



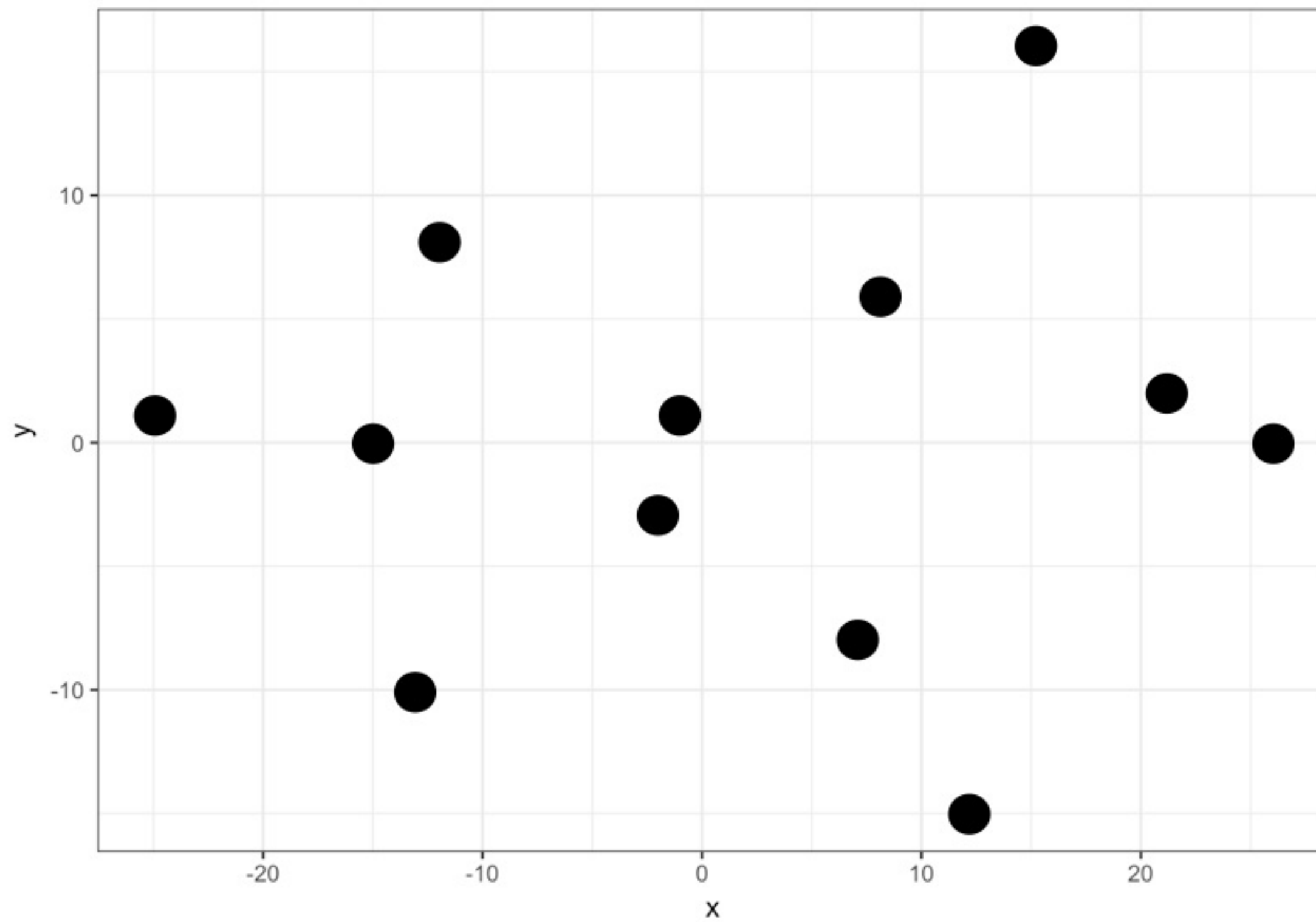
CLUSTER ANALYSIS IN R

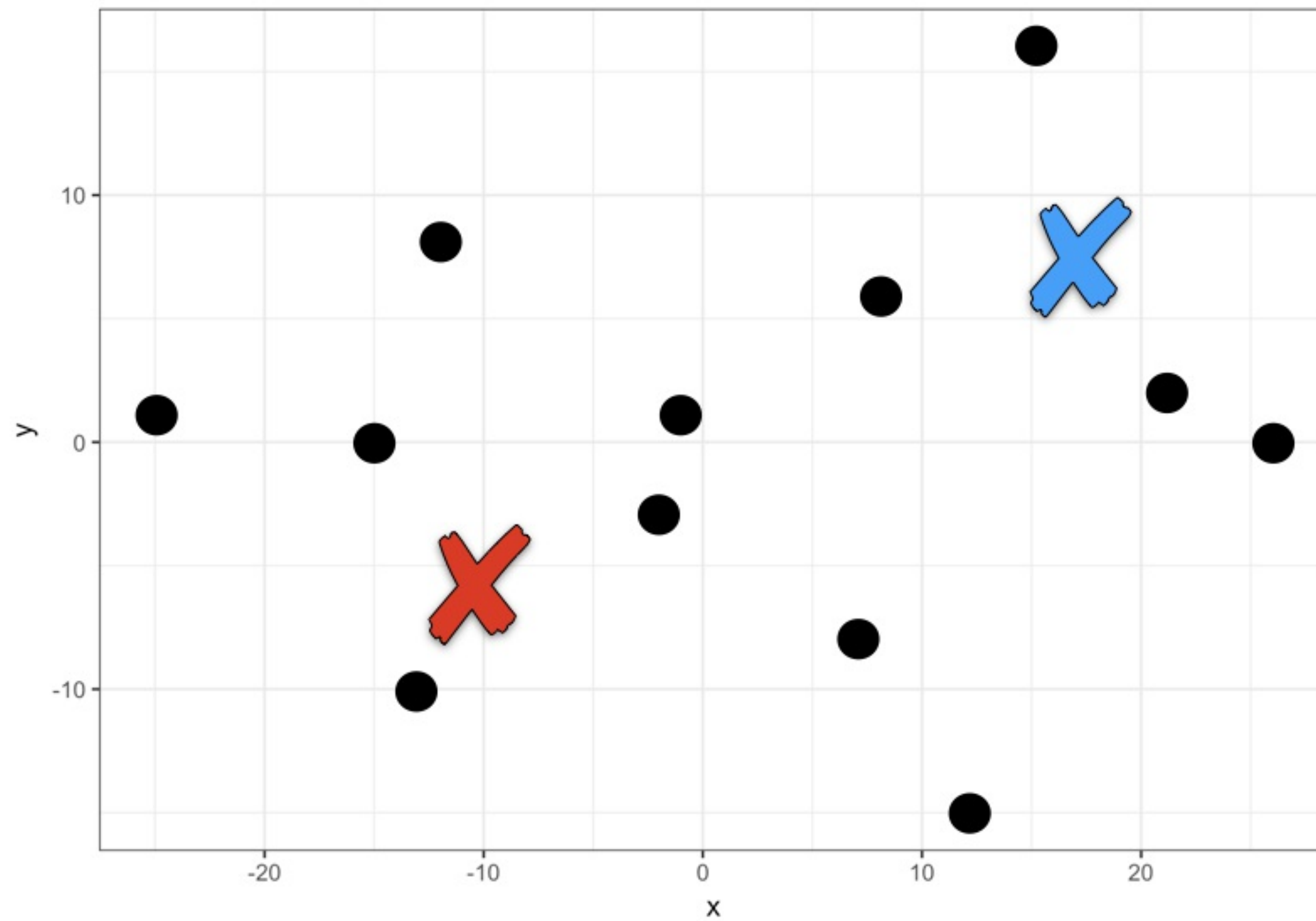
# Introduction to K-means

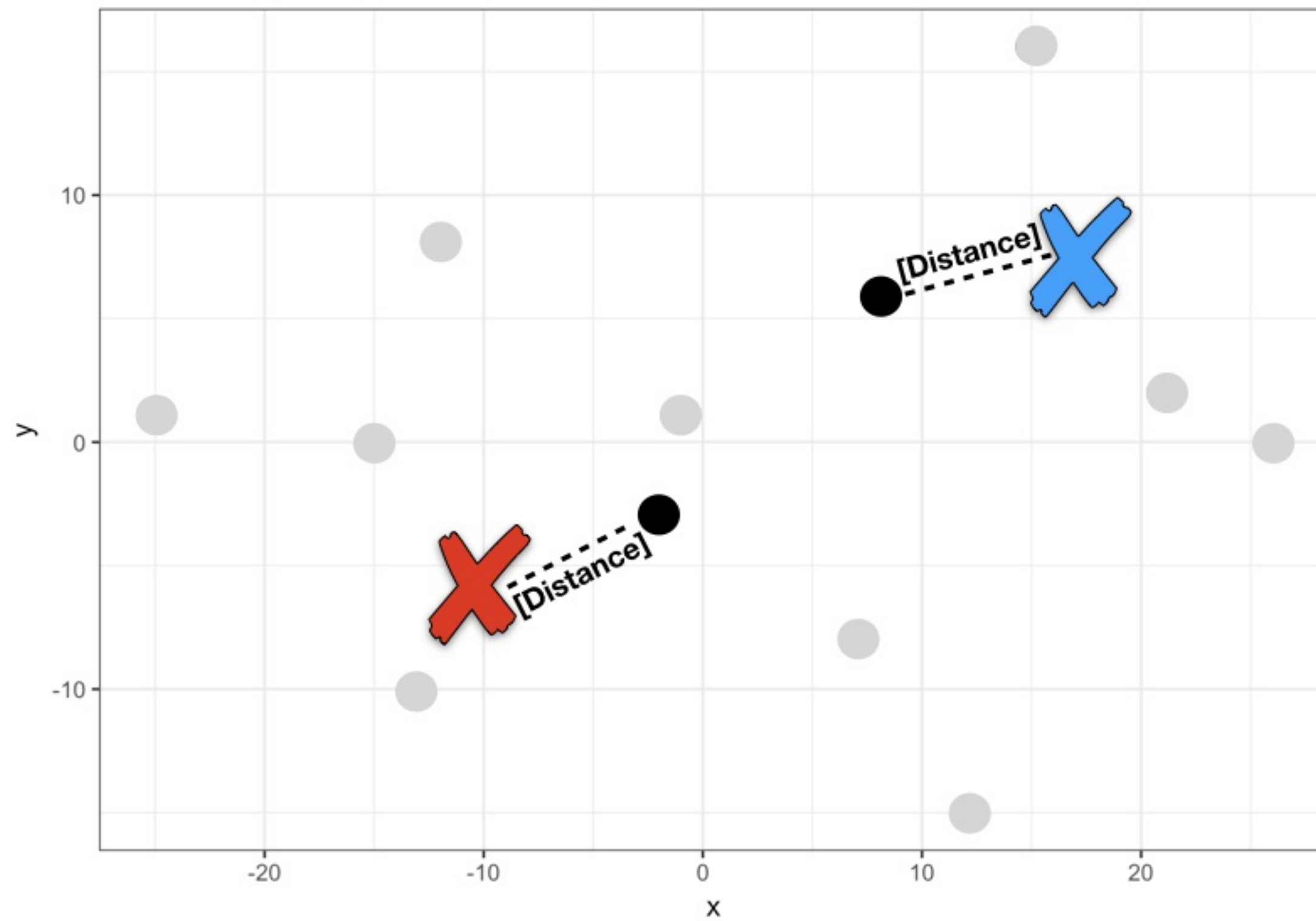
Dmitriy (Dima) Gorenshteyn

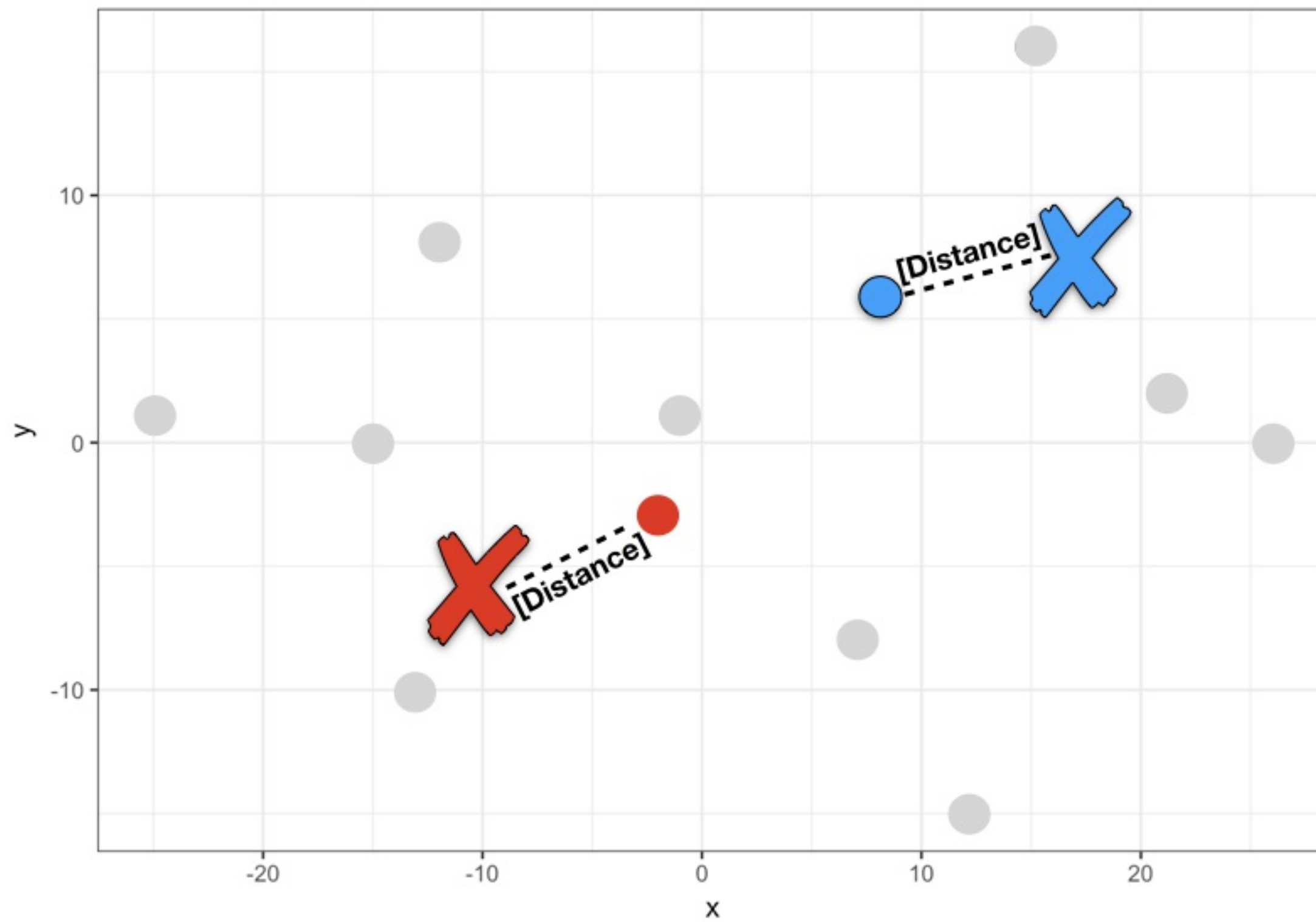
Sr. Data Scientist,

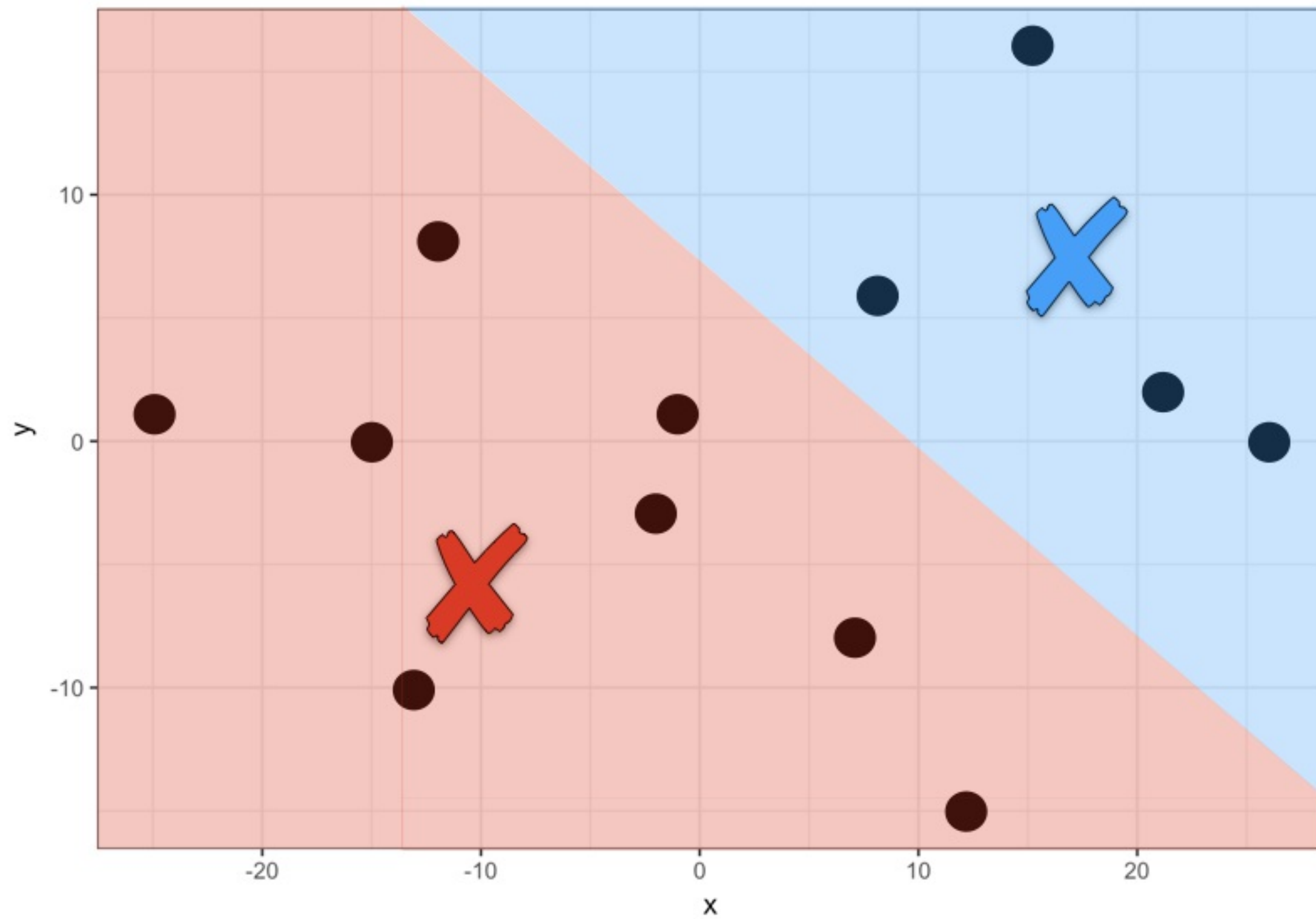
Memorial Sloan Kettering Cancer Center

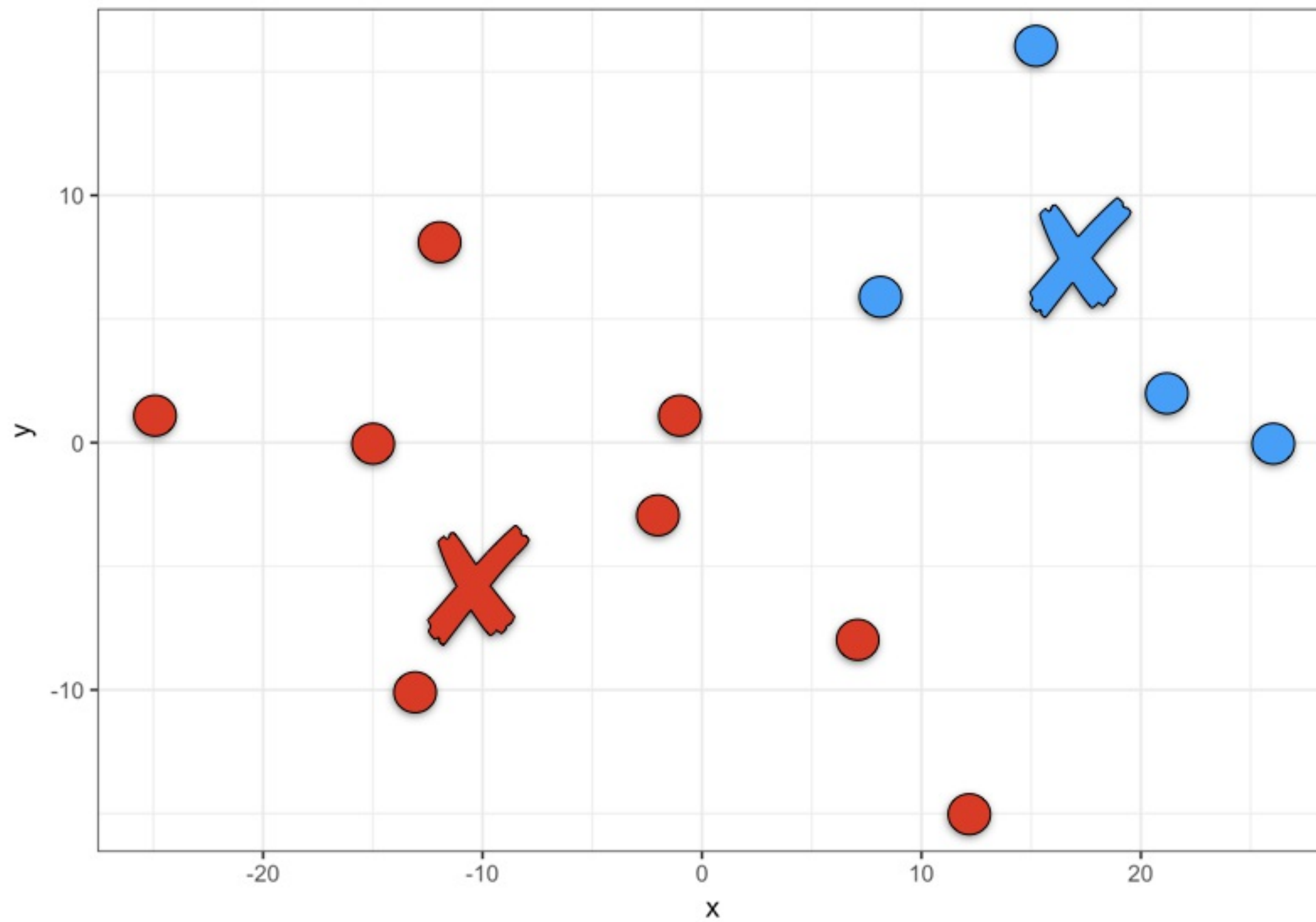


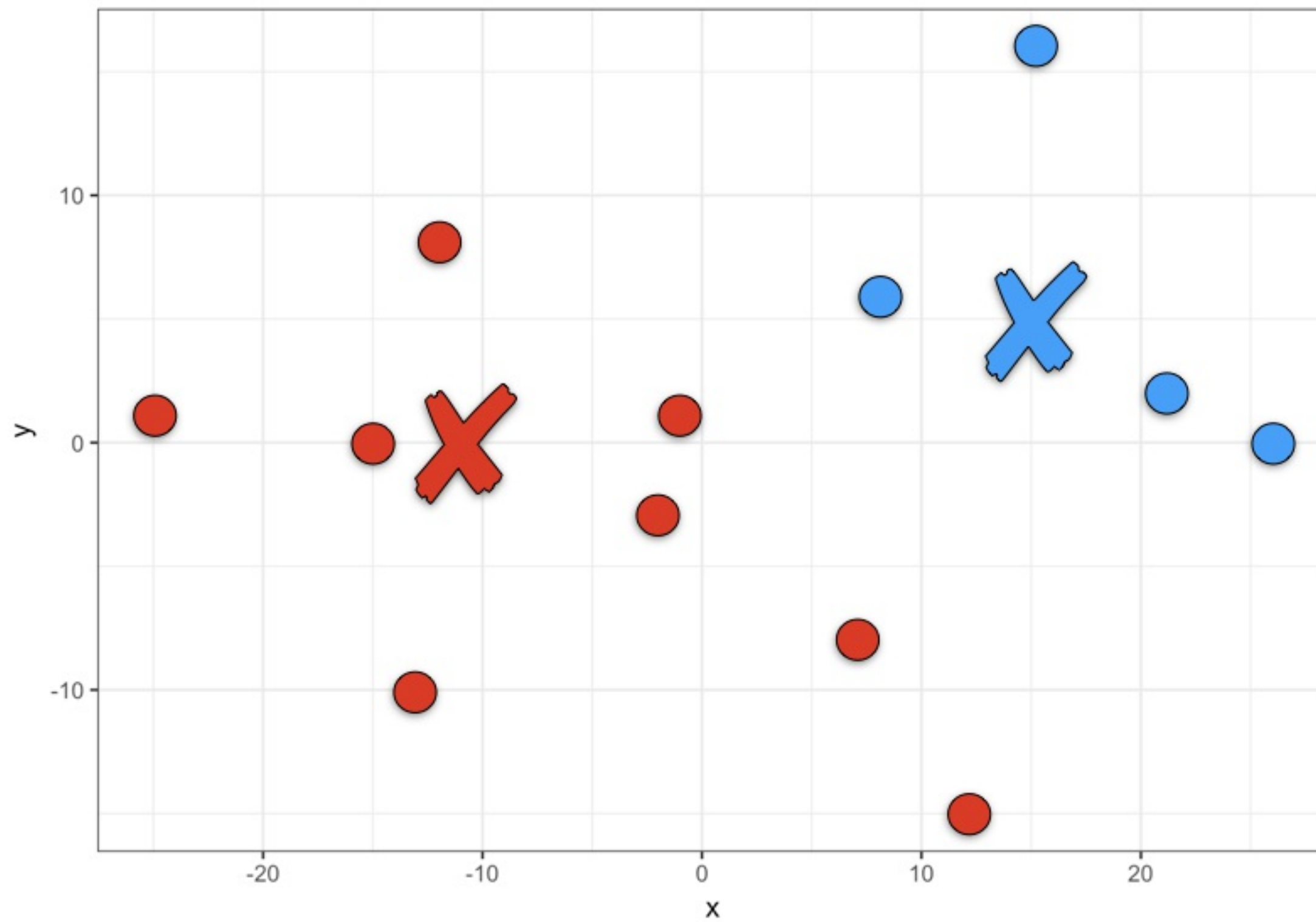




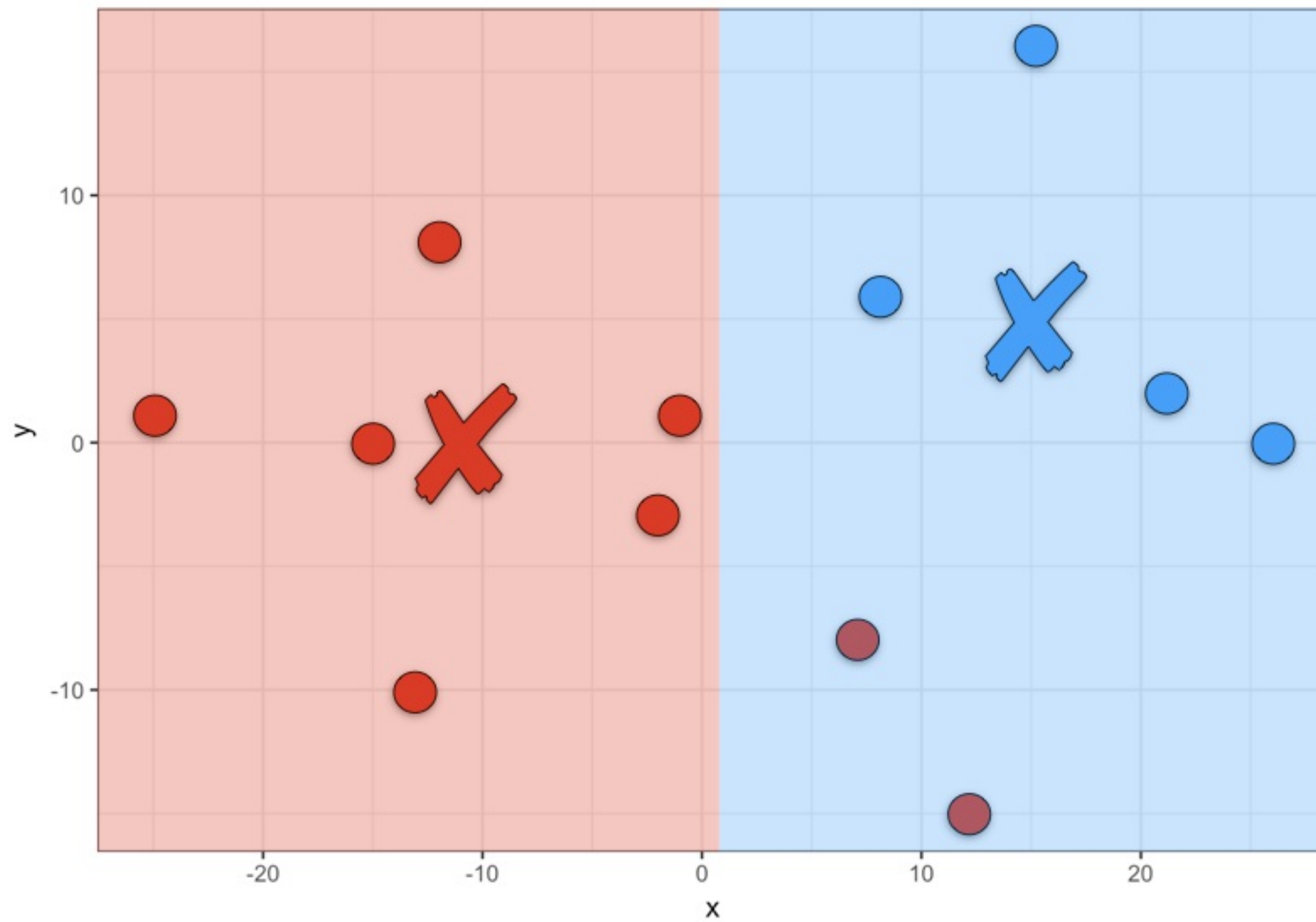


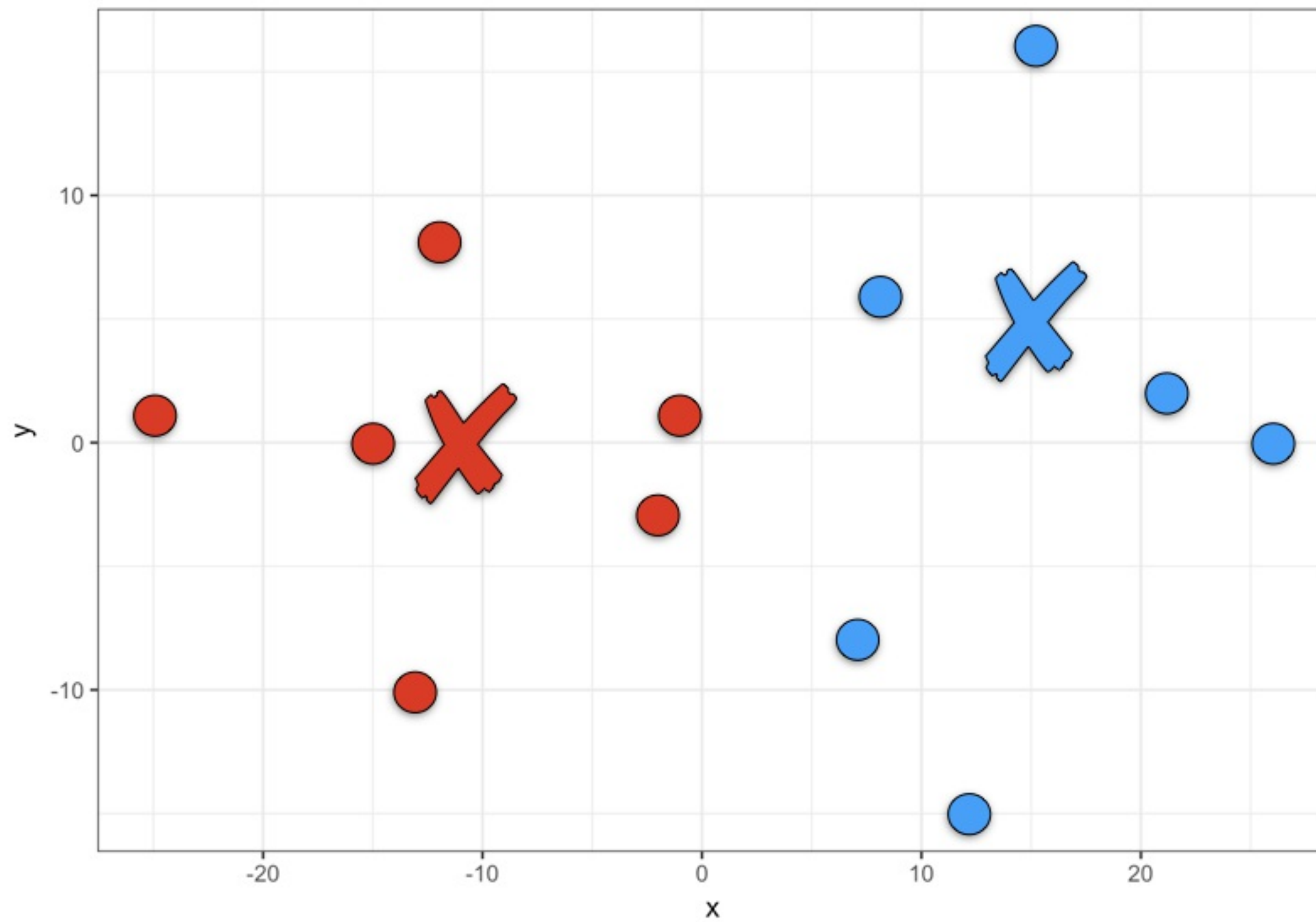


