# Channel Estimation Techniques for Multicarrier OFDM 5G Wireless Communication Systems

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#### Abstract

- We will discuss about channel estimation techniques in multicarrier orthogonal frequency-division-multiplexing (OFDM) 5G wireless communication systems in Rayleigh and Rician channels.
- Proposed M-estimator based channel estimation technique in comparison with classical least squares (LS) and linear minimum mean-squared error (LMMSE) estimation is studied and analyzed.
- We will compare the proposed technique over LS and LMMSE through simulations.

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# System Model

 OFDM is one of the efficient modulation formats used in present 5G wireless communication systems.

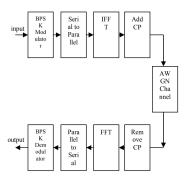


Figure: Block diagram of OFDM system with FFT

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# System Model

The received signal (at the receiver) may be described by

$$Y = HX + W \tag{1}$$

where

$$H = [H[0], H[1], ...., H[N-1]]^{T}$$
(2)

$$W = [W[0], W[1], ...., W[N-1]]^{T}$$
(3)

$$X = \begin{bmatrix} X[0] & 0 & \cdots & 0 \\ 0 & X[1] & & \vdots \\ \vdots & & \ddots & 0 \\ 0 & \cdots & 0 & X(N-1) \end{bmatrix}$$
(4)

# M-Estimator

consider a signal model

$$r_j = \sum_{k=1}^K s_j^k \theta_k + n_j, \quad j = 1, 2, ...., N$$
 (5)

or in matrix notation

$$\underline{r} = \underline{S\theta} + \underline{n} \tag{6}$$

where

$$\underline{S} \triangleq [\underline{s_1}, \underline{s_2}, \dots \underline{s_K}]$$

$$\underline{\theta} \triangleq [\theta_1, \theta_2, \dots \theta_K]^T$$
(8)

$$\underline{\theta} \triangleq \left[\theta_1, \theta_2, \cdots \theta_K\right]^T \tag{8}$$

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## M-Estimator

Huber proposed to minimize a sum of a less rapidly increasing function  $\rho$  of the residuals

$$\underline{\hat{\theta}} = \arg\min_{\theta \in \mathcal{R}^K} \sum_{j=1}^N \rho \left( r_j - \sum_{k=1}^K s_j^k \theta_k \right)$$
 (9)

suppose that  $\rho$  has a derivative  $\psi=\rho'$ ; then , the solution to (9) satisfies the equation

$$\sum_{j=1}^{N} \psi \left( r_j - \sum_{l=1}^{K} s_j^l \theta_l \right) s_j^k = 0, \quad k = 1, 2, \dots, K$$
 (10)

or in vector form

$$S^{T}\psi\left(\underline{r}-\underline{S}\underline{\theta}\right)=\underline{0}_{K} \tag{11}$$

where  $\psi(\underline{x}) \triangleq [\psi(x_1), ...., \psi(x_K)]^T$  for any  $\underline{x} \in \mathcal{R}^K$  (12)

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### M-Estimator

Assume that the penalty function  $\rho(x)$  in (9) has a bounded second-order derivative i.e.,  $|\rho''(x)| = |\psi'(x)| \le \mu$  for some  $\mu > 0$ . Then (10) can be solved iteratively by the following modified residual method . Let  $\underline{\theta}^t$  be the estimated at the tth step;then it is updated according to

$$\underline{z}^t \triangleq \psi\left(\underline{r} - \underline{S}\underline{\theta}^t\right) \tag{13}$$

$$\underline{\theta}^{t+1} = \underline{\theta}^t + \frac{1}{\mu} \left( \underline{S}^T \underline{S} \right)^{-1} \underline{S}^T \underline{z}^t \tag{14}$$

where  $\mu$  is a step-size parameter  $.\left(\mu = \frac{1}{N}\sum_{j=1}^N \psi'\left(r_j - \sum_{k=1}^K s_j^k \theta_k^t\right)\right)$ 

For initial estimate  $\underline{\theta}^0$ , we can take

$$\underline{\theta}^{0} = \frac{1}{\mu} \left( \underline{S}^{T} \underline{S} \right)^{-1} \underline{S}^{T} \underline{r}. \tag{15}$$

The iteration is stopped if  $\|\underline{\theta}^t - \underline{\theta}^{t-1}\| \le \epsilon$  for some small number  $\epsilon$  .

