



DIMENSIONALITY REDUCTION IN R

Rotating Factors

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Steps to perform EFA

- Check for data factorability
- Extract factors
- Choose the "right" number of factors to retain
- **Rotate factors**
- **Interpret the results**



Factor rotation in EFA

Why further rotate the factors?

- To ease interpretation

- **Orthogonal** methods

- Quartimax
- Equimax
- **Varimax**

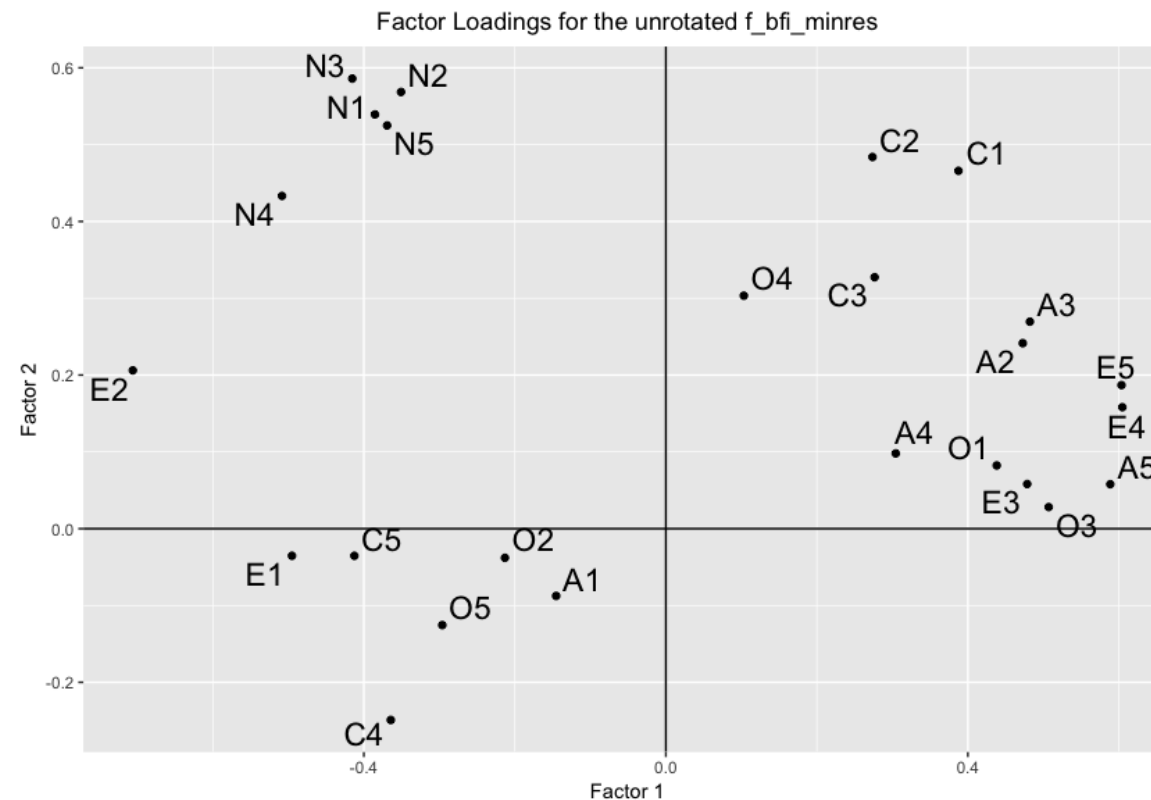
- **Oblique** methods

- Direct Oblimin
- Promax

Plotting unrotated factor loadings

5 putative factors behind the 25 self report items:

