Model Selection

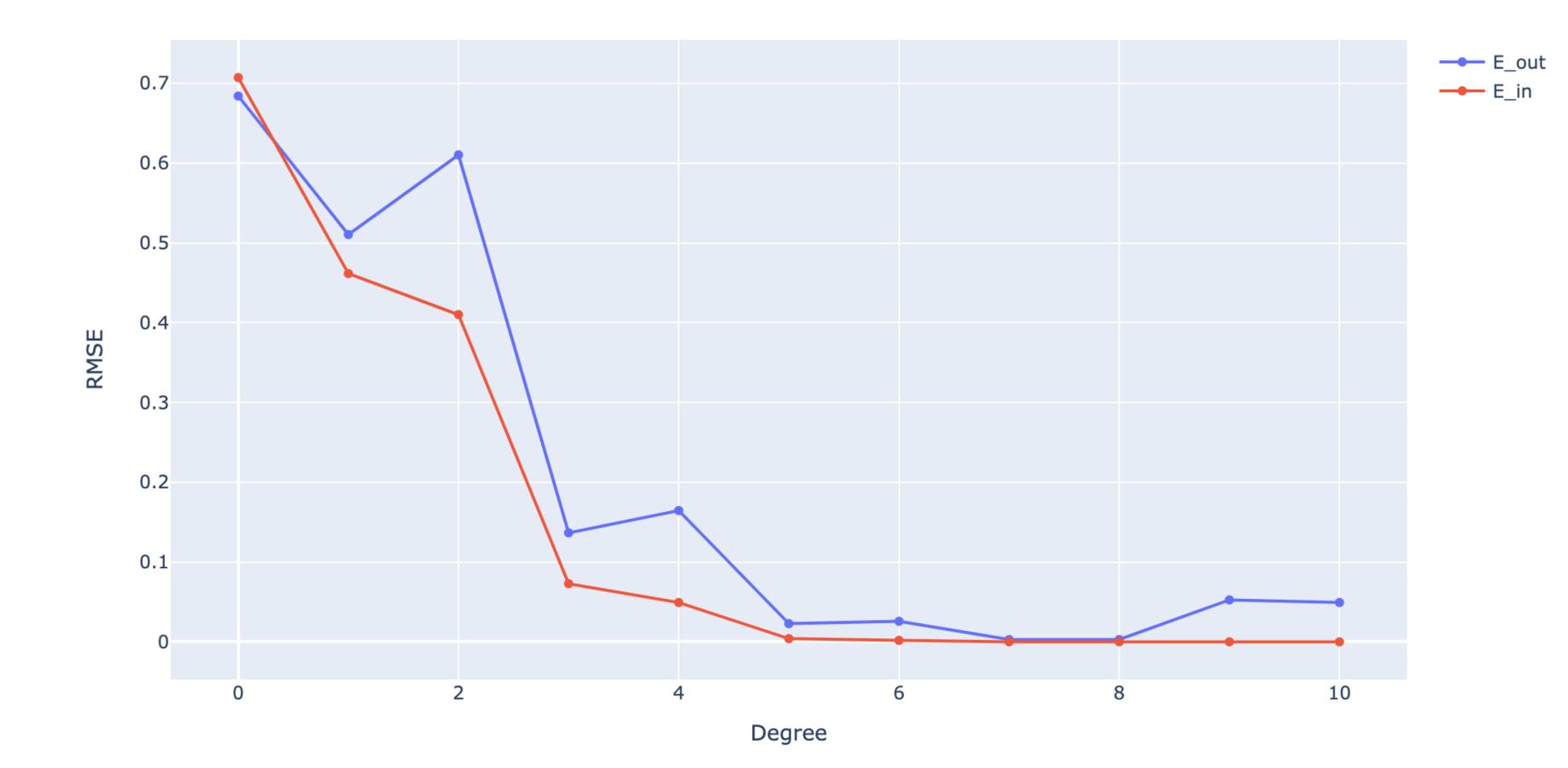
สมาชิกกลุ่ม นายกฤตพล ผ้าเจริญ 6401012620161 นายเจษฎา ศรีจุลโพธิ์ 6401012620170 นายศุภกร ผลศิริ 6401012620234 นายสิรภพ ห่วงวิไล 6401012630132

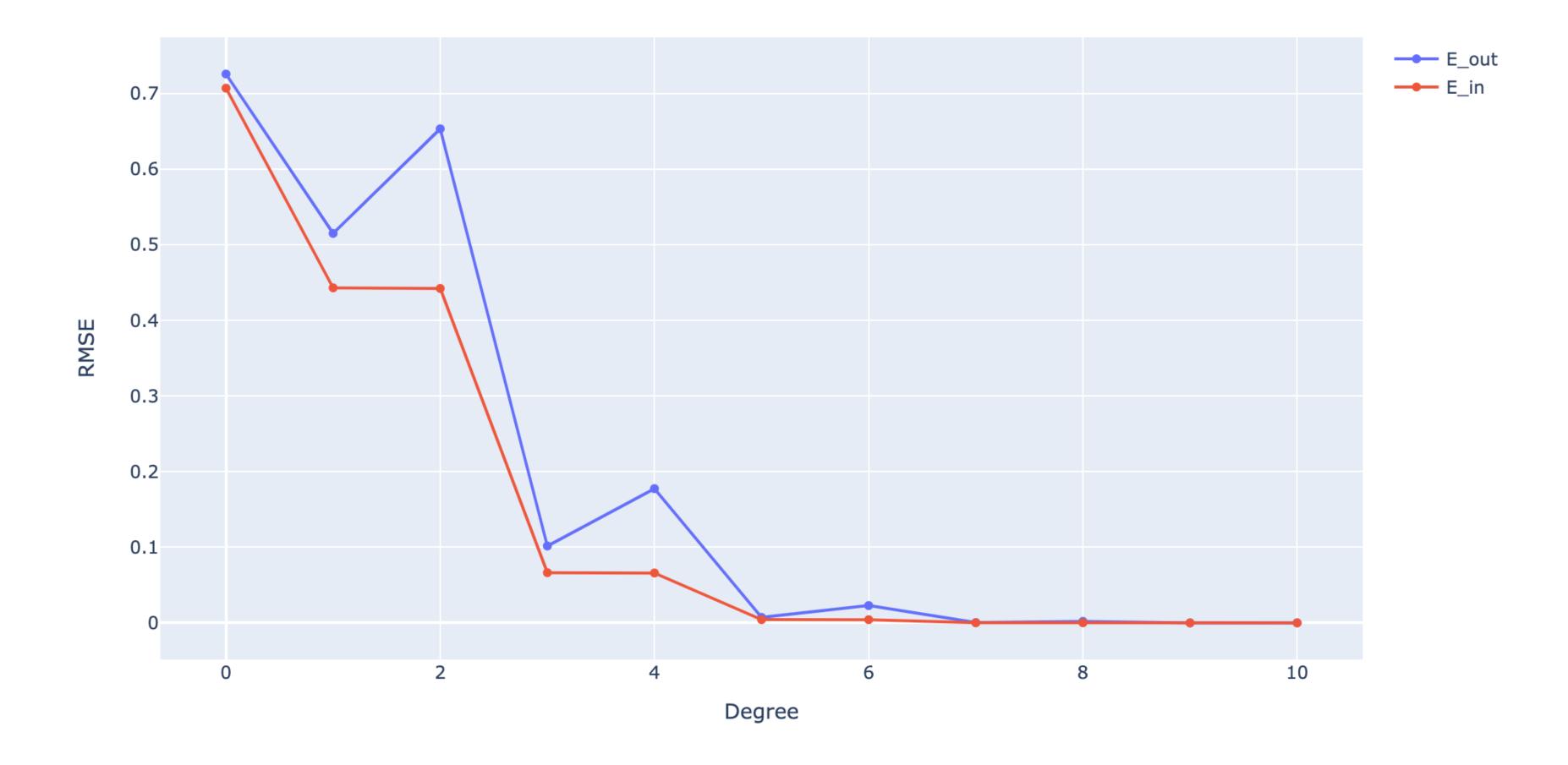
1. ทดลองซ้ำและการปรับพารามิเตอร์ให้ มากกว่าใน lecture หรือลอง generate data ที่แตกต่างจากที่เรียน

