Investigation of the exponential distribution in R

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Abstract

This project investigates the exponential distribution in R and compare it with the Central Limit Theorem. It investigates the distribution of averages of forty exponentials. Thousand simulations are performed.

The aims of the project are listed below:

- 1. Show the sample mean and compare it to the theoretical mean of the distribution.
- 2. Show how variable the sample is (via variance) and compare it to the theoretical variance of the distribution.
- 3. Show that the distribution is approximately normal, i.e. the difference between the distribution of a large collection of random exponentials and the distribution of a large collection of averages of 40 exponentials is negligible.

Import the necessary packages

The following packages are to be imported.

• ggplot2

library(ggplot2)

Initialization of important Variables

The seed is initialized with 100. The lambda (rate parameter) is set as 0.2. The sample size is set to 40. The number of simulations is 1000.

```
set.seed(100)

lambda <- 0.2
nsim <- 1000
sampleSize <- 40</pre>
```

Run the simulations

The simulations are run and stored in the matrix sims.

```
sims <- matrix(rexp(nsim*sampleSize, lambda), nsim, sampleSize)</pre>
```

Comparision between Sample Mean and Theoritical Mean

The value of the Theoritical mean is 1/lambda = 5.

The Sample mean is calculated below.

```
tMean <- 1/lambda # Theoritical Mean
sMean <- mean(rowMeans(sims)) #Sample Mean
```

The value of the Sample mean is 4.999702.

The difference between the two means is -0.000298, which is -0.00006% of the Theoritical mean.

Comparision between Sample Variance and Theoritical Variance

The value of the Theoritical variance is (1/lambda^2)*(1/sampleSize) = 0.625.

The Sample mean is calculated below.

```
tVar <- (1/lambda^2)*(1/sampleSize) # Theoritical Variance
sVar <- var(rowMeans(sims)) #Sample Variance
```

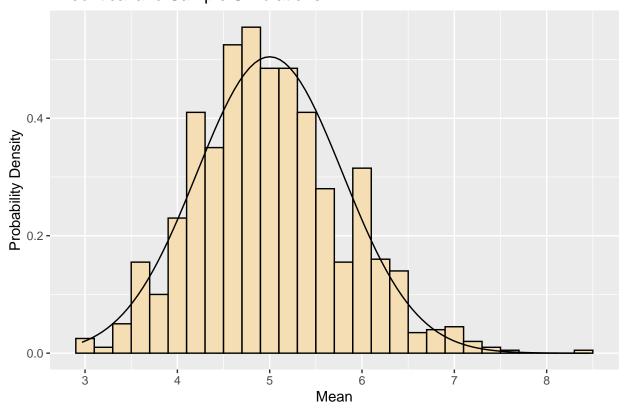
The value of the Sample variance is 0.63353.

The difference between the two variances is 0.00853, which is 0.013648% of the Theoritical variance.

Comparisions of the Distributions

Plot the Theoritical as well as the sample Distributions.

Theoritical and Sample Simulations



Both the distributions follow the same pattern.

Results

- 1. Theoritical Mean is 5, Sample Mean is 4.999702. The difference between the two means is -0.000298, which is -0.00006% of the Theoritical Mean.
- 2. Theoritical Variance is 0.625, Sample Variance is 0.63353. The difference between the two variances is 0.00853, which is 0.013648% of the Theoritical Variance.
- 3. Both the distributions follow the same pattern.

End