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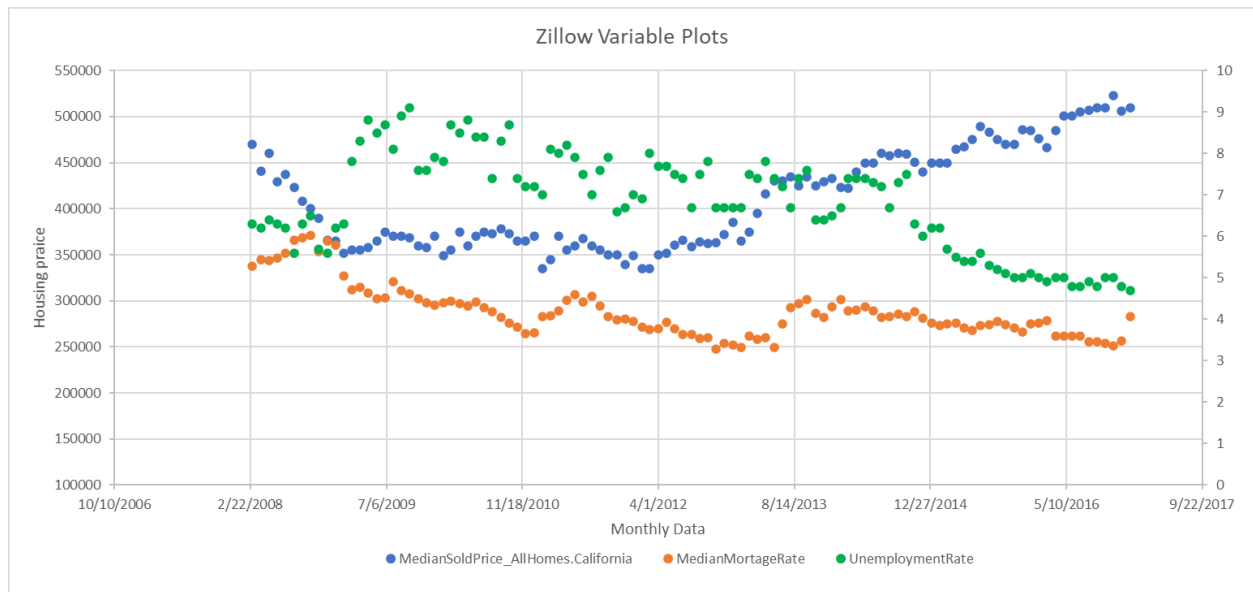
Zillow Housing Price Prediction Jan -Dec 2016

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Introduction:

Using a combination of monthly historical data of California median housing prices, median mortgage rate, and unemployment rate from Feb 2008 to Dec 2015, we attempted to predict the future housing market for 2016. We utilized three different time series models (FBPROPHET, ETS, and SARIMAX) to calculate this data. Our approach was to exhaustively try all possible variable combinations presented to use and choose the best of the models selected from the RMSE cross-validation score.

The Data



Target:

Median Sold Price All Homes California

Additional Variables:

