

Correcction

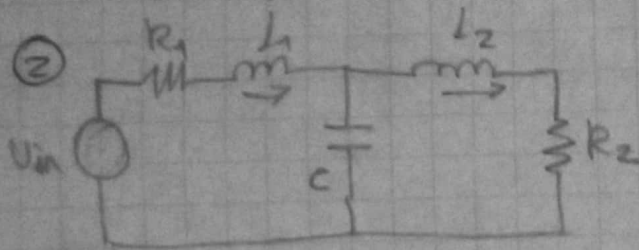
① $\ddot{x} + \dot{x} + 2x + x = 2 f(\omega)$

$$V(\omega) (s^3 + s^2 + 2s + 1) = 2 f(\omega)$$

$$\frac{V(\omega)}{f(\omega)} = \frac{2}{s^3 + s^2 + 2s + 1}$$

$$\dot{x}_3 = 2u - x_3 - 2x_2 - x_1$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -2 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix} u$$



$$i_c = C \frac{dv_c}{dt}, \quad v_c = \int \frac{di_c}{dt}$$

$$i_1 + i_3 + i_2; \quad v_{R2} + v_{L2} = v_c$$

$$v_{R2} = v_c - v_{L2}$$

$$v_c = x_1; \quad \dot{v}_c = \dot{x}_1; \quad i_1 = x_2; \quad \dot{i}_1 = \dot{x}_2$$

$$x_2 = \frac{x_2}{C} - \frac{x_3}{C}$$

$$i_2 = x_3; \quad \dot{i}_2 = \dot{x}_3$$

$$x_1 = v_{in} - R_1 x_2 - L_1 \dot{x}_2$$

$$\dot{x}_2 = \frac{v_{in}}{L_1} - \frac{R_1 x_2}{L_1} - \frac{x_1}{L_1}$$

$$\dot{x}_3 = \frac{x_1}{L_2} - \frac{R_2 x_3}{L_2}$$

$$\dot{x}_1 = \frac{x_2}{C} - \frac{x_3}{C}$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1/C & -1/C \\ 1/L_1 & -R_1/L_1 & 0 \\ 1/L_2 & 0 & -R_2/L_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 1/L_1 \\ 0 \end{bmatrix} v_{in}$$

$$[v_{R2}] = \begin{bmatrix} 0 & 0 & R_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

$$\textcircled{3} \quad M \frac{d^2 y_2}{dt^2} = M \ddot{x}_1 \quad y_2 = x_1 \quad x_1 = q_1; \quad x_2 = q_2; \quad \dot{x}_1 = \dot{q}_1; \quad \dot{x}_2 = \dot{q}_2$$

$$B \frac{dy_2}{dt} = B \dot{x}_1$$

$$K(y_1 - y_2) = K(x_2 - x_1)$$

$$M \ddot{x}_1 + B \dot{x}_1 = K(x_2 - x_1)$$

Punto

$$K(y_1 - y_2) = f(t) \rightarrow K(x_2 - x_1) = f$$

$$Kx_2 - Kx_1 = f \rightarrow x_2 = \frac{f + Kx_1}{K}$$

$$M \ddot{x}_1 + B \dot{x}_1 = K \left(\frac{f + Kx_1}{K} \right) - Kx_1$$

$$M \ddot{x}_1 + B \dot{x}_1 = f + Kx_1 - Kx_1$$

$$\ddot{x}_1 = \frac{Kx_1 - Kx_1 + f + B \dot{x}_1}{M}$$

$$\begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ \frac{K-1}{m} & \frac{B}{m} \end{bmatrix} \begin{bmatrix} q_1 \\ q_2 \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{1}{m} \end{bmatrix} f$$