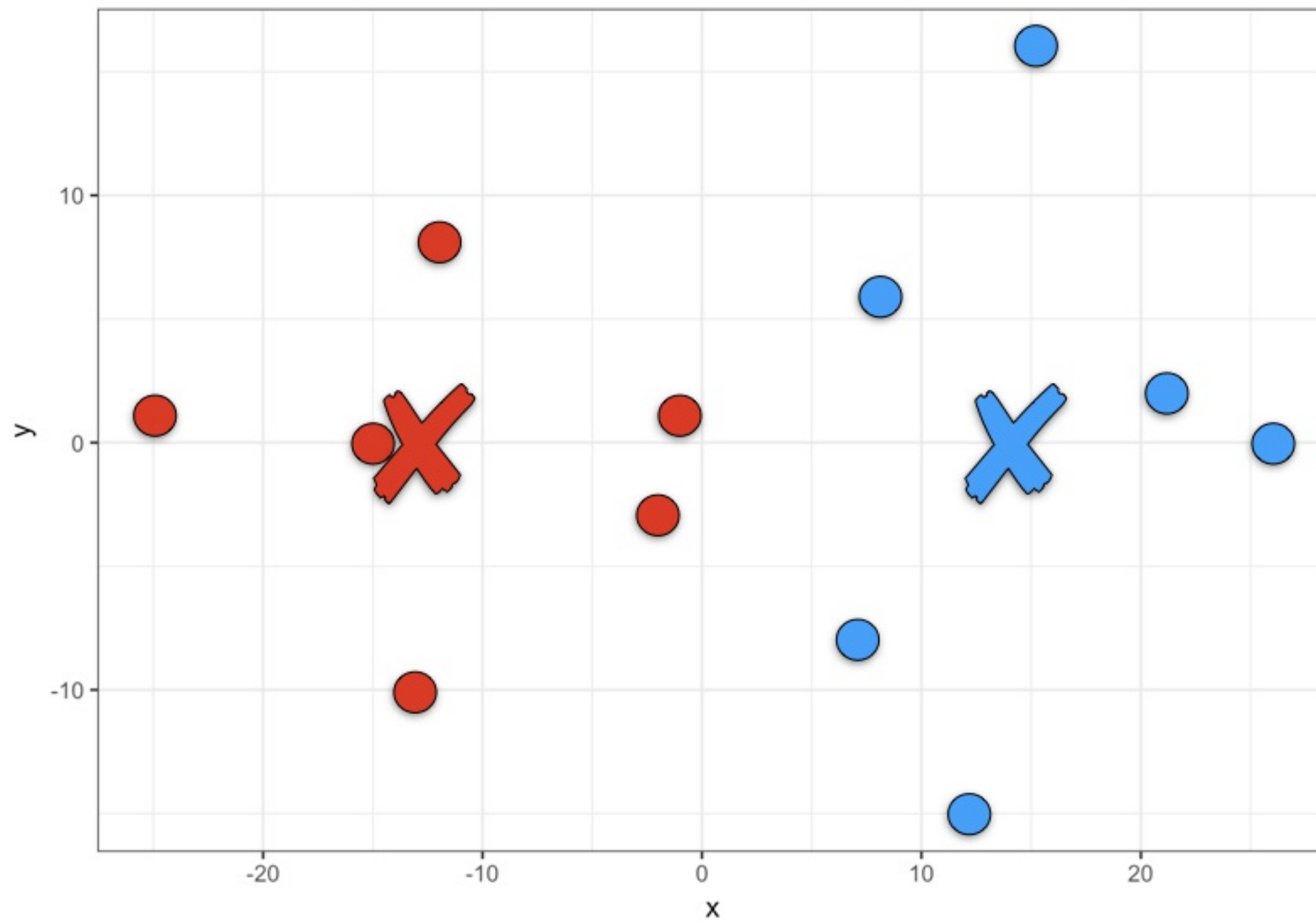












# kmeans()

```
print(lineup)
```

|     | x   | y   |
|-----|-----|-----|
| 1   | -1  | 1   |
| 2   | -2  | -3  |
| 3   | 8   | 6   |
| 4   | 7   | -8  |
| ... | ... | ... |

```
model <- kmeans(lineup, centers = 2)
```



# Assigning Clusters

```
print(model$cluster)

[1] 1 1 2 2 1 1 1 2 2 2 1 2

lineup_clustered <- mutate(lineup, cluster = model$cluster)

print(lineup_clustered)
```

|     | x     | y     | cluster |
|-----|-------|-------|---------|
|     | <dbl> | <dbl> | <int>   |
