А3

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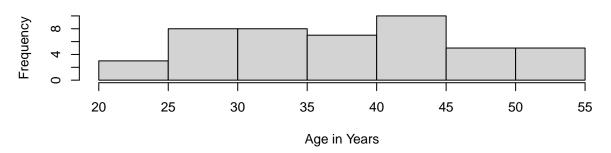
09/03/2021

$\mathbf{Q}\mathbf{1}$

a)

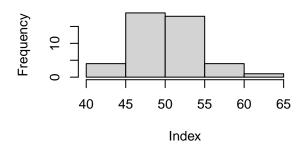
```
Data = read.table("PatientSatisfaction.txt", col.names=c("Satisfaction", "Age", "Severity", "Anxiety")
layout(matrix(c(1,1,2,3), 2, 2, byrow = TRUE))
hist(Data$Age,
 main="Patient Age",
 xlab="Age in Years",
  xlim=c(20,55),
hist(Data$Severity,
 main="Severity of Illness",
 xlab="Index",
  xlim=c(40,65),
hist(Data$Anxiety,
  main="Anxiety Level",
  xlab="Index",
  xlim=c(1.5,3),
  breaks=c(1,1.25,1.5,1.75,2,2.25,2.5,2.75,3)
)
```

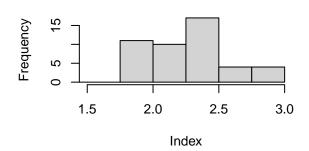
Patient Age



Severity of Illness

Anxiety Level

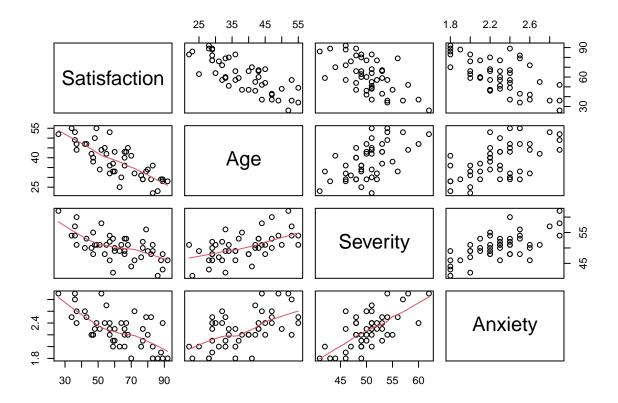




It is noteworthy that it seems all 3 plots are normally distributed.

b)

```
# scatter plot matrix
pairs(~Satisfaction +Age + Severity+ Anxiety, data = Data, lower.panel = panel.smooth)
```



cor(cbind(Data\$Age, Data\$Severity, Data\$Anxiety))

```
## [,1] [,2] [,3]
## [1,] 1.0000000 0.5679505 0.5696775
## [2,] 0.5679505 1.0000000 0.6705287
## [3,] 0.5696775 0.6705287 1.0000000
```

Our scatter plot matrix shows that all 3 predictor value are positively correlated with each other, however, all 3 are negatively correlated with patient satisfaction.

Since none of the correlations between the predictor variables exceed 0.7, the correlations are not extreme enough to raise any concerns of multicollinearity.

c)

```
fit = lm(Satisfaction ~ Age + Severity + Anxiety, data = Data)
summary(fit)

##
## Call:
## lm(formula = Satisfaction ~ Age + Severity + Anxiety, data = Data)
##
## Residuals:
```

```
##
                      Median
                                   3Q
                 1Q
## -18.3524 -6.4230
                      0.5196
                               8.3715 17.1601
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 158.4913
                          18.1259
                                    8.744 5.26e-11 ***
                           0.2148 -5.315 3.81e-06 ***
## Age
               -1.1416
## Severity
               -0.4420
                           0.4920
                                   -0.898
                                            0.3741
## Anxiety
              -13.4702
                           7.0997 -1.897
                                            0.0647 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 10.06 on 42 degrees of freedom
## Multiple R-squared: 0.6822, Adjusted R-squared: 0.6595
## F-statistic: 30.05 on 3 and 42 DF, p-value: 1.542e-10
```

The estimated regression function is

$$Y = 158.4912517 + -1.1416118 \cdot X_1 + -0.4420043 \cdot X_2 + -13.4701632 \cdot X_3$$

 $\hat{\beta}_2$ is interpreted as, controlling for X_1 and X_3 , a 1-unit increase in X_2 corresponds to a predicted increase of -1.1416118 in patient satisfaction.

