Project 4: PMF with KNN and Kernel Ridge Postprocessing

In this project, we explore probabilistic matrix factorization for recommender system. The goal is to match consumers with most appropriate products. We use two different methods for post-processing: KNN and Kernel Ridge Regression. We combine the prediction results from PMF and post-processing by using linear regression.

Step 1: Load Data and Train-test Split

Import modules and packages.

```
In [12]: import pandas as pd
import numpy as np
from sklearn.model_selection import train_test_split
from sklearn.metrics import mean_squared_error
from math import sqrt
import seaborn as sns
import matplotlib.pylab as plt
import PMF_model
%matplotlib inline
```

Load data and do train_test_split. Here we split again the train set into train set and validation set.

```
In [13]: data = pd.read_csv('ratings.csv')

# train_test_split
train, test = train_test_split(data, test_size = 0.2, stratify = data['userId'])

# Comment out the line below not to include validation set
train, validation = train_test_split(train, test_size = 0.1, stratify = train['userId'])

train_data = np.array(train.iloc[:,:-1])
test_data = np.array(test.iloc[:,:-1])

# Comment out the line below not to include validation set
validation_data = np.array(validation.iloc[:,:-1])

num_users = max(data['userId'].values)
num_items = max(data['movieId'].values)
```

Step 2: Matrix Factorization and Parameter Tuning

PMF from module PMF_model perform gradien descent to do probabilistic matrix factorization. The algorithm consider case that there are new users and movies adding to the dataset used to train. That is, the dimension of the matrix R (nm), U(fn), $V(f^*m)$ is dynamic.

Define function for grid search cross validation. The function takes in lists for sigma, sigma_u, sigma_v and latent size each and return lists of sets of parameters and corresponding test rmse.

```
# grid search for PMF
In [14]:
         def GridSearch(sigma, sigma u, sigma v, latent size):
             from sklearn.model selection import KFold
             from statistics import mean
             params = []
             test rmse = []
             # performing cv with k=3 for each set of parameters
             kf = KFold(n splits=3, shuffle=True, random state=1)
             for s in sigma:
                 for su in sigma u:
                      for sv in sigma v:
                          for ls in latent size:
                              print("Training with sigma={:f}, sigma_u={:f}, sigma_v={:
         f}, latent size={:d}".format(s, su, sv, ls))
                              params.append([s, su, sv, ls])
                              model=PMF model.PMF(m = num items, n=num users, sigma=s, s
         igma_u=su, sigma_v=sv, latent size=ls)
                              rmse_list = []
                              # KFold
                              cnt=1
                              for train_index, test_index in kf.split(train_data):
                                  print(" Training fold {:d}".format(cnt))
                                  train k = train data[train index, :]
                                  test k = train data[test index, :]
                                  U, V, validation rmse = model.fit(train data=train k,
         validation data=validation data)
                                  preds = model.predict(data=test_k)
                                  # get rmse for the given fold
                                  rmse = sqrt(mean squared error(test k[:, 2],preds))
                                  rmse list.append(rmse)
                                  cnt+=1
                              # Get average rmse for all folds for the given set of para
         meters
                              test rmse.append(mean(rmse list))
                              print(" rmse:{:f}\n".format(mean(rmse list)))
             return params, test rmse
```

