

$$D) f(x) = 20 e^{-20(d-12.5)}$$

Limit: 12.5 to 12.6

$$\Rightarrow \int_{12.5}^{12.6} 20 e^{-20(d-12.5)} dd$$

$$\Rightarrow 20 \left[\frac{1}{-20} e^{-20(d-12.5)} \right]_{12.5}^{12.6}$$

$$\Rightarrow - \left[e^{-20(d-12.5)} \right]_{12.5}^{12.6}$$

$$\Rightarrow - \left[e^{-20(12.6-12.5)} - e^{-20(12.5-12.5)} \right]$$

$$\Rightarrow - \left[-e^{-20(0)} + e^{-20(0.1)} \right]$$

$$\Rightarrow - [-e^0 + e^{-2}]$$

$$= -[-1 + e^{-2}]$$

$$= 1 - e^{-2}$$

$$= 0.863$$

$$\text{Area} = 1 - 0.863$$

$$\text{Area} = 0.137$$

CDF at 11 is zero due it will not lies

$$R2) i) P(Z > 1.26)$$

$$= 1 - 0.8962$$

$$\approx 0.11$$

$$ii) P(Z < -0.86) = 1 - 0.805$$

$$\approx 0.195$$

$$iii) P(Z > -1.37) = 1 - 0.9147$$

$$\approx 0.17$$

$$iv) P(-1.25 < Z < 0.37) = (1 - 0.8944) + 0.6444$$

$$= 0.21 + 0.64$$

$$\approx 0.85$$

$$b) P(Z > z) = 0.05 = 1 - 0.05$$

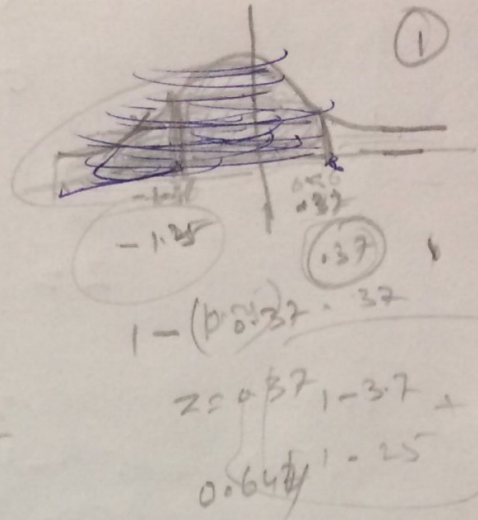
$$= \underline{0.95}$$

$$z = \underline{1.65}$$

$$c) \text{ find the value } (-2 < Z < 2) = 0.99$$

$$= (-\infty < Z < 2.33)$$

$$= 0.99$$



Q3) Normal distribution:

$$\mu = 10$$

$$\sigma^2 = 4$$

$$x = 13$$

$$z = \frac{13-10}{2}$$

$$= \frac{3}{2}$$

$$= 1.5$$

$$z = 0.9332$$

$$P(z > 1.5) = 1 - 0.9332$$

$$= 0.0668$$

0.07

b) $\mu = 9, 11$

$$\sigma = 4$$

$$z = \frac{9-10}{2}$$

$$= -\frac{1}{2}$$

$$= -0.5$$

$$z = \frac{11-10}{2}$$

$$= \frac{1}{2}$$

$$= 0.5$$

$$P(-0.5 < z < 0.5) =$$

$$= 0.6915 - (1 - 0.6915)$$

$$= 0.6915 - 0.3085$$

$$= 0.383$$

a) probability of error

$$P(x) = 0.98$$

$$z = 2.06$$

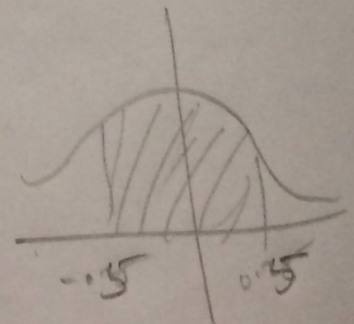
$$\frac{x-\mu}{\sigma} = 2.06$$

$$\frac{x-10}{2} = 2.06$$

$$x-10 = 4.12$$

$$x = 14.12$$

14.12



$$4) \mu = 0.2508$$

$$\sigma = 0.0005$$

shaft size 0.2500 ± 0.0015

$$P(0.2485 \leq Z \leq 0.2495)$$

$$= \frac{0.2495 - 0.2508}{0.0005} > Z > \frac{0.2485 - 0.2508}{0.0005}$$

$$= 1.4 > Z > -4.6$$

$$= 0.9192$$

(1) probability of shaft in spec with specification is 0.2485 to 0.2495

$$\mu = 0.2508 \text{ (original)}$$

$$\text{if } \mu = 0.2500$$

$$P(0.2485 \leq Z \leq 0.2495) = \frac{0.2495 - 0.2500}{0.0005} \leq Z \leq \frac{0.2485 - 0.2500}{0.0005}$$

$$= P(-3 \leq Z \leq -3)$$

$$= 0.9986 - (1 - 0.9986)$$

$$= 0.9972$$

Conclusion: It will get keep increasing