 \mathbf{d})

Fstat

$$H_0: \hat{\beta}_1 = \hat{\beta}_2 = \hat{\beta}_3 = 0, \quad H_a: \hat{\beta}_1 \neq 0 \lor \hat{\beta}_2 \neq 0 \lor \hat{\beta}_3 \neq 0$$

Decision rule: reject if

P Value =
$$pf(F, 3, n - p') < \alpha$$

then we reject H_0

```
alpha = 0.10
anova = anova(fit)
anova
## Analysis of Variance Table
## Response: Satisfaction
            Df Sum Sq Mean Sq F value
##
                                         Pr(>F)
## Age
              1 8275.4 8275.4 81.8026 2.059e-11 ***
             1 480.9
                        480.9 4.7539
                                        0.03489 *
## Severity
## Anxiety
             1 364.2
                         364.2 3.5997
                                        0.06468 .
## Residuals 42 4248.8
                        101.2
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
SSR = sum(anova[2][1:3,1])
MSE = anova[3][4,1]
Fstat = SSR/MSE/3
```

Fstatistic = 30.0520779

```
Pval = pf(Fstat,4-1, anova[1][4,1],lower.tail=F)
Pval
```

[1] 1.541973e-10

Since the P value of $1.5419726 \times 10^{-10}$ is less than the level of significance of $\alpha = 0.1$ we can reject H_0 My test implies that we are 90% confident that $\beta_1, \beta_2, \beta_3$ are not all 0.

e)

```
SSE = anova[2][4,1]
SST = (SSR + SSE)
SSE

## [1] 4248.841

R = SSR/SST
R

## [1] 0.6821943

Radj = 1 - ((anova[1][4,1]+4-1)/anova[1][4,1])*(SSE/SST)
Radj
```

[1] 0.6594939

1 69.01029 51.50965 86.51092

The R^2 value of 0.6821943 means that $100 \cdot (0.6821943)\%$ of the data fit the regression model. Furthermore, since the adjusted R^2 value is close to R^2 , we can say most prediction variables are having an effect on predictions.

f)

```
#fit
pred = predict(fit, data.frame(Age = 35, Severity = 45, Anxiety = 2.2 ) , interval="prediction", level
pred
## fit lwr upr
```

I am 90% confident that a future patient with age 35, severity of illness 45, and anxiety level 2.2 will have a patient satisfaction within the range

[51.5096525, 86.51092]

a)

```
Data = read.table("egyptcttn.txt", col.names=c("Variety", "Luminance", "lnGrade"))
D1 = as.numeric(Data$Variety=="Giza67")
D2 = as.numeric(Data$Variety=="Giza68")
D3 = as.numeric(Data$Variety=="Giza69")
D4 = as.numeric(Data$Variety=="Giza70")
# base = Menoufi
fullFit = lm(Luminance ~ lnGrade*D1 + lnGrade*D2 + lnGrade*D3 + lnGrade*D4, data = Data)
summary(fullFit)
##
## Call:
## lm(formula = Luminance ~ lnGrade * D1 + lnGrade * D2 + lnGrade *
                     D3 + lnGrade * D4, data = Data)
##
##
## Residuals:
                        Min
                                                        1Q
                                                                      Median
                                                                                                                3Q
                                                                                                                                         Max
         -0.66004 -0.05597 -0.00598 0.10859
##
                                                                                                                            0.32705
##
## Coefficients:
##
                                              Estimate Std. Error t value Pr(>|t|)
                                                                                       1.3976 56.386 7.47e-14 ***
## (Intercept) 78.8034
## lnGrade
                                                    3.3137
                                                                                       0.4243
                                                                                                                  7.810 1.45e-05 ***
## D1
                                                    2.0524
                                                                                      1.9765
                                                                                                                   1.038 0.32352
## D2
                                                    5.0801
                                                                                       1.9765
                                                                                                                   2.570 0.02788 *
## D3
                                                    7.2233
                                                                                       1.9765
                                                                                                                   3.655 0.00443 **
## D4
                                                    5.1151
                                                                                      1.9765
                                                                                                                  2.588 0.02704 *
## lnGrade:D1
                                                 -1.1507
                                                                                      0.6000
                                                                                                                -1.918 0.08411 .
                                                 -1.0797
                                                                                      0.6000
## lnGrade:D2
                                                                                                                -1.800
                                                                                                                                      0.10212
## lnGrade:D3
                                                 -2.2741
                                                                                       0.6000
                                                                                                                -3.790 0.00354 **
## lnGrade:D4
                                                 -2.0709
                                                                                       0.6000 -3.452 0.00621 **
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.2907 on 10 degrees of freedom
## Multiple R-squared: 0.9794, Adjusted R-squared: 0.9609
## F-statistic: 52.82 on 9 and 10 DF, p-value: 2.986e-07
Full Model:
                                 Y_i = \beta_0 + \beta_1 \cdot lnGrade + \beta_2 D1 + \beta_3 D2 + \beta_4 D3 + \beta_5 D4 + 
                                             \beta_6 \cdot lnGrade \cdot D1 + \beta_7 \cdot lnGrade \cdot D2 + \beta_8 \cdot lnGrade \cdot D3 + \beta_9 \cdot lnGrade \cdot D4
b)
                                                                                                        H_0: \beta_6 = \beta_7 = \beta_8 = \beta_9 = 0
```