| 1   | -1    | 1     | 1       |
| 2   | -2    | -3    | 1       |
| 3   | 8     | 6     | 2       |
| 4   | 7     | -8    | 2       |
| ... | ...   | ...   | ...     |



## CLUSTER ANALYSIS IN R

**Let's practice!**



CLUSTER ANALYSIS IN R

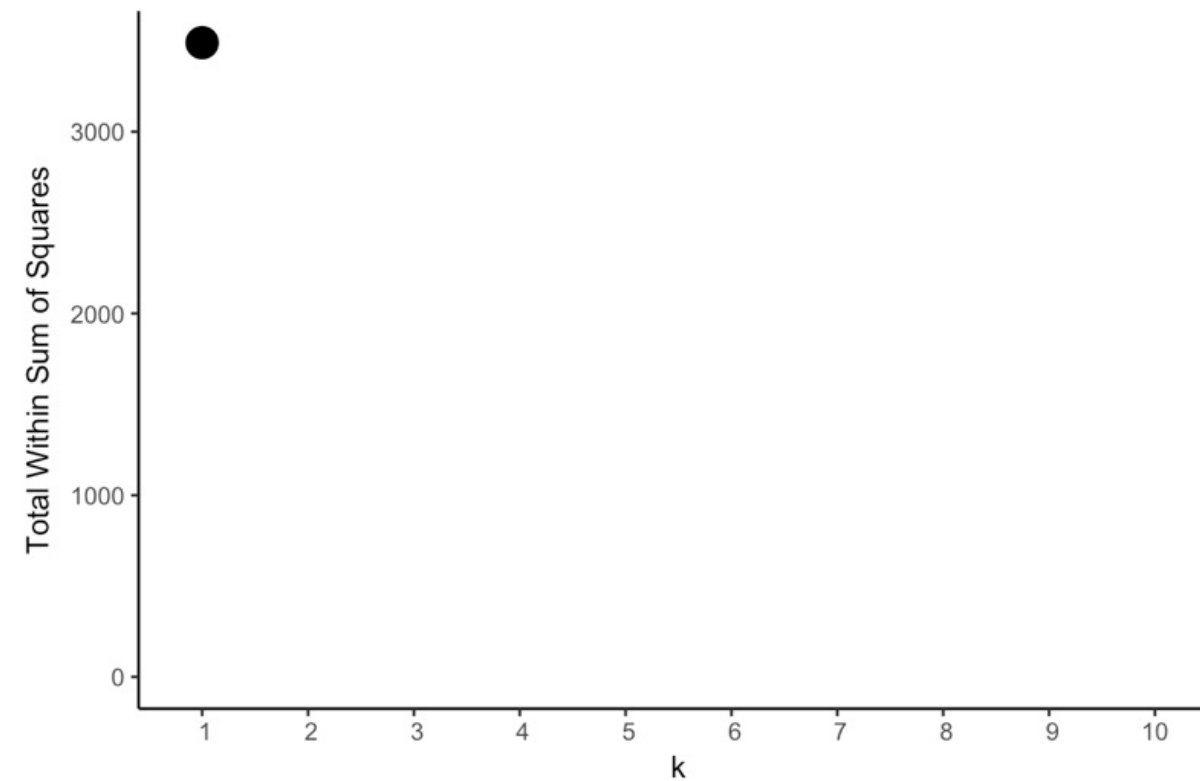
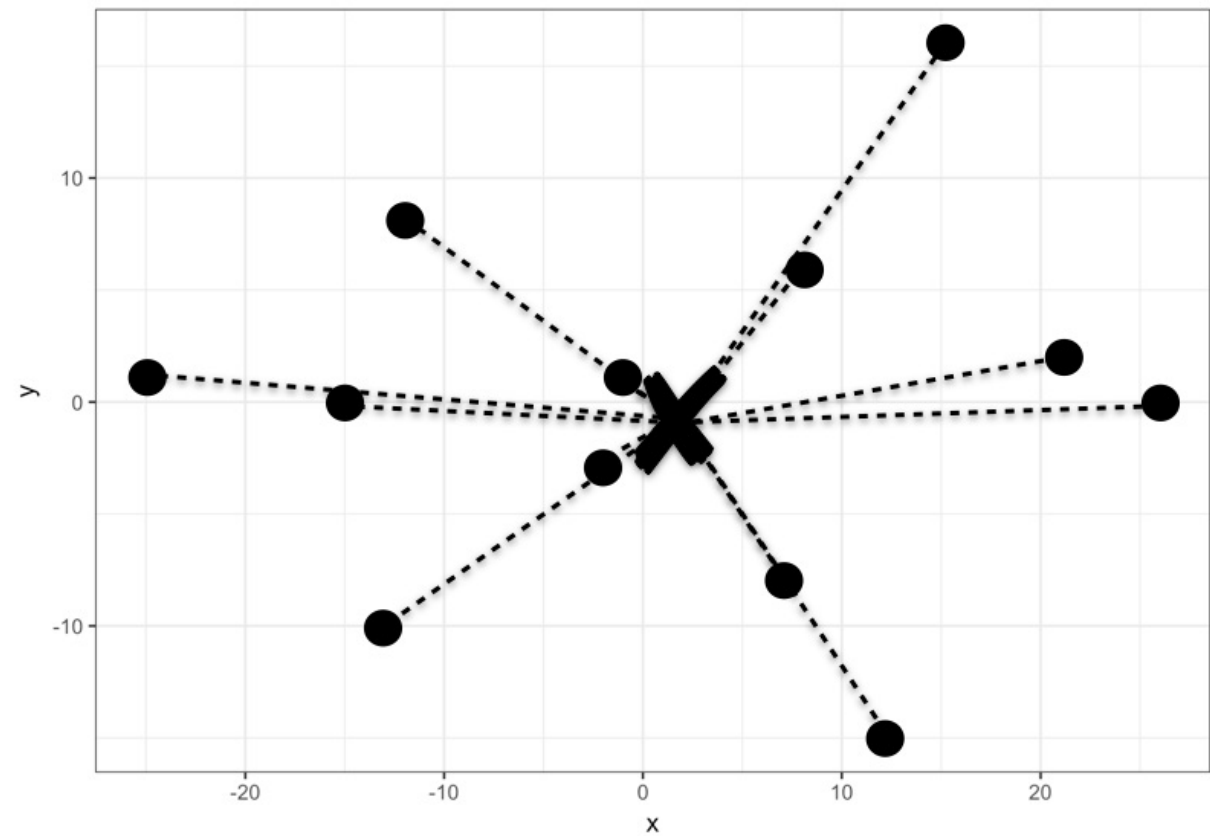
# Evaluating Different Values of K by Eye

Dmitriy (Dima) Gorenshteyn

Sr. Data Scientist,

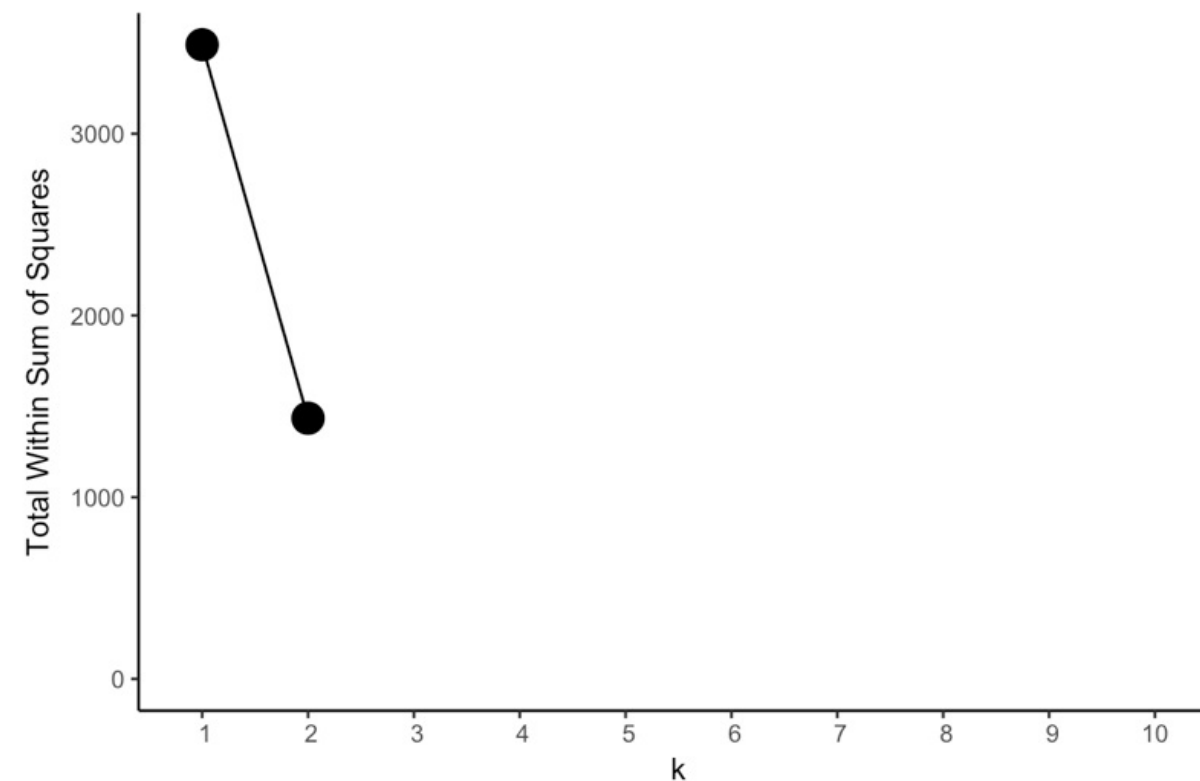
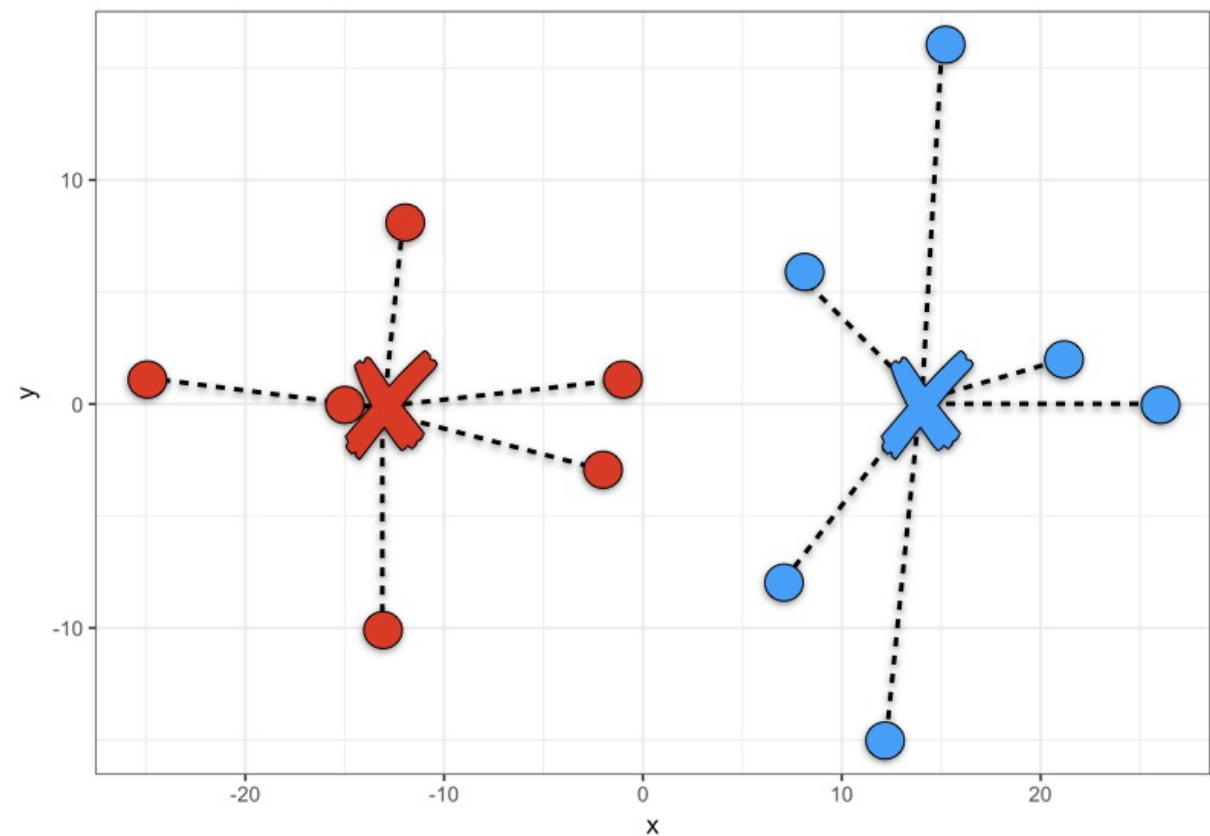
Memorial Sloan Kettering Cancer Center

