C2 W2 Lab 1 training-basics

March 8, 2021

1 Custom Training Basics

In this ungraded lab you'll gain a basic understanding of building custom training loops. - It takes you through the underlying logic of fitting any model to a set of inputs and outputs. - You will be training your model on the linear equation for a straight line, wx + b. - You will implement basic linear regression from scratch using gradient tape. - You will try to minimize the loss incurred by the model using linear regression.

1.1 Imports

1.2 Define Model

You define your model as a class. - x is your input tensor. - The model should output values of wx+b. - You'll start off by initializing w and b to random values. - During the training process, values of w and b get updated in accordance with linear regression so as to minimize the loss incurred by the model. - Once you arrive at optimal values for w and b, the model would have been trained to correctly predict the values of wx+b.

Hence, - \mathbf{w} and \mathbf{b} are trainable weights of the model. - \mathbf{x} is the input - $\mathbf{y} = \mathbf{w}\mathbf{x} + \mathbf{b}$ is the output

```
[2]: class Model(object):
    def __init__(self):
```

```
# Initialize the weights to `2.0` and the bias to `1.0`
# In practice, these should be initialized to random values (for example, with `tf.random.normal`)
self.w = tf.Variable(2.0)
self.b = tf.Variable(1.0)

def __call__(self, x):
    return self.w * x + self.b
model = Model()
```

1.2.1 Define a loss function

A loss function measures how well the output of a model for a given input matches the target output. - The goal is to minimize this difference during training. - Let's use the standard L2 loss, also known as the least square errors

$$Loss = \sum_{i} (y_{pred}^{i} - y_{target}^{i})^{2}$$

```
[3]: def loss(predicted_y, target_y):
    return tf.reduce_mean(tf.square(predicted_y - target_y))
```

1.2.2 Obtain training data

First, synthesize the training data using the "true" w and "true" b.

$$y = w_{true} \times x + b_{true}$$

```
[4]: TRUE_w = 3.0
TRUE_b = 2.0
NUM_EXAMPLES = 1000

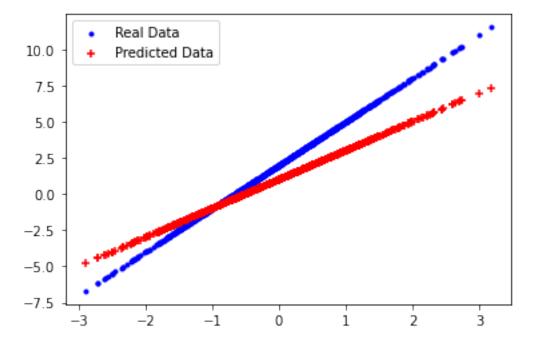
xs = tf.random.normal(shape=[NUM_EXAMPLES])

ys = (TRUE_w * xs) + TRUE_b
```

Before training the model, visualize the loss value by plotting the model's predictions in red crosses and the training data in blue dots:

```
[5]: def plot_data(inputs, outputs, predicted_outputs):
    real = plt.scatter(inputs, outputs, c='b', marker='.')
    predicted = plt.scatter(inputs, predicted_outputs, c='r', marker='+')
    plt.legend((real,predicted), ('Real Data', 'Predicted Data'))
    plt.show()
```

```
[6]: plot_data(xs, ys, model(xs))
print('Current loss: %1.6f' % loss(model(xs), ys).numpy())
```



Current loss: 2.004804

1.2.3 Define a training loop

With the network and training data, train the model using gradient descent - Gradient descent updates the trainable weights \mathbf{w} and \mathbf{b} to reduce the loss.