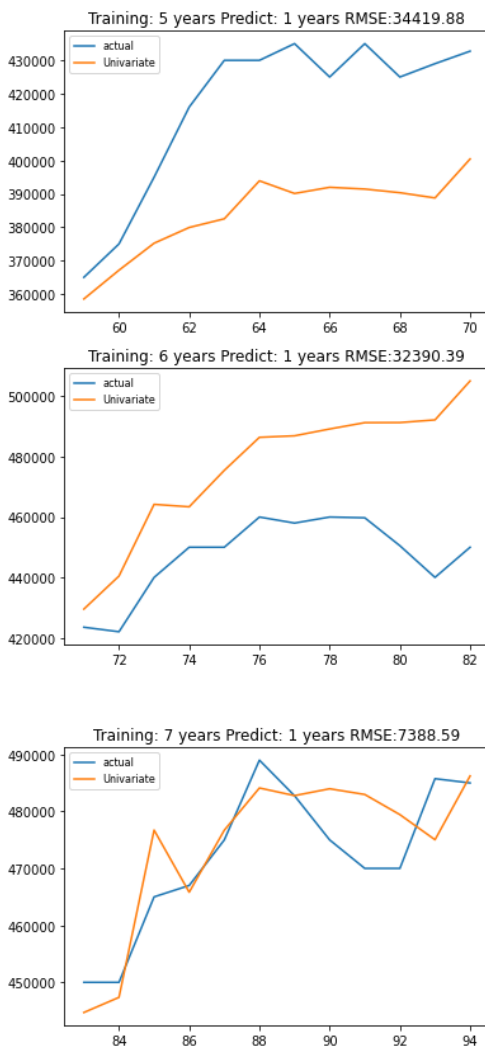
Median Mortgage Rate

Unemployment Rate

FB Time series model testing

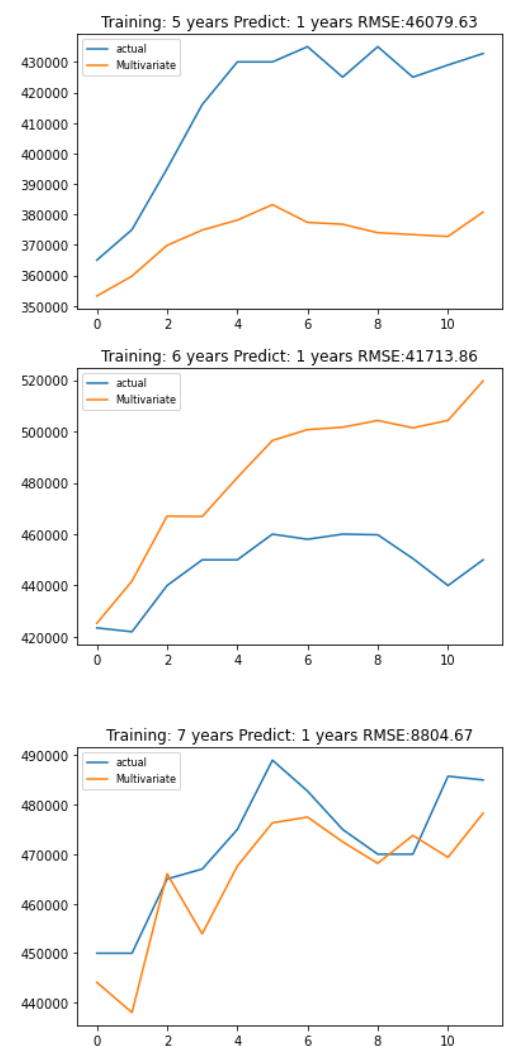
In this section, we attempted to fit the data using the FB prophet model, a time series forecasting procedure made by Facebook. We tried both the Univariate and Multivariable monthly Prophet models in our implementation. To see the effectiveness of these models, we cross-validated them below by training for five years, then predicting a window of 1 year and rolling that year. For cross-validation, it seemed as if each model drastically improved with the last two testing years for both Univariate and Multivariate Models