# Total Within-Cluster Sum of Squares: $k = 1$

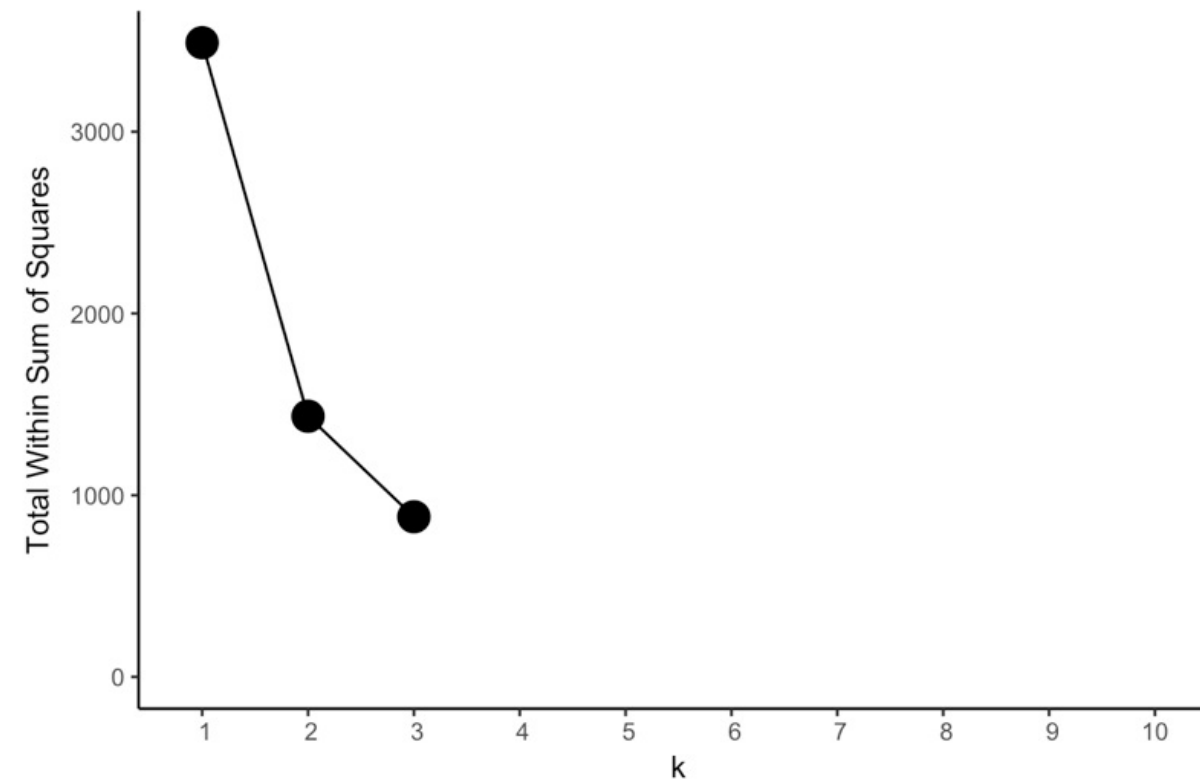
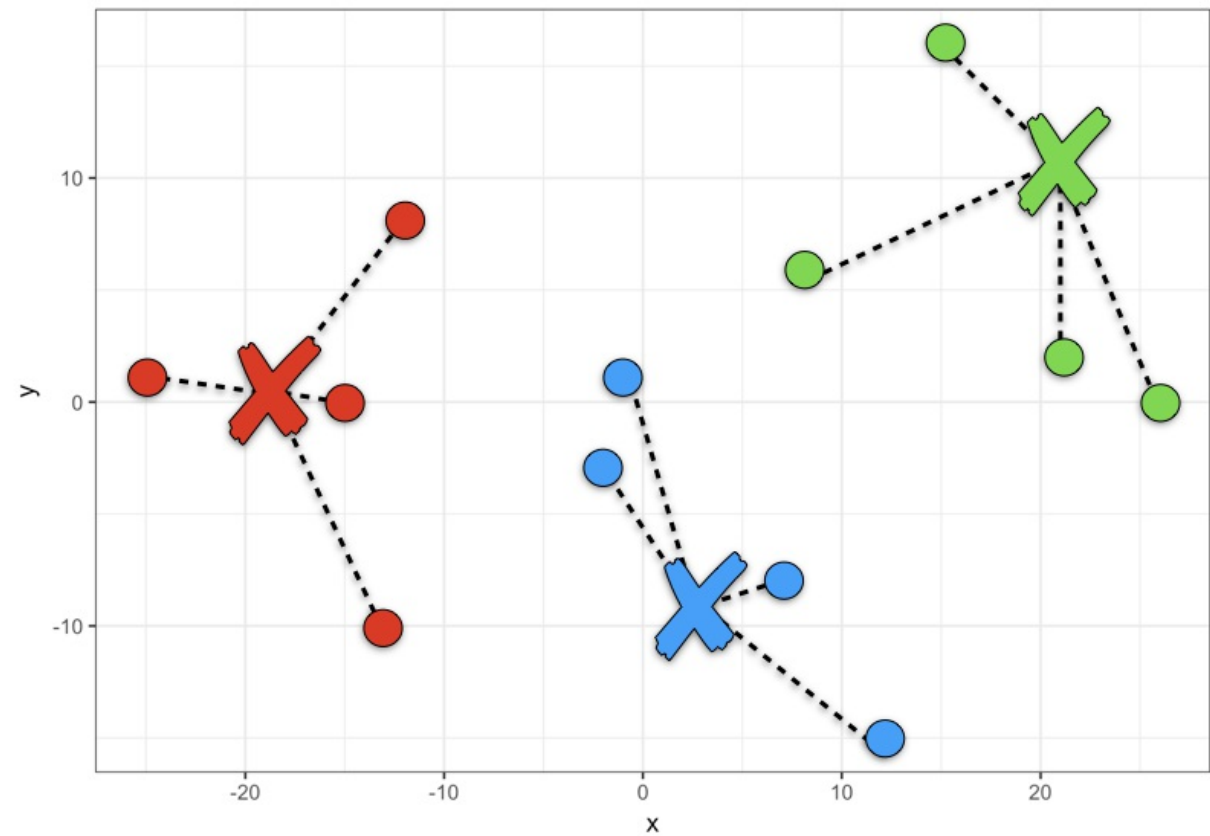




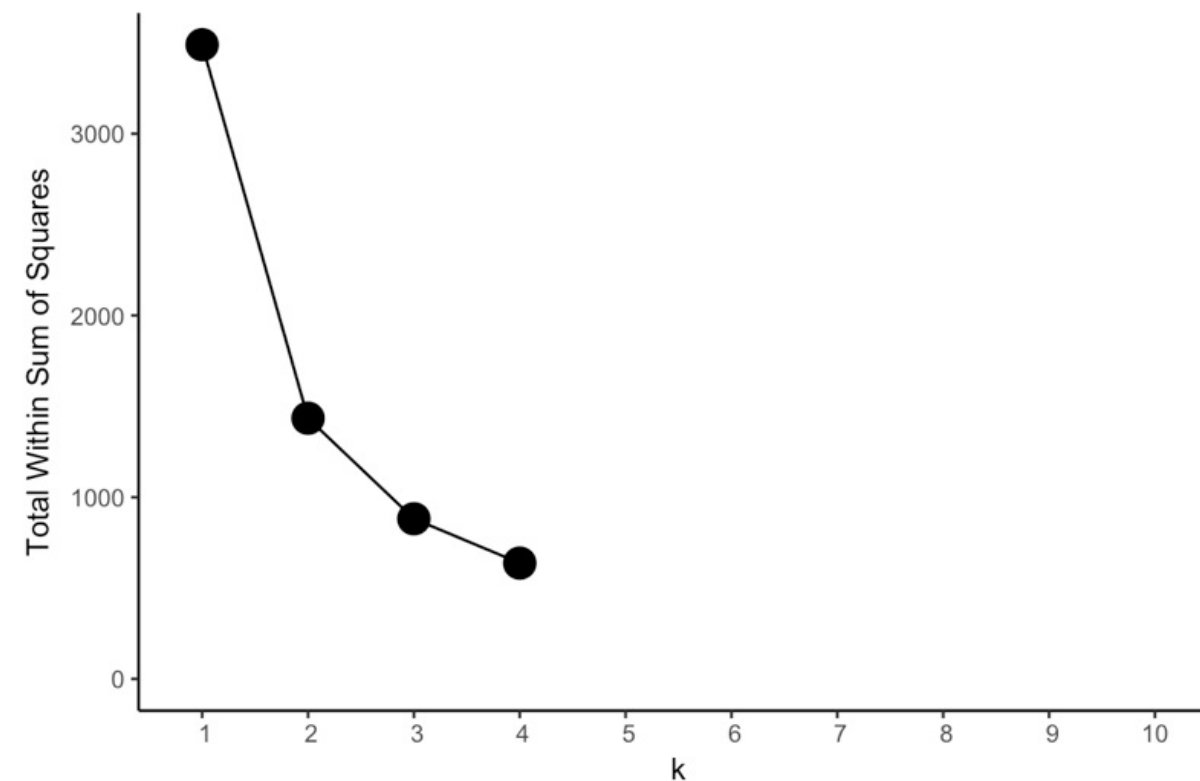
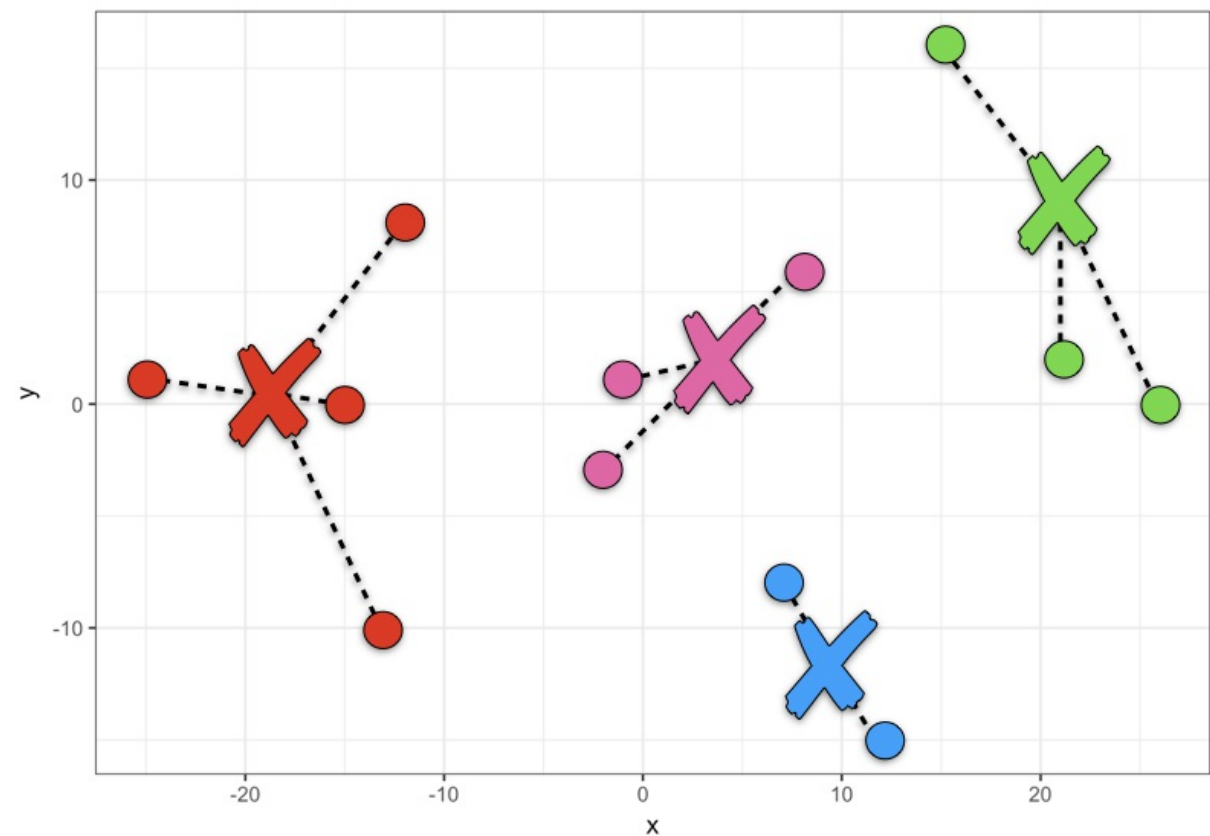
# Total Within-Cluster Sum of Squares: $k = 2$



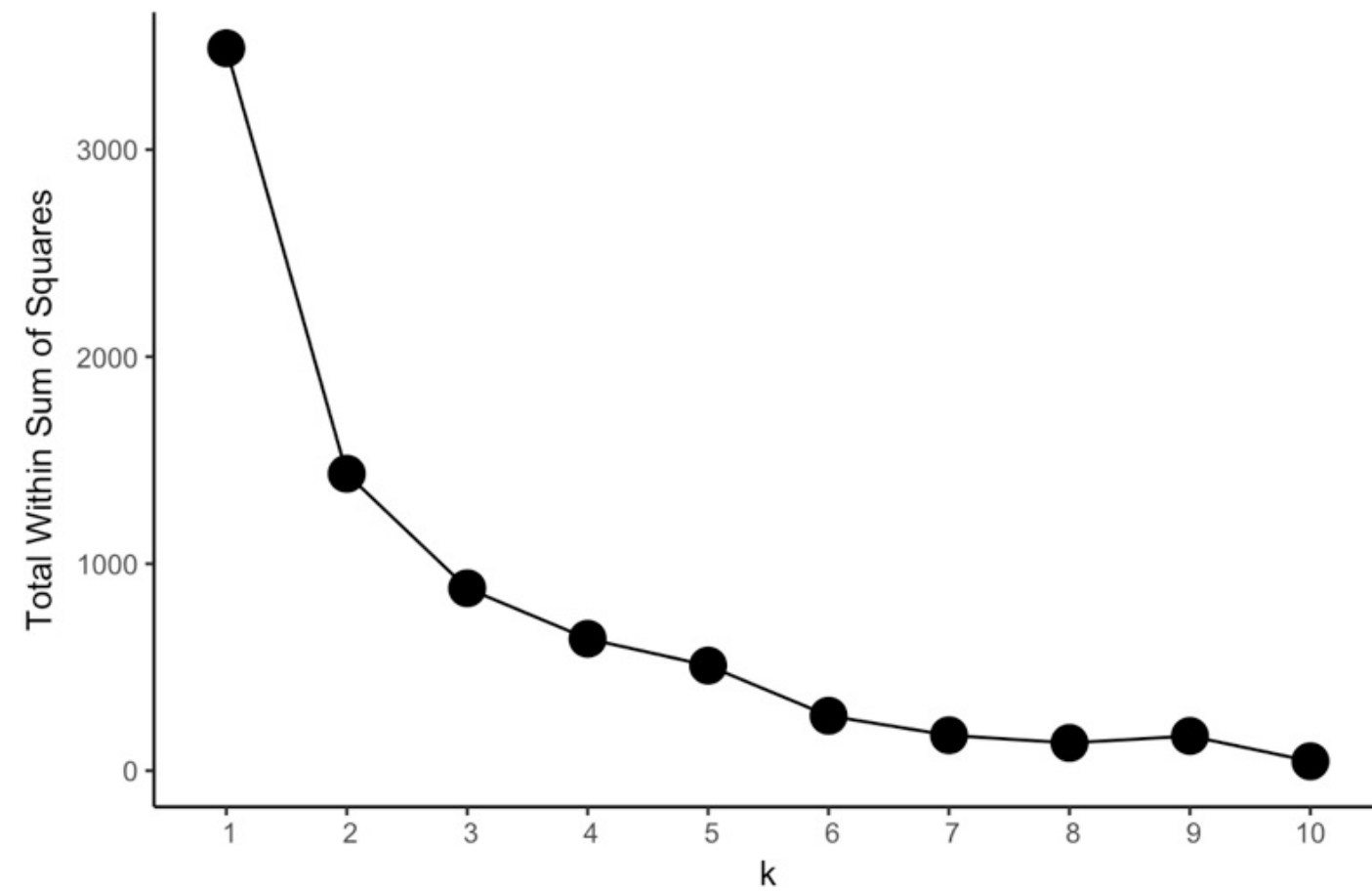
# Total Within-Cluster Sum of Squares: $k = 3$