 H_a : One of $\beta_6, \beta_7, \beta_8, \beta_9$ is not 0

```
reducedFitB = lm(Luminance ~ lnGrade + D1 + D2 + D3 + D4, data = Data)
anova = anova(reducedFitB, fullFit)
anova
## Analysis of Variance Table
## Model 1: Luminance ~ lnGrade + D1 + D2 + D3 + D4
## Model 2: Luminance ~ lnGrade * D1 + lnGrade * D2 + lnGrade * D3 + lnGrade *
       D4
     Res.Df
                 RSS Df Sum of Sq
                                       F Pr(>F)
## 1
          14 2.39566
         10 0.84501 4 1.5507 4.5876 0.02313 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Pval = anova$`Pr(>F)`[2]
Pval
## [1] 0.02313061
since
                                  P value = 0.0231306 < \alpha = 0.05
we reject H_0.
c)
                          H_0: \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = \beta_7 = \beta_8 = \beta_9 = 0
                            H_a: One of \beta_2, \beta_3, \beta_4, \beta_5, \beta_6, \beta_7, \beta_8, \beta_9 is not 0
reducedFitC = lm(Luminance ~ lnGrade, data = Data)
anova = anova(reducedFitC, reducedFitB)
anova
## Analysis of Variance Table
## Model 1: Luminance ~ lnGrade
## Model 2: Luminance ~ lnGrade + D1 + D2 + D3 + D4
   Res.Df
                RSS Df Sum of Sq
                                    F
## 1
          18 31.639
## 2
         14 2.396 4
                         29.243 42.723 1.066e-07 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Pval = anova$`Pr(>F)`[2]
Pval
## [1] 1.066057e-07
since
                               P value = 1.0660575 \times 10^{-7} < \alpha = 0.05
we reject H_0.
```

d)

The model I would choose for this data is the full model, with all dummy variables and interactions. This is because we rejected that the interactions have no effect on slope, so we know the interactions have some significant effects on the model. So we want to use the full model to capture that.

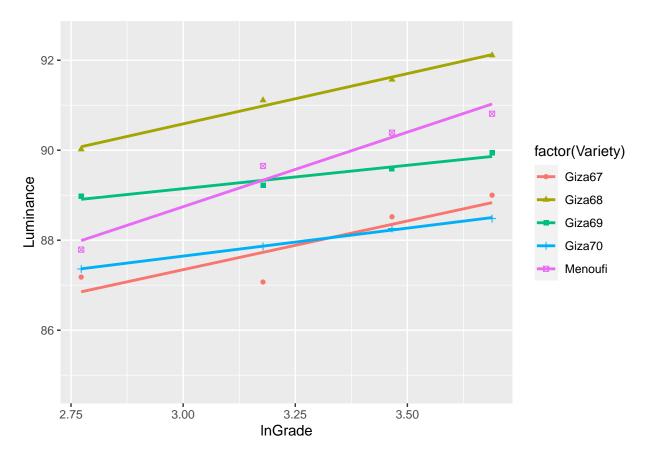
e)

```
if(!require("ggplot2")) install.packages("ggplot2")
## Loading required package: ggplot2
```

