## Jeff Rowell

# CS143 Spring 2025 – Written Assignment 2 Due Monday, April 28, 2025 11:59 PM PDT

This assignment covers context free grammars and parsing. You may discuss this assignment with other students and work on the problems together. However, your write-up should be your own individual work, and you should indicate in your submission who you worked with, if applicable. Assignments can be submitted electronically through Gradescope as a PDF by 11:59 PM PDT. Please review the the course policies for more information: https://web.stanford.edu/class/cs143/policies/. A LATEX template for writing your solutions is available on the course website. If you need to draw parse trees in LATEX, you may use the forest package: https://ctan.org/pkg/forest.

g/fore	est.					
acc	_	g ambiguous g	,		ages. Any grammar is correct language. The	
(a	where the expres	The set of all strings over the alphabet $\{3,4,*,-\}$ representing valid products of integers where the expression evaluates to some positive odd value. Example Strings in the Language:				
		3	3*433	-3*3*-3343	3	
	Strings not in the Language:					
		arepsilon	3	-3*3*-3344		
	Solution:					
(b)	The set of all strings over the alphabet $\{a,b,[,],,\}$ representing nested lists of $a$ and $b$ 's where each list has an even length. Nested lists are defined as comma separated sequences of elements enclosed with a pair of square brackets $[]$ , where an element may be an $a$ , $b$ , or another list. Example Strings in the Language:					
		[a, [	[[b,a],a]]	[[],[a,b],[a,a]	, [[], [b, b]]]	
	Strings not in the Language:					
	arepsilon	b	[a, b,]	[a	[a, [[b], a]]	

## Solution:

(c) The set of all strings over the alphabet  $\{0,1\}$  where the number of 1's is more than the number of 0's.

Example Strings in the Language:

1 101 001111

Strings not in the Language:

 $\varepsilon$  0 01100101

#### **Solution:**

(d) The set of all strings over the alphabet  $\{0,1\}$  in the language  $L:\{1^i0^j1^k\mid j\geq i+k\}$ . Example Strings in the Language:

 $\begin{array}{ccc} 0 & 100011 & \varepsilon \\ \\ \text{Strings not in the Language:} & & & \\ 1 & 010 & 101 \\ \end{array}$ 

2. Consider the following grammar for if-then-else expressions that involve a variable x:

$$E \to \text{if } x \text{ then } E \mid M$$
 
$$M \to \text{if } x \text{ then } M \text{ else } E \mid x$$

Is this grammar ambiguous or not? If yes, give an example of an expression with two different parse trees and draw the two parse trees. If not, explain why that is the case.

3. (a) Left factor the following grammar:

$$S \rightarrow T \mid T + T \mid T * T$$
 
$$T \rightarrow Ta \mid Tb \mid cU$$
 
$$U \rightarrow U0 \mid U1 \mid \varepsilon$$

## Solution:

(b) Eliminate left recursion from the following grammar:

$$\begin{split} S &\to S + S \mid (S) \mid T \\ T &\to UUb \mid Ta \\ U &\to TTc \mid c \end{split}$$

4. Consider the following CFG, where the set of terminals is  $\{a, b, c, <, >\}$ :

$$S \rightarrow T < U \mid b > U$$
 
$$T \rightarrow aS < S \mid cU \mid > b$$
 
$$U \rightarrow > Ta \mid < Sb$$

(a) Construct the FIRST sets for each of the nonterminals.

#### **Solution:**

(b) Construct the FOLLOW sets for each of the nonterminals.

#### Solution:

(c) Construct the LL(1) parsing table for the grammar. Where applicable, list all possible productions for every parse table cell.

#### **Solution:**

(d) Show the sequence of stack, input, and action configurations that occur during an LL(1) parse of the string "> b <>> ba". At the beginning of the parse, the stack should contain a single S. The acceptable actions include: "out production>", "match <terminal>", "accept", and "error".

5. Consider the following grammar G over the alphabet  $\Sigma = \{a, b, c\}$ :

$$S' \to S$$

$$S \to Aa$$

$$S \to Bb$$

$$A \to Ac$$

$$A\to\varepsilon$$

$$B \to Bc$$

$$B \to \varepsilon$$

You want to implement G using an SLR(1) parser (note that we have already added the S'  $\rightarrow$  S production for you).

- (a) Construct the first state of the LR(0) machine, compute the FOLLOW sets of A and B, and point out the conflicts that prevent the grammar from being SLR(1)
  - Solution:
- (b) Show modifications to production  $4 (A \to Ac)$  and production  $6 (B \to Bc)$  that make the grammar SLR(1) while having the same language as the original grammar G. Explain the intuition behind this result.