



# Intro to EFA and Data Factorability

Alexandros Tantos
Assistant Professor
Aristotle University of Thessaloniki



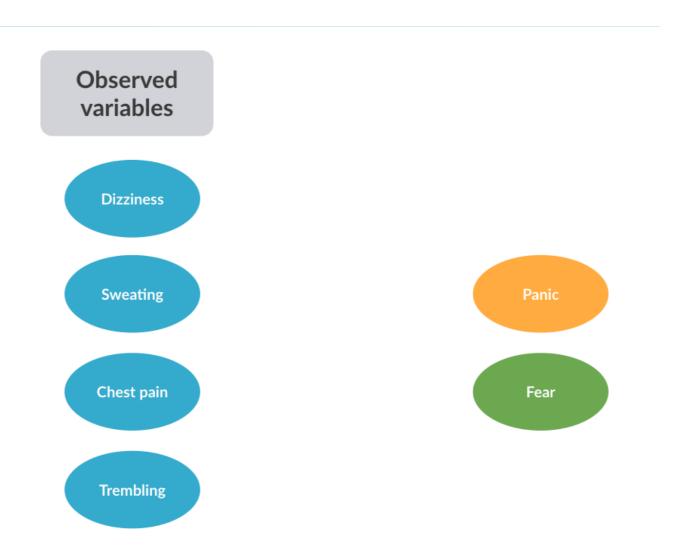
#### EFA: a realistic model for reducing and exploring

- Variance/covariance are only partially explained by factors
- Factors are labels for the underlying constructs
- Causal relationship between factors and observed variables