# Total Within-Cluster Sum of Squares: $k = 4$

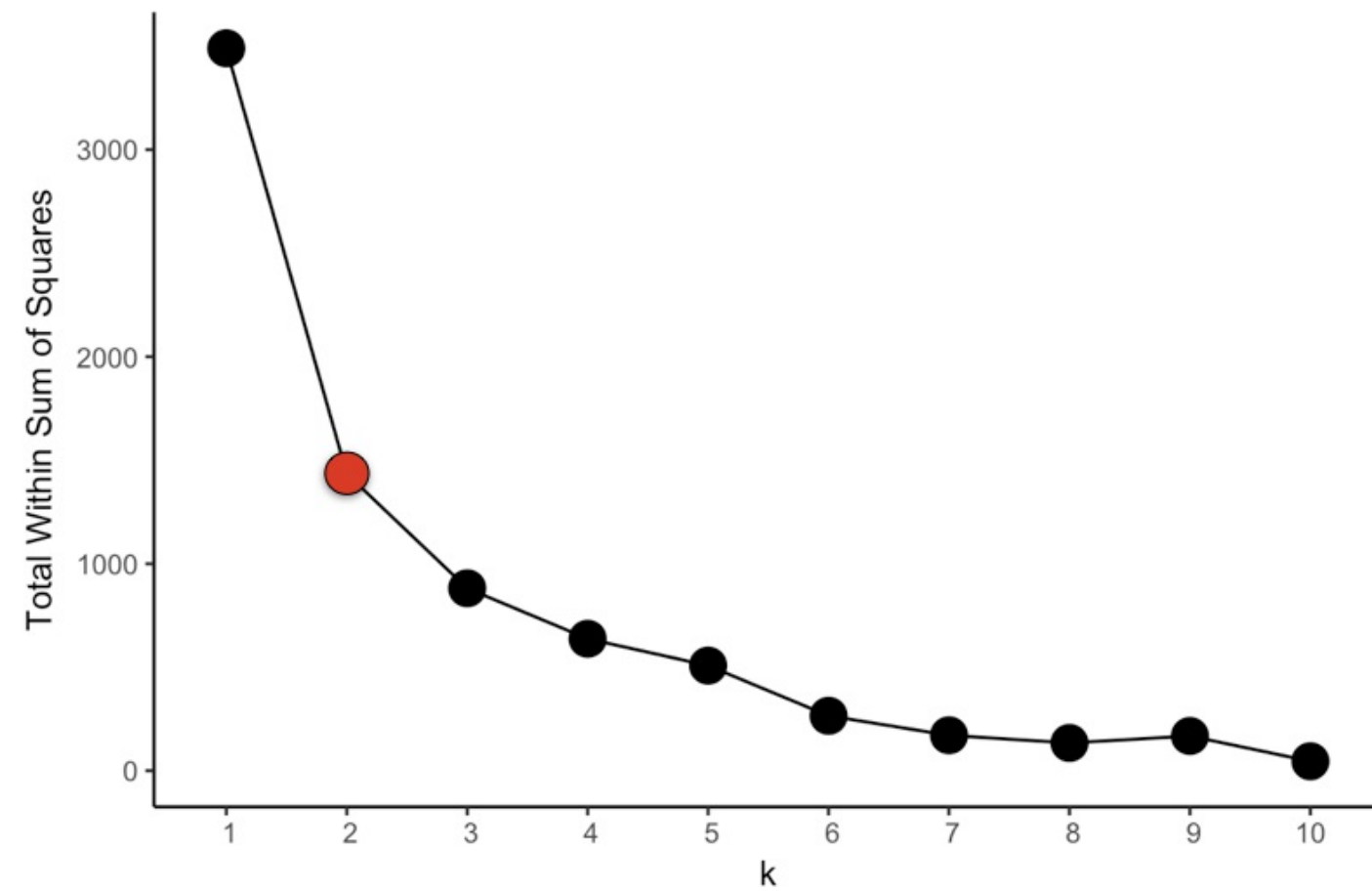


# Elbow Plot





# Elbow Plot





# Generating the Elbow Plot

```
model <- kmeans(x = lineup, centers = 2)
```

```
model$tot.withinss  
[1] 1434.5
```



# Generating the Elbow Plot

```
library(purrr)

tot_withinss <- map_dbl(1:10, function(k){
  model <- kmeans(x = lineup, centers = k)
  model$tot.withinss
})

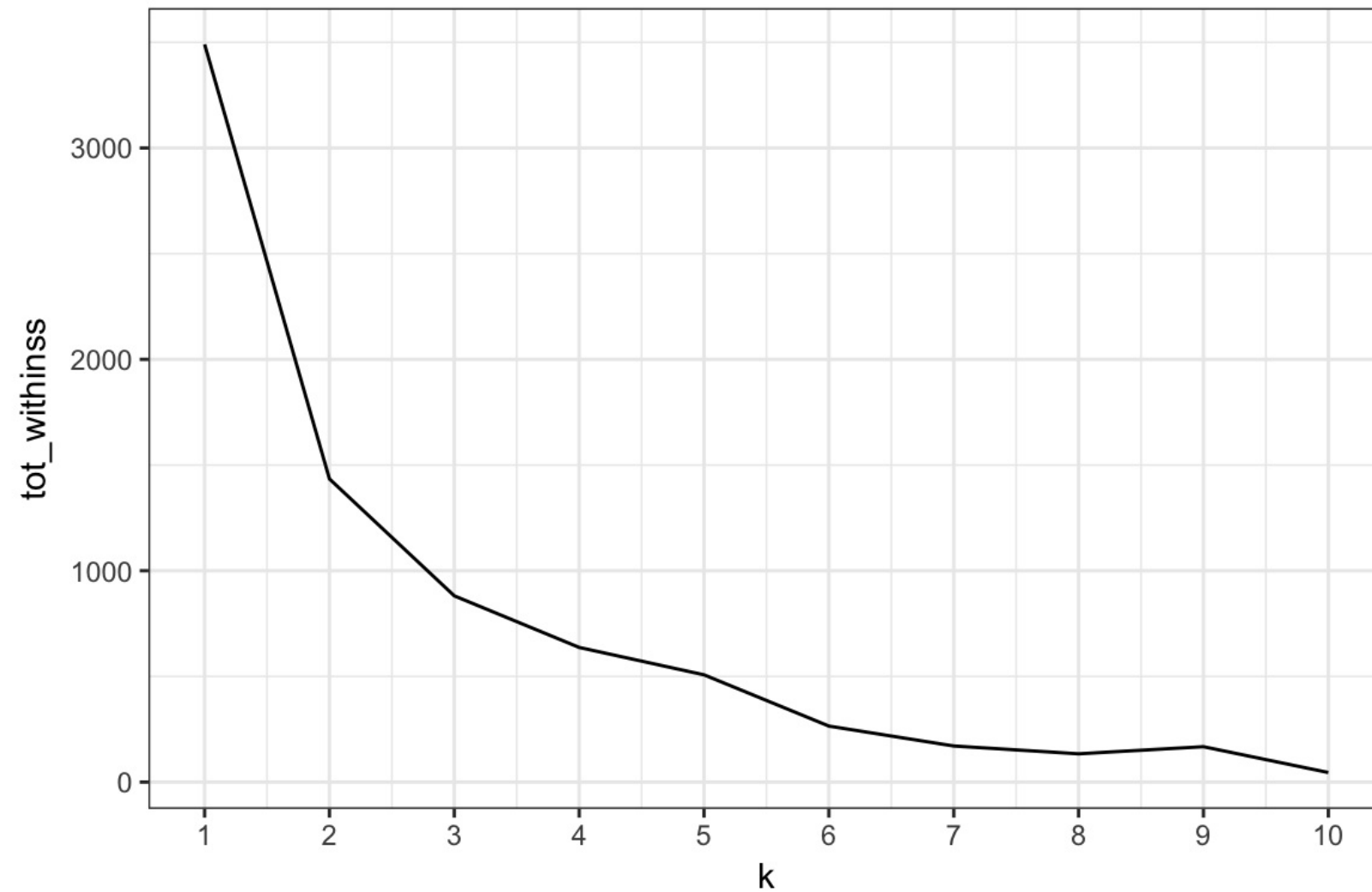
elbow_df <- data.frame(
  k = 1:10,
  tot_withinss = tot_withinss
)

print(elbow_df)
```

|     | k   | tot_withinss |
|-----|-----|--------------|
| 1   | 1   | 3489.9167    |
| 2   | 2   | 1434.5000    |
| 3   | 3   | 881.2500     |
| 4   | 4   | 637.2500     |
| ... | ... | ...          |

# Generating the Elbow Plot

```
ggplot(elbow_df, aes(x = k, y = tot_withinss)) +  
  geom_line() +  
  scale_x_continuous(breaks = 1:10)
```