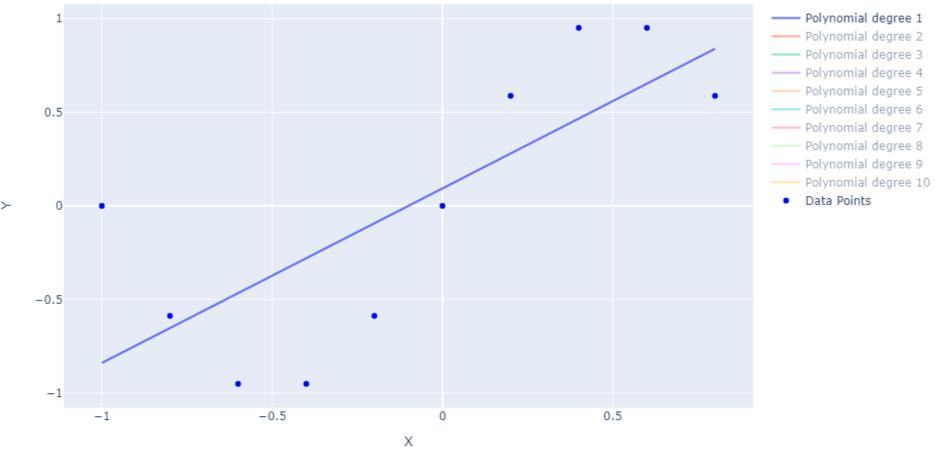
Noiseless

Noiseless	Degr	ee = 1	Degree = 3		Degre	ee = 8	Degree = 10		
Sample Size	Training	CV	Training	CV	Training	CV	Training	CV	
10	0.4615	0.5104	0.0729	0.1366	0	0.0029	0	0.0493	
20	0.4475	0.5126	0.0686	0.1051	0.0001	0.0021	0	0.0001	
40	0.444	0.5145	0.0669	0.1023	0.0001	0.002	O	0.0001	
80	0.4431	0.5151	0.0664	0.1017	0.0002	0.002	0	0.0001	

