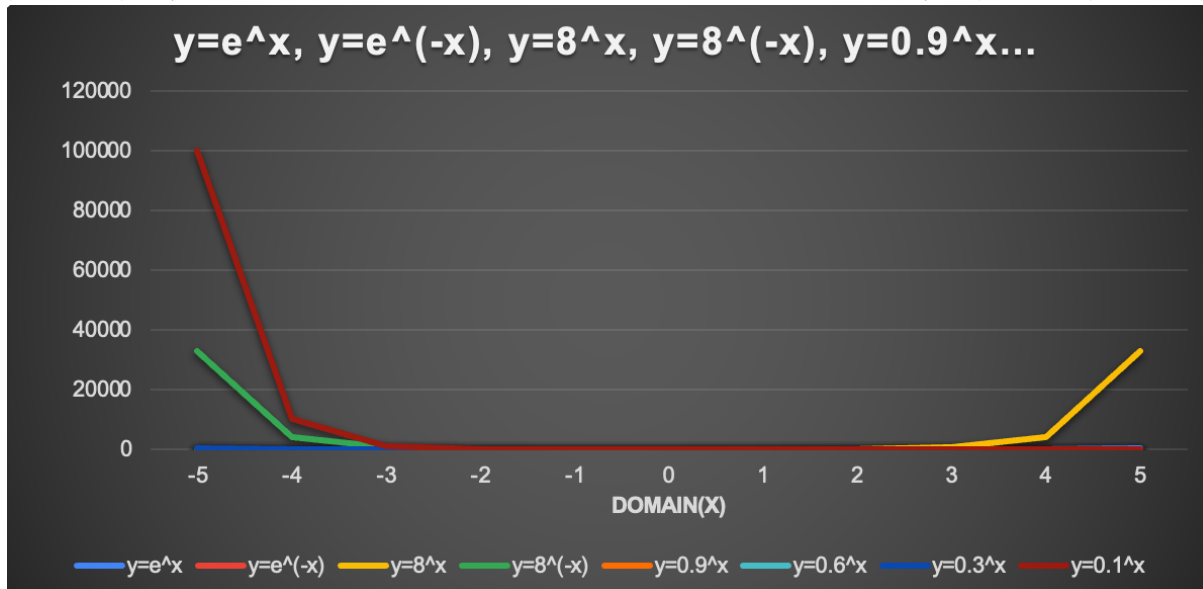


### Question-1:

Question-1								
Domain(x)	$y=e^x$	$y=e^{-x}$	$y=8^x$	$y=8^{-x}$	$y=0.9^x$	$y=0.6^x$	$y=0.3^x$	$y=0.1^x$
-5	0.0067	148.4132	0	32768	1.6935	12.8601	411.5226	100000
-4	0.0183	54.5982	0.0002	4096	1.5242	7.716	123.4568	10000
-3	0.0498	20.0855	0.002	512	1.3717	4.6296	37.037	1000
-2	0.1353	7.3891	0.0156	64	1.2346	2.7778	11.1111	100
-1	0.3679	2.7183	0.125	8	1.1111	1.6667	3.3333	10
0	1	1	1	1	1	1	1	1
1	2.7183	0.3679	8	0.125	0.9	0.6	0.3	0.1
2	7.3891	0.1353	64	0.0156	0.81	0.36	0.09	0.01
3	20.0855	0.0498	512	0.002	0.729	0.216	0.027	0.001
4	54.5982	0.0183	4096	0.0002	0.6561	0.1296	0.0081	0.0001
5	148.4132	0.0067	32768	0	0.5905	0.0778	0.0024	0