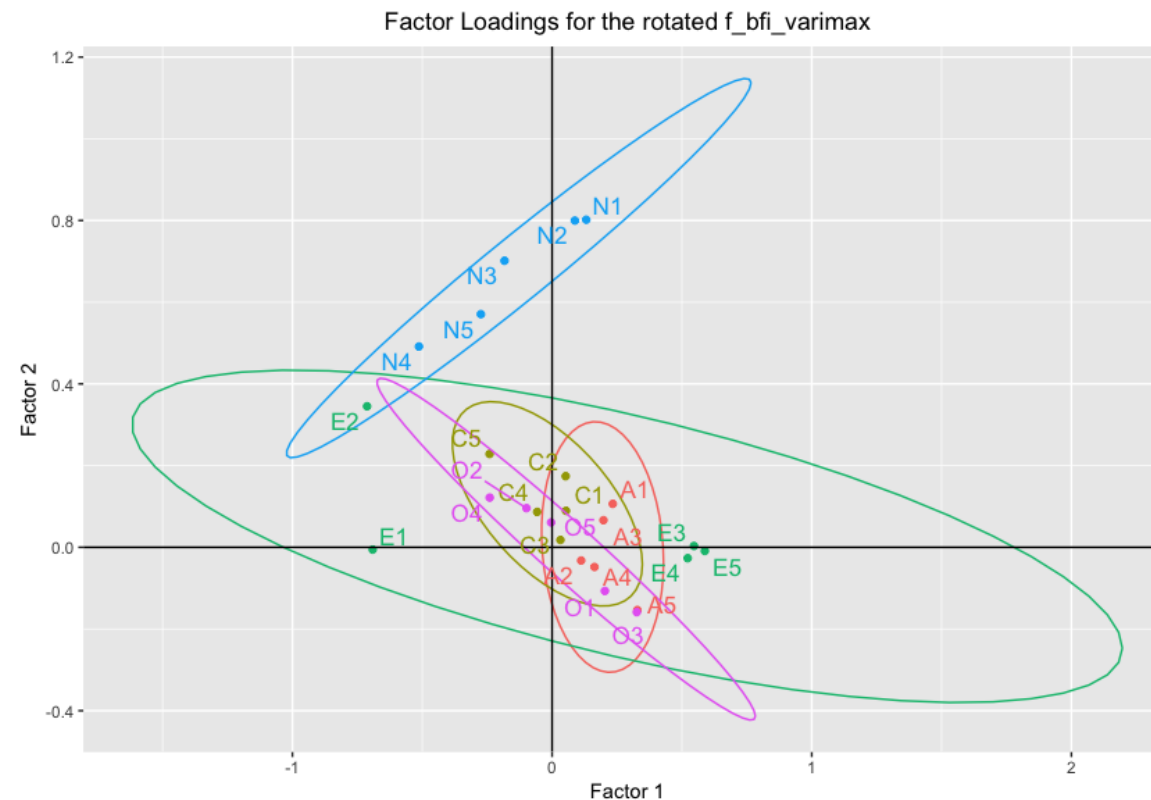
- **A**greeableness (A1,A2,A3,A4,A5)
- **C**onscientiousness (C1,C2,C3,C4,C5)
- **E**xtraversion (E1,E2,E3,E4,E5)
- **N**euroticism (N1,N2,N3,N4,N5)
- **O**penness (O1,O2,O3,O4,O5)



Rotating with varimax

```
# Applying varimax.  
f_bfi_varimax <- fa(bfi_c,  
  fm = "minres",  
  nfactors = 5,  
  rotate = "varimax")
```

- **E1:** "Don't talk a lot"
- **E2:** "Find it difficult to approach others"
- **E3:** "Know how to captivate people"
- **E4:** "Make friends easily"
- **E5:** "Take charge"





DIMENSIONALITY REDUCTION IN R

Let's practice!



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Path diagrams

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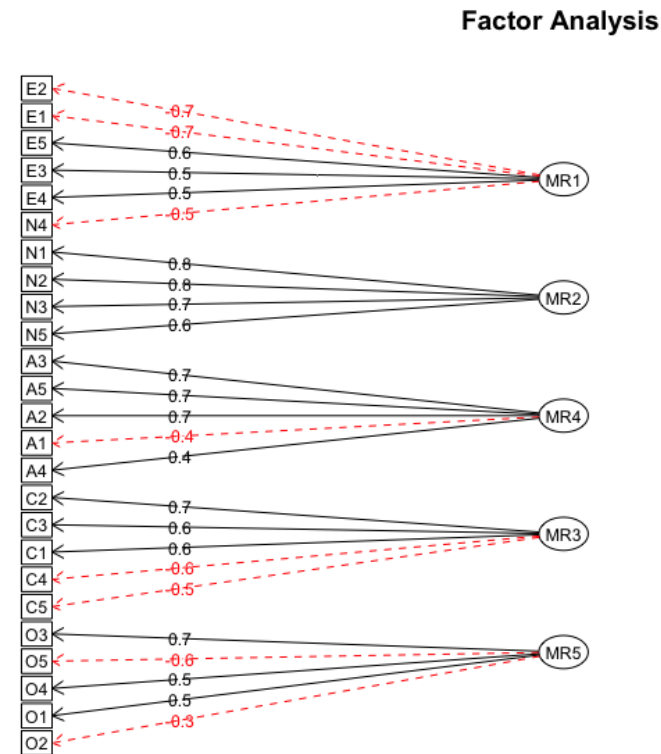
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Interpretation: a crucial part of EFA

```
library(psych)

# Creating the path diagram.
fa.diagram(f_bfi_varimax)
```

- **Agreeableness** (A1,A2,A3,A4,A5)
- **Conscientiousness** (C1,C2,C3,C4,C5)
- **Extraversion** (E1,E2,E3,E4,E5)
- **Neuroticism** (N1,N2,N3,N4,N5)
- **Openness** (O1,O2,O3,O4,O5)