sin_noiseless_10sample



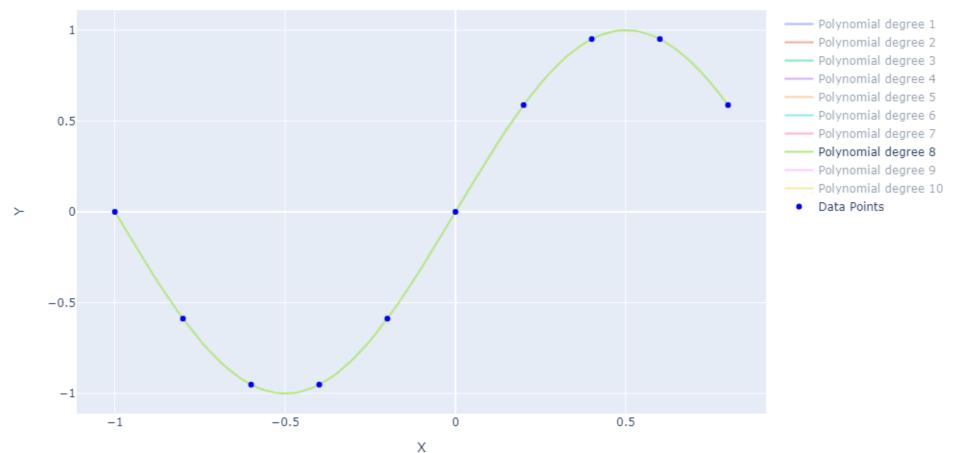


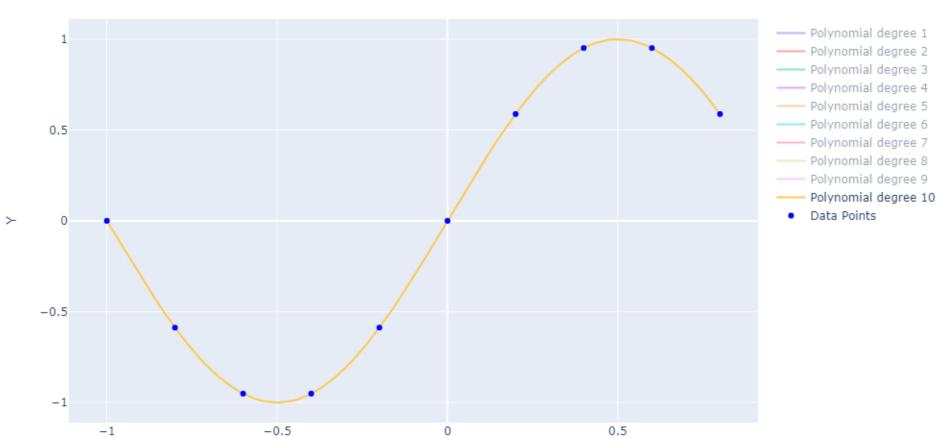


0.5 -0.5 -1 -1 -0.5 0

Data and Polynomial Regression 10 Samples

Data and Polynomial Regression 10 Samples





0.5

—— Polynomial degree 1

---- Polynomial degree 2

—— Polynomial degree 3

Polynomial degree 4Polynomial degree 5

—— Polynomial degree 6

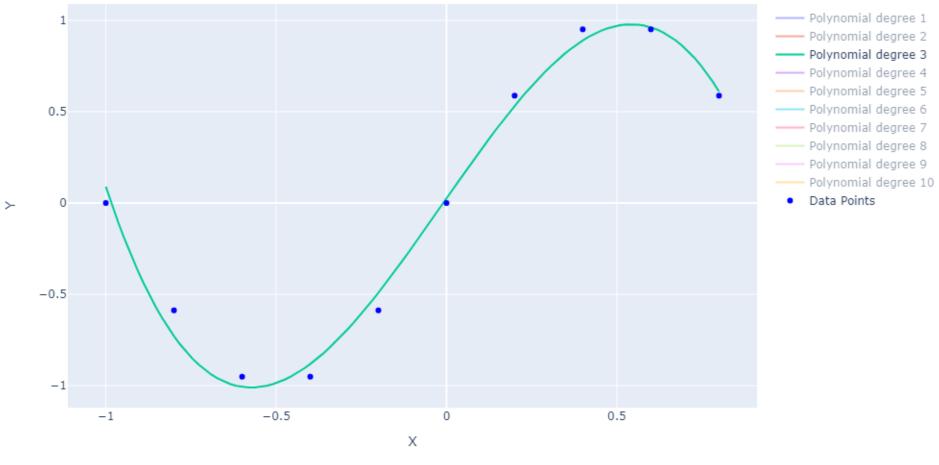
---- Polynomial degree 7

—— Polynomial degree 8

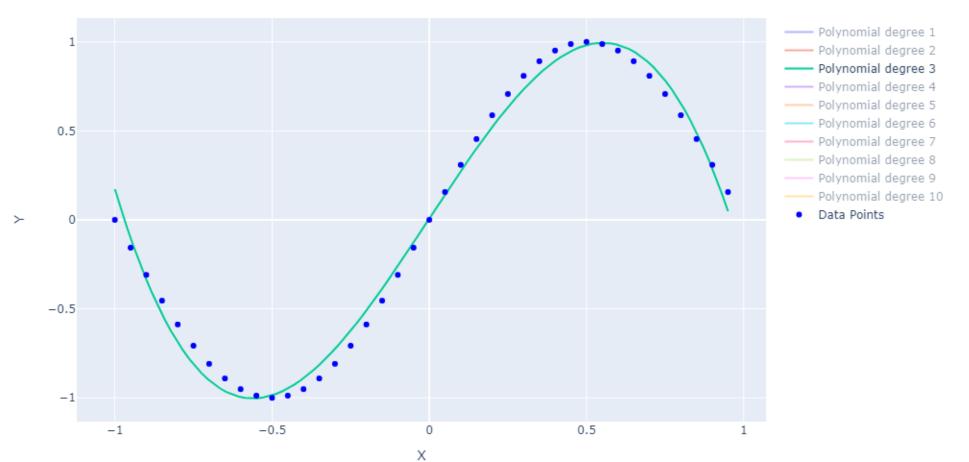
—— Polynomial degree 9

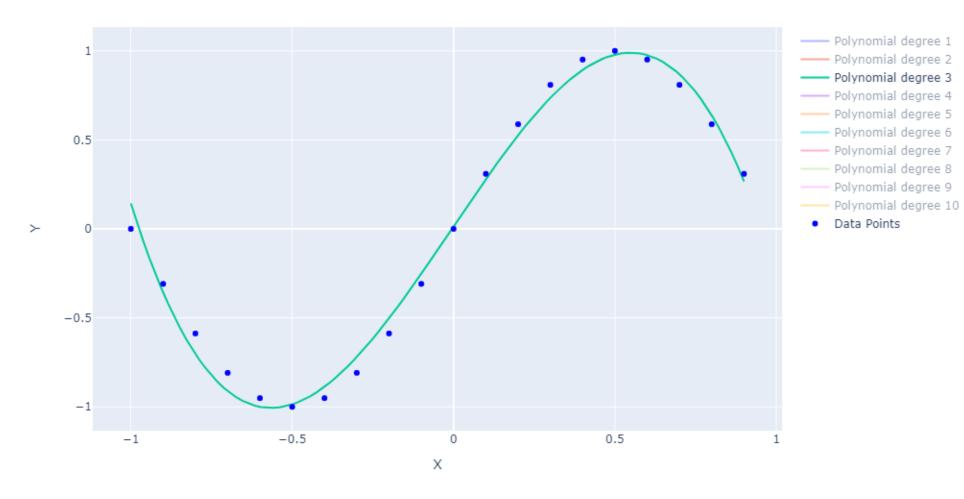
—— Polynomial degree 10

Data Points

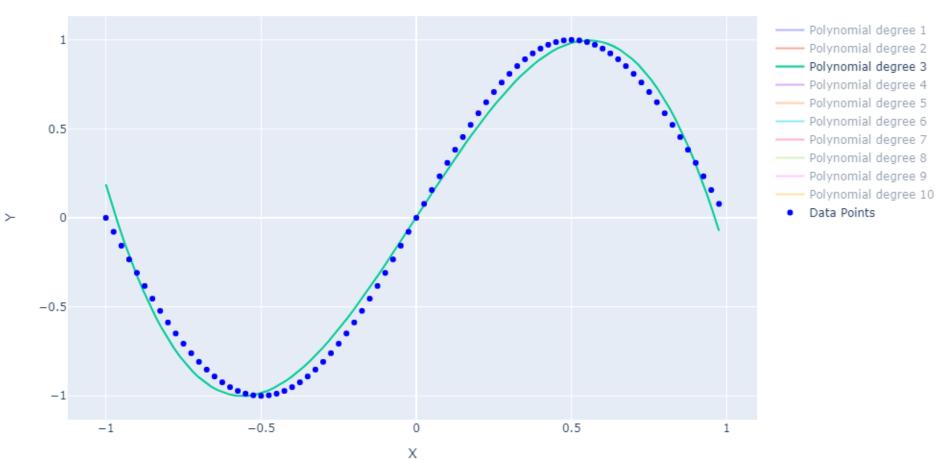


Data and Polynomial Regression 40 Samples



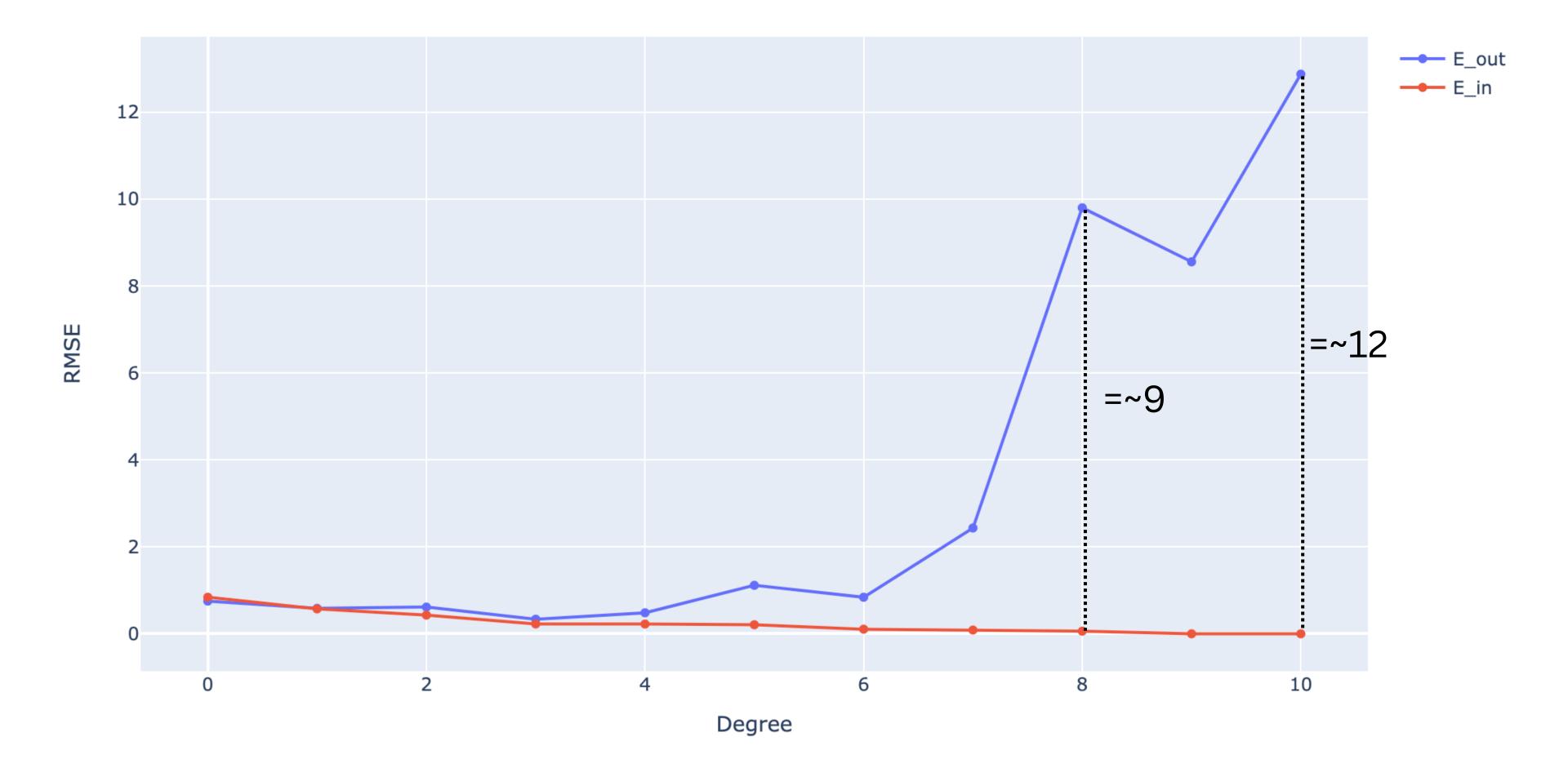


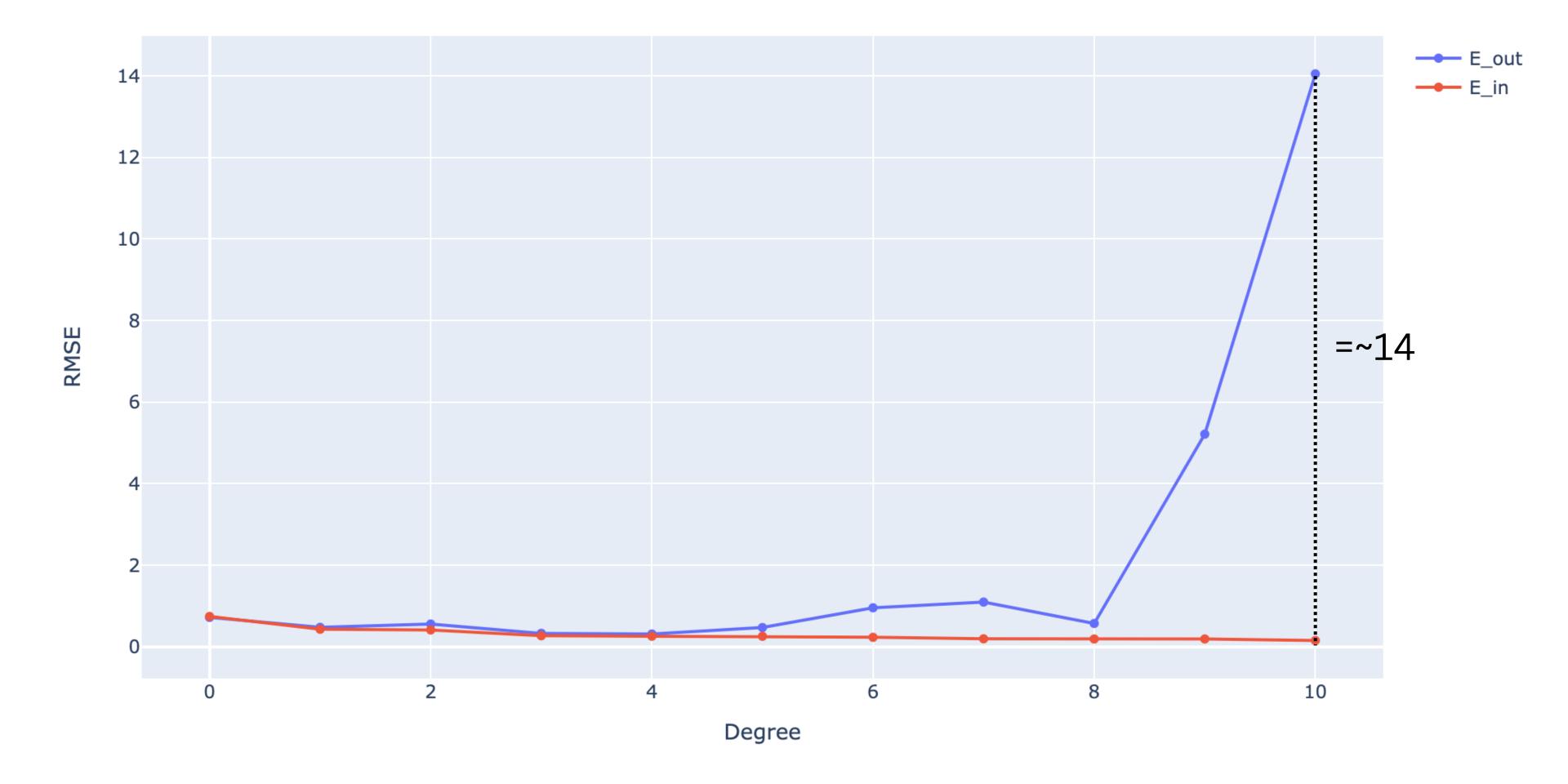
Data and Polynomial Regression 80 Samples

