CSci 2041 - Advanced Programming Principles

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Homework 3

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**Question 1:**

We would like to show that

The principle of induction for natural numbers is

In this case, our property P is defined as

is

Our induction proof would have two cases:

* : show that

by definition of

* : show that where holds by the inductive hypothesis.

by definition of

by property of addition and subtraction

by inductive hypothesis

by property of multiplication and power

has been proven.

**Question 2:**

We would like to show that

The principle of induction for this typeis

In this case, our property P is defined as

is

Our induction proof would have two cases:

* : show that

by definition of

by definition of power

by definition of

* : show that when holds by the inductive hypothesis.

by the definition of

by induction hypothesis

by the definition of multiplication and power

by the definition of

has been proven.

**Question 3:**

We would like to show that

The principle of induction for list is

In this case, our property is defined as

Our induction proof would have two cases:

by properties of lists

by properties of addition

by definition of

by definition of

by induction hypothesis

by definition of

has been proven.

**Question 4:**

We would like to show that

The principle of induction for list is

In this case, our property is defined as

Our induction proof would have two cases:



by definition of



by the definition of

by the property ofproven in Question 3

by induction hypothesis

by definition of

by property of addition

by definition of

has been proven.

**Question 5:**

The principle of induction for list is

We would like to prove first while

is

Our induction proof for would have two cases:



by definition of

by properties of lists



by definition of

by induction hypothesis

by properties of lists

has been proven.

Now we would like to prove while

is

Our induction proof for would have two cases:



by property ofproven by

­ by properties of lists

by properties of lists

by definition of

by property of proven by



by property ofproven by

­ by properties of lists

by definition of

by property of proven by

by induction hypothesis

by property of proven by

by property of lists

by definition of

by property proven by

has been proved.

**Question 6:**

**Question 7:**