### Question-2:

We've given that  $f(x)=10^x$

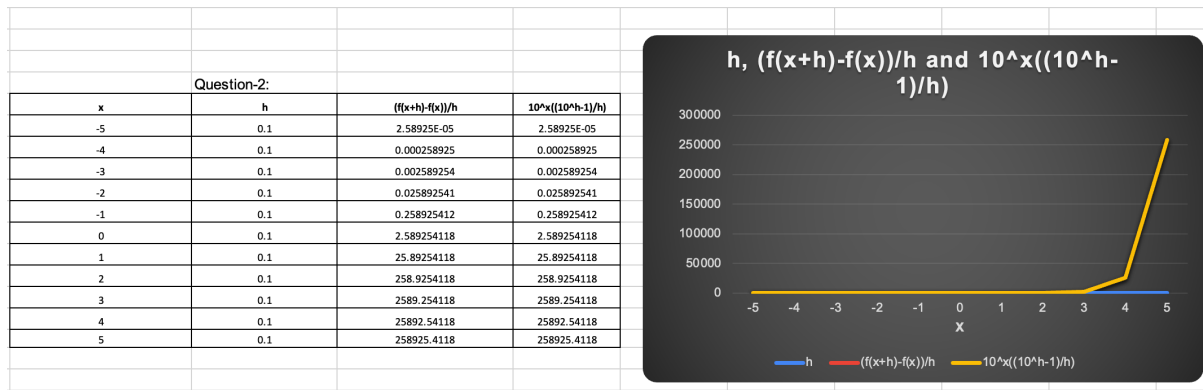
To prove,

$$\frac{f(x+h)-f(x)}{h} = 10^x \left( \frac{10^h - 1}{h} \right)$$

Here, taking LHS

$$\begin{aligned}
 & \frac{f(x+h)-f(x)}{h} \\
 &= \frac{10^{x+h}-10^x}{h} \quad (\text{Since, } f(x)=10^x) \\
 &= \frac{10^x \cdot 10^h - 10^x}{h} \\
 &= \frac{10^x (10^h - 1)}{h}
 \end{aligned}$$

Hence, LHS = RHS



### Question-3:

To compare the functions  $f(x) = x^5$  and  $g(x) = 5^x$  and determine which grows more rapidly when  $x$  is large, we can plot their curves in Excel and observe their behavior.

Let's create a table in Excel with the  $x$ -values ranging from, for example, 0 to 10. In the adjacent column, we can calculate the corresponding  $y$ -values for each function using the formulas  $f(x) = x^5$  and  $g(x) = 5^x$ .

After inputting the formulas and generating the values, we can select the data and create a scatter plot in Excel. The  $x$ -values will be plotted on the horizontal axis, and the corresponding  $y$ -values will be plotted on the vertical axis.

Upon examining the graph, we can observe that both curves start at the point  $(0, 0)$  since  $f(0) = 0^5 = 0$  and  $g(0) = 5^0 = 1$ . As  $x$  increases, the function  $f(x) = x^5$  grows rapidly but still follows a polynomial growth pattern. On the other hand, the function  $g(x) = 5^x$  grows even more rapidly and exhibits an exponential growth pattern.

We can compare their derivatives to prove mathematically that  $g(x) = 5^x$  grows more rapidly than  $f(x) = x^5$  as  $x$  becomes large.

