

# Statistical Data Analysis

## Exercise Session 8

### Exercise 1 : PCR Regression.

Load the pollution dataset from the SMPracticals package. More information about this data can be found in ?SMPracticals::pollution. The variables hc, nox and so are right-skewed distributed. Work with the logarithm of these variables.

1. Investigate the presence of multicollinearity in this data set, based on the correlation matrix and the VIF values.
2. Perform a PCR regression on the first 50 observations.
  - Select the number of components based on the PCA analysis on the predictor variables.
  - Perform the PCR regression using the pcr function from the pls package.
  - Check that the coefficients obtained correspond with performing an LS analysis on the selected PCA scores.
  - Compared the obtained coefficients with an analysis of the complete data.
3. Now select the number of PCR components based on
  - The RMSEP of the training data set (observations 1 to 50)
  - The RMSEP based on leave-one-outcross validation (from the training data set)
  - The RMSEP calculated on the validation set (observations 51 to 60). Use the validation plot function for this.

### Exercise 2: Ridge Regression.

Consider the same dataset as in exercise 1. Perform a ridge regression with the first 50 observations:

1. Determine a good optimal value for  $\lambda$ , the ridge parameter, based on the ridge trace and the VIF values.
2. Perform ridge regression with this chosen value for  $\lambda$ .
3. Calculate the RMSEP of the validation set (observations 51 to 60). Compare the results of the RMSEP values based on PCR.

### Exercise 3: Robust Regression.

Load the hills data set from the MASS library.

1. Perform an LS analysis. Determine the observations with the largest studentized residual. Also make a residual plot and normal quantile plot.
2. Determine LS-based diagnostics to detect outliers: diagonal elements of the hat matrix, DFFITS, DFBETAS, Cook's distance. Always identify the points that are outliers according to the corresponding criteria.
3. Perform LTS regression with 50% breakpoint. Compare the parameter estimates with the LS solution.
4. Identify the outliers according to the LTS method. Make the diagnostic plot to divide them into good / bad leverage points and vertical outliers.

5. Make a scatter plot of the predictor variables. Add the tolerance ellipse to this, based on the classical average and covariance matrix. Also add the MCD-based tolerance ellipse. Compare the robust distances with the Mahalanobis distances.
6. Compare the LTS results when you lower the breakpoint.

Some useful functions:

1. `lm.ridge()` in the MASS library.
2. `ltsReg()` and `covMcd()` in the robustbase library.