Introduction to Algorithms Notes

Jean philo Gong

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Chapter 1

The Role of Algorithms in Computing Notes

1.1 Algorithms

An example of an algorithm is as follows:

> Input: A sequence of n numbers $(a_1, a_2, \ldots, a_n)$.
> Output: A permutation (reordering) $(a'_1, a'_2, \ldots, a'_n)$
> such that $a'_1 \leq a'_2 \leq \ldots \leq a'_n$.

1.1.1 What kinds of problems are solved by algorithms

1.1.2 Data structures

Definition:

> A data structure is a way to store and organize data in order to facilitate access and modifications.

1.1.3 Technique

1.2 Algorithms as a technology

Chapter 2

Getting Started

2.1 Insertion sort

Input: A sequence of n numbers $(a_1, a_2, \ldots, a_n)$.
Output: A permutation (reordering) $(a'_1, a'_2, \ldots, a'_n)$
such that $a'_1 \leq a'_2 \leq \ldots \leq a'_n$.

Methods

2.1.1 Insertion Sort Algorithm

The insertion sort algorithm can be broken down into the following steps:

1. Define a function to perform the insertion sort operation.
2. Loop starts from the second element.
3. Store the current element as the key.
4. Initialize j as the element just before i.
5. Move elements that are greater than the key to one position ahead of their current position.
6. Place the key in its correct position.

2.1.2 Code Implementation

The Python code for the insertion sort algorithm is given below:

```
def insertion_sort(arr):
    for i in range(1, len(arr)):
        key = arr[i]
```

```
j = i - 1
while j >= 0 and key < arr[j]:
    arr[j + 1] = arr[j]
    j -= 1
arr[j + 1] = key
```

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