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# Proposed M-Estimator

Penalty, influence and weight functions of the proposed M-estimator for channel estimation in 5G multicarrier wireless communications in Rayleigh and Rician fading channels are given by

$$\rho_{PROPOSED}(x) = \begin{cases} \frac{x^2}{2} & |x| \le a \\ a^2 - a|x| & a < |x| \le b \\ \frac{-ab}{2} \exp\left(1 - \frac{x^2}{b^2}\right) + d & |x| > b \end{cases}$$
(16)

$$\psi_{PROPOSED}(x) = \begin{cases} x & |x| \le a \\ asgn(x) & a < |x| \le b \\ \frac{a}{b}x \exp\left(1 - \frac{x^2}{b^2}\right) & |x| > b \end{cases}$$
(17)

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# Proposed M-Estimator

$$w_{PROPOSED}(x) = \begin{cases} 1 & |x| \le a \\ \frac{asgn(x)}{x} & a < |x| \le b \\ \frac{a}{b} \exp\left(1 - \frac{x^2}{b^2}\right) & |x| > b \end{cases}$$
 (18)

where a and b are any constants and x is any data. From an influence function, robustness measures are derived and  $a(=kv^2)$  and  $b(=2kv^2)$  are selected (where k is any constant).

where  $\rho(x)$  is penalty function,  $\psi(x) = \frac{d\rho(x)}{dx}$  is the influence function and  $w(x) = \frac{\psi(x)}{x}$  is the weight function.

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# Proposed M-Estimator

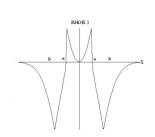


Figure: Proposed M-estimator penalty function.

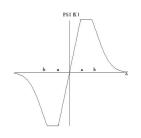


Figure: Proposed M-estimator influence function

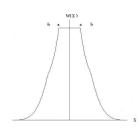


Figure: Proposed M-estimator weight function

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# Channel Estimation

#### LS channel estimation

$$\hat{H}_{LS} = \left(X^{H}X\right)^{-1} X^{H}Y = X^{-1}Y \tag{19}$$

where estimate of H is  $\hat{H}$  and  $X^H$  is the Hermitian matrix of X

#### MMSE channel estimation

$$\hat{H}_{MMSE} = R_{HH} \left[ R_{HH} + \left( XX^H \right)^{-1} W v^2 \right]^{-1} \hat{H}_{LS}$$
 (20)

where  $R_{HH}$  is the matrix form of auto-covariance of X and  $v^2$  is variance of noise vector.

## Channel Estimation

#### proposed estimation

Proposed technique estimates channel parameters for 5G multicarrier wireless communications in Rayleigh and Rician fading channels using

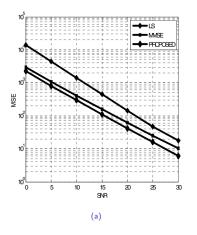
$$H^{t+1} = H^t + \frac{1}{\mu} \left( X^H X \right)^{-1} X^H \psi \left( Y - H X \right)$$
 (21)

for some  $\mu > 0$  where  $H^0 = \frac{1}{\mu} \hat{H}_{LS}$ 

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## SIMULATION RESULTS

In this simulation , the comparison shows the performance gains achieved by the proposed technique over LS and MMSE estimation in multicarrier OFDM 5G wireless communication systems



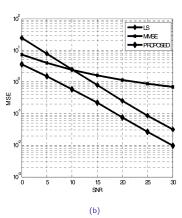


Figure: MSE vs. SNR Performance of LS, MMSE and Proposed channel estimators in (a) Rayleigh and (b) Rician fading 🔊 🤉 🖰

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## CONCLUSION

- M-estimator based channel estimation technique for 5G multicarrier OFDM wireless communication systems in Rayleigh and Rician fading channels is analyzed in this paper.
- Observations from simulation results imply that the proposed M-estimator based channel estimation technique for 5G multicarrier OFDM wireless communication systems offers better performance than LS and MMSE techniques in Rayleigh and Rician fading channels.

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