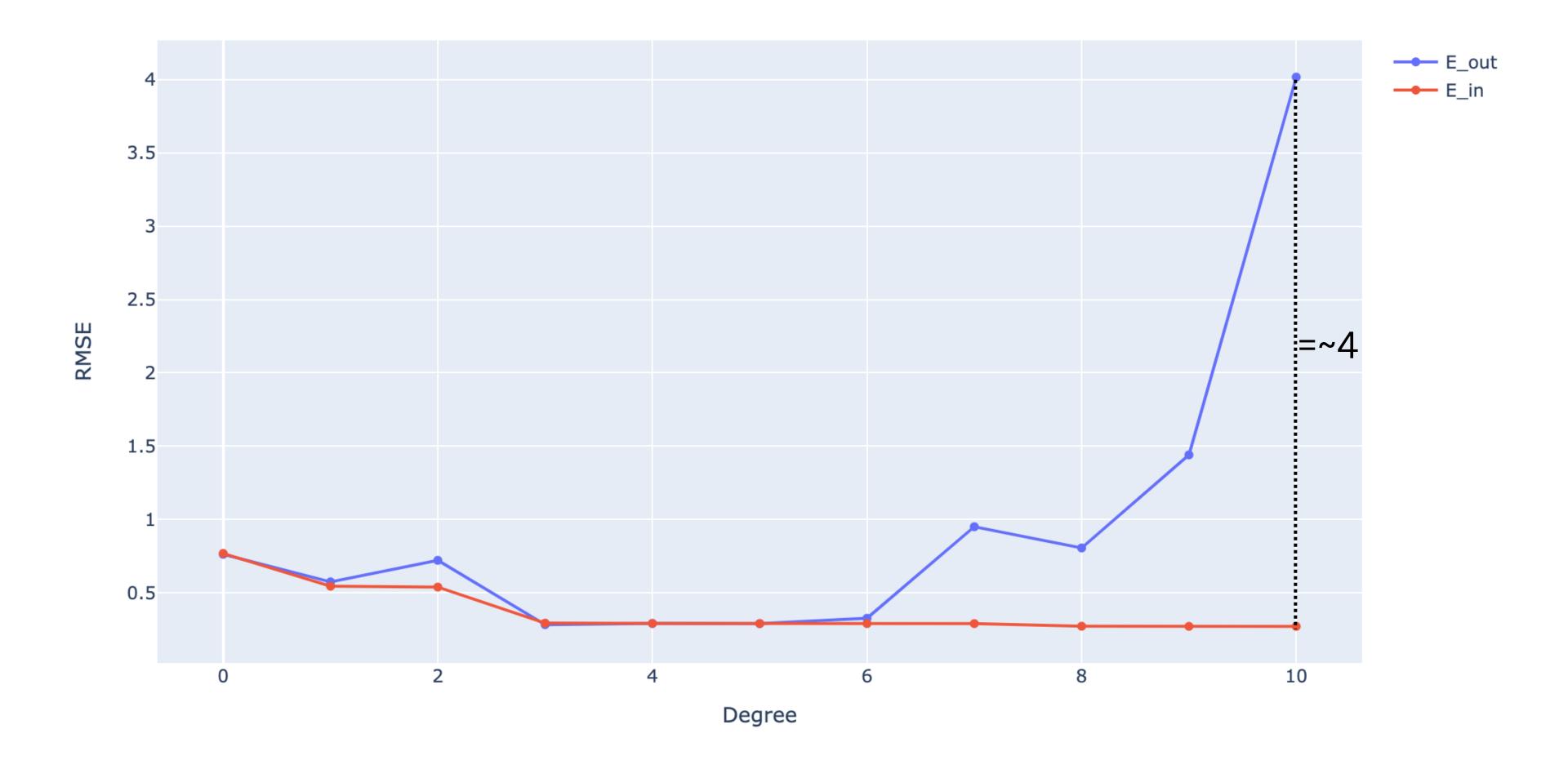


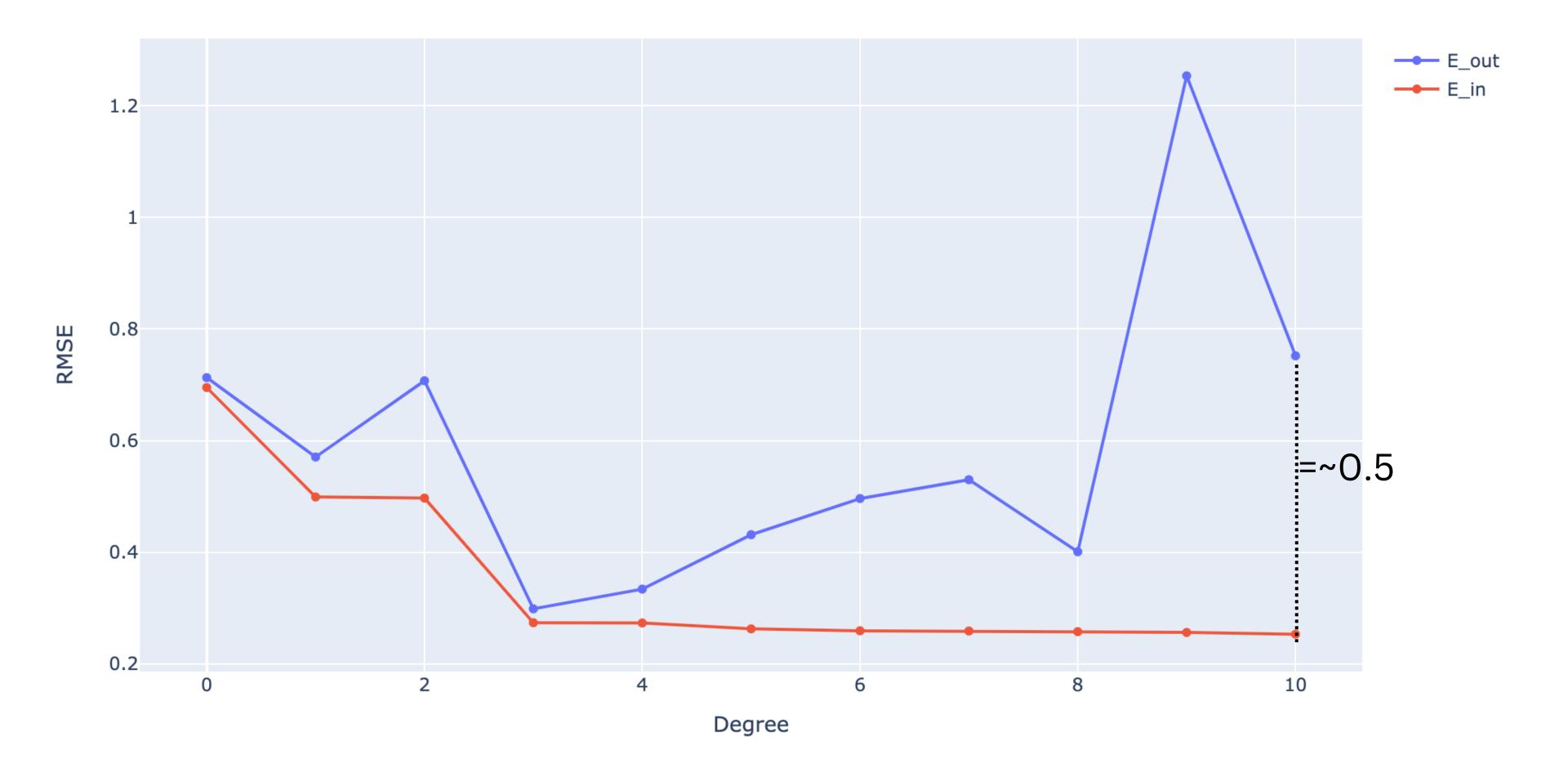
Noisy

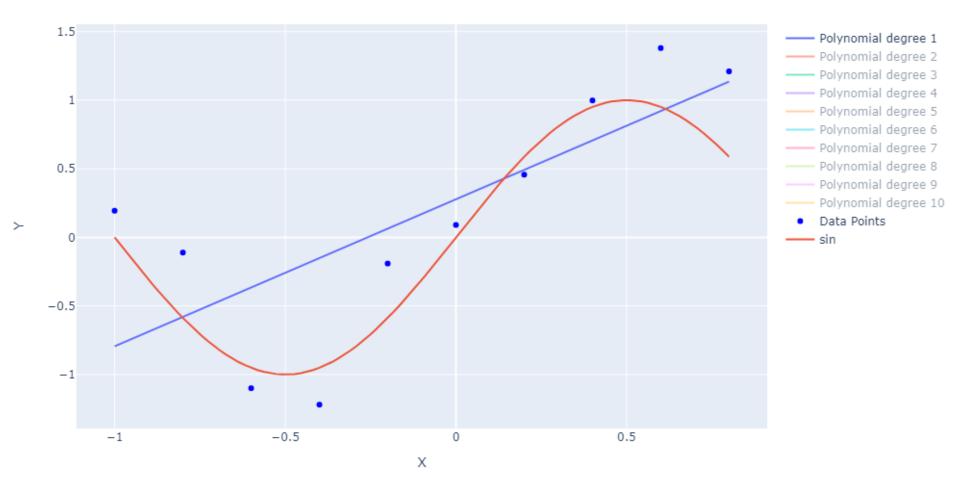
Noisy	Degr	ee = 1	Degree = 3		Degree = 8		Degree = 10		
Sample Size	Training	CV	Training	CV	Training	CV	Training	CV	
10	0.5728	0.5861	0.2265	0.3355	0.0607	9.8027	0	12.8773	
20	0.4316	0.4783	0.272	0.3315	0.1936	0.5742	0.1563	14.0502	
40	0.5445	0.5745	0.2929	0.2827	0.2718	0.8057	0.2707	4.0169	
80	0.499	0.5706	0.2737	0.2987	0.2578	0.4009	0.2531	0.7520	







