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1 Note that the points are:
2 pts = [(2, 3), (5, 2), (12, 15), (23, 10), (17, 13), (0, 3), (4, 2), (18, 21)]
3
4 Initial Distance Matrix
5
6      [1]      [2]      [3]      [4]      [5]      [6]      [7]      [8]
7      [1]      0.0000      3.1623      15.6205      22.1359      18.0278      2.0000      2.2361      24.0832
8      [2]      3.1623      0.0000      14.7648      19.6977      16.2788      5.0990      1.0000      23.0217
9      [3]      15.6205      14.7648      0.0000      12.0830      5.3852      16.9706      15.2643      8.4853
10     [4]      22.1359      19.6977      12.0830      0.0000      6.7082      24.0416      20.6155      12.0830
11     [5]      18.0278      16.2788      5.3852      6.7082      0.0000      19.7231      17.0294      8.0623
12     [6]      2.0000      5.0990      16.9706      24.0416      19.7231      0.0000      4.1231      25.4558
13     [7]      2.2361      1.0000      15.2643      20.6155      17.0294      4.1231      0.0000      23.6008
14     [8]      24.0832      23.0217      8.4853      12.0830      8.0623      25.4558      23.6008      0.0000
15 The minimum distance is 1.0000 between clusters [2] and [7].
16 The centroid of the merged cluster [2, 7] is [4.5, 2.0], calculated from (1*(5, 2) + 1*(4, 2))/2.
17
18      [1]      [3]      [4]      [5]      [6]      [8]      [2, 7]
19      [1]      0.0000      15.6205      22.1359      18.0278      2.0000      24.0832      2.6926
20      [3]      15.6205      0.0000      12.0830      5.3852      16.9706      8.4853      15.0083
21      [4]      22.1359      12.0830      0.0000      6.7082      24.0416      12.0830      20.1556
22      [5]      18.0278      5.3852      6.7082      0.0000      19.7231      8.0623      16.6508
23      [6]      2.0000      16.9706      24.0416      19.7231      0.0000      25.4558      4.6098
24      [8]      24.0832      8.4853      12.0830      8.0623      25.4558      0.0000      23.3077
25      [2, 7]      2.6926      15.0083      20.1556      16.6508      4.6098      23.3077      0.0000
26 The minimum distance is 2.0000 between clusters [1] and [6].
27 The centroid of the merged cluster [1, 6] is [1.0, 3.0], calculated from (1*(2, 3) + 1*(0, 3))/2.
28
29      [3]      [4]      [5]      [8]      [2, 7]      [1, 6]
30      [3]      0.0000      12.0830      5.3852      8.4853      15.0083      16.2788
31      [4]      12.0830      0.0000      6.7082      12.0830      20.1556      23.0868
32      [5]      5.3852      6.7082      0.0000      8.0623      16.6508      18.8680
33      [8]      8.4853      12.0830      8.0623      0.0000      23.3077      24.7588
34      [2, 7]      15.0083      20.1556      16.6508      23.3077      0.0000      3.6401
35      [1, 6]      16.2788      23.0868      18.8680      24.7588      3.6401      0.0000
36 The minimum distance is 3.6401 between clusters [2, 7] and [1, 6].
37 The centroid of the merged cluster [2, 7, 1, 6] is [2.75, 2.5], calculated from (2*[4.5, 2.0] + 2*[1.0, 3.0])/4.
38
39      [3]      [4]      [5]      [8] [2, 7, 1, 6]
40      [3]      0.0000      12.0830      5.3852      8.4853      15.5503
41      [4]      12.0830      0.0000      6.7082      12.0830      21.5943
42      [5]      5.3852      6.7082      0.0000      8.0623      17.7006
43      [8]      8.4853      12.0830      8.0623      0.0000      23.9752
44      [2, 7, 1, 6]      15.5503      21.5943      17.7006      23.9752      0.0000
45 The minimum distance is 5.3852 between clusters [3] and [5].
46 The centroid of the merged cluster [3, 5] is [14.5, 14.0], calculated from (1*(12, 15) + 1*(17, 13))/2.
47
48      [4]      [8] [2, 7, 1, 6]      [3, 5]
49      [4]      0.0000      12.0830      21.5943      9.3941
50      [8]      12.0830      0.0000      23.9752      7.8262
51      [2, 7, 1, 6]      21.5943      23.9752      0.0000      16.4412
52      [3, 5]      9.3941      7.8262      16.4412      0.0000

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48 The minimum distance is 7.8262 between clusters [8] and [3, 5].
49 The centroid of the merged cluster [8, 3, 5] is [15.666666666666666, 16.333333333333332], calculated from (1*(18, 21) + 2*[14.5, 14.0])/3.
50           [4] [2, 7, 1, 6] [8, 3, 5]
51           [4]      0.0000      21.5943      9.6896
52 [2, 7, 1, 6]      21.5943      0.0000      18.9262
53 [8, 3, 5]         9.6896      18.9262      0.0000
54 The minimum distance is 9.6896 between clusters [4] and [8, 3, 5].
55 The centroid of the merged cluster [4, 8, 3, 5] is [17.5, 14.75], calculated from (1*(23, 10) + 3*[15.666666666666666, 16.333333333333332])/4.
56           [2, 7, 1, 6] [4, 8, 3, 5]
57 [2, 7, 1, 6]      0.0000      19.1735
58 [4, 8, 3, 5]      19.1735      0.0000
59 The minimum distance is 19.1735 between clusters [2, 7, 1, 6] and [4, 8, 3, 5].
60 The centroid of the merged cluster [2, 7, 1, 6, 4, 8, 3, 5] is [10.125, 8.625], calculated from (4*[2.75, 2.5] + 4*[17.5, 14.75])/8.

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