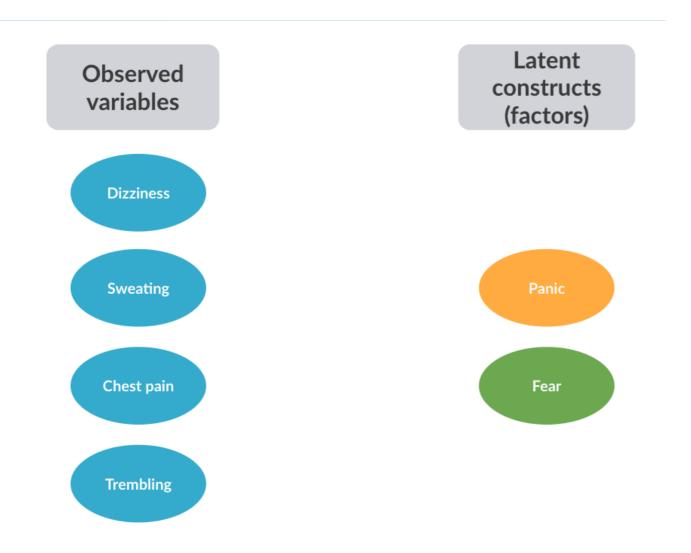




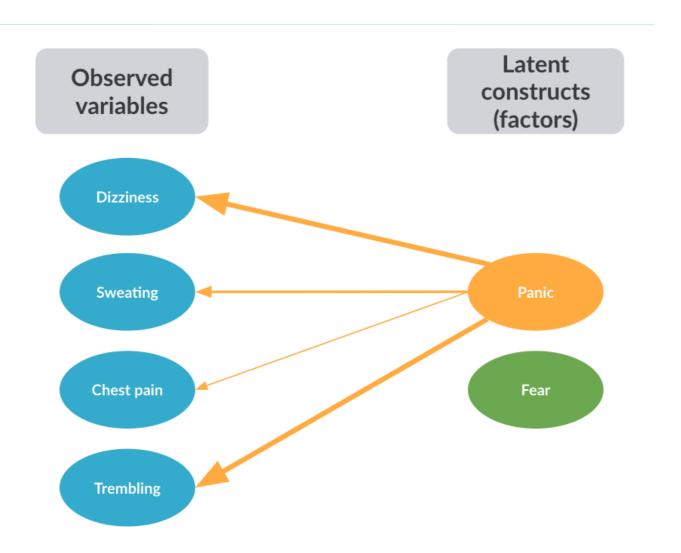




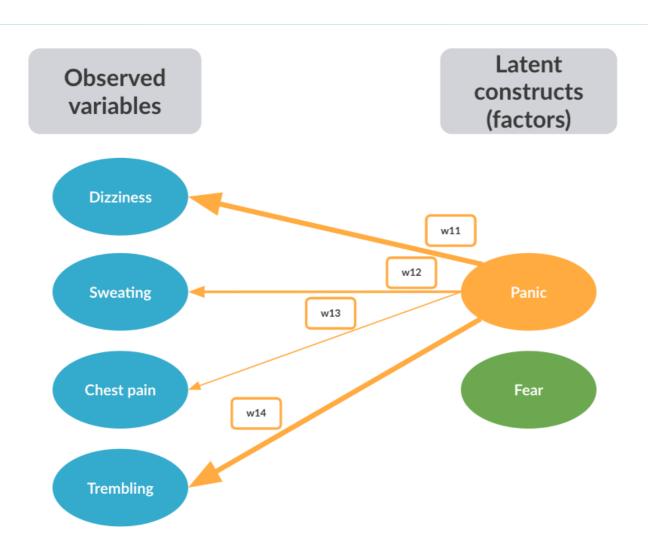




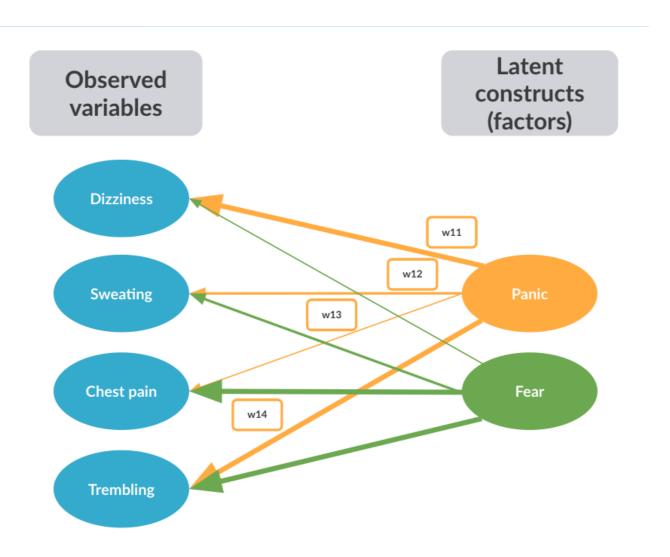




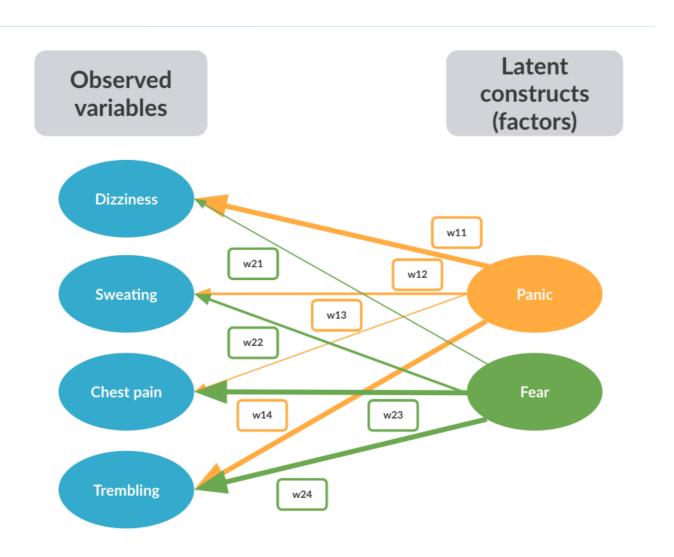




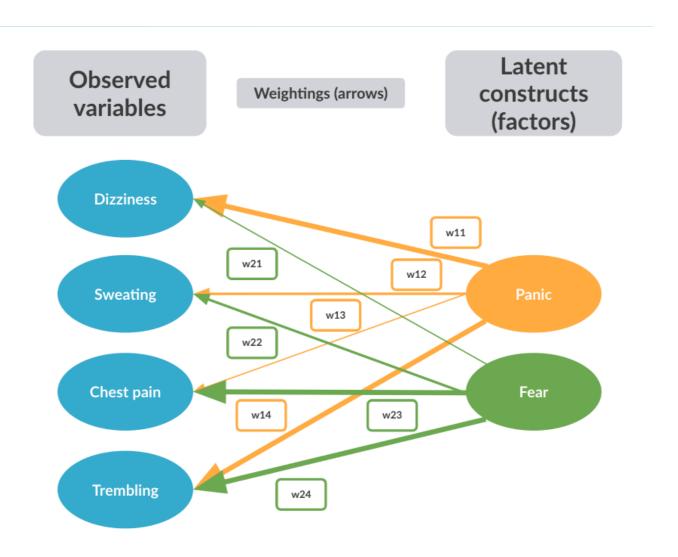




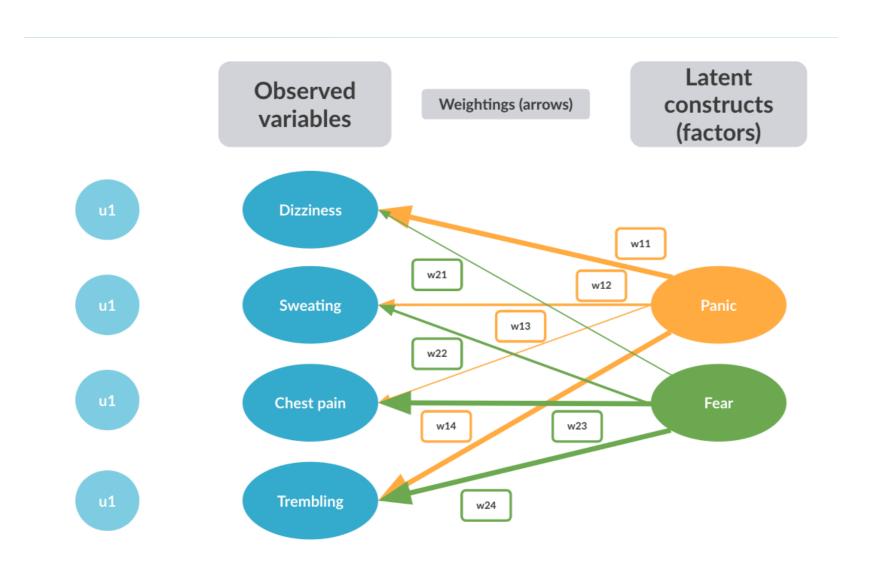




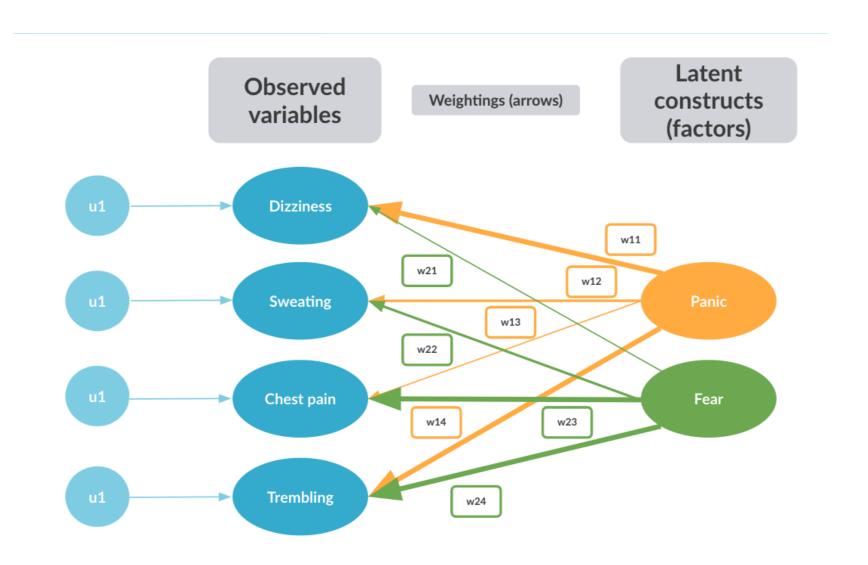




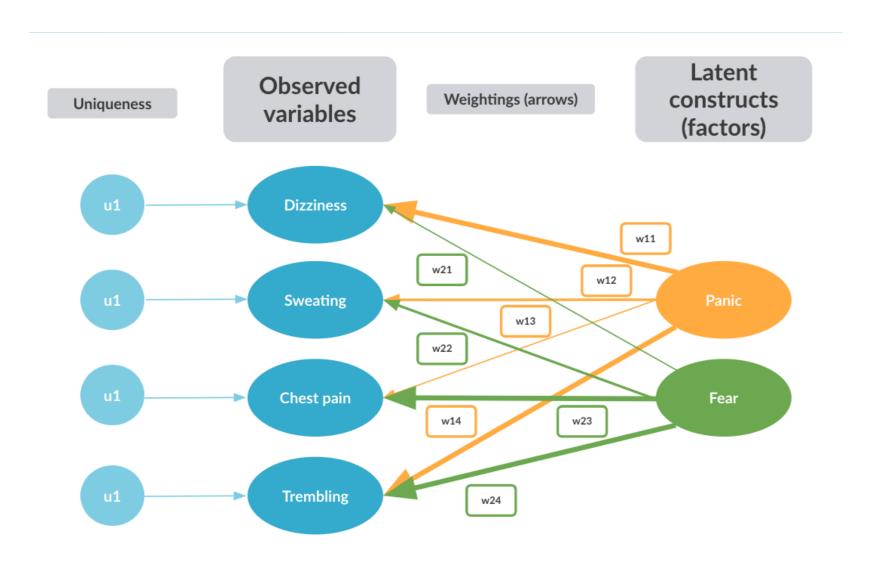






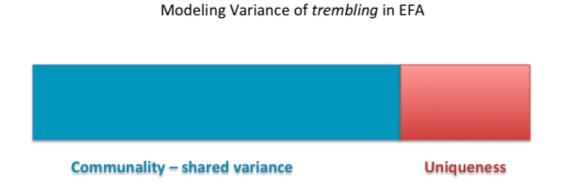








#### EFA: A realistic model of explaining variance





#### Steps to perform EFA

- Check for data factorability
- Extract factors
- Choose the "right" number of factors to retain
- Rotate factors
- Interpret the results



#### A first look at the bfi dataset

```
library(psych)
data(bfi)

# Take a look at the head of bfi dataset.
head(bfi)
```





# Let's practice!





# Checking for data factorability

Alexandros Tantos