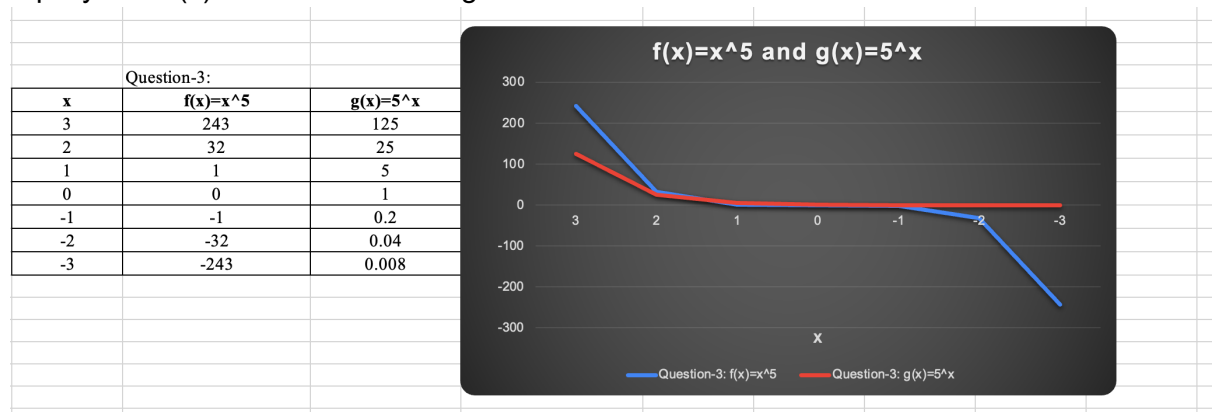
The derivative of  $f(x) = x^5$  can be calculated as follows:  $f'(x) = 5x^4$ . The derivative of  $g(x) = 5^x$  can be determined using the chain rule and logarithmic differentiation:

$$g'(x) = 5^x \cdot \ln(5)$$

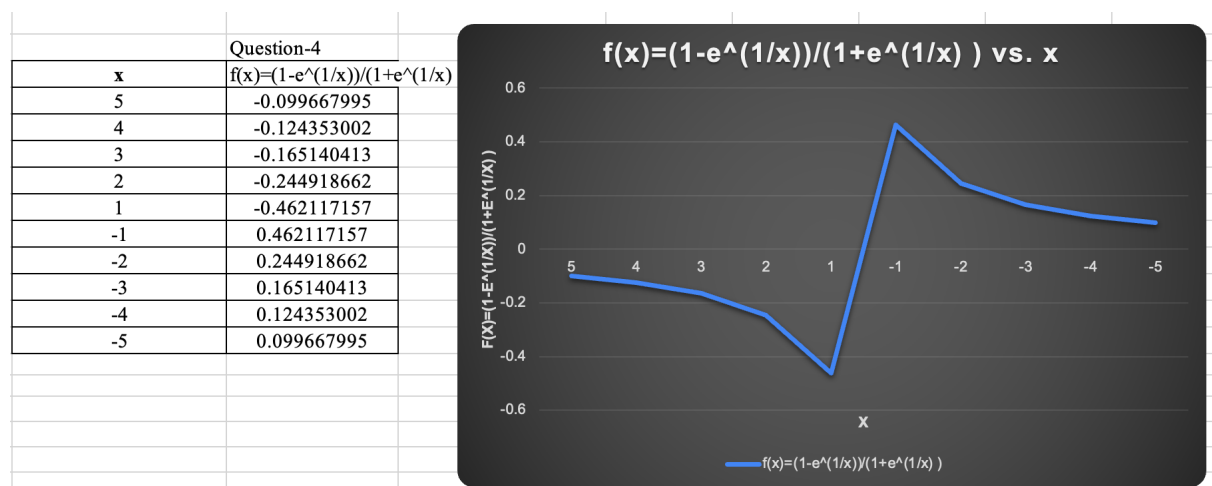
When evaluating these derivatives, it becomes evident that the rate of change of  $f(x)$  is dependent on the value of  $x$  and is limited by the power of  $x^4$ . As  $x$  approaches infinity, the derivative will tend to infinity but remain constrained by the power term.

However, the derivative of  $g(x) = 5^x$  includes the function value  $5^x$  itself, multiplied by the natural logarithm of 5. This implies that the rate of change of  $g(x)$  is directly proportional to its function value, resulting in exponential growth. As  $x$  becomes large, no limiting factor restricts the growth of  $g(x)$ .

Therefore, based on the mathematical analysis, we can conclude that  $g(x) = 5^x$  grows more rapidly than  $f(x) = x^5$  when  $x$  is large.