Warning: package 'ggplot2' was built under R version 4.0.4

```
library(ggplot2)
ggplot(data=Data, aes(x=lnGrade, y=Luminance, color= factor(Variety), shape=factor(Variety))) + geom_po
```

'geom_smooth()' using formula 'y ~ x'



Normality:

p = shapiro.test(fullFit\$residuals)\$p.value

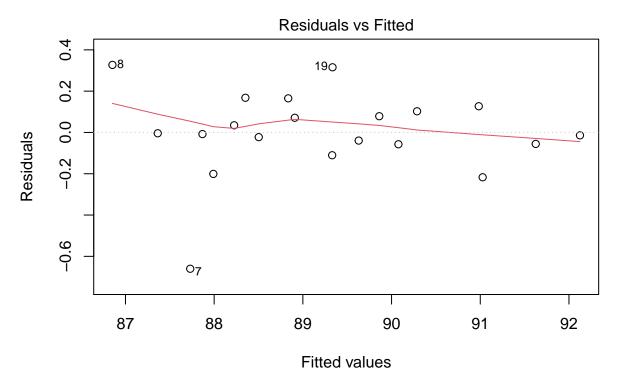
since

P value =
$$0.0190846 < \alpha = 0.05$$

we reject that this fit satisfies the normality assumption.

Equal Variance:

```
plot(fullFit, which=1)
```



Im(Luminance ~ InGrade * D1 + InGrade * D2 + InGrade * D3 + InGrade * D4)

Visually, aside from 1 outlier at (87.7, -0.66), the residuals are uniformly distributed, and Equal Variance holds.

 ${\bf Linearity}:$

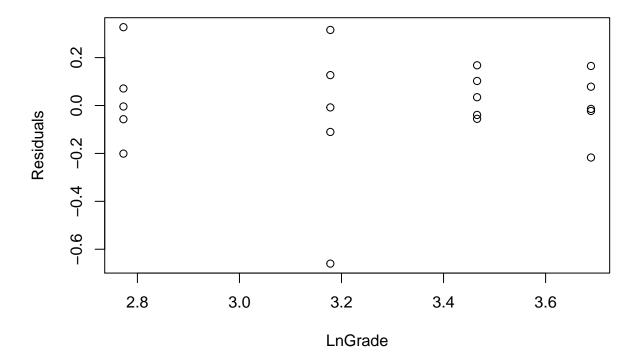
summary(fullFit)

```
##
## Call:
## lm(formula = Luminance ~ lnGrade * D1 + lnGrade * D2 + lnGrade *
## D3 + lnGrade * D4, data = Data)
##
## Residuals:
## Min 1Q Median 3Q Max
## -0.66004 -0.05597 -0.00598 0.10859 0.32705
```

```
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                           1.3976 56.386 7.47e-14 ***
## (Intercept) 78.8034
## lnGrade
                3.3137
                           0.4243
                                    7.810 1.45e-05 ***
## D1
                2.0524
                           1.9765
                                    1.038 0.32352
## D2
                5.0801
                           1.9765
                                    2.570 0.02788 *
## D3
                7.2233
                           1.9765
                                    3.655 0.00443 **
## D4
                5.1151
                           1.9765
                                    2.588 0.02704 *
## lnGrade:D1
              -1.1507
                           0.6000 -1.918 0.08411 .
## lnGrade:D2
              -1.0797
                           0.6000 -1.800 0.10212
                                   -3.790 0.00354 **
## lnGrade:D3
               -2.2741
                           0.6000
               -2.0709
                           0.6000 -3.452 0.00621 **
## lnGrade:D4
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2907 on 10 degrees of freedom
## Multiple R-squared: 0.9794, Adjusted R-squared: 0.9609
## F-statistic: 52.82 on 9 and 10 DF, p-value: 2.986e-07
```

As we can see from the P values, we reject that any of the 5 slopes are 0. Also, from the graph we can confidently see that there is a linear relationship between luminance and lnGrade for all 5 categories. from these 2 observations, we can say our model satisfies linearity.

Independent/uncorrelated error terms:



From this plot, I visually access that there is no major deviate patterns, therefor Independent/uncorrelated error terms is satisfied.