Assistant Professor
Aristotle University of Thessaloniki



#### Steps to perform EFA

- Check for data factorability
- Extract factors
- Choose the "right" number of factors to retain
- Rotate factors
- Interpret the results

#### Factorability tests:

- The Bartlett sphericity test
- The Kaiser-Meyer-Olkin (KMO) test



#### The Bartlett sphericity test

```
      1
      0
      0
      0

      0
      1
      0
      0

      0
      0
      1
      0

      0
      0
      0
      1
```

A 4X4 identity matrix

- H0: There is **no** significant difference between the correlation matrix and the identity matrix of the same dimensionality.
- H1: There is significant difference betweeen them and, thus, we have strong evidence that there are underlying factors.



#### The Bartlett sphericity test

```
library(polycor)
# A subset of the bfi dataset.
bfi s <- bfi[1:200, 1:25]
# Calculate the correlations.
bfi hetcor <- hetcor(bfi s)</pre>
# Retrieve the correlation matrix.
bfi c <- bfi hetcor$correlations
# Apply the Bartlett test.
bfi factorability <- cortest.bartlett(bfi c)</pre>
bfi factorability
$chisq
[1] 891.1536
$p.value
[1] 5.931663e-60
$df
[1] 300
```



#### The Kaiser-Meyer-Olkin (KMO) test for sampling adequacy

```
Library(psych)

KMO(bfi_c)
Kaiser-Meyer-Olkin factor adequacy
Call: KMO(r = bfi_c)
Overall MSA = 0.76
MSA for each item =
    A1    A2    A3    A4    A5    C1    C2    C3    C4    C5    E1    E2    E3    E4    E5    N1
0.66    0.77    0.69    0.73    0.75    0.74    0.79    0.76    0.76    0.74    0.80    0.81    0.79    0.81    0.83    0.70
    N3    N4    N5    O1    O2    O3    O4    O5
0.82    0.79    0.82    0.79    0.65    0.81    0.62    0.77
```





