

```
# 8.a
A = [8 1 0 -6 2;
5 4 1 3 11;
2 1 -2 0 -4;
4 2 1 0 7]
```

```
A =
```

```
      8      1      0     -6      2
      5      4      1      3     11
      2      1     -2      0     -4
      4      2      1      0      7
```

```
rref(A)
```

```
ans =
```

```
      1      0      0     -1      0
      0      1      0      2      2
      0      0      1      0      3
      0      0      0      0      0
```

```
# 8.b
```

```
rank(A)
```

```
ans =
```

```
      3
```

```
# 8.c
```

These vectors do NOT span  $\mathbb{R}^4$ .

For  $\text{rref}(A)$ , its echelon form just has three non-zero rows and thus, the system just has three linearly independent vectors and three linearly independent vectors cannot span  $\mathbb{R}^4$

For  $\text{rank}(A)$ , the answer told us there're 3 linearly independent vectors in this system and they cannot span  $\mathbb{R}^4$ .

```
# 9.a
```

For K:  $x_1 + 0 + 0 - 0 - 2x_5 - 0 = 0$

For Mn:  $x_1 + x_2 + 0 - x_4 - 0 - 0 = 0$

For O:  $4x_1 + 4x_2 + x_3 - 2x_4 - 4x_5 - 4x_6 = 0$

For S:  $0 + x_2 + 0 - 0 - x_5 - x_6 = 0$

For H:  $0 + 0 + 2x_3 - 0 - 0 - 2x_6 = 0$

```
# 9.b
```

```
A = [1 0 0 0 -2 0;
      1 1 0 -1 0 0;
      4 4 1 -2 -4 -4;
      0 1 0 0 -1 -1;
      0 0 2 0 0 -2]
```

A =

1	0	0	0	-2	0
1	1	0	-1	0	0
4	4	1	-2	-4	-4
0	1	0	0	-1	-1
0	0	2	0	0	-2

rref(A)

ans =

1.0000	0	0	0	0	-1.0000
0	1.0000	0	0	0	-1.5000
0	0	1.0000	0	0	-1.0000
0	0	0	1.0000	0	-2.5000
0	0	0	0	1.0000	-0.5000

# 9.c

2(KMnO<sub>4</sub>) + 3(MnSO<sub>4</sub>) + 2(H<sub>2</sub>O) → 5(MnO<sub>2</sub>) + 1(K<sub>2</sub>SO<sub>4</sub>) + 2(H<sub>2</sub>SO<sub>4</sub>)

# 10.a

```
for i = 1:20
    t = [0:i];
    A = fliplr(vander(t));
    cond(A)
```

end

ans =

2.6180

ans =

13.9125

ans =

154.4565

ans =

2.5929e+03

ans =

5.7689e+04

ans =

1.5973e+06

ans =

5.2938e+07

ans =

2.0437e+09

ans =

9.0078e+10

ans =

4.4628e+12

ans =

2.4547e+14

ans =

1.5305e+16

ans =

1.4907e+18

ans =

1.0963e+19

ans =

2.0174e+20

ans =

2.3561e+21

ans =

3.2774e+23

ans =

2.9348e+24

ans =

6.7488e+26

ans =

9.3218e+27

diary off

# 10.b

Since the condition number of the matrix that arises in polynomial interpolation with 20 points is very large, approximately  $9.3218 \times 10^{27}$ , and that means this matrix is ill-conditioned and is also hard to invert. Thus, it is not a good idea to do polynomial interpolation with 20 points.