From testing different values, we observed that the sigmas' are the parameters that affects RMSE the most. So we tuned them first. To aim for lambdas 0.01, 0.001, and 0.0001, we did grid search with sigma fixed and only changed sigma u and sigma v. We repeated this process with different sigmas.

```
In [15]:
         sigma=[0.001]
         sigma u=[0.1, 0.03, 0.01]
         sigma_v=[0.1, 0.03, 0.01]
         latent size=[10]
         params, test rmse = GridSearch(sigma, sigma u, sigma v, latent size)
         best idx = test rmse.index(min(test rmse))
         print("Best parameters: {}".format(params[best idx]))
         print("Best rmse:{}".format(min(test_rmse)))
         best rmse = min(test rmse)
         best params = params[best idx]
In [16]: | sigma=[0.01]
         sigma u=[1.0, 0.3, 0.1]
         sigma_v=[1.0, 0.3, 0.1]
         latent size=[10]
         params, test_rmse = GridSearch(sigma, sigma_u, sigma_v, latent_size)
         best idx = test rmse.index(min(test rmse))
         print("Best parameters: {}".format(params[best idx]))
         print("Best rmse:{}".format(min(test_rmse)))
         if min(test rmse)<best rmse:</pre>
              best rmse = min(test rmse)
              best params = params[best idx]
In [17]:
         sigma=[1.0]
          sigma u=[10.0, 3.0, 1.0]
         sigma v=[10.0, 3.0, 1.0]
         latent size=[10]
         params, test rmse = GridSearch(sigma, sigma u, sigma v, latent size)
         best idx = test rmse.index(min(test rmse))
         print("Best parameters: {}".format(params[best idx]))
         print("Best rmse:{}".format(min(test_rmse)))
         if min(test rmse)<best rmse:</pre>
              best_rmse = min(test_rmse)
```

From the above grid search, we concluded that smaller sigmas work better. Then we performed cross validation for a different latent size for the smaller sigmas.

best params = params[best idx]

```
In [18]: sigma=[best_params[0]]
    sigma_u=[best_params[1]]
    sigma_v=[best_params[2]]
    latent_size=[20]

    params, test_rmse = GridSearch(sigma, sigma_u, sigma_v, latent_size)
    best_idx = test_rmse.index(min(test_rmse))
    if min(test_rmse) < best_rmse:
        best_rmse = min(test_rmse)
        best_params = params[best_idx]
    print("Best parameters: {}".format(best_params))
    print("Best rmse:{}".format(best_rmse))</pre>
```

Finally, train the model with the whole training data, using the best parameters(sigma=0.001, sigma_u=0.03, sigma_v=0.03, latent_size=10) found from grid search.

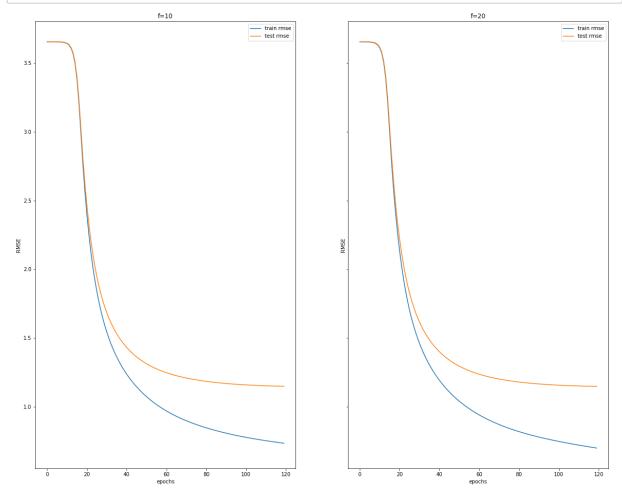
```
In [19]:
         # construct model
         sigma = [best params[0]]
         sigma u = [best params[1]]
         sigma v = [best params[2]]
         latent size = [best params[3]]
         num iter = 2000
         model = PMF model.PMF(m = num items, n = num users, sigma = sigma, sigma u = s
         igma u, sigma v = sigma v, lr=0.001, latent size=latent size)
         print('PMF(sigma={:f}, sigma_u={:f}, sigma_v={:f}, latent_size={:d})'.format(s
         igma, sigma u, sigma v, latent size))
         print('\ntraining model...')
         U, V, validation_rmse = model.fit(train_data=train_data, validation_data=valid
         ation data)
         train preds = model.predict(data=train data)
         train['pmf preds'] = train preds
         train rmse = sqrt(mean squared error(train data[:, 2],train preds))
         print('train rmse:{:f}'.format(train_rmse))
         print('\ntesting model...')
         preds = model.predict(data=test data)
         test['pmf preds']=preds
         test_rmse = sqrt(mean_squared_error(test_data[:, 2],preds))
         print('test rmse:{:f}'.format(test rmse))
         # np.save('U.npy', U)
         # np.save('V.npy', V)
         PMF(sigma=0.001000, sigma u=0.030000, sigma v=0.030000, latent size=10)
         training model...
         training iteration: 0, loss: 484617.041984, validation_rmse: 3.659554)
         training iteration: 100, loss: 21772.462191, validation rmse: 1.162506
         convergence at iterations: 139
         train rmse:0.699220
         testing model...
         test rmse:1.153616
In [20]: # U=np.load('U.npy')
         # V=np.load('V.npy')
```

Training and testing RMSE by different dimensions of factors and epochs are visualized below.

```
In [22]: # train_rmse_10 = np.load('train_rmse_10.npy')
# test_rmse_10 = np.load('test_rmse_10.npy')
# train_rmse_20 = np.load('train_rmse_20.npy')
# test_rmse_20 = np.load('test_rmse_20.npy')
```

```
In [41]: # Visualize RMSE
fig, ax = plt.subplots(1,2,figsize=(20,16), sharey=True)
    sns.lineplot(x=range(120), y=train_rmse_10, ax=ax[0], label='train rmse')
    sns.lineplot(x=range(120), y=test_rmse_10, ax=ax[0], label='test rmse')
    ax[0].set_title('f=10')
    ax[0].set_xlabel('epochs')
    ax[0].set_ylabel('RMSE')
    ax[0].legend()

sns.lineplot(x=range(120), y=train_rmse_20, ax=ax[1], label='train rmse')
    sns.lineplot(x=range(120), y=test_rmse_20, ax=ax[1], label='test rmse')
    ax[1].set_title('f=20')
    ax[1].set_xlabel('epochs')
    ax[1].set_ylabel('RMSE')
    ax[1].legend();
```



Step 3: Post-processing

Postporcessing is performed to improve accuracy.

1) KNN with K=1

We define similarity between movies i1 and i2 as the cosine similarity between vectors V_i1 and V_i2. Then we use the average rating of most similar movie as prediction. If there is no ratings for the closest movie, we set the prediction to 0.

```
In [24]: # Post processing using K Nearest Neighbors with K=1
         from sklearn.neighbors import NearestNeighbors
         model knn = NearestNeighbors(metric='cosine', algorithm='brute', n neighbors=1
         , n jobs=-1)
         model knn.fit(V.T)
         dist, ind = model knn.kneighbors(V.T,2)
         nearest_movie = ind[:,1]+1
In [25]: # Average rating of the nearest neighbor (0 if no ratings)
         movie_rates = data.groupby(['movieId'])['rating'].mean()
         test_nn = nearest_movie[test['movieId']-1]
         train nn = nearest movie[train['movieId']-1]
         test['knn preds'] = list(movie rates[test nn].fillna(0))
         train['knn_preds'] = list(movie_rates[train_nn].fillna(0))
In [26]:
         # test and train RMSE of KNN prediction
         print(sqrt(np.array(mean squared error(test['rating'],test['knn preds']))))
         print(sqrt(np.array(mean squared error(train['rating'],train['knn preds']))))
         1.5262818256469137
         1.3493580175869981
```

2) Kernel Ridge Regression

Define y as user specific ratings. X consists of normalized vector of factors for movies rated by the user in each row. Using y and X, we solve Kernel Ridge Regression.

```
In [27]: # Post processing using Kernel Ridge Regression
         from sklearn.kernel ridge import KernelRidge
         from sklearn.preprocessing import normalize
         # For user specific ratings
         most rated = data.groupby(['movieId']).count().sort values(by = 'rating', asce
         nding=False)
         for userId in range(1,num_users+1):
             # get user specific data
             user spec = train.loc[train['userId'] == userId]
             user_spec_test = test.loc[test['userId'] == userId]
             if (len(user_spec)!=0) and (len(user_spec_test)!=0):
                 # use 500 most rated movies if the user rated more than 500 movies
                 if(len(user spec)>500):
                     user spec['num rates']=list(most rated.loc[user spec['movieId'],'r
         ating'])
                     user spec=user spec.sort values(by='num rates', ascending=False)[:
         500]
                 # get X and y for Kernel Ridge Regression
                 X train = normalize(V.T[user spec['movieId']-1,:], axis=0)
                 y_train = user_spec['rating']
                 X test = normalize(V.T[user spec test['movieId']-1,:], axis=0)
                 # Construct and train model
                 model kr = KernelRidge(kernel='rbf', alpha=0.5)
                 cls = model kr.fit(X train,y train)
                 y preds = cls.predict(X test)
                 train preds = cls.predict(X train)
                 # get predictions
                 test.loc[list(user spec test.index), 'krr preds'] = y preds
                 train.loc[list(user spec.index),'krr preds'] = train preds
                 if len((user_spec>500)): train['krr_preds'].fillna(0, inplace=True)
In [30]:
         # test and train RMSE of Kerner Ridge Regression prediction
         print(sqrt(np.array(mean squared error(test['rating'],test['krr preds']))))
         print(sqrt(np.array(mean_squared_error(train['rating'],train['krr_preds']))))
```

0.9329271334055824
1.385064219328171

Step 4: Evaluation

Using linear regression, we combine the predictions from PMF and each post-processed predictions. Then we use RMSE to evaluate the combined models.

1) KNN with K=1

```
In [31]: # Linear regression to combine PMF and KNN
         from sklearn.linear model import LinearRegression
         lm knn = LinearRegression(fit intercept=False)
         lm knn.fit(X = np.vstack([train['knn preds'], train['pmf preds']]).T, y = trai
         n['rating'])
         knn_beta1, knn_beta2 = lm_knn.coef_
In [32]: # test rmse of KNN processed results
         test['knn_processed_preds'] = knn_beta1*test['knn_preds'] + knn_beta2*test['pm
         f preds']
         sqrt(mean_squared_error(test['rating'], test['knn_processed_preds']))
         1.1541276068819433
In [33]: # train rmse of KNN processed results
         train['knn processed preds'] = knn beta1*train['knn preds'] + knn beta2*train[
         'pmf preds']
         sqrt(mean_squared_error(train['rating'], train['knn_processed_preds']))
         0.6987678769303419
```

2) Kernel Ridge Regression

```
In [34]: # Linear regression to combine PMF and KRR
         from sklearn.linear model import LinearRegression
         lm_krr = LinearRegression(fit_intercept=False)
         lm_krr.fit(X = np.vstack([train['krr_preds'], train['pmf_preds']]).T, y = trai
         n['rating'])
         krr_beta1, krr_beta2 = lm_krr.coef_
In [35]: # test rmse of KRR processed results
         test['krr_processed_preds'] = krr_beta1*test['krr_preds'] + krr_beta2*test['pm
         sqrt(mean_squared_error(test['rating'], test['krr_processed_preds']))
         1.1426347248810556
In [36]:
        # train rmse of KRR processed results
         train['krr_processed_preds'] = krr_beta1*train['krr_preds'] + krr_beta2*train[
         'pmf preds']
         sqrt(mean_squared_error(train['rating'], train['krr_processed_preds']))
         0.6984023019886008
In [37]: # train.to csv('train.csv')
         # test.to_csv('test.csv')
In [38]: # train = pd.read csv('train.csv')
         # test = pd.read_csv('test.csv')
```

From the results above, we can observe that KRR post-processed results are better off by 0.01 RMSE compared to PMF predictions. On the other hand, KNN post-processed results are similar to PMF (worse off by 0.0005 RMSE). A possible explanation is that we use K=1 so the KNN predictions only depend on a single nearest item. This may have caused noised due to overfitting and have evened out the ensemble effect. Also, we are not given ratings for every movie in the first place, and more movies have been omitted as we set the KNN prediction to 0 for movies without ratings. Accordingly, almost half of the test prediction with KNN was set to 0. KNN may perform better with more data available.

3) Visualization in Boxplot

```
In [40]: fig, ax = plt.subplots(1,2,figsize=(20,16), sharey=True)
    sns.boxplot(x='rating', y='knn_processed_preds', data=test, ax = ax[0])
    sns.boxplot(x='rating', y='krr_processed_preds', data=test, ax = ax[1])
    ax[0].set_title('KNN processed predictions')
    ax[1].set_title('KRR processed predictions');
```