Univariate Cross-Validation



Mean RMSE: \$24,732

Multivariate Cross-Validation



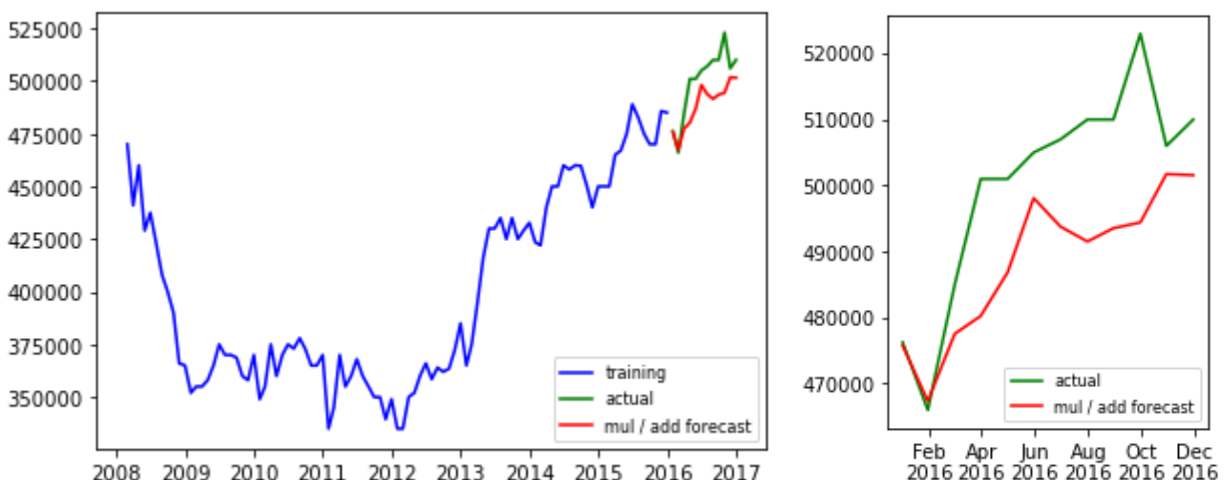
Mean RMSE: \$32,199

ETS Time series model testing

Next, we attempted to fit the data using Holt-Winters triple exponential smoothing models. We compared four different models, each fit with the trend and seasonality parameters set to all possible combinations of 'additive' and 'multiplicative'. Frequency was kept at the default monthly value, with seasonal periods set to 12 months and the damped trend parameter left on True for all models.

frequency	seasonal period	damped trend	trend	seasonality	model avg c-v RMSE
Monthly	12 months	True	ADDitive	ADDitive	46915
Monthly	12 months	True	ADDitive	MULTiplicative	40154
Monthly	12 months	True	MULTiplicative	ADDitive	29876
Monthly	12 months	True	MULTiplicative	MULTiplicative	32672

The ETS model achieved the best RMSE value of \$29,876 during cross-validation using the 'multiplicative' trend and 'additive' seasonality. After re-fitting an ETS model with the same parameters on the entire training dataset and using it to make forecasts for the 12 months of the test data (2016), the results had an RMSE score of \$11,205 on the test period.



SARIMAX Time series model testing

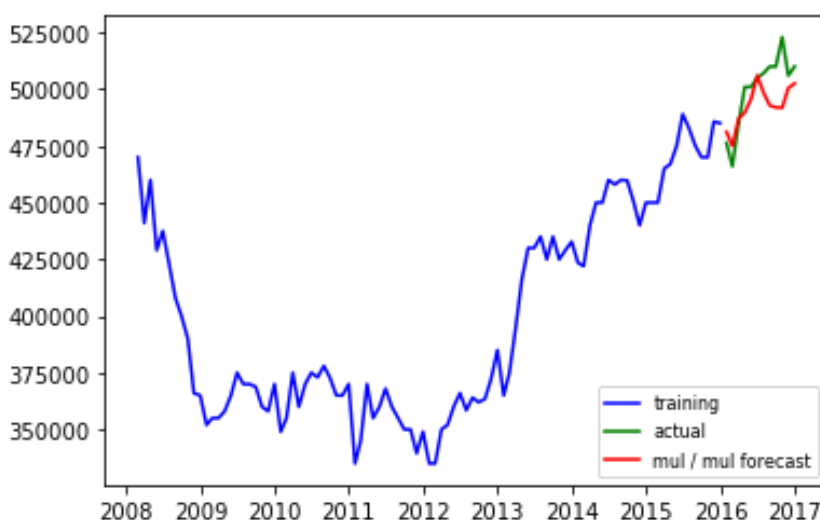
Finally, we fitted the Autoregressive Integrated Moving Average Model (ARIMA), the most widely used forecasting method in timer series data forecasting. From the time series plot we generated below, we can see an obvious seasonality existing in the data (one year as a period), which also corresponds to reality.

After an ADF test and seasonal differencing, we decided on the trend parameter $d = 1$ and seasonal parameter $D = 1$. Next, we performed the grid search to obtain other parameters. The two candidates we got from the SARIMA family are:
SARIMA(1,1,0)(0,1,0,12) for univariate model and SARIMAX(1,0,0)(0,1,3,12) for multivariate model.