## CLUSTER ANALYSIS IN R

**Let's practice!**



CLUSTER ANALYSIS IN R

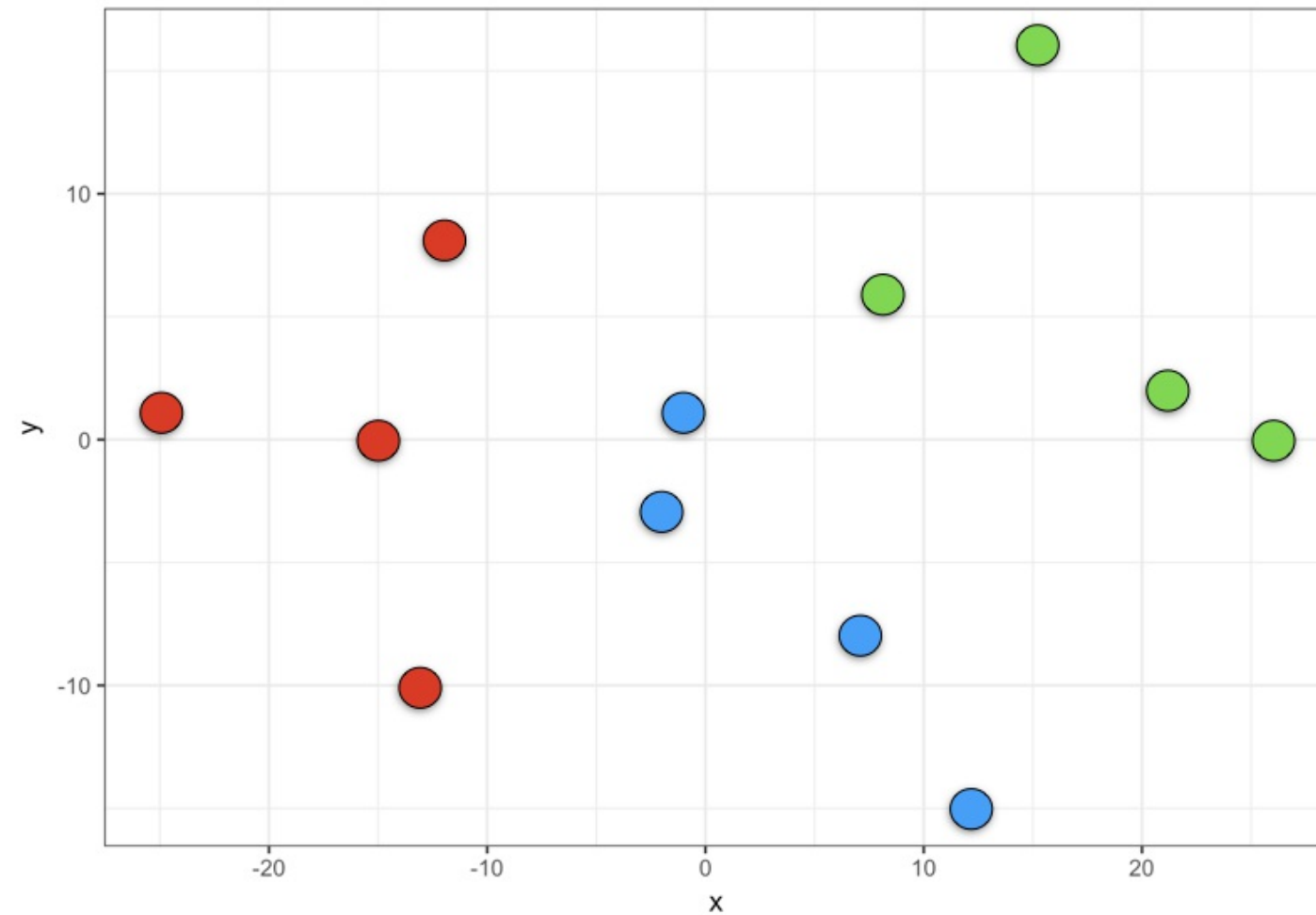
# Silhouette Analysis

Dmitriy (Dima) Gorenshteyn

Sr. Data Scientist,

Memorial Sloan Kettering Cancer Center

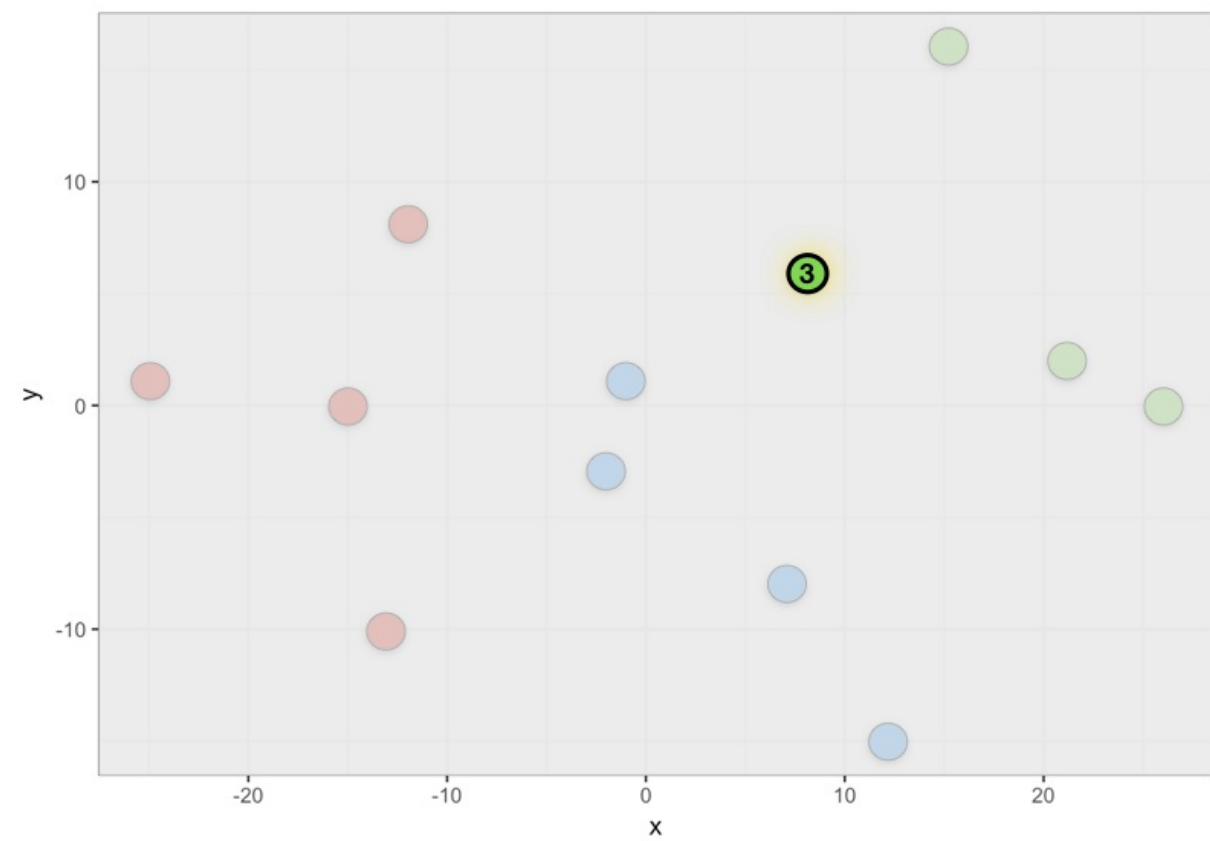
# Soccer Lineup with $K = 3$



# Silhouette Width

**Within Cluster Distance:  $C(i)$**

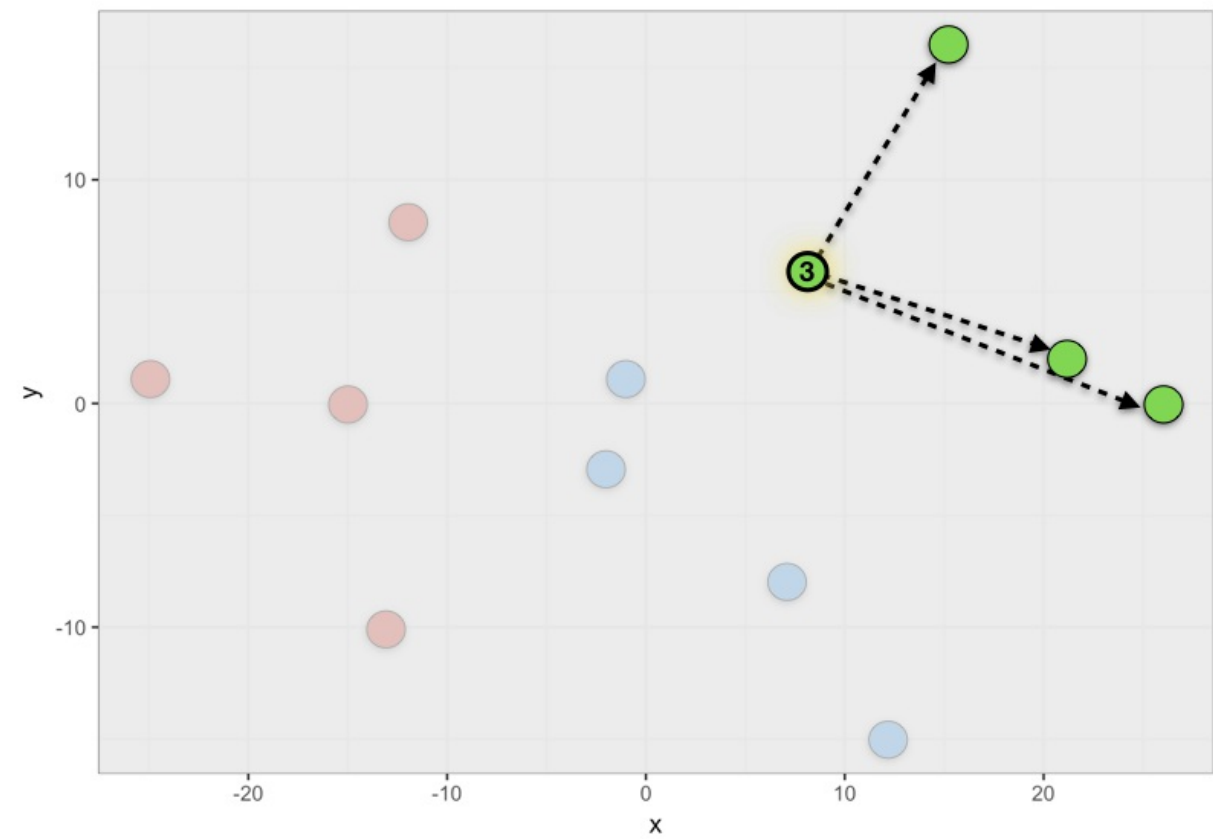
**Closest Neighbor Distance:  $N(i)$**





# Silhouette Width

**Within Cluster Distance:  $C(i)$**

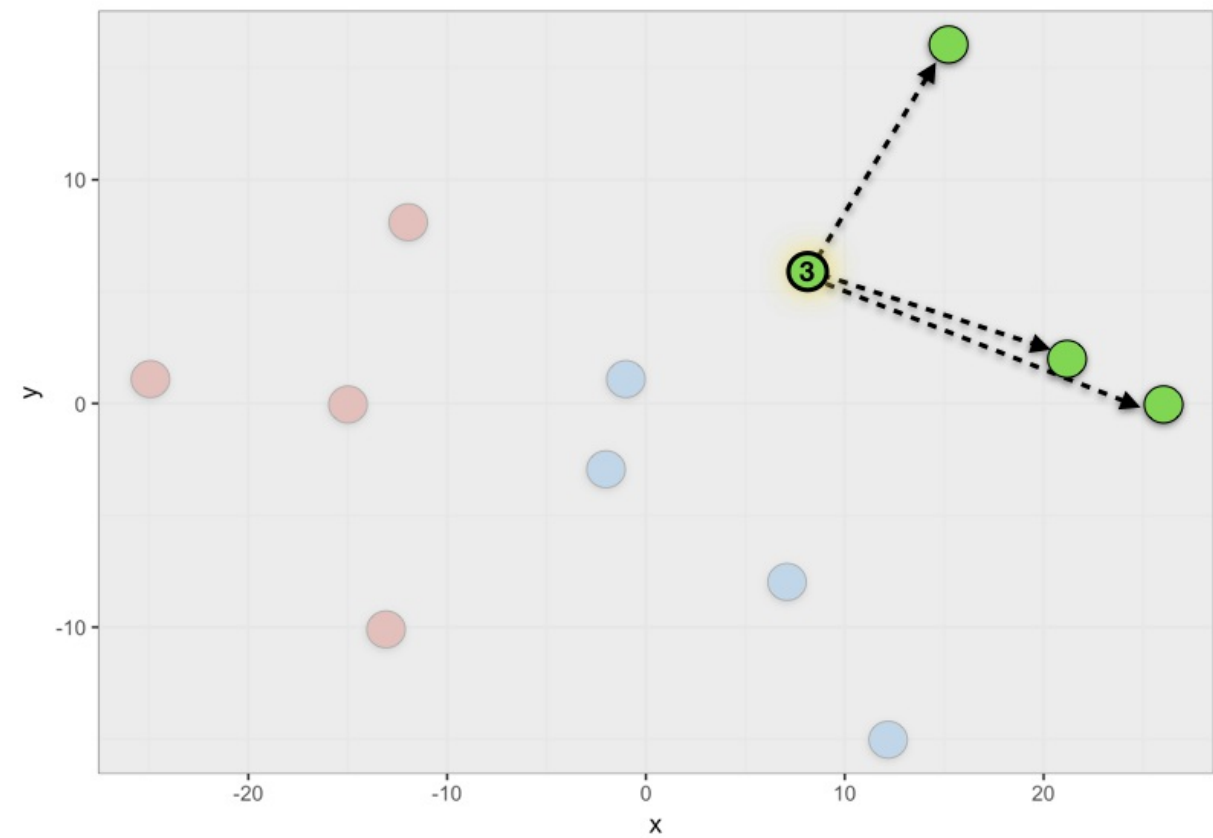


**Closest Neighbor Distance:  $N(i)$**

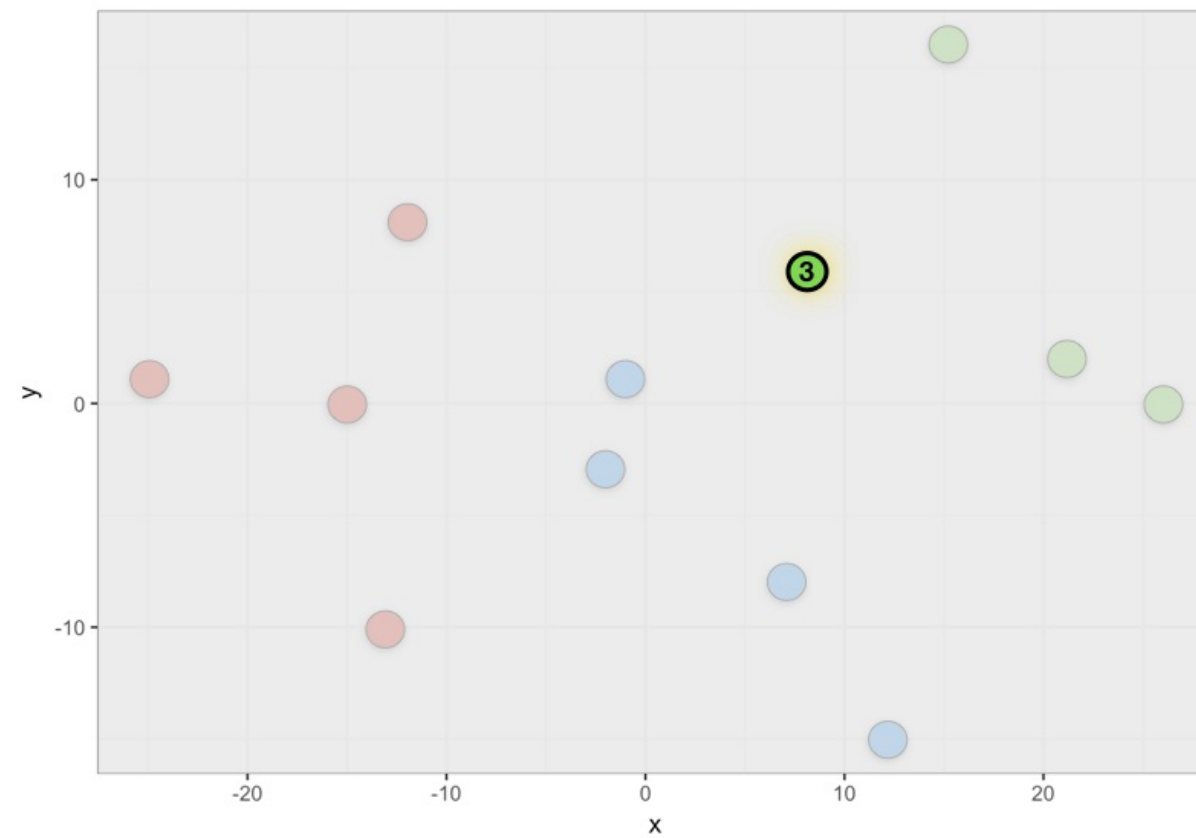


# Silhouette Width

**Within Cluster Distance:  $C(i)$**

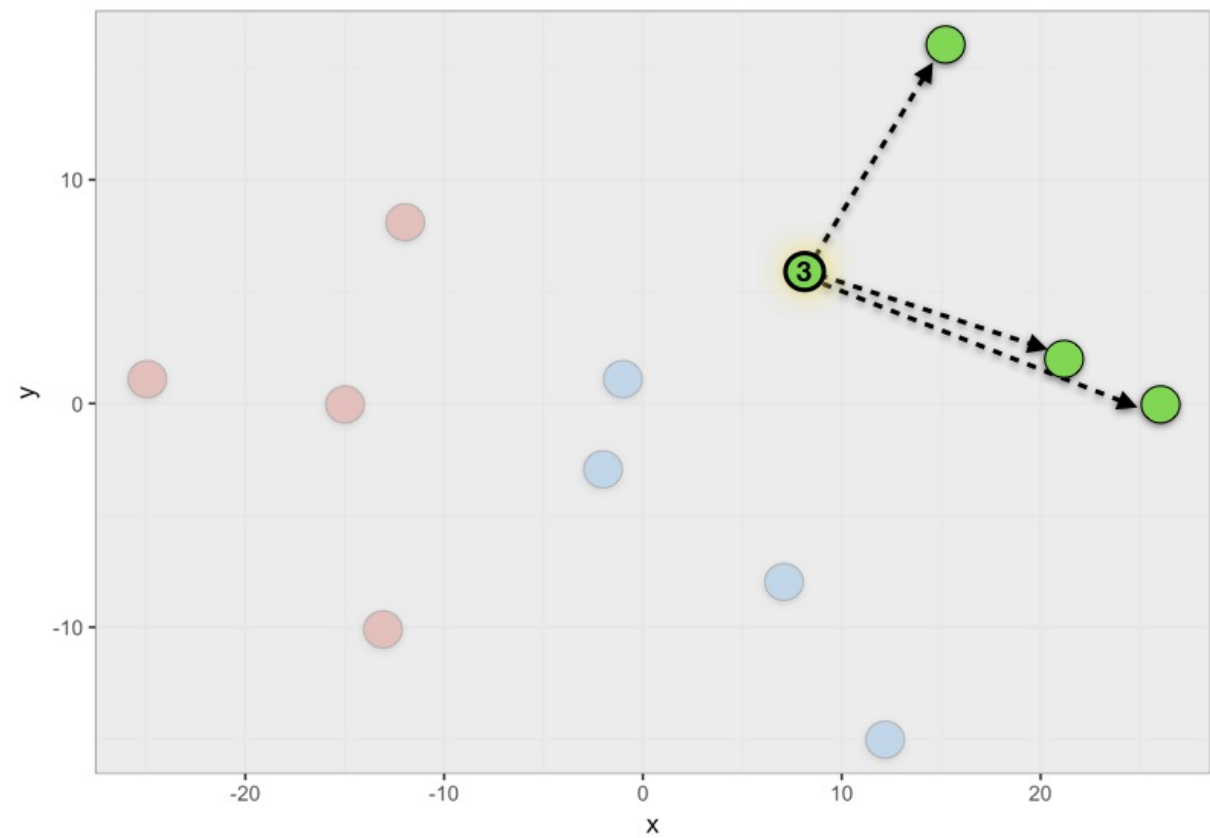


**Closest Neighbor Distance:  $N(i)$**

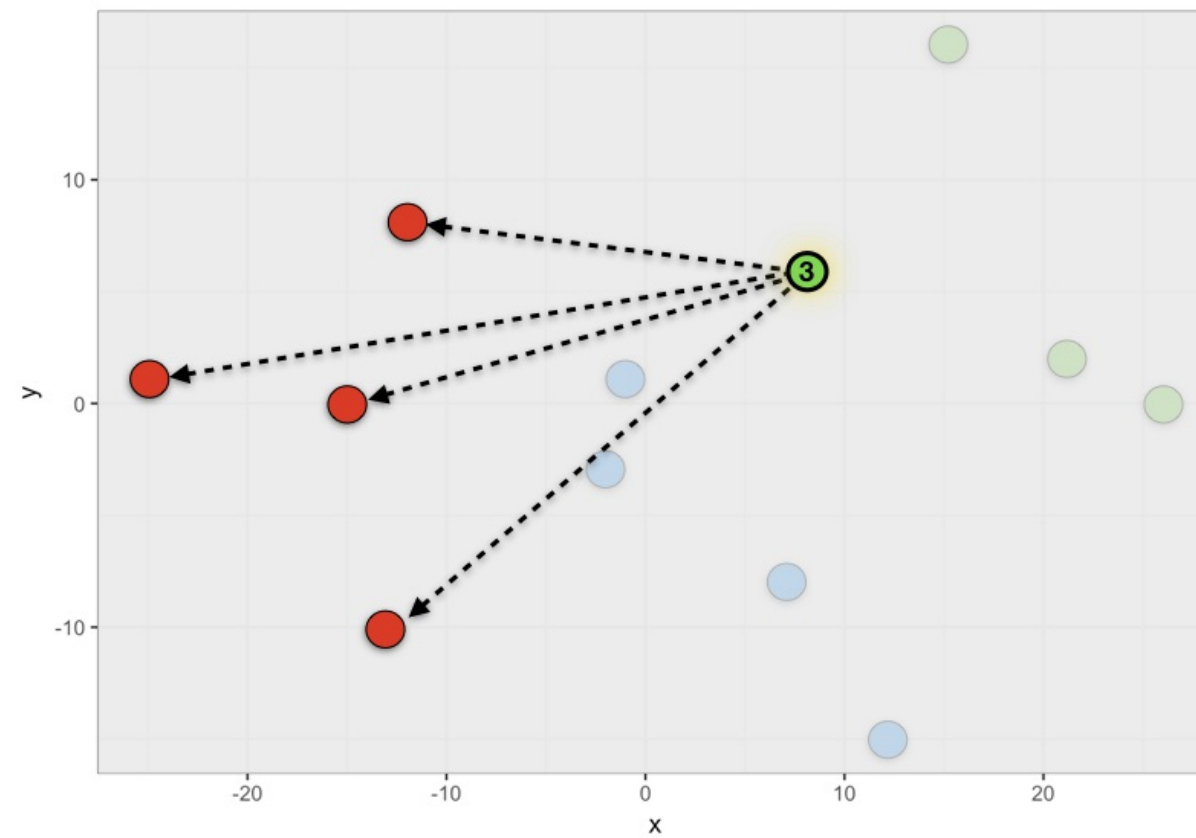


# Silhouette Width

**Within Cluster Distance:  $C(i)$**

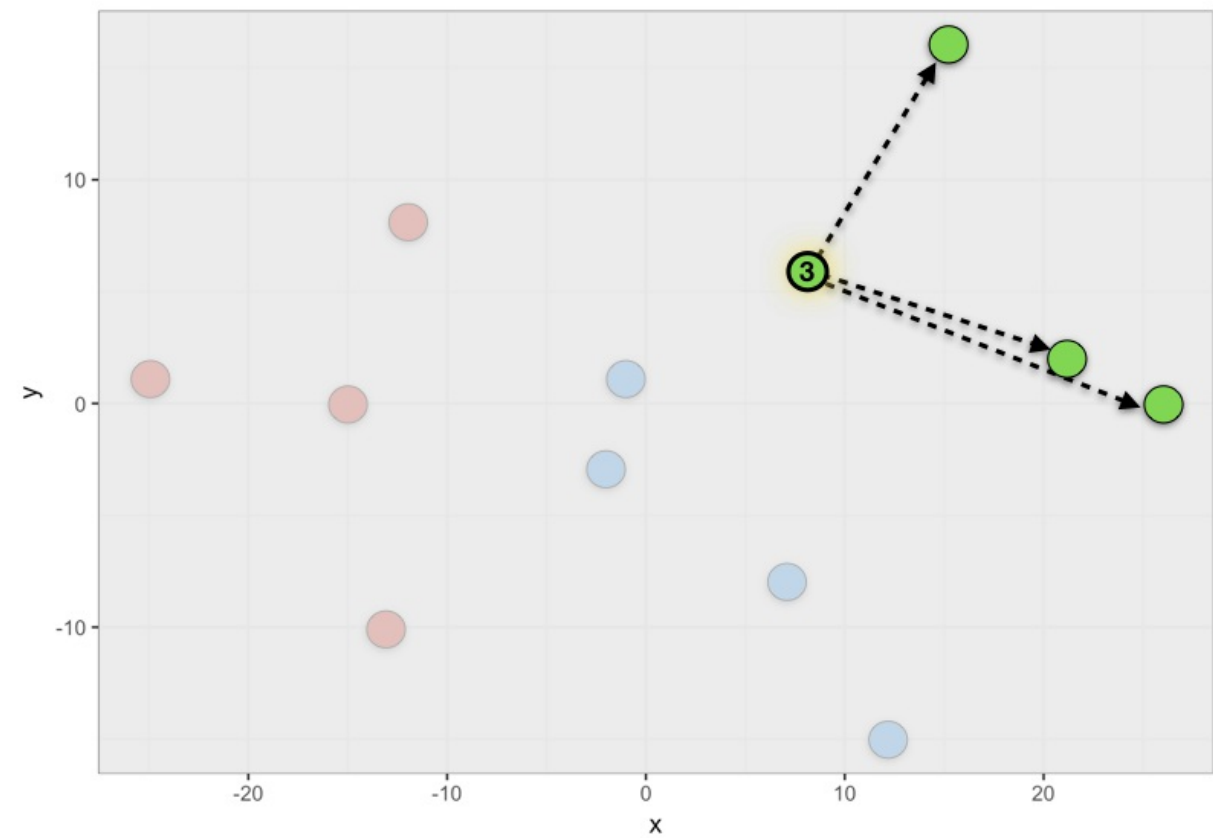


**Closest Neighbor Distance:  $N(i)$**

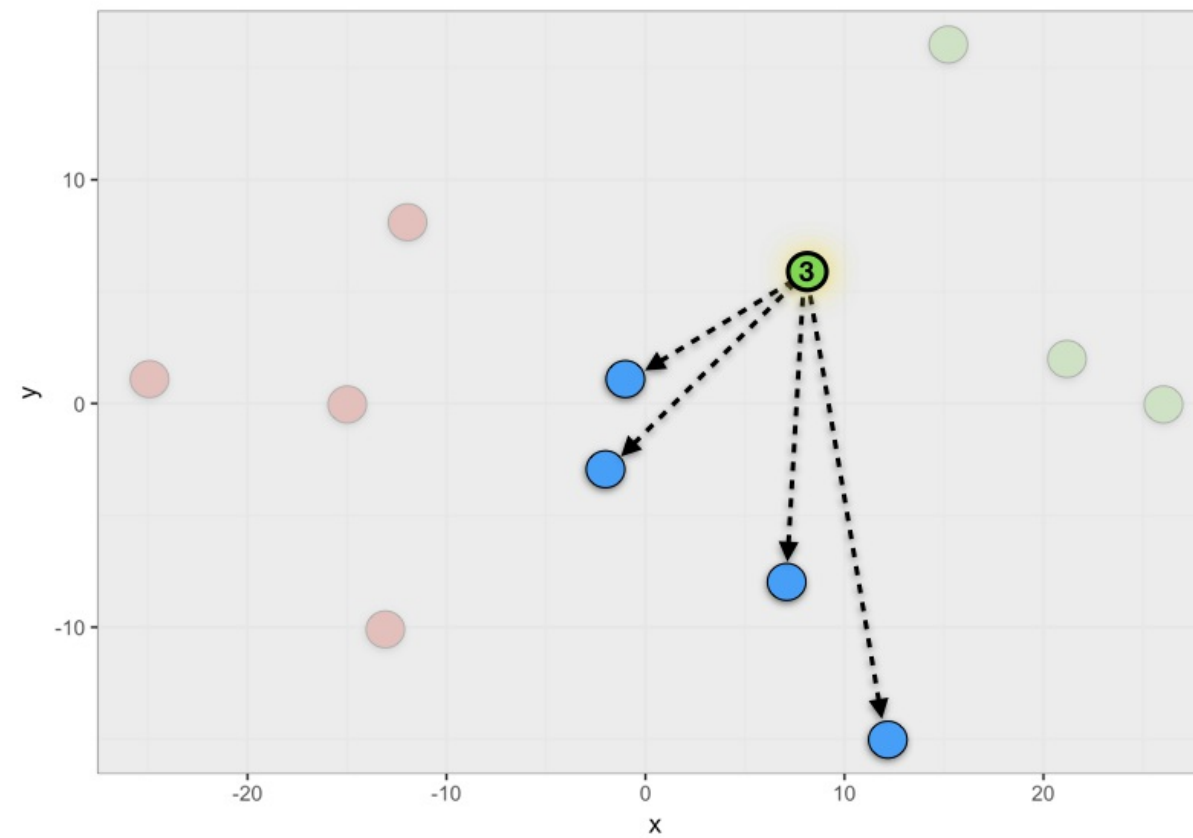


