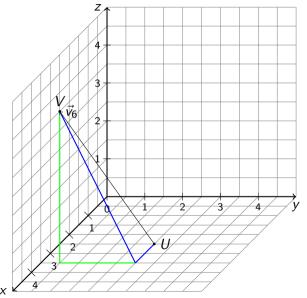
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 $|\vec{v}_6| = \sqrt{1 + 4 + 16}$



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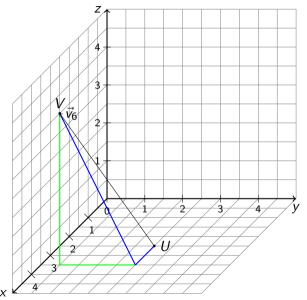
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$$|\vec{v}_6| = \begin{bmatrix} x^2 + \left| \begin{pmatrix} 0 \\ y \end{pmatrix} \right|^2$$

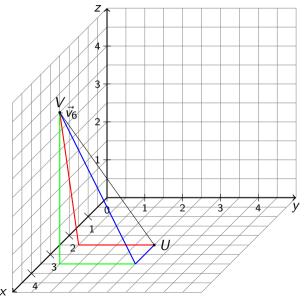
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 $|\vec{v}_6| = \sqrt{1 + 4 + 16} = \sqrt{21} \approx 4.5826$



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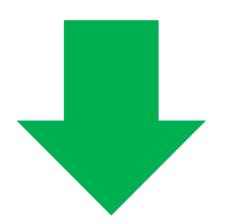
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