Then we performed both one-step cross-validation and twelve-step cross-validation to see the cross-validation RMSE score and decide the best one in the SARIMA family. And the scores are:

	1 step	12 step
SARIMA(1,1,0)(0,1,0,12)	10032	20607
SARIMAX(1,0,0)(0,1,3,12)	25242	37299

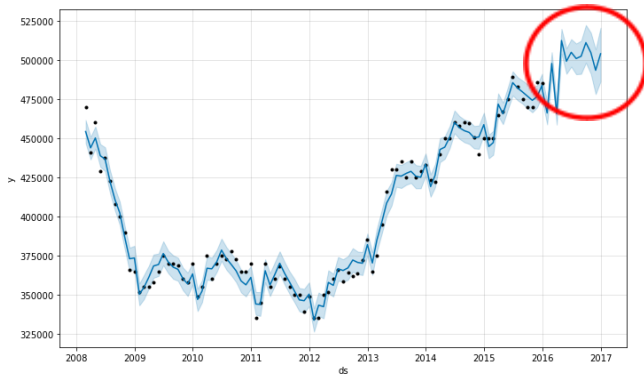
And the prediction result of the SARIMA is as the graph shows below.



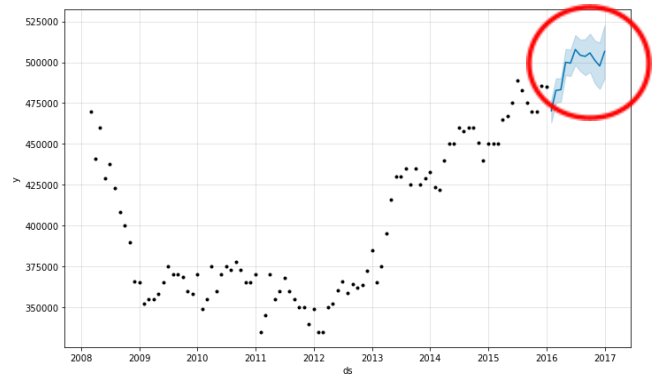
Test score(RMSE) is:
12944

Final Model Selection-Mulivariate FBProphet

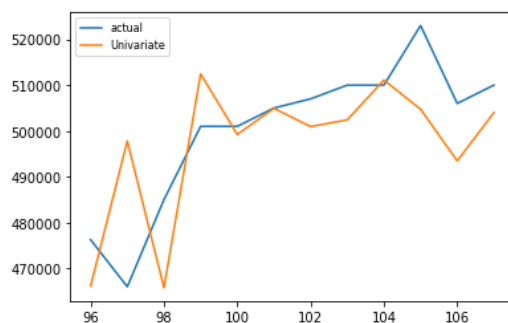
Univariate Model Forecast



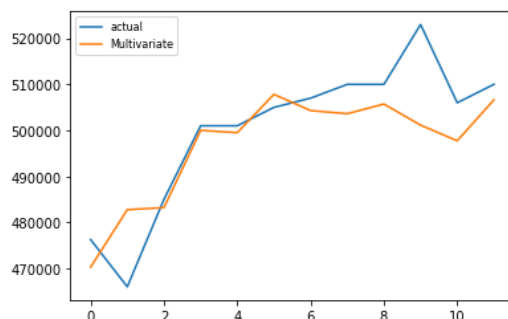
Multivariate Test Forecast



With the similar cross-validation error scores and the significant drop in RMSE with both models, it was a simple procedure to run both Univariate and Multivariate FBprophet on the test data to determine the final model. The **Multivariate FB prophet utilizing both the Unemployment and MedianMortgageRate within the model** yielded the best RMSE results. From this model, we can guess the median house price with only a small margin of error.



This univariate fit was a little noisy initially but ended with an **RMSE of \$13,663**. This means that our average error prediction on each house is around \$13663, which is a pretty good estimate compared to the average housing price.



The Multivariate fit was more accurate, but I worked with aligning the dates to the Fb-Prophets model standard. With this method, the **RMSE was \$7720**. This was the best estimate by far.