School of Data and Computer Science, Sun Yat-sen University

E14 BP Algorithm (C++/Python)

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Contents

1 Horse Colic Data Set

The description of the horse colic data set (http://archive.ics.uci.edu/ml/datasets/Horse+Colic) is as follows:

Data Set Characteristics:	Multivariate	**Number of Instances:**	368	**Area:**	Life
Attribute Characteristics:	Categorical, Integer, Real	**Number of Attributes:**	27	**Date Donated**	1989-08-06
Associated Tasks:	Classification	**Missing Values?**	Yes	**Number of Web Hits:**	108569

We aim at trying to predict if a horse with colic will live or die.

Note that we should deal with missing values in the data! Here are some options:

- Use the feature' s mean value from all the available data.
- Fill in the unknown with a special value like -1.
- Ignore the instance.
- Use a mean value from similar items.
- Use another machine learning algorithm to predict the value.

2 Reference Materials

1. Stanford: **CS231n: Convolutional Neural Networks for Visual Recognition** by Fei-Fei Li,etc.
   - Course website: http://cs231n.stanford.edu/2017/syllabus.html
   - Video website: https://www.bilibili.com/video/av17204303/?p=9&tdsourcetag=s_pctim_aiomsg
2. **Machine Learning** by Hung-yi Lee
   - Course website: http://speech.ee.ntu.edu.tw/~tlkagk/index.html
   - Video website: https://www.bilibili.com/video/av9770302/from=search
3. A Simple neural network code template

```
# -*- coding: utf-8 -*
import random
import math

# Shorthand:
# "pd_" as a variable prefix means "partial derivative"
# "d_" as a variable prefix means "derivative"
# "_wrt_" is shorthand for "with respect to"
```

```
# "w_ho" and "w_ih" are the index of weights from hidden to output layer neurons
    and input to hidden layer neurons respectively

class NeuralNetwork:
    LEARNING_RATE = 0.5
    def __init__(self, num_inputs, num_hidden, num_outputs, hidden_layer_weights =
        None, hidden_layer_bias = None, output_layer_weights = None,
        output_layer_bias = None):
    #Your Code Here

    def init_weights_from_inputs_to_hidden_layer_neurons(self, hidden_layer_weights
        ):
    #Your Code Here

    def init_weights_from_hidden_layer_neurons_to_output_layer_neurons(self,
        output_layer_weights):
    #Your Code Here

    def inspect(self):
        print('------')
        print('* Inputs: {}'.format(self.num_inputs))
        print('------')
        print('Hidden Layer')
        self.hidden_layer.inspect()
        print('------')
        print('* Output Layer')
        self.output_layer.inspect()
        print('------')

    def feed_forward(self, inputs):
        #Your Code Here

    # Uses online learning, ie updating the weights after each training case
    def train(self, training_inputs, training_outputs):
        self.feed_forward(training_inputs)

        # 1. Output neuron deltas
        #Your Code Here
        #  E/ z

        # 2. Hidden neuron deltas
```

```
45          # We need to calculate the derivative of the error with respect to the
                output of each hidden layer neuron
46          # dE/dy = Σ E/z * z/y = Σ E/z * w
47          # E/z = dE/dy * z/
48          #Your Code Here
49
50          # 3. Update output neuron weights
51          # E/w = E/z * z/w
52          # Δw = * E/w
53          #Your Code Here
54
55          # 4. Update hidden neuron weights
56          # E/w = E/z * z/w
57          # Δw = * E/w
58          #Your Code Here
59
60      def calculate_total_error(self, training_sets):
61          #Your Code Here
62          return total_error
63
64  class NeuronLayer:
65      def __init__(self, num_neurons, bias):
66
67          # Every neuron in a layer shares the same bias
68          self.bias = bias if bias else random.random()
69
70          self.neurons = []
71          for i in range(num_neurons):
72              self.neurons.append(Neuron(self.bias))
73
74      def inspect(self):
75          print('Neurons:', len(self.neurons))
76          for n in range(len(self.neurons)):
77              print('␣Neuron', n)