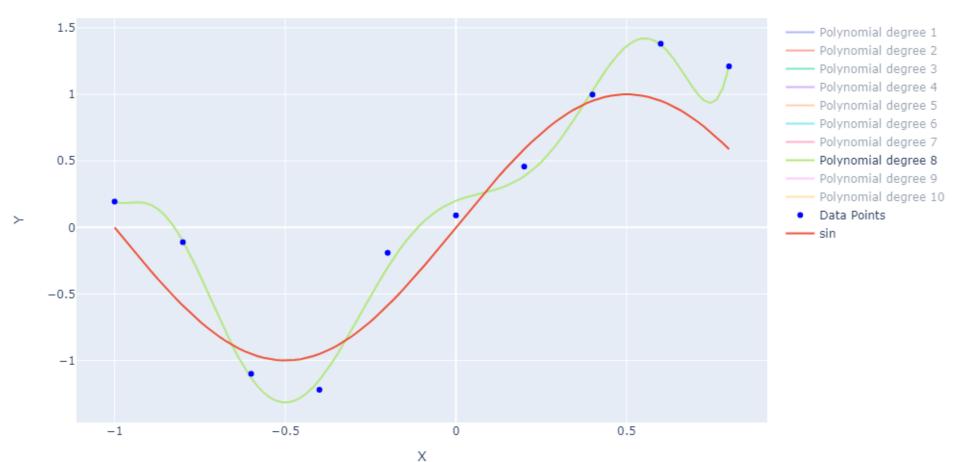


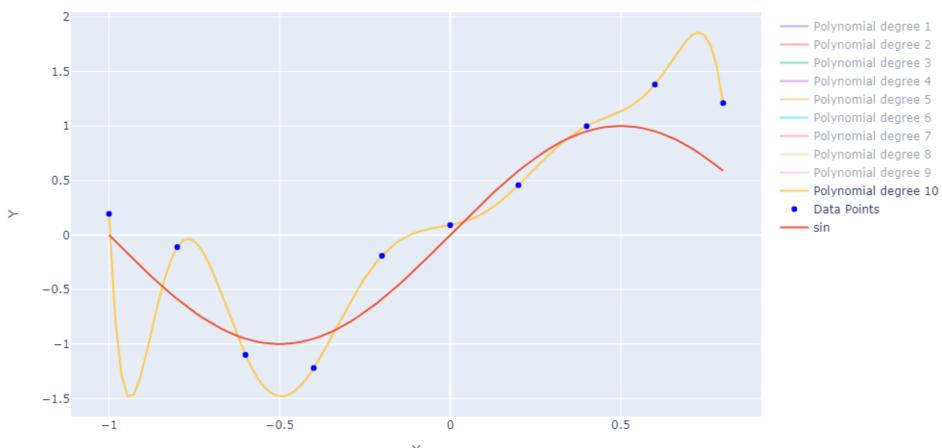


1.5 —— Polynomial degree 1 Polynomial degree 2 —— Polynomial degree 3 —— Polynomial degree 4 ---- Polynomial degree 5 —— Polynomial degree 6 ---- Polynomial degree 7 —— Polynomial degree 8 0.5 —— Polynomial degree 9 —— Polynomial degree 10 Data Points ---- sin -0.5 -0.5-10.5 Χ

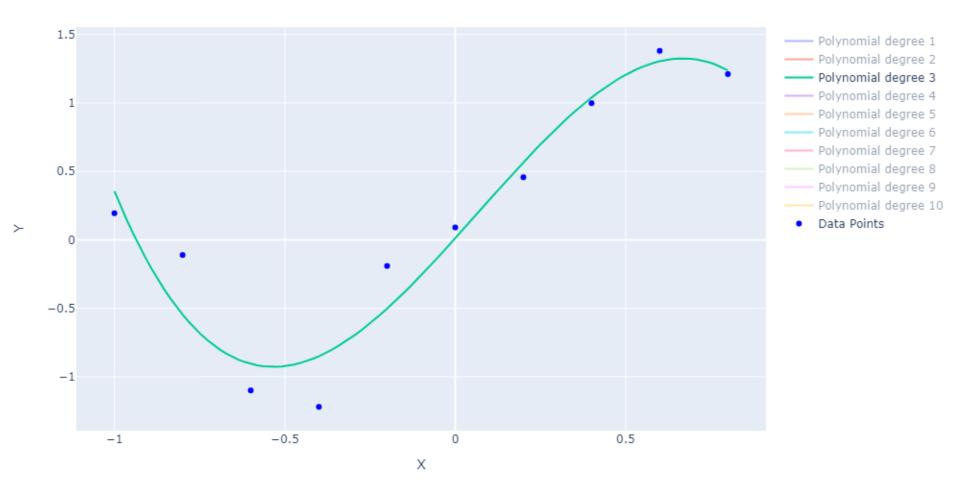
Data and Polynomial Regression 10 Samples

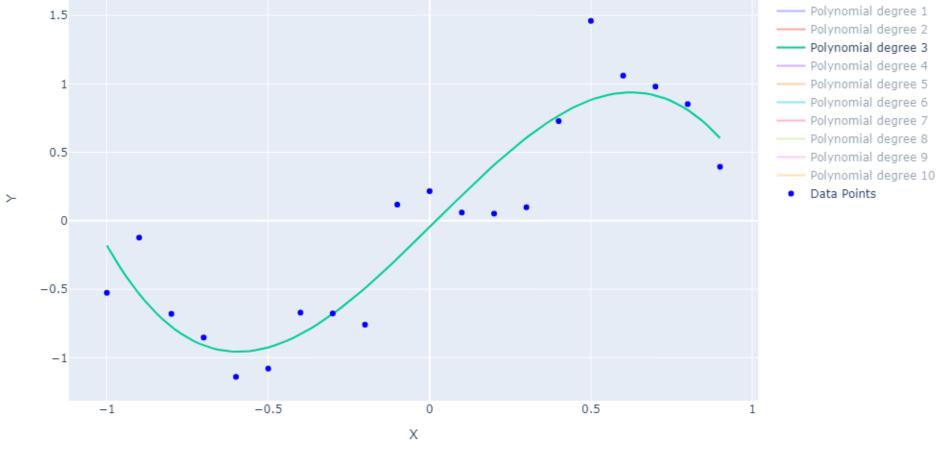
Data and Polynomial Regression 10 Samples





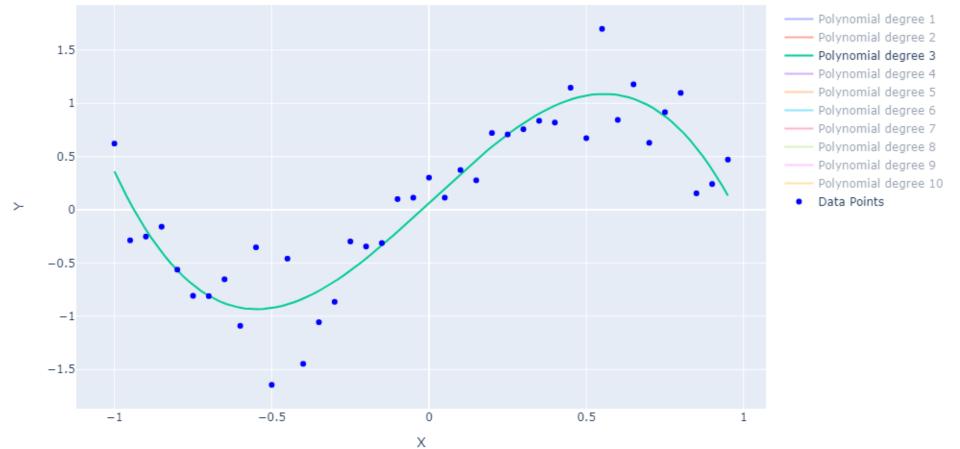
Data and Polynomial Regression 20 Samples