Interpretation: a crucial part of EFA

```
# Checking out factor loadings.  
print(f_bfi_varimax$loadings, cut=0)
```

```
Loadings:  
      MR1  MR2  MR4  MR3  MR5  
A1  0.234  0.106 -0.422 -0.072 -0.092  
A2  0.112 -0.032  0.653  0.190  0.113  
A3  0.198  0.066  0.744  0.051  0.169  
A4  0.163 -0.048  0.413  0.137 -0.142  
A5  0.328 -0.154  0.692 -0.009  0.115  
C1  0.054  0.089  0.140  0.634  0.287  
C2  0.052  0.174  0.114  0.690  0.050  
C3  0.032  0.018  0.076  0.642  0.016  
C4 -0.058  0.087 -0.090 -0.559 -0.159  
C5 -0.241  0.228 -0.040 -0.459  0.014  
E1 -0.691 -0.006 -0.066 -0.084 -0.017  
E2 -0.713  0.345 -0.138 -0.133 -0.025  
E3  0.546  0.003  0.157 -0.008  0.221  
E4  0.522 -0.027  0.416  0.167  0.048  
E5  0.588 -0.009  0.148  0.308  0.159  
N1  0.131  0.802 -0.150 -0.074 -0.133  
N2  0.088  0.800 -0.151 -0.038 -0.008  
N3 -0.183  0.701  0.005  0.037 -0.087  
N4 -0.513  0.491 -0.006  0.004  0.034  
N5 -0.274  0.571  0.059  0.096 -0.082  
O1  0.203 -0.107  0.148  0.076  0.535  
O2 -0.099  0.096  0.144 -0.191 -0.330  
O3  0.326 -0.159  0.034  0.062  0.680  
O4 -0.240  0.122  0.169  0.105  0.548  
O5 -0.004  0.061 -0.074 -0.077 -0.636  
  
      MR1  MR2  MR4  MR3  MR5  
SS loadings  2.823 2.667 2.223 2.103 1.867  
Proportion Var 0.113 0.107 0.089 0.084 0.075  
Cumulative Var 0.113 0.220 0.309 0.393 0.467
```



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EFA: case study

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The Short Dark Triad

- A dataset that resulted from measuring the 3 *dark* personality traits:
 - machiavellianism (a manipulative behaviour),
 - narcissism (excessive self-admiration), and
 - psychopathy (lack of empathy)

(Interactive version of the test: <https://openpsychometrics.org/tests/SD3/>)

The SD3 dataset

```
sdt_test <- read.csv("SD3.csv", sep = "\t")  
dim(sdt_test)
```

```
[1] 18192 29
```

```
head(sdt_test)
```

	M1	M2	M3	M4	M5	M6	M7	M8	M9	N1	N2	N3	N4	N5	N6	N7	N8	N9	P1	P2	P3	P4	P5	P6	P7	P8	P9	country	source
1	4	4	4	4	4	4	4	3	4	2	4	2	3	4	4	2	3	4	3	4	3	2	4	4	4	4	4	GB	1
2	2	1	5	2	2	1	2	2	3	1	5	1	1	5	5	1	5	2	1	1	1	5	4	1	5	3	2	US	1
3	3	3	3	5	1	1	5	5	3	2	5	1	1	1	5	1	5	5	3	5	3	1	3	1	2	3	1	US	1
4	5	5	4	5	5	5	5	5	5	5	1	5	5	5	1	5	1	5	5	1	5	2	5	5	5	1	5	GB	3
5	4	4	2	5	5	5	4	1	4	3	4	3	1	5	4	3	2	5	4	5	3	1	4	3	5	4	1	GB	3
6	4	2	2	4	2	3	5	2	2	2	5	2	2	2	4	1	3	5	3	5	4	4	2	2	1	1	5	IT	1



EFA: The steps

- Check for data factorability
- Extract factors
- Choose the "right" number of factors to retain
- Rotate factors
- Interpret the results



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Overview of the course

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Dimensionality Reduction: the bigger picture

Biggest challenge of handling high-dimensional data:

- data interpretability
- remove noise and keep a reduced, interpretable representation



PCA and N-NMF

PCA

- **mathematically-sound** method
- suitable for **continuous data**

N-NMF

- **computationally efficient** (suitable for images and big data manipulation)
- suitable for data with **positive entries**



EFA

EFA

- **exploratory** method
- suitable for **ordinal data**
- discovering underlying latent constructs



Common steps in practicing dimensionality reduction

- Factor/Component/Dimension extraction
- Decision on the number of Factor/Component/Dimension to retain
 - parsimonious representation
 - least information loss
 - most interpretable representation
- Use visual aid for interpretation (e.g. biplot)



Where to go from here? My two cents..

- Deepen your freshly-acquired `R` knowledge
 - `FactoMiner`, `factoextra`, `NMF`, `psych`, ...
- Test alternative packages for performing these methods
 - `stats`, `ade4`, `amap`, `ca`, `MASS`
- Extend your theoretical knowledge on commonly used notions:
 - eigenvalues, eigenvectors, orthogonality (for starters)
- Explore more dimensionality reduction methods



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Good luck!