78              for w in range(len(self.neurons[n].weights)):
79                  print('␣␣Weight:', self.neurons[n].weights[w])
80              print('␣␣Bias:', self.bias)
81
82      def feed_forward(self, inputs):
83          outputs = []
84          for neuron in self.neurons:
```

```
85              outputs.append(neuron.calculate_output(inputs))
86          return outputs
87
88      def get_outputs(self):
89          outputs = []
90          for neuron in self.neurons:
91              outputs.append(neuron.output)
92          return outputs
93
94  class Neuron:
95      def __init__(self, bias):
96          self.bias = bias
97          self.weights = []
98
99      def calculate_output(self, inputs):
100     #Your Code Here
101
102     def calculate_total_net_input(self):
103     #Your Code Here
104
105     # Apply the logistic function to squash the output of the neuron
106     # The result is sometimes referred to as 'net' [2] or 'net' [1]
107     def squash(self, total_net_input):
108     #Your Code Here
109
110     # Determine how much the neuron's total input has to change to move closer to
            the expected output
111     #
112     # Now that we have the partial derivative of the error with respect to the
            output ( E/ y ) and
113     # the derivative of the output with respect to the total net input (dy /dz ) we
             can calculate
114     # the partial derivative of the error with respect to the total net input.
115     # This value is also known as the delta ( ) [1]
116     #   = E/ z  =  E/ y  * dy /dz
117     #
118     def calculate_pd_error_wrt_total_net_input(self, target_output):
119     #Your Code Here
120
121     # The error for each neuron is calculated by the Mean Square Error method:
122     def calculate_error(self, target_output):
```

```
123     #Your Code Here
124
125     # The partial derivate of the error with respect to actual output then is
            calculated by:
126     # = 2 * 0.5 * (target output - actual output) ^ (2 - 1) * -1
127     # = -(target output - actual output)
128     #
129     # The Wikipedia article on backpropagation [1] simplifies to the following, but
             most other learning material does not [2]
130     # = actual output - target output
131     #
132     # Alternative, you can use (target - output), but then need to add it during
            backpropagation [3]
133     #
134     # Note that the actual output of the output neuron is often written as y  and
            target output as t  so:
135     # =  E/ y  = -(t  - y )
136     def calculate_pd_error_wrt_output(self, target_output):
137     #Your Code Here
138
139     # The total net input into the neuron is squashed using logistic function to
            calculate the neuron's output:
140     # y  =   = 1 / (1 + e^(-z ))
141     # Note that where   represents the output of the neurons in whatever layer we'
            re looking at and   represents the layer below it
142     #
143     # The derivative (not partial derivative since there is only one variable) of
            the output then is:
144     # dy /dz  = y  * (1 - y )
145     def calculate_pd_total_net_input_wrt_input(self):
146     #Your Code Here
147
148     # The total net input is the weighted sum of all the inputs to the neuron and
            their respective weights:
149     # = z  = net  = x w  + x w  ...
150     #
151     # The partial derivative of the total net input with respective to a given
            weight (with everything else held constant) then is:
152     # =  z / w  = some constant + 1 * x w ^(1-0) + some constant ... = x
153     def calculate_pd_total_net_input_wrt_weight(self, index):
154     #Your Code Here
```

```
155
156 # An example:
157
158 nn = NeuralNetwork(2, 2, 2, hidden_layer_weights=[0.15, 0.2, 0.25, 0.3],
        hidden_layer_bias=0.35, output_layer_weights=[0.4, 0.45, 0.5, 0.55],
        output_layer_bias=0.6)
159 for i in range(10000):
160     nn.train([0.05, 0.1], [0.01, 0.99])
161     print(i, round(nn.calculate_total_error([[[0.05, 0.1], [0.01, 0.99]]]), 9))
```

