

Initially,

w_1	w_2	b
0.7	0.7	0.7

Iteration 1

$$(x_1, x_2, d) = (170, 90, 1)$$

$$\begin{aligned}\text{net} &= w_1 x_1 + w_2 x_2 + b \\ &= 0.7 \times 170 + 0.7 \times 90 + 0.7 \\ &= 182.7\end{aligned}$$

$$\begin{aligned}y &= \tanh(\