There are many variants of the gradient descent scheme that are captured in tf.train.Optimizer—our recommended implementation. In the spirit of building from first principles, here you will implement the basic math yourself. - You'll use tf.GradientTape for automatic differentiation - Use tf.assign_sub for decrementing a value. Note that assign_sub combines tf.assign and tf.sub

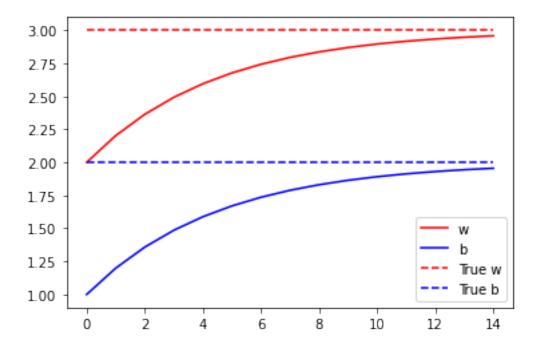
```
[7]: def train(model, inputs, outputs, learning_rate):
    with tf.GradientTape() as t:
        current_loss = loss(model(inputs), outputs)
    dw, db = t.gradient(current_loss, [model.w, model.b])
    model.w.assign_sub(learning_rate * dw)
    model.b.assign_sub(learning_rate * db)

return current_loss
```

Finally, you can iteratively run through the training data and see how w and b evolve.

```
Epoch 0: w=2.00 b=1.00, loss=2.00480
Epoch 1: w=2.20 b=1.20, loss=1.28150
Epoch 2: w=2.36 b=1.36, loss=0.81916
Epoch 3: w=2.49 b=1.49, loss=0.52364
Epoch 4: w=2.59 b=1.59, loss=0.33473
Epoch 5: w=2.68 b=1.67, loss=0.21398
Epoch 6: w=2.74 b=1.74, loss=0.13679
Epoch 7: w=2.79 b=1.79, loss=0.08745
Epoch 8: w=2.84 b=1.83, loss=0.05590
Epoch 9: w=2.87 b=1.86, loss=0.03574
Epoch 10: w=2.90 b=1.89, loss=0.02285
Epoch 11: w=2.92 b=1.91, loss=0.01461
Epoch 12: w=2.93 b=1.93, loss=0.00597
Epoch 14: w=2.96 b=1.96, loss=0.00382
```

In addition to the values for losses, you also plot the progression of trainable variables over epochs.



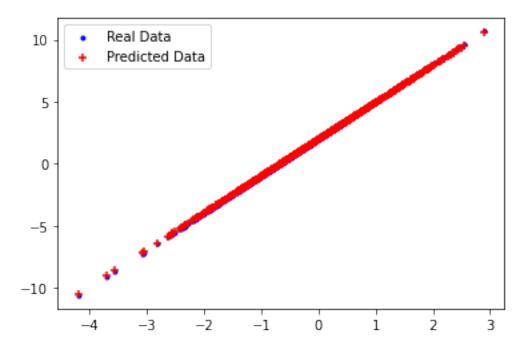
1.3 Plots for Evaluation

Now you can plot the actual outputs in red and the model's predictions in blue on a set of random test examples.

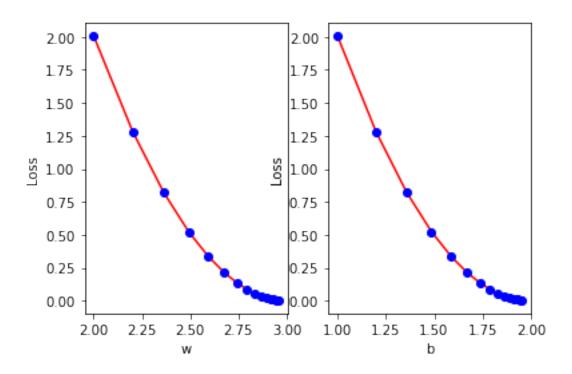
You can see that the model is able to make predictions on the test set fairly accurately.

```
[10]: test_inputs = tf.random.normal(shape=[NUM_EXAMPLES])
    test_outputs = test_inputs * TRUE_w + TRUE_b

predicted_test_outputs = model(test_inputs)
    plot_data(test_inputs, test_outputs, predicted_test_outputs)
```



Visualize the cost function against the values of each of the trainable weights the model approximated to over time.



[]: