

Measuring the Deviations from Simple Harmonic Motion of a Pendulum

Introduction

This experiment focuses on analyzing the motion of a pendulum, specifically when the pendulum's bob is released far from its equilibrium point. At these positions, the motion of the pendulum becomes much harder to predict analytically as the linear relationship between force and displacement described by Hooke's Law using the small angle approximation begins to deviate.

Developing a sophisticated model of a pendulum which accurately describes the mechanics of its non-linear motion has been the focus of renowned physicists like Christiaan Huygens and Leonhard Euler. With such a model of harmonic motion being prevalent to areas such as springs and oscillators in physical systems to wave propagation, radiation of light and particle physics. By studying the non-simple harmonic motion of a pendulum we better our understanding of classical mechanics and shed light on the motivations behind the mathematical and numerical methods used in modern physics to model complex behaviour.

The goal of this experiment is to determine the angle at which simple harmonic motion and the small angle approximation begin to deviate drastically determined by a set threshold error. To do so we will analyze both the period and energy of a pendulum taken at increasing starting angles to compare with the period and energy as predicted by simple harmonic motion. Additionally, we will develop a computer simulation of a pendulum using modern numerical methods to show that this description of motion fits our experimentally determined values much more accurately.

Materials / Equipment / Setup

The required materials to complete this experiment include:

- Scale & Meter Stick
- String
- Fixed Rod, Adjustable Clamp & Protractor
- Hanging Mass
- Smartphone

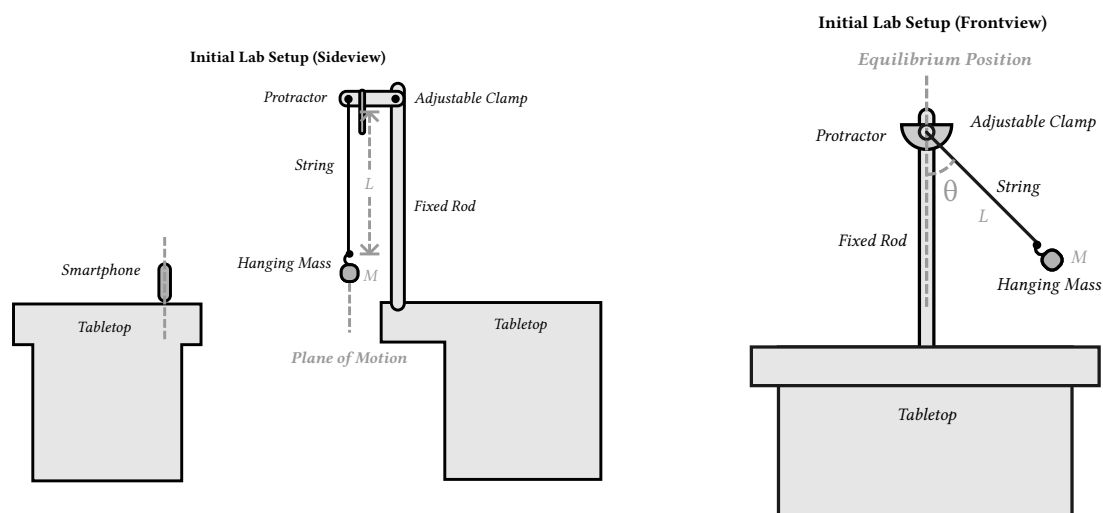


Figure 1: Diagrams of Initial Experimental Setup (Sideview & Frontview)

Design (Error & Bias)

Some possible sources of error and uncertainty come from measuring the angle of release for each trial, friction and air resistance dampening the oscillation of the pendulum, precession of the pendulum bob outside of the plane of motion and motion blur affecting the video analysis. To ensure an accurate measurement of angle we fix a protractor as part of our pendulum setup. To mitigate the effects of dampening we choose to utilize a string with negligible mass when compared to the hanging mass. To prevent the precession of the pendulum bob, we utilize the adjustable clamp and attempt to release the mass parallel to the intended plane of motion, taking multiple measurements if necessary. Finally, we attempt to mitigate motion blur by taking higher frame per second video and utilizing a string with maximal length to increase the period of the oscillation (decreasing the angular velocity).

Timeline & Procedure

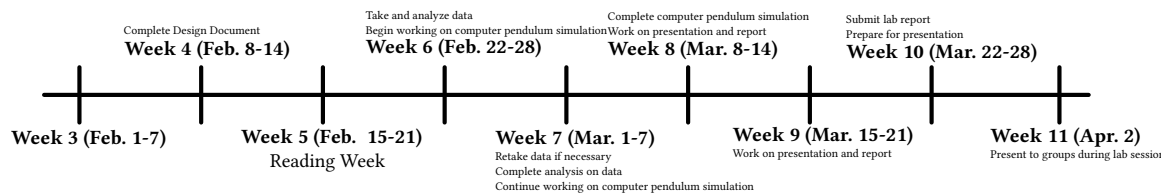


Figure 2: Timeline of Experiment

Timeline

- **Week 4:** Complete Design Document.
- **Week 5:** Reading Week
- **Week 6:** Take and analyze data, begin working on computer pendulum simulation and implementation of Runge-Katta method.
- **Week 7:** Retake data if necessary, complete analysis on data. Continue work on computer pendulum simulation comparing simulation to experimental data.
- **Week 8:** Complete computer pendulum simulation. Work on presentation and report completing up to the *Methods* section.
- **Week 9:** Work on presentation and report.
- **Week 10:** Submit lab report and prepare for presentation.
- **Week 11:** Present to groups during lab session.

To take data and complete the experiment:

1. Measure the length of the pendulum's string using the meter stick and the mass of the pendulum's bob (hanging mass) using the scale.
2. Setup the pendulum and smartphone as diagrammed, making sure to keep the smartphone parallel to the plane of motion.
3. Perform six trials starting from an initial angle $\theta = 15^\circ$ and increasing by 15° increments until $\theta = 90^\circ$ (horizontal) using the smartphone's camera to record each trial.
4. Analyze the motion of the pendulum for each trial using video analysis software like Tracker or Logger Pro as well as note down the period of each trial.

Chronicling Strategy

Measurements will be taken in the form of video to be analyzed later on. Analysis and data extracted from measurements will be stored as Tracker files and .csv files.

All data, measurements, reports and source code will be chronicled and versioned remotely using Git source control and made publicly available using GitHub. Full repository available at <https://github.com/JeffKhuu/phys181lab>