3 Tasks

- Given the training set `horse-colic.data` and the testing set `horse-colic.test`, implement the BP algorithm and establish a neural network to predict if horses with colic will live or die. In addition, you should calculate the accuracy rate.
- Please submit a file named `E14_YourNumber.pdf` and send it to `ai_201901@foxmail.com`

4 Codes and Results

将前馈和反向传播过程向量化后就很好写代码了，使用矩阵与向量乘法，可以避免用循环逐个更新每个参数。最终，我的准确率为 75%。

前馈过程：

$$a^l = g(W^l a^{l-1} + b^l)$$

反向传播：

$$\delta^L = \frac{\partial J}{\partial z^L} \circ g'(z^L)$$

$$\delta^l = ((W^{l+1})^T \delta^{l+1}) \circ g'(z^l)$$

$$\frac{\partial J}{\partial W^l_{jk}} = a^{l-1}_k \delta^l_j$$

$$\frac{\partial J}{\partial b^l_j} = \delta^l_j$$

以下的页面是从 Jupyter Notebook 导出的，但排版不是很美观。为了更好地阅读体验，也可以点击以下链接：https://down.jeddd.com/temp/BackPropagation.html。

[1]:
```
import numpy as np
import pandas as pd
from scipy.stats import zscore
```

[2]:
```
def sigmoid(z):
    """The sigmoid function."""
    return 1.0 / (1.0 + np.exp(-z))

def sigmoid_d(z):
    """Derivative of the sigmoid function."""
    s = sigmoid(z)
    return s * (1 - s)
```

[3]:
```
class NeuralNetwork:
    def __init__(self, input_dim, hidden_dim, out_dim, g=sigmoid,␣
 ↪g_d=sigmoid_d):
        self.W_ih = 0.1 * np.random.rand(hidden_dim, input_dim)  # 输入层到隐含
层的权重矩阵
        self.b_ih = 0.1 * np.random.rand(hidden_dim)             # 输入层到隐含
层的偏置
        self.W_ho = 0.1 * np.random.rand(out_dim, hidden_dim)    # 隐含层到输出
层的权重矩阵
        self.b_ho = 0.1 * np.random.rand(out_dim)                # 隐含层到输出
层的偏置

        self.g = g      # 激活函数
        self.g_d = g_d  # 激活函数的梯度

    def feedForward(self, x):
        """ 输入 x，前馈产生输出。"""
        self.x = x                                          # 输入
        self.in_h = self.W_ih @ self.x + self.b_ih          # 隐含层输入
        self.out_h = self.g(self.in_h)                      # 隐含层输出
        self.in_o = self.W_ho @ self.out_h + self.b_ho      # 输出层输入
        self.out_o = self.g(self.in_o)                      # 输出层输出，即网络最终
输出
        return self.out_o

    def backPropagate(self, target):
        """ 反向传播并产生各层敏感度。"""
        self.delta_o = (self.out_o - target) * self.g_d(self.in_o)          # 输
出层敏感度
        self.delta_h = (self.W_ho.T @ self.delta_o) * self.g_d(self.in_h)  # 隐
含层敏感度

    def update(self, rate):
        """ 更新各个参数。"""
```

```
        self.W_ho -= rate * (np.mat(self.delta_o).T @ np.mat(self.out_h))
        self.b_ho -= rate * self.delta_o
        self.W_ih -= rate * (np.mat(self.delta_h).T @ np.mat(self.x))
        self.b_ih -= rate * self.delta_h

    def predict(self, x):
        """ 对输入特征 x 进行预测，返回预测结果的下标。"""
        in_h = self.W_ih @ x + self.b_ih
        out_h = self.g(in_h)
        in_o = self.W_ho @ out_h + self.b_ho
        out_o = self.g(in_o)
        return out_o.argmax()  # 返回结果中最大值的下标
```

---

[4]:
```
data_df = pd.read_csv('dataset/horse-colic-data.csv')
data_df['outcome'] = data_df.pop('outcome')
for column in data_df.columns:
    if column == 'outcome' or data_df[column].var() == 0:
        continue
#     data_df[column] = zscore(data_df[column])
    data_df[column] = (data_df[column] - data_df[column].min()) /␣
 ↪(data_df[column].max() - data_df[column].min())  # 归一化
# data_df

test_df = pd.read_csv('dataset/horse-colic-test.csv')
test_df['outcome'] = test_df.pop('outcome')
for column in test_df.columns:
    if column == 'outcome' or test_df[column].var() == 0:
        continue
#     test_df[column] = zscore(test_df[column])
    test_df[column] = (test_df[column] - test_df[column].min()) /␣
 ↪(test_df[column].max() - test_df[column].min())  # 归一化
# test_df
```

[5]:
```
EPOCHS = 400
RATE = 0.01  # 学习率
nn = NeuralNetwork(35, 12, 3)

for epoch in range(EPOCHS):
    for i in range(len(data_df)):
        sample = data_df.iloc[i].to_numpy()
        x = sample[:-1]
        target = np.zeros(3)
        target[int(sample[-1])-1] = 1

        output = nn.feedForward(x)
        nn.backPropagate(target)
```

```
        nn.update(RATE)

    data_df = data_df.sample(frac=1)  # 打乱样本顺序
    RATE *= 0.99  # 减少学习率
```

[6]:
```
count = 0
for i in range(len(test_df)):
    sample = test_df.iloc[i].to_numpy()
    x, target = sample[:-1], sample[-1]
    if nn.predict(x) + 1 == target:
        count += 1
print('{} / {} = {:.2%}'.format(count, len(test_df), count/len(test_df)))
```

```
51 / 68 = 75.00%
```

[ ]:
```

```