## Guide de l'outil **Coq** Passage de la déduction naturelle à **Coq**

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## Tactiques existantes en Coq

D/1 // N/ //	3.7	7	
Déduction Naturelle	Nom	$cute{Equivalent}$ Coq	Tactique
$A \vdash A$	$\mid Hyp \mid$	$\overline{\Gamma,\ H:A\vdash A}$	exact H.
$\Gamma \vdash G$	11 9P	$\Gamma \vdash G$	onder m
$\Gamma, A \vdash G$	Aff	$\Gamma, H: A dash G$	clear H.
$\Gamma \vdash A \to G  \Gamma \vdash A$			
$\Gamma \vdash G$	$E_{\rightarrow}$	=	cut A.
$\Gamma, A \vdash G$		$\Gamma, H: A \vdash G$	
$\Gamma \vdash A \to G$	$I_{ ightarrow}$	$\Gamma \vdash A \to G$	intro H.
$\Gamma \vdash A  \Gamma \vdash B$			
$\Gamma \vdash A \land B$	$I_{\wedge}$	=	split.
$\Gamma \vdash A$			
$\Gamma \vdash A \lor B$	$I_{\lor}^{1}$	=	left.
$\Gamma \vdash B$			
$\Gamma \vdash A \lor B$	$I_{\vee}^2$	=	right.
$\Gamma \vdash A \lor \neg A$	TiersExclu	=	apply (classic A).
$\Gamma, x : A \vdash (G \ x)$			
$\Gamma \vdash \forall x : A.(G \ x)$	$\mid I_{orall} \mid$	=	intro x.
$\Gamma \vdash x = x$	$I_{=}$	=	reflexivity.
$\Gamma \vdash [b \mid a]G$		$\Gamma, \ H: a = b \vdash [b \mid a]G$	,
$\Gamma, \ a = b \vdash G$	$E_{=}$	$\Gamma, H: a = b \vdash G$	rewrite -> H.

## Tactiques équivalentes en Coq

Déduction Naturelle	Nom	$ec{E}quivalent$ Coq	Tactique
		$\overline{\Gamma,\ H:\bot \vdash G}$	cut False.
		$\Gamma \vdash \bot \to G$ $\Gamma \vdash \bot$	intro H.
	$E_{\perp}$	$\Gamma \vdash G$	contradiction.
			cut (G \/ ~G).
			intro Hgng.
			elim Hgng.
			intros Hg Hng.
			exact Hg.
			cut False.
		$\Gamma,\ H: \bot \vdash G$	intro H.
		$\Gamma \vdash \bot \to G \qquad \Gamma \vdash \bot$	contradiction
	$E_{\perp}$	$\Gamma \vdash G$	apply (classic G).
		$\Gamma,\ H:A\wedge B,\ HA:A,\ HB:B\vdash A$	cut $(A \land B)$ .
		$\Gamma,\ H:A\wedge B\vdash A\to B\to A$	intro H.
			elim H.
	,	$\Gamma \vdash A \land B \rightarrow A$ $\Gamma \vdash A \land B$	intros HA HB.
	$E^1_\wedge$	$\Gamma \vdash A$	exact HA.
			cut (A // B).
			intro H.
			elim H.
			intros HA HB.
	$E^2_\wedge$	idem	exact HB.
$\Gamma, H2: B \vdash G$		$\Gamma, H: A \lor B \vdash A \to G \ \Gamma, H: A \lor B \vdash B \to G$	
	$E_{\lor}$	$\Gamma, H: A \lor B \vdash G$	elim H.
$\Gamma, H: A \vdash \neg B  \Gamma, H: A \vdash B$		$\Gamma, H: A \vdash \bot$	unfold not.
	$I_{\neg}$	$\Gamma \vdash \neg A$	intro H.
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## Tactiques propres à Coq

Nom
$E_{\neg}$
TiersExclu
Pierce
Modus Ponens
$I_{\!\!\!\!\!\!\wedge}$
$E_{\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!$
$I_{\exists}$
$E_{\exists}$
$E_{Nat}$
$Cas\ sur\ Nat$
$I\ inductif$
$C \neq C'$
C injectif
$G \rhd G'$
b = a
$E'_{\wedge}$
$E_{\lor}'$