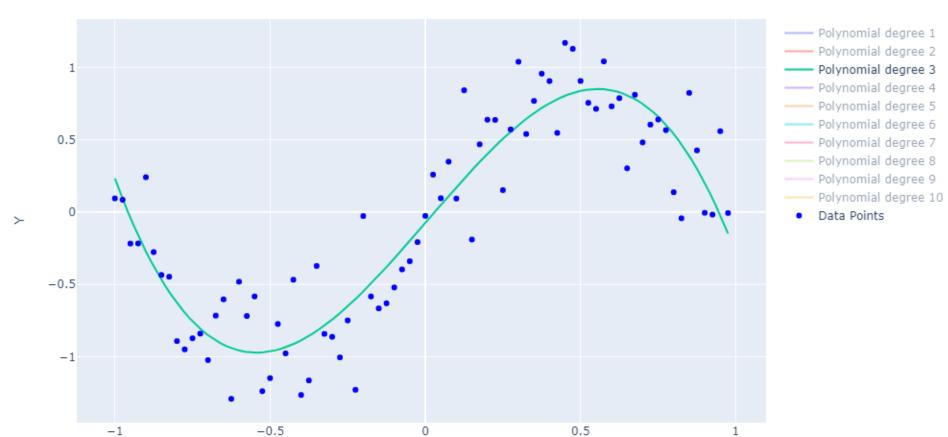


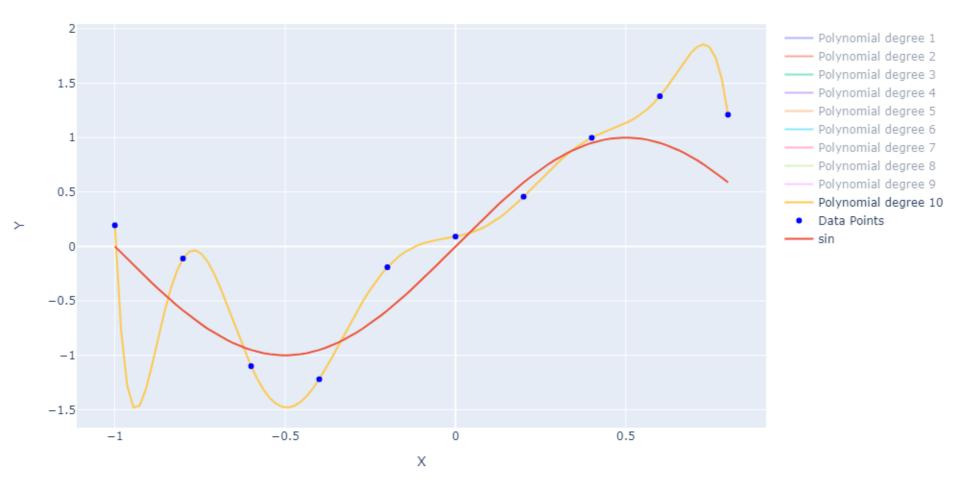


Data and Polynomial Regression 40 Samples

Data and Polynomial Regression 80 Samples



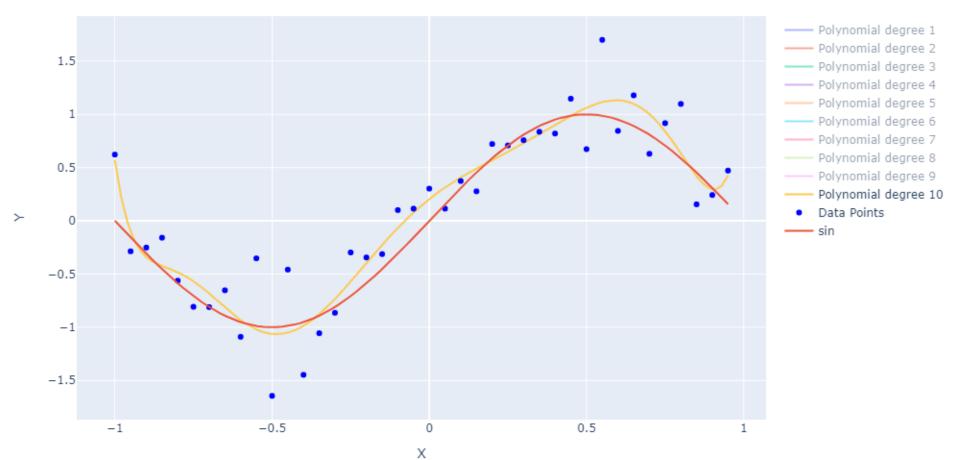


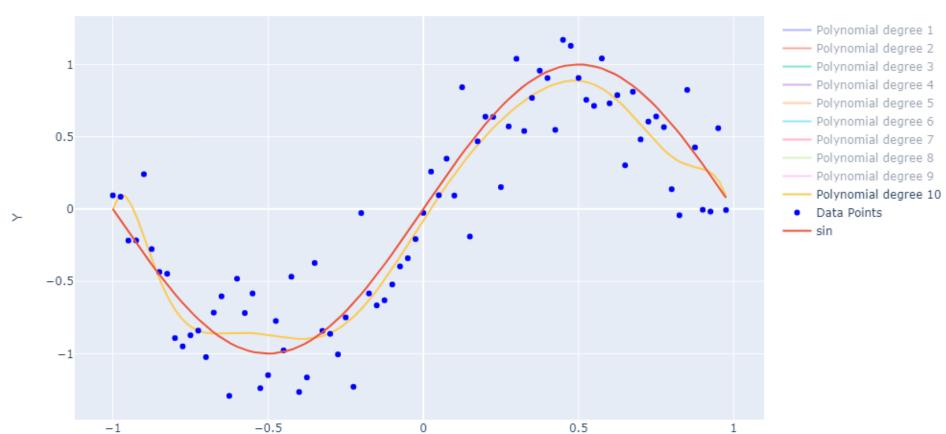


—— Polynomial degree 1 1.5 --- Polynomial degree 2 —— Polynomial degree 3 ---- Polynomial degree 4 ---- Polynomial degree 5 Polynomial degree 6 —— Polynomial degree 7 —— Polynomial degree 8 0.5 —— Polynomial degree 9 —— Polynomial degree 10 Data Points ---- sin -0.5 -0.50.5 -1Χ

Data and Polynomial Regression 40 Samples

Data and Polynomial Regression 80 Samples



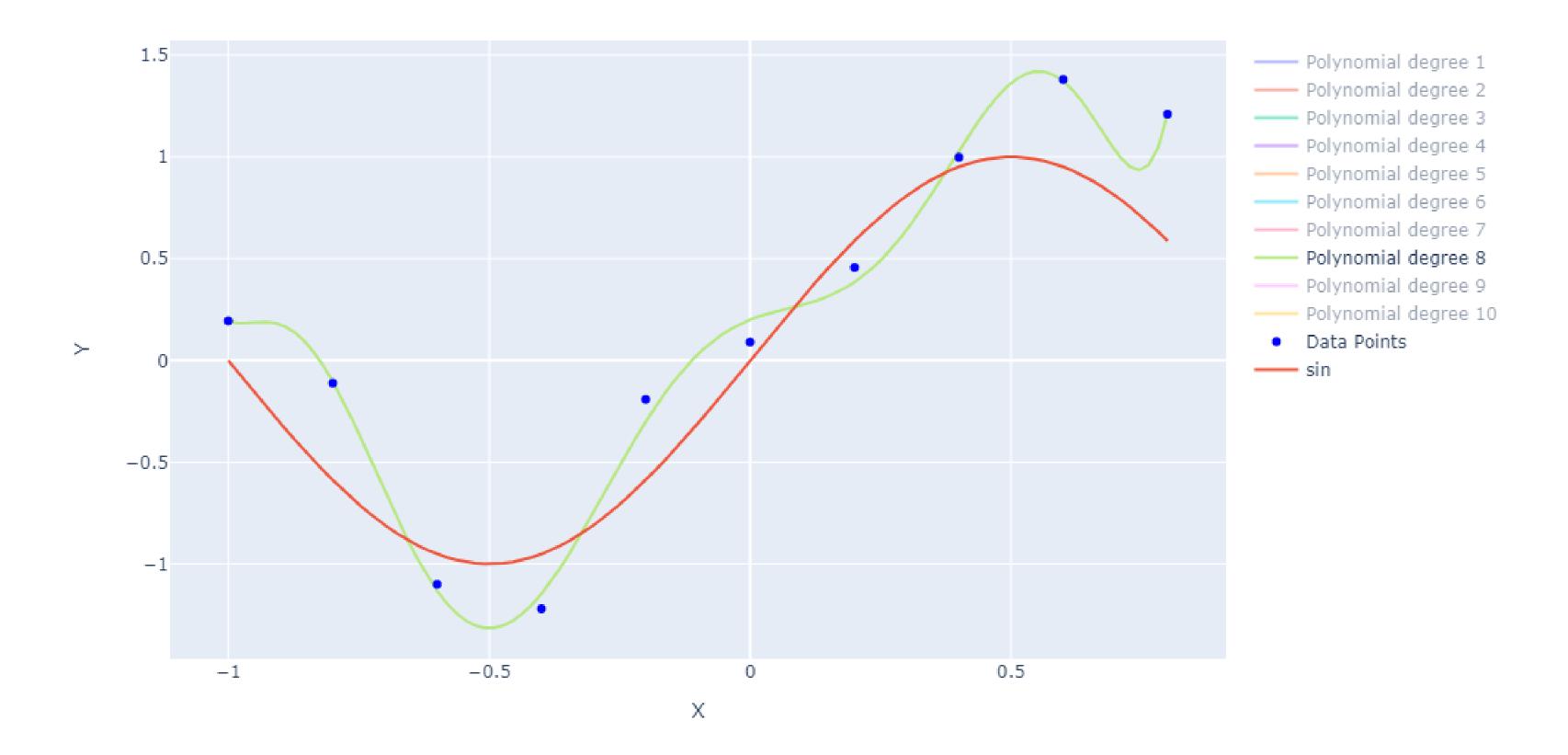


Coefficients

degree of polynomial = 8

อันดับ	Noiseless N = 10	Noisy N = 10	Noiseless N = 80	Noisy N = 80
wO	O	0.1999	O	-0.1266
w1	3.1414	1.0153	3.1399	3.1207
w2	0.0023	-5.1034	0.0009	1.758
w3	-5.163	20.0053	-5.1425	-6.4256
w4	-0.0234	31.2838	-0.0058	-8.0255
w5	2.5146	-67.3317	2.4489	5.2356
w6	0.0699	-67.4224	0.0117	11.603
w7	-0.5049	55.6246	-0.4471	-1.9941
w8	-0.0606	50.5487	-0.0071	-5.1145