# Let's practice!





#### **Extraction methods**

Alexandros Tantos
Assistant Professor
Aristotle University of Thessaloniki

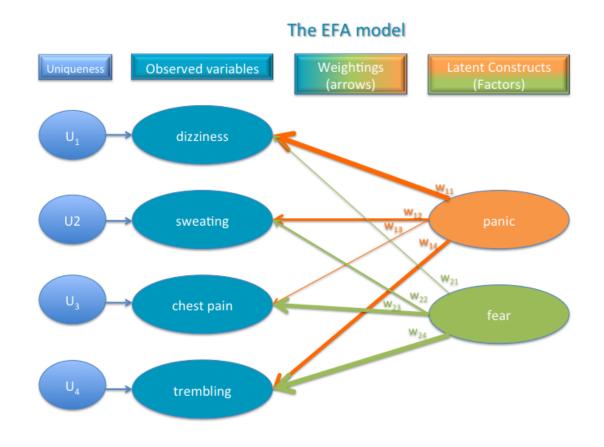


#### Steps to perform EFA

- Check for data factorability
- Extract factors
- Choose the "right" number of factors to retain
- Rotate factors
- Interpret the results



#### Methods for extracting factors



EFA aims to:

- extract factors
- estimate factor loadings



#### Factor extraction with fa()

#### **Extraction methods:**

- minres: minimum residual [default] (slightly modified methods: ols, wls, gls)
- mle: Maximum Likelihood Estimation (MLE)
- paf: Principal Axes Factor (PAF) extraction
- minchi: minimum sample size weighted chi square
- minrank: minimum rank
- alpha: alpha factoring

#### **Commonality**:

• First extract the factor that accounts for the most variance, and then successively



#### The minres extraction method

```
library(psych)
library(GPArotation)

# EFA with 3 factors
f_bfi_minres <- fa(bfi_c, nfactors = 3, rotate = "none")

# Sorted communality
f_bfi_minres_common <- sort(f_bfi_minres$communality, decreasing = TRUE)

# create a dataframe for an improved overview
data.frame(f_bfi_minres_common)</pre>
```



#### The minres extraction method

```
# Sorted uniqueness
f_bfi_minres_unique <- sort(f_bfi_minres$uniqueness, decreasing = TRUE)
# create a dataframe for an improved overview
data.frame(f_bfi_minres_unique)</pre>
```



#### The MLE extraction method

```
# MLE factor extraction.
f_bfi_mle <- fa(bfi_c, nfactors = 3, fm = "mle", rotate = "none")

# Sorted communality of the f_bfi_mle.
f_bfi_mle_common <- sort(f_bfi_mle$communality, decreasing = TRUE)

# create a dataframe for an improved overview
data.frame(f_bfi_mle_common)</pre>
```





# Let's practice!





# Choosing the right number of factors

?lexandros Tantos
Assistant Professor
Aristotle University of Thessaloniki

#### EFA: How many factors to retain?

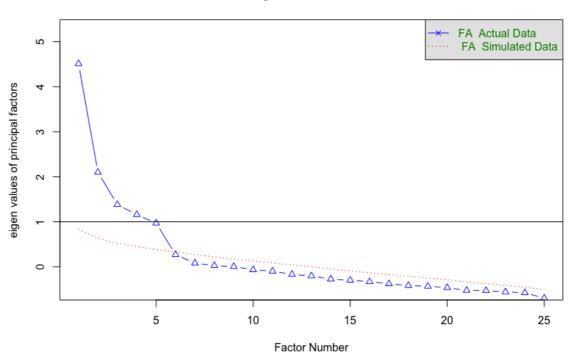
"Solving the number of factors problem is easy, I do it everyday before breakfast. But knowing the right solution is harder" (Kaiser, 195x).

- Kaiser-Guttman criterion
- the Scree test
- Parallel analysis
- very simple structure (VSS) criterion (VSS () function in psych)
- Wayne Velicer's Minimum Average Partial (MAP) criterion (vss () function in psych)



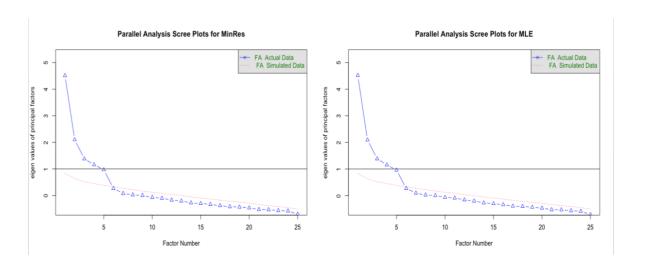
#### Determining the number of factors: fa.parallel()

#### Parallel Analysis Scree Plots for MinRes





#### Determining the number of factors: fa.parallel()







# Let's practice!