Question 5.

```
WoolStrengthData <- read.table("StrengthWool.txt", header = TRUE)</pre>
```

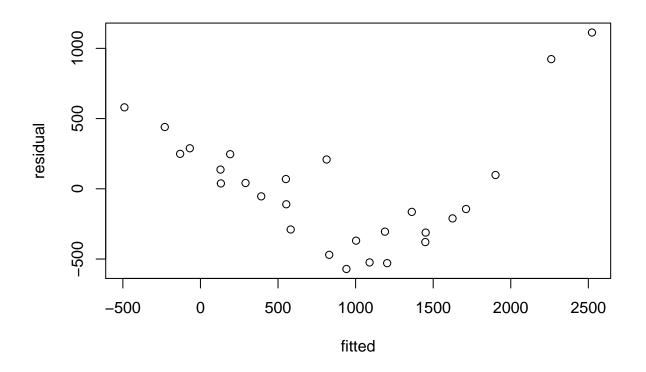
Part a.

Fit a linear model with just main effects for the three class variables and show that this is not a good fit to the data

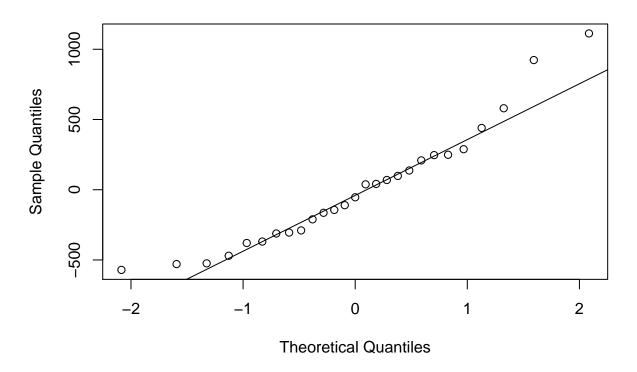
```
Cycles = WoolStrengthData$Cycles
lenCut <- cut(WoolStrengthData$Len, breaks=c(0,250, 300, 350), labels = c("250", "300", "350"))
ampCut <- cut(WoolStrengthData$Amp, breaks=c(0,8,9,10), labels = c("8", "9", "10"))
loadCut <- cut(WoolStrengthData$Load, breaks=c(0,40,45,50), labels=c("40", "45", "50"))
fit <- lm(Cycles ~ lenCut + ampCut + loadCut, data = WoolStrengthData)
summary(fit)
```

```
##
## Call:
## lm(formula = Cycles ~ lenCut + ampCut + loadCut, data = WoolStrengthData)
```

```
##
## Residuals:
##
       Min
                1Q Median
  -570.81 -308.43 -53.81 227.57 1112.63
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                              246.0
                                      4.891 8.83e-05 ***
## (Intercept)
                 1203.4
## lenCut300
                  421.4
                              227.8
                                      1.850 0.079096 .
## lenCut350
                 1320.0
                              227.8
                                      5.795 1.14e-05 ***
## ampCut9
                 -811.6
                              227.8
                                    -3.563 0.001948 **
## ampCut10
                -1071.7
                                    -4.705 0.000136 ***
                              227.8
## loadCut45
                 -262.6
                              227.8 -1.153 0.262611
                              227.8 -2.729 0.012918 *
## loadCut50
                 -621.7
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 483.2 on 20 degrees of freedom
## Multiple R-squared: 0.7692, Adjusted R-squared: 0.6999
## F-statistic: 11.11 on 6 and 20 DF, p-value: 1.769e-05
residual <- fit$residuals</pre>
fitted <- fit$fitted.values</pre>
plot(x=fitted, y=residual)
```



```
qqnorm(residual)
qqline(residual)
```



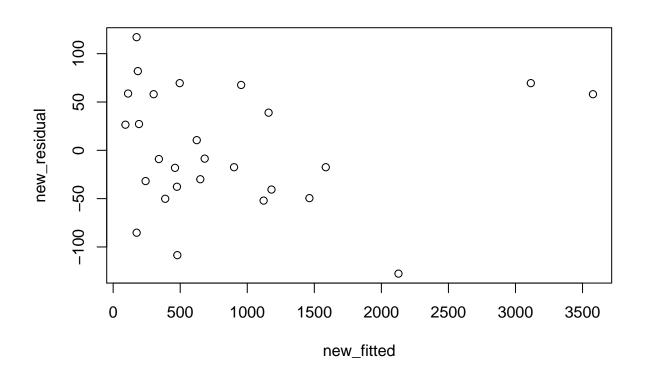
If we look at the plot of the Residual Plot as well as the QQ Plot of the model, we can see that this model is not a good fit to the data, where the QQ Plot shows many points not following the linear line, as well as the curved shape in the residual plot not showing signs of a good fit.

#5.b)

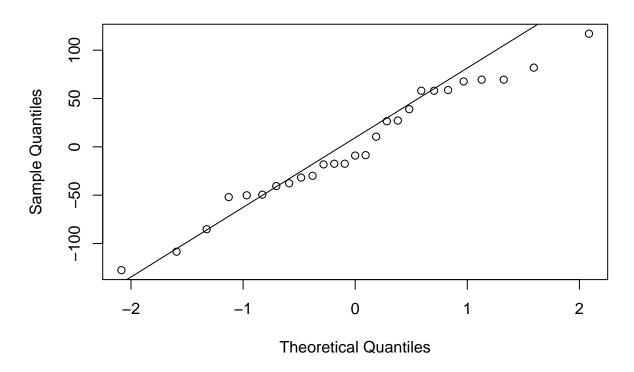
```
new_fit <- lm(Cycles ~ ampCut + lenCut + loadCut + ampCut*lenCut + ampCut*loadCut + lenCut*loadCut, dat
summary(new_fit)</pre>
```

```
##
## Call:
## lm(formula = Cycles ~ ampCut + lenCut + loadCut + ampCut * lenCut +
       ampCut * loadCut + lenCut * loadCut, data = WoolStrengthData)
##
##
##
  Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
  -127.593
            -39.148
                       -9.037
                                58.074
                                        117.074
##
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        6.826e+02 9.237e+01
                                                7.390 7.69e-05 ***
## ampCut9
                       -2.944e+02 1.161e+02 -2.537 0.034879 *
## ampCut10
                       -5.713e+02 1.161e+02 -4.923 0.001160 **
```

```
## lenCut300
                        7.809e+02
                                  1.161e+02
                                                6.728 0.000148 ***
                        2.895e+03
                                   1.161e+02
## lenCut350
                                              24.946 7.13e-09 ***
## loadCut45
                       -2.041e+02
                                   1.161e+02
                                              -1.759 0.116697
## loadCut50
                                               -4.374 0.002368 **
                       -5.077e+02
                                   1.161e+02
  ampCut9:lenCut300
                       -2.147e+02
                                   1.271e+02
                                              -1.688 0.129813
  ampCut10:lenCut300
                       -4.310e+02
                                              -3.390 0.009502 **
                                   1.271e+02
                                   1.271e+02 -13.355 9.45e-07 ***
  ampCut9:lenCut350
                       -1.698e+03
## ampCut10:lenCut350
                                   1.271e+02 -14.362 5.40e-07 ***
                       -1.826e+03
   ampCut9:loadCut45
                        1.255e-12
                                   1.271e+02
                                                0.000 1.000000
  ampCut10:loadCut45
                        1.843e+02
                                   1.271e+02
                                                1.450 0.185155
## ampCut9:loadCut50
                        3.613e+02
                                   1.271e+02
                                               2.842 0.021747 *
## ampCut10:loadCut50
                        5.717e+02
                                   1.271e+02
                                                4.496 0.002012 **
## lenCut300:loadCut45 -1.003e+02
                                   1.271e+02
                                              -0.789 0.452782
## lenCut350:loadCut45 -2.593e+02
                                              -2.040 0.075709 .
                                   1.271e+02
## lenCut300:loadCut50 -3.323e+02
                                   1.271e+02
                                              -2.614 0.030944 *
## lenCut350:loadCut50 -9.427e+02
                                  1.271e+02
                                              -7.414 7.52e-05 ***
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 110.1 on 8 degrees of freedom
## Multiple R-squared: 0.9952, Adjusted R-squared: 0.9844
## F-statistic: 92.25 on 18 and 8 DF, p-value: 2.537e-07
new_residual <- new_fit$residuals</pre>
new_fitted <- new_fit$fitted.values</pre>
plot(x=new_fitted, y=new_residual)
```



```
qqnorm(new_residual)
qqline(new_residual)
```

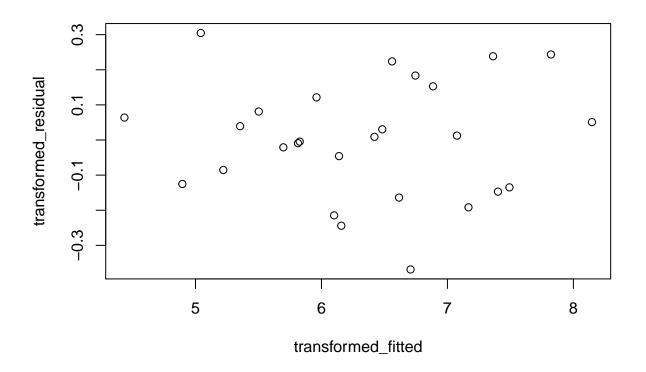


If we look at the new residual plot of the new model, we can see that this model is a better fit to the data, as we can see that the variance is linear around 0 but does not have constant variance. Hence, the model which considers all the interactions between pairs of the class variables is a better model for fitting the data.

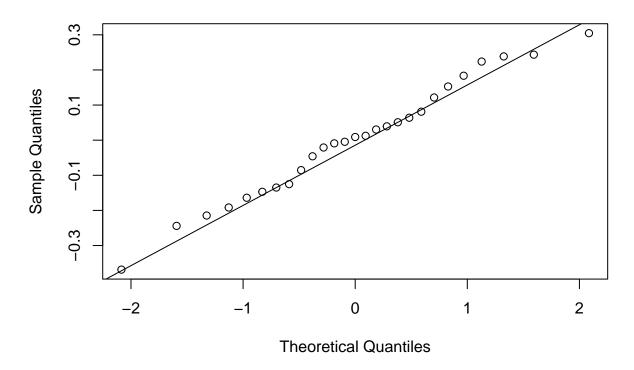
Part c.

```
transformed_fit <- lm(log(Cycles)~(lenCut + ampCut + loadCut))
summary(transformed_fit)</pre>
```

```
## lenCut300
                0.91833
                           0.08928 10.286 1.97e-09 ***
## lenCut350
                1.66477
                           0.08928
                                    18.646 4.10e-14 ***
## ampCut9
               -0.65521
                           0.08928
                                    -7.339 4.31e-07 ***
## ampCut10
               -1.26173
                           0.08928 -14.132 7.19e-12 ***
## loadCut45
               -0.32529
                           0.08928
                                    -3.643 0.00162 **
## loadCut50
               -0.78524
                           0.08928
                                    -8.795 2.62e-08 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.1894 on 20 degrees of freedom
## Multiple R-squared: 0.9691, Adjusted R-squared: 0.9598
## F-statistic: 104.5 on 6 and 20 DF, p-value: 4.979e-14
transformed_residual <- transformed_fit$residuals</pre>
transformed_fitted <- transformed_fit$fitted.values</pre>
plot(x=transformed_fitted, y=transformed_residual)
```



```
qqnorm(transformed_residual)
qqline(transformed_residual)
```



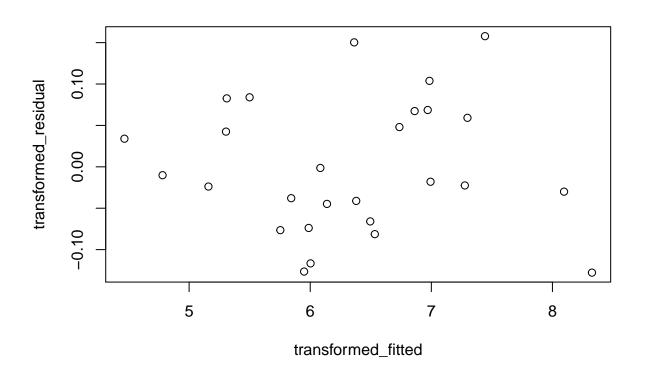
After performing the log transformation on the model, we can see that the variance is constant and linear around 0. The high R/Radj values also show that almost all of the variance can be explained by the model. This is a better fit for the model.

Part d.