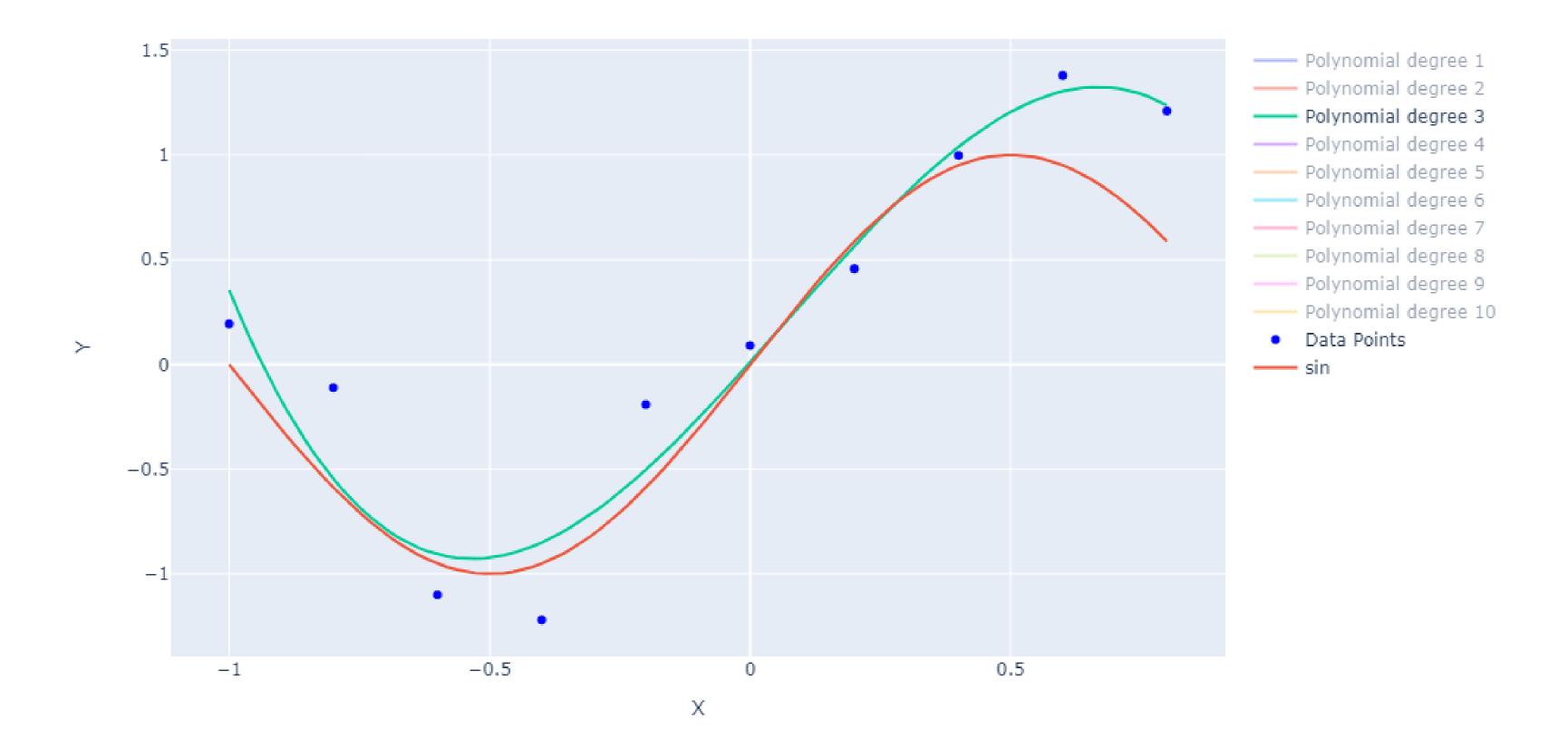
Data and Polynomial Regression 10 Samples



degree of polynomial = 3

อันดับ	Noiseless N = 10	Noisy N = 10	Noiseless N = 80	Noisy N = 80
wO	0.0254	0.0108	0.0038	-0.0752
w1	2.6739	2.7772	2.6920	2.4884
w2	-0.1323	0.5232	-0.0190	0.0491
w3	-2.8698	-2.5980	-2.8952	-2.7469

Data and Polynomial Regression 10 Samples

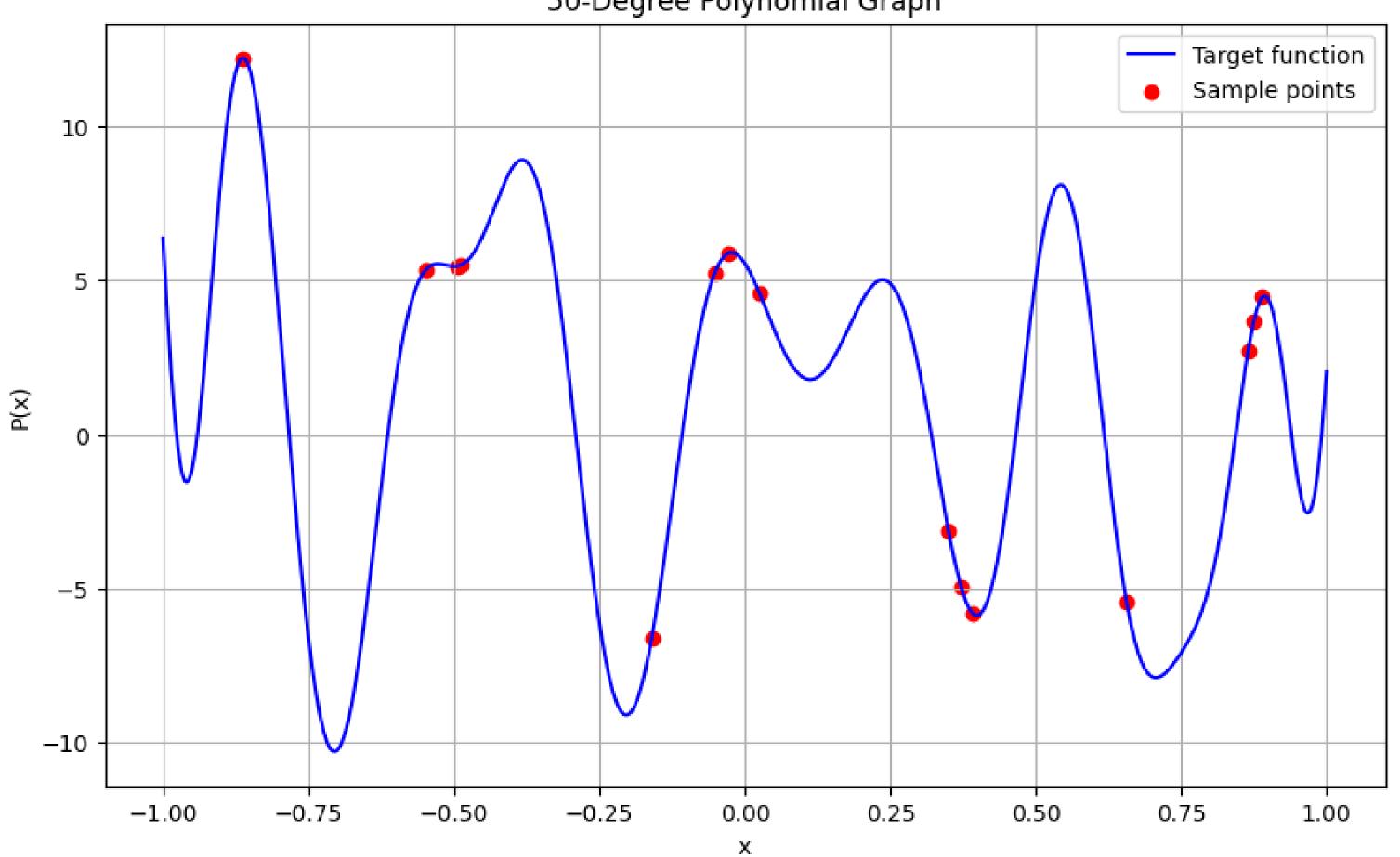


การทดลองเพิ่มเติม

สุ่มจุดมา 15 จุด จาก High order target function

Noiseless high-order Target







2. เขียนโปรแกรมสำหรับการทำ Nested Cross-Validation และ ออกแบบการทดลองเพื่อแสดงให้เห็นถึง ความจำเป็นของการทำสองลูปแทนที่จะ ทำเพียงแค่ลูปเดียว

ผลการทดลอง Estimate ค่า Error ของ Model ที่มี Hyperparameter ด้วย Nested Cross Validation และ Cross Validation