# Silhouette Width

**Within Cluster Distance:  $C(i)$**

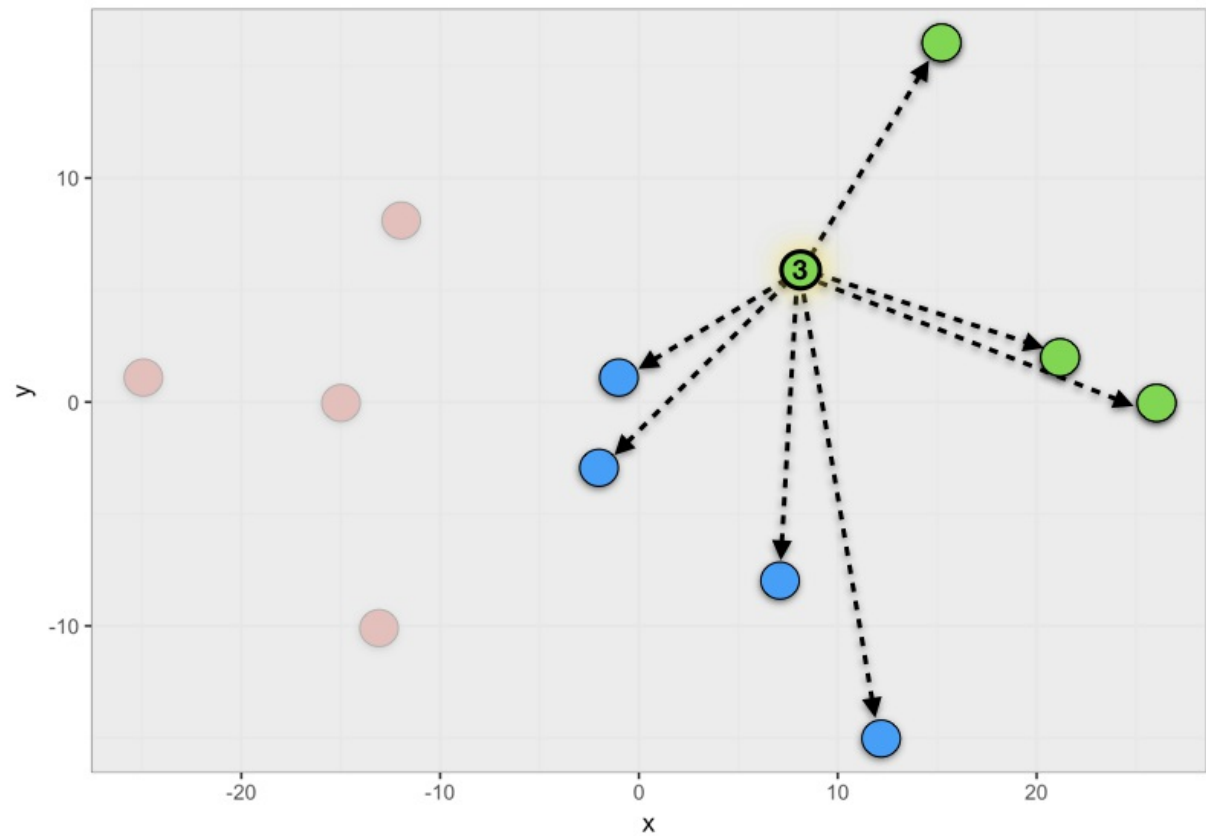


**Closest Neighbor Distance:  $N(i)$**



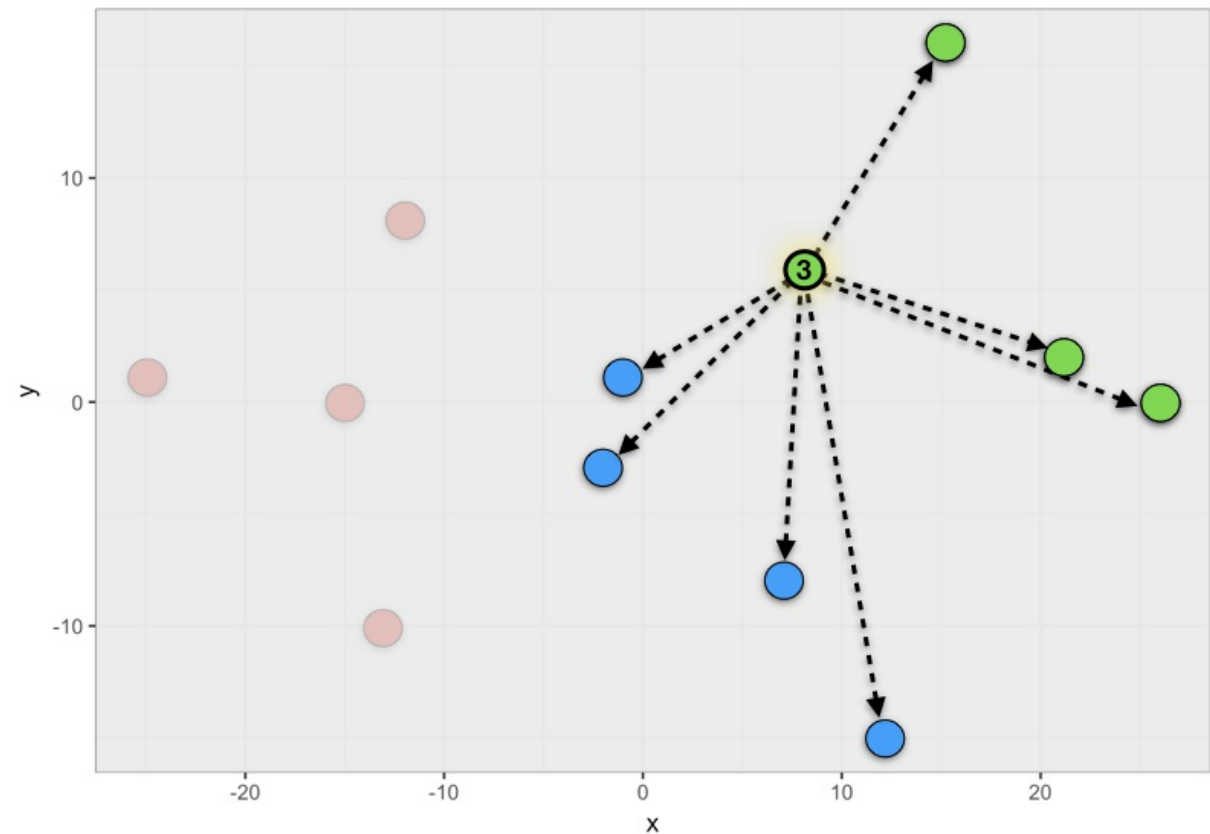


# Silhouette Width: $S(i)$



$$s(i) = \begin{cases} 1 - C(i)/N(i), & \text{if } C(i) < N(i) \\ 0, & \text{if } C(i) = N(i) \\ N(i)/C(i) - 1, & \text{if } C(i) > N(i) \end{cases}$$

# Silhouette Width: $S(i)$



- **1:** Well matched to cluster
- **0:** On border between two clusters
- **-1:** Better fit in neighboring cluster



# Calculating $S(i)$

```
library(cluster)
pam_k3 <- pam(lineup, k = 3)

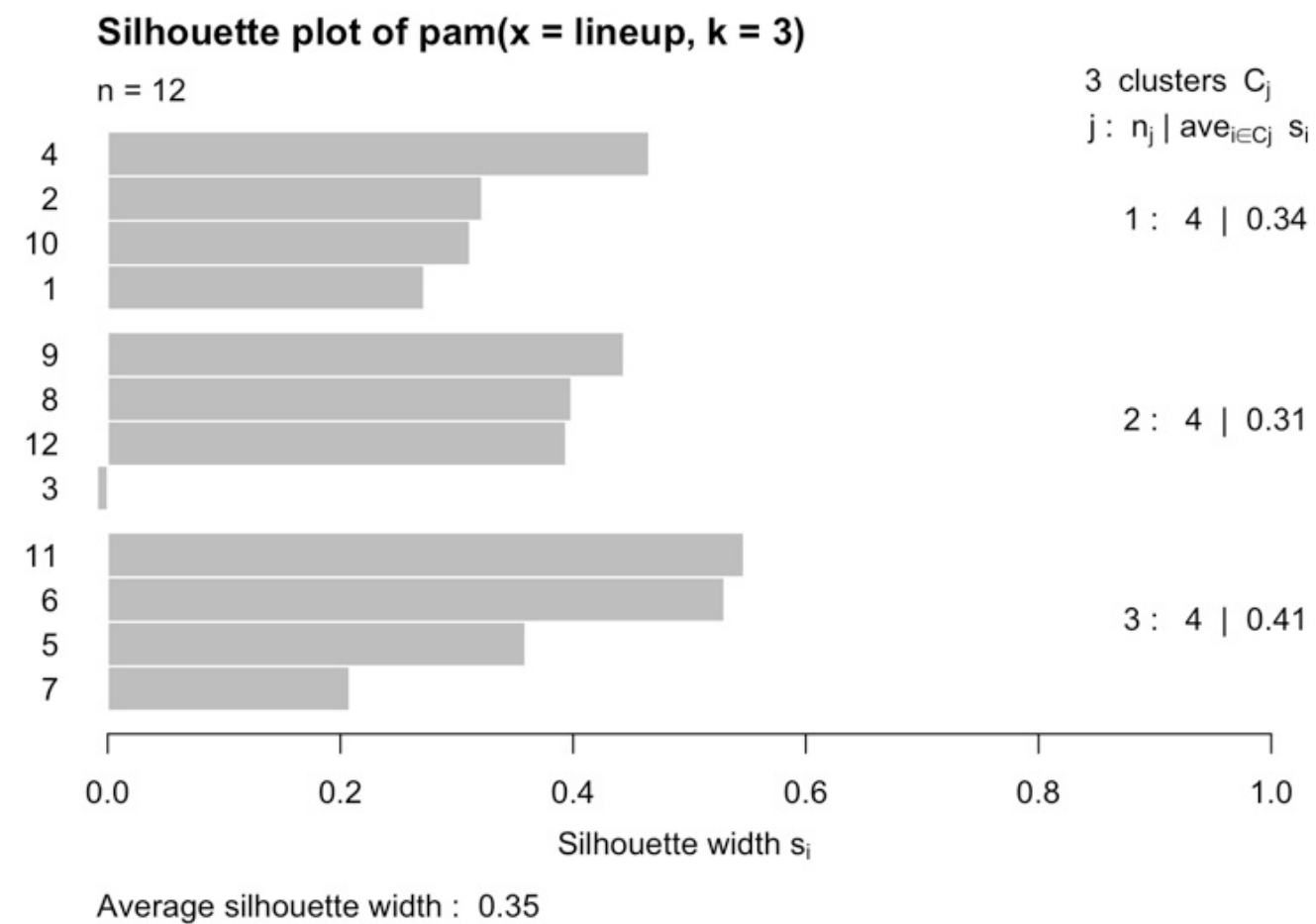
pam_k3$silinfo$widths
```

|     | cluster | neighbor | sil_width   |
|-----|---------|----------|-------------|
| 4   | 1       | 2        | 0.465320054 |
| 2   | 1       | 3        | 0.321729341 |
| 10  | 1       | 2        | 0.311385893 |
| 1   | 1       | 3        | 0.271890169 |
| 9   | 2       | 1        | 0.443606497 |
| ... | ...     | ...      | ...         |