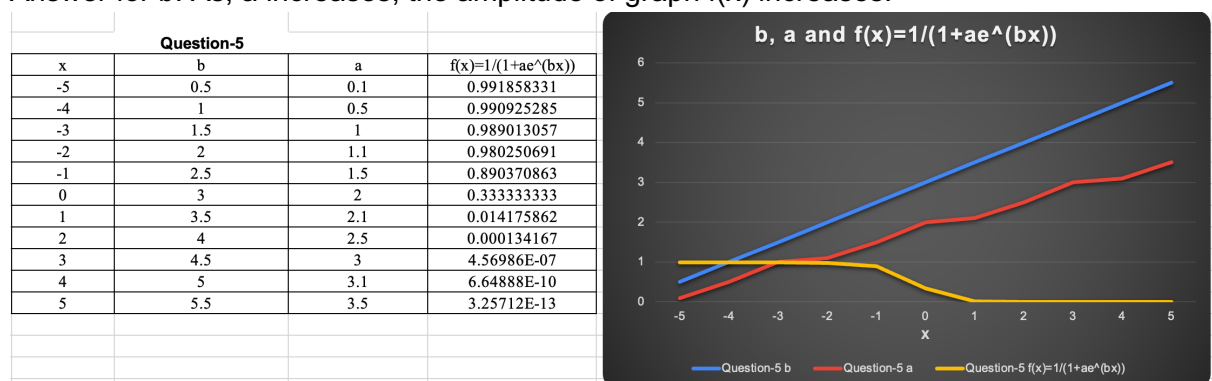
Question-4:



Question-5:

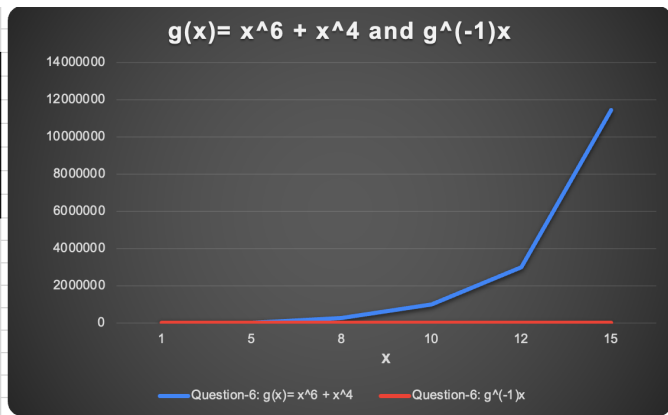
Answer for a: The graph  $f(x)$  becomes steeper as  $b$  increases when the value of  $a > 0$ .

Answer for b: As,  $a$  increases, the amplitude of graph  $f(x)$  increases.



Question-6:

Question-6:		
x	g(x)= x^6 + x^4	g^(-1)x
1	2	0.5
5	16250	6.15385E-05
8	266240	3.75601E-06
10	1010000	9.90099E-07
12	3006720	3.32588E-07
15	11441250	8.7403E-08



### Question-7:

#### #Solution-a

We've Given that,

$$Q(t) = Q_o(1 - e^{-\frac{t}{a}})$$

$$\frac{Q}{Q_o} = 1 - e^{-\frac{t}{a}}$$

Rearranging the equation we get,

$$1 - \frac{Q}{Q_o} = e^{-\frac{t}{a}}$$

Taking log on both sides, we get

$$\ln\left(1 - \frac{Q}{Q_o}\right) = -\frac{t}{a}$$

$$t = -a * \ln\left(1 - \frac{Q}{Q_o}\right) \text{ (eqn -1)}$$

$$\text{Therefore, } Q'(t) = -a * \ln\left(1 - \frac{Q}{Q_o}\right)$$

#### #Solution-b:

Given:

$$a = 2$$

$$Q(t) = 0.9Q_0 \text{ (90\% capacity represented by 0.9 times } Q_0)$$

Substituting these values into the equation:

$$t = -2 * \ln(1 - 0.9)$$

$$t = -2 * \ln(0.1)$$

$$t = -2 * (-2.3)$$

$$t = 4.6 \text{ seconds.}$$