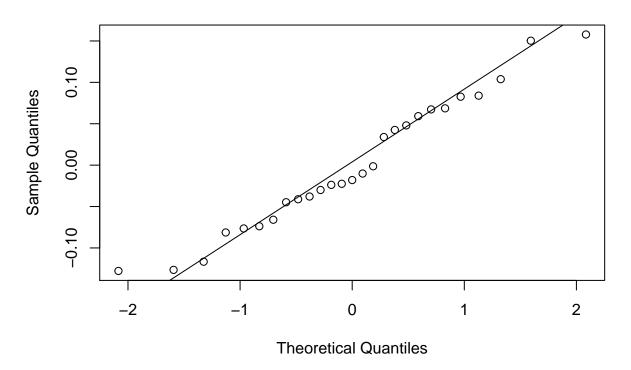
```
transformed_fit2 <- lm(log(Cycles)~(ampCut + lenCut + loadCut + ampCut*lenCut + ampCut*loadCut + lenCut
summary(transformed_fit2)</pre>
```

```
##
## Call:
## lm(formula = log(Cycles) ~ (ampCut + lenCut + loadCut + ampCut *
       lenCut + ampCut * loadCut + lenCut * loadCut))
##
##
##
  Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
  -0.12779 -0.05537 -0.01802 0.06325
                                         0.15780
##
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                    0.120807
                                             52.670 1.87e-11 ***
                        6.362917
## ampCut9
                       -0.413379
                                    0.151801
                                             -2.723 0.026121 *
## ampCut10
                                    0.151801 -7.927 4.67e-05 ***
                       -1.203298
```

```
## lenCut300
                        0.913780
                                   0.151801
                                               6.020 0.000316 ***
## lenCut350
                                   0.151801 12.935 1.21e-06 ***
                        1.963516
## loadCut45
                       -0.375588
                                   0.151801
                                             -2.474 0.038457 *
## loadCut50
                       -0.609676
                                   0.151801
                                             -4.016 0.003861 **
  ampCut9:lenCut300
                       -0.001114
                                   0.166290
                                             -0.007 0.994817
  ampCut10:lenCut300
                                   0.166290
                                               0.391 0.706242
                        0.064964
                                             -3.696 0.006074 **
  ampCut9:lenCut350
                       -0.614678
                                   0.166290
  ampCut10:lenCut350
                       -0.152966
                                   0.166290
                                             -0.920 0.384537
   ampCut9:loadCut45
                       -0.074416
                                   0.166290
                                             -0.448 0.666379
  ampCut10:loadCut45
                       -0.003211
                                   0.166290
                                             -0.019 0.985067
  ampCut9:loadCut50
                       -0.035285
                                   0.166290
                                             -0.212 0.837264
  ampCut10:loadCut50
                       -0.084089
                                   0.166290
                                             -0.506 0.626717
  lenCut300:loadCut45 0.083463
                                   0.166290
                                               0.502 0.629248
## lenCut350:loadCut45
                                   0.166290
                                               0.872 0.408448
                        0.145059
## lenCut300:loadCut50 -0.133655
                                   0.166290
                                             -0.804 0.444766
  lenCut350:loadCut50 -0.273658
                                   0.166290
                                             -1.646 0.138450
##
                  0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Signif. codes:
## Residual standard error: 0.144 on 8 degrees of freedom
## Multiple R-squared: 0.9928, Adjusted R-squared: 0.9768
## F-statistic: 61.71 on 18 and 8 DF, p-value: 1.236e-06
transformed_residual <- transformed_fit2$residuals</pre>
transformed_fitted <- transformed_fit2$fitted.values</pre>
plot(x=transformed_fitted, y=transformed_residual)
```



```
qqnorm(transformed_residual)
qqline(transformed_residual)
```



anova(transformed_fit, transformed_fit2)

```
## Analysis of Variance Table
##
## Model 1: log(Cycles) ~ (lenCut + ampCut + loadCut)
## Model 2: log(Cycles) ~ (ampCut + lenCut + loadCut + ampCut * lenCut +
## ampCut * loadCut + lenCut * loadCut)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 20 0.71742
## 2 8 0.16591 12 0.55151 2.216 0.1325
```

We can see that the result of this is very similar to that of part c. However, it is not a significant change in terms of deciding a better fit, and we can use F-test. Since the p-value of F-test is 0.1325 > 0.05, With 95% confidence we cannot reject H0 as there is evidence that the interaction terms have no effect on the model with transformations