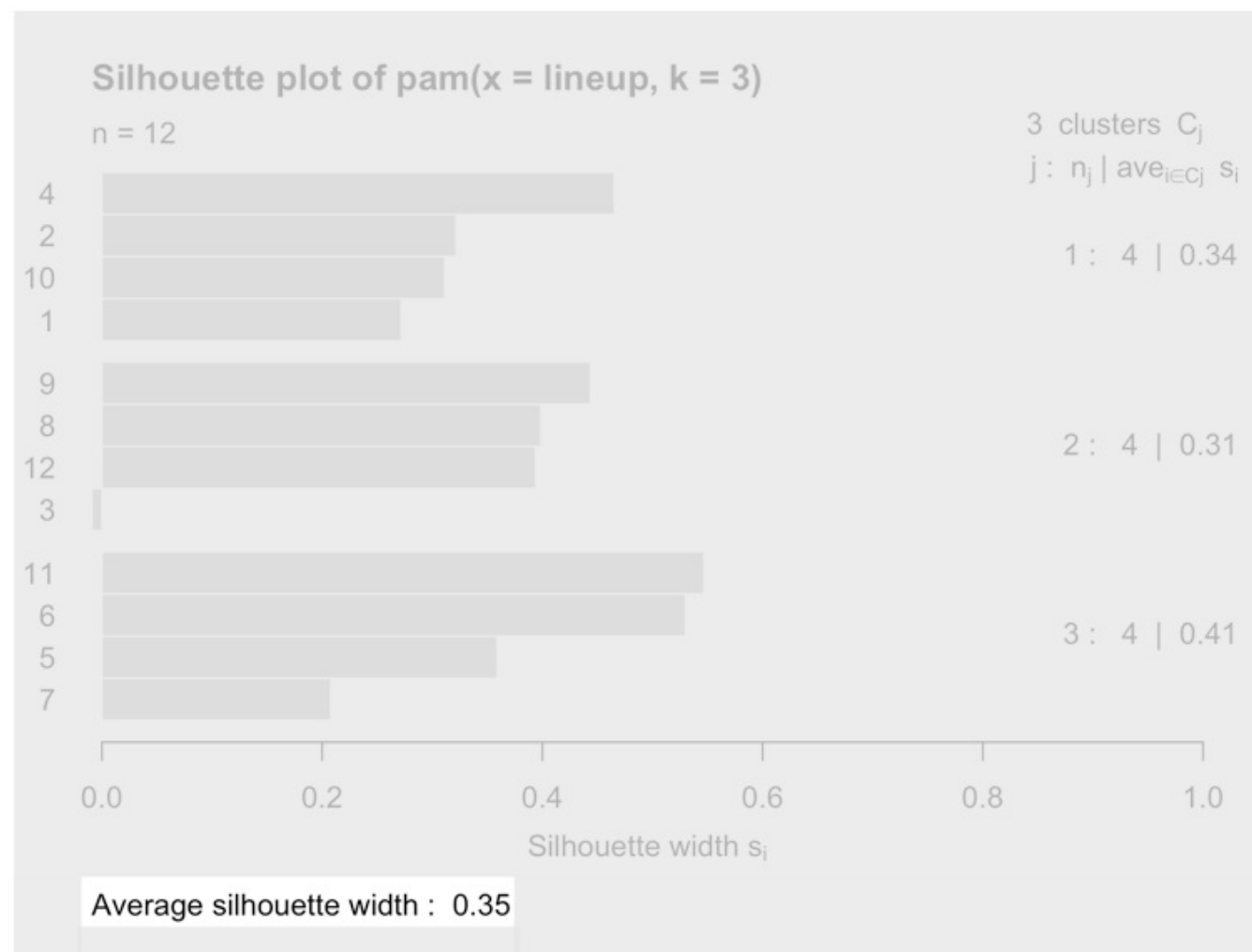
# Silhouette Plot

```
sil_plot <- silhouette(pam_k3)
plot(sil_plot)
```



# Silhouette Plot

```
sil_plot <- silhouette(pam_k3)
plot(sil_plot)
```





# Average Silhouette Width

```
pam_k3$silinfo$avg.width  
[1] 0.353414
```

- **1:** Well matched to each cluster
- **0:** On border between clusters
- **-1:** Poorly matched to each cluster



# Highest Average Silhouette Width

```
library(purrr)

sil_width <- map_dbl(2:10, function(k){
  model <- pam(x = lineup, k = k)
  model$silinfo$avg.width
})

sil_df <- data.frame(
  k = 2:10,
  sil_width = sil_width
)

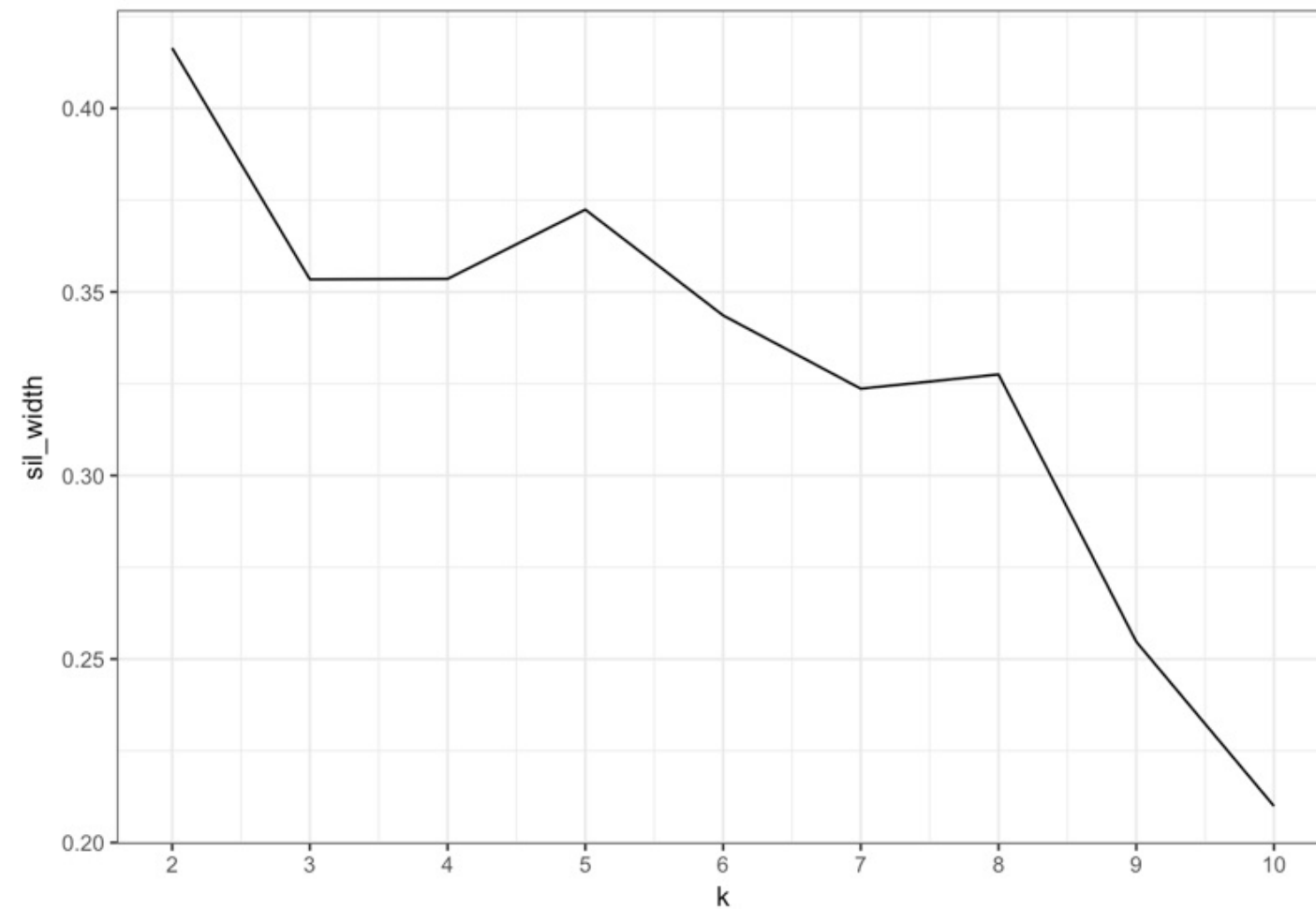
print(sil_df)
```

|     | k   | sil_width |
|-----|-----|-----------|
| 1   | 2   | 0.4164141 |
| 2   | 3   | 0.3534140 |
| 3   | 4   | 0.3535534 |
| 4   | 5   | 0.3724115 |
| ... | ... | ...       |



# Choosing K Using Average Silhouette Width

```
ggplot(sil_df, aes(x = k, y = sil_width)) +  
  geom_line() +  
  scale_x_continuous(breaks = 2:10)
```

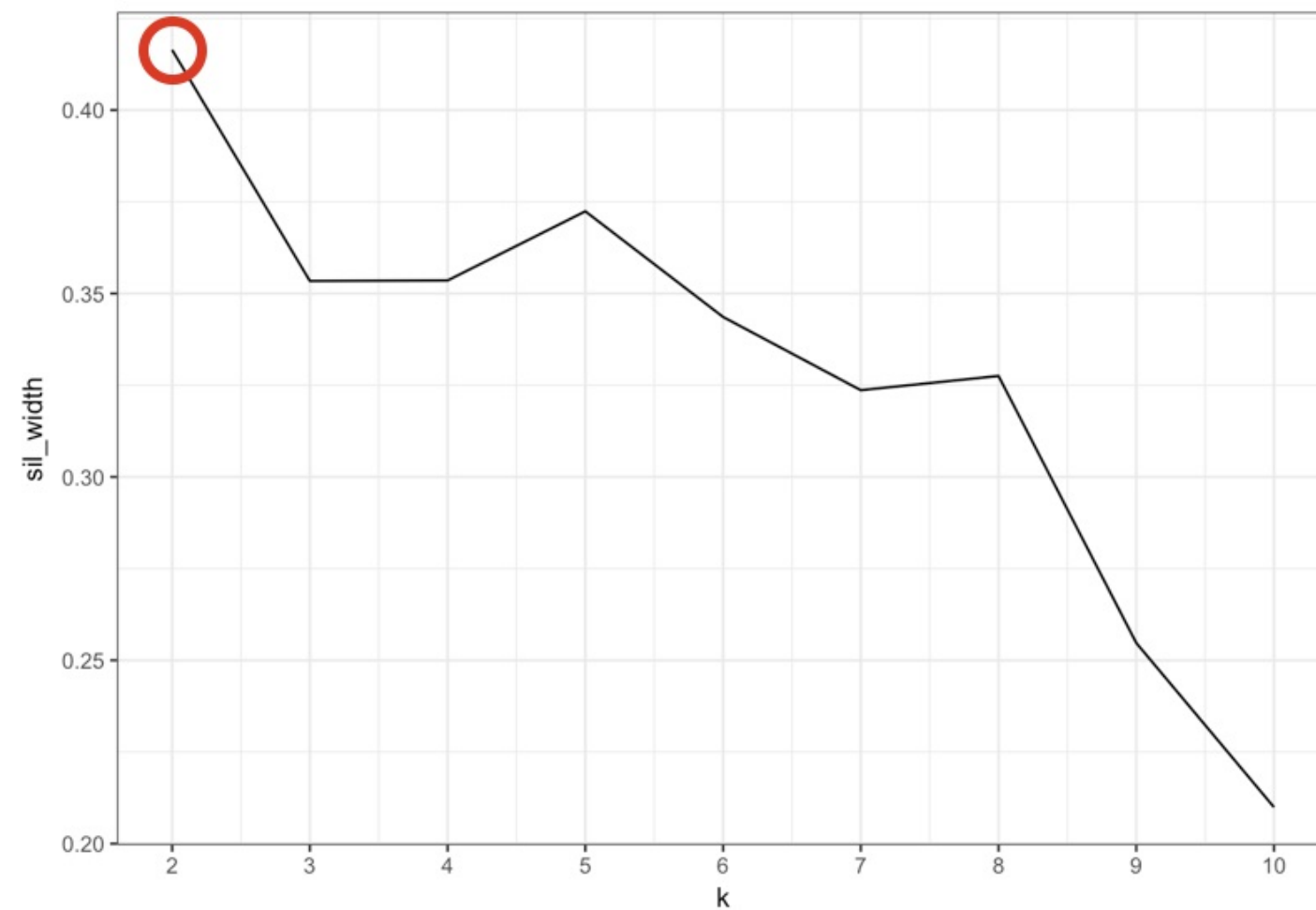






# Choosing K Using Average Silhouette Width

```
ggplot(sil_df, aes(x = k, y = sil_width)) +  
  geom_line() +  
  scale_x_continuous(breaks = 2:10)
```





## CLUSTER ANALYSIS IN R

**Let's practice!**



CLUSTER ANALYSIS IN R

# Making Sense of the K-Means Clusters

Dmitriy (Dima) Gorenshteyn

Sr. Data Scientist,

Memorial Sloan Kettering Cancer Center

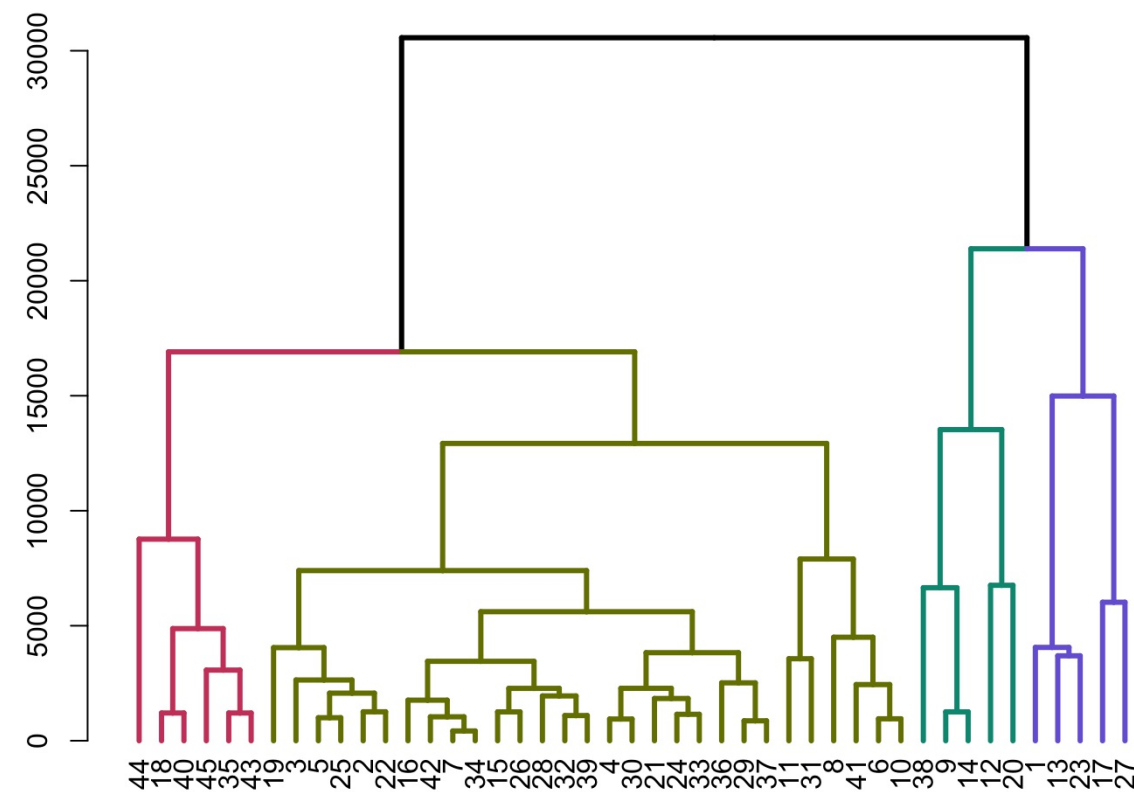


# Wholesale Dataset

- 45 observations
- 3 features:
  - Milk Spending
  - Grocery Spending
  - Frozen Food Spending

```
print(customers_spend)
      Milk Grocery Frozen
1  11103   12469    902
2   2013    6550    909
3   1897    5234    417
4   1304    3643   3045
5   3199    6986   1455
...     ...     ...     ...
```

# Segmenting with Hierarchical Clustering





# Segmenting with Hierarchical Clustering

| cluster | Milk         | Grocery      | Frozen       | cluster size |
|---------|--------------|--------------|--------------|--------------|
| 1       | <b>16950</b> | 12891        | 991          | 5            |
| 2       | 2512         | 5228         | 1795         | 29           |
| 3       | 10452        | <b>22550</b> | 1354         | 5            |
| 4       | 1249         | 3916         | <b>10888</b> | 6            |



# Segmenting with K-means

- Estimate the "best"  $k$  using average silhouette width
- Run k-means with the suggested  $k$
- Characterize the spending habits of these clusters of customers



## CLUSTER ANALYSIS IN R

# Let's cluster!