Linear Regression, Degree 1 - 8

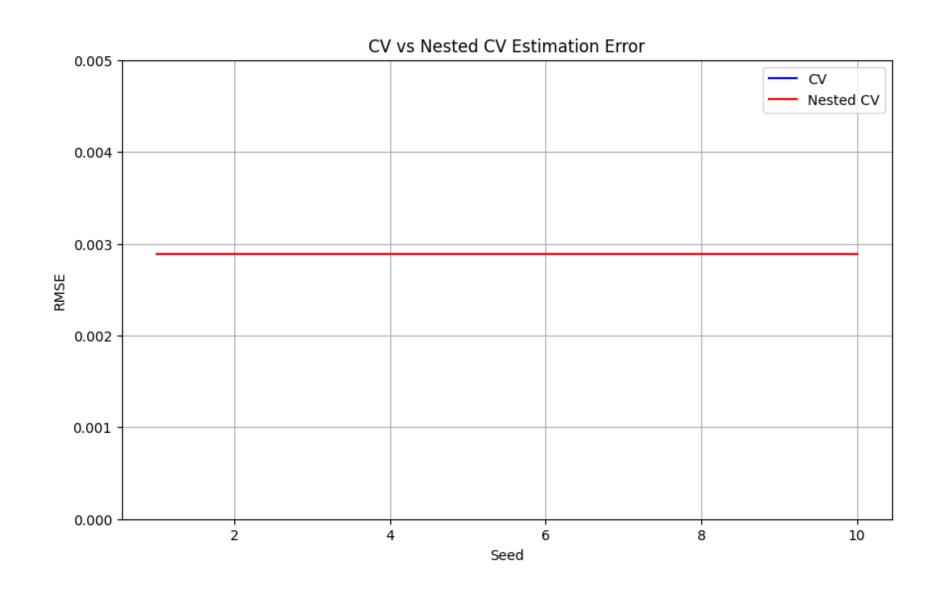
Noiseless Sin

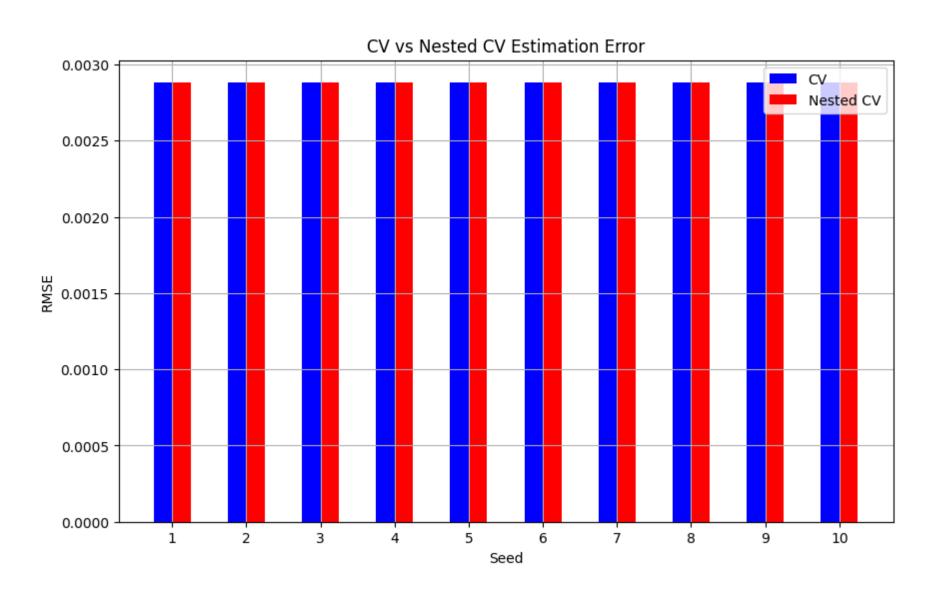
Sample	CV	Nested CV		
10	0.0029	0.0029		
20	0.0012	0.0016		
40	0.0007	0.002		
80	0.0005	0.002		

Noisy Sin

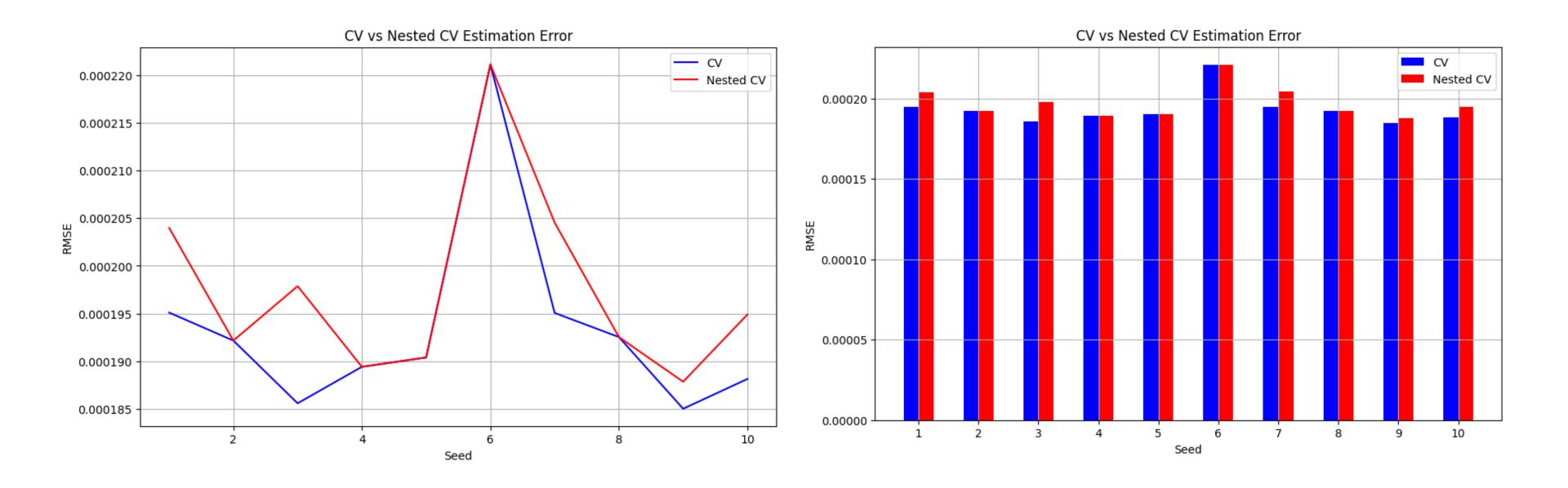
Sample	CV	Nested CV		
10	0.3355	0.3391		
20	0.3154	0.3341		
40	0.2827	0.2827		
80	0.2987	0.4239		

Noiseless Sin, 10 Samples

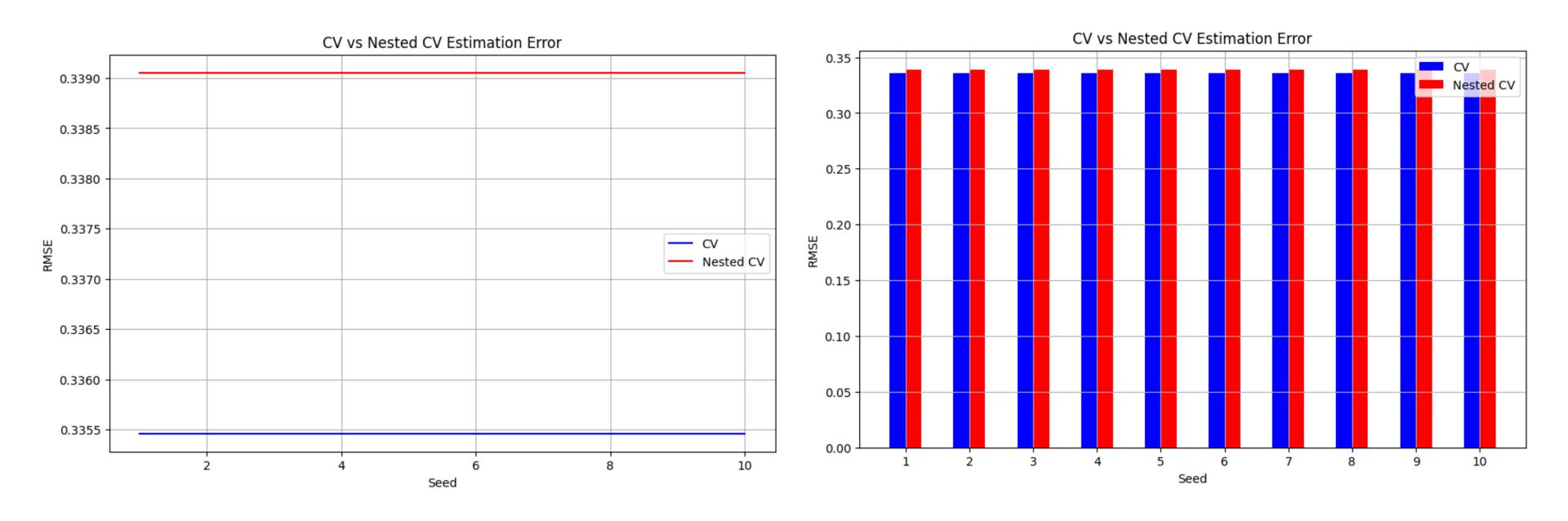




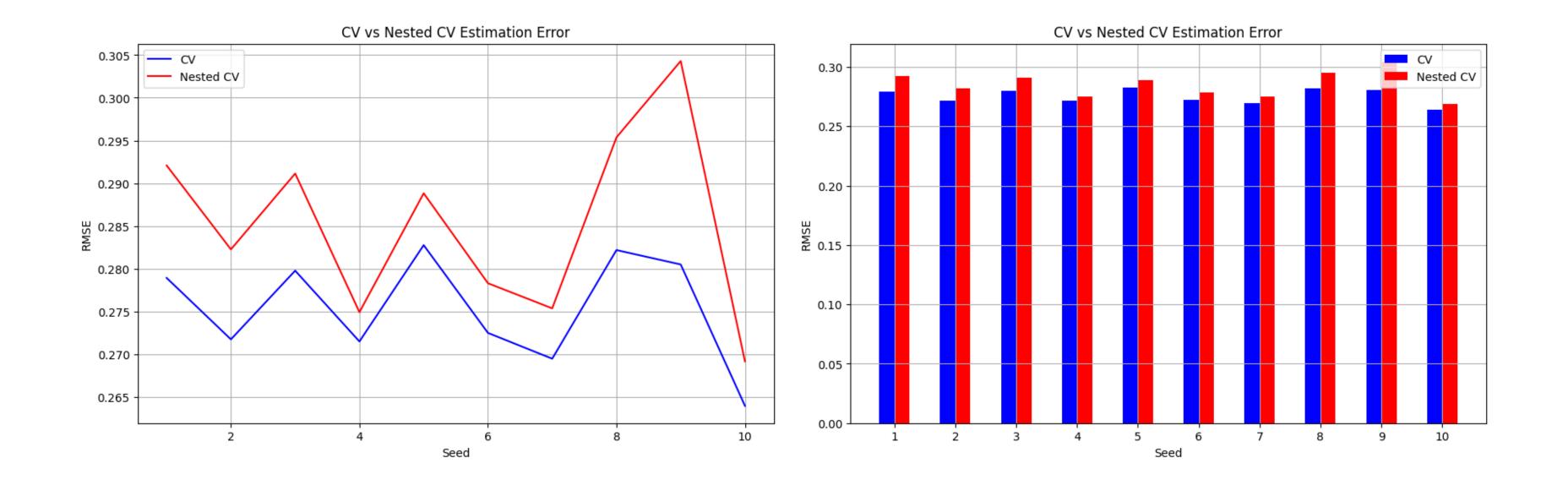
Noiseless Sin, 80 Samples



Noisy Sin, 10 Samples



Noisy Sin, 80 Samples



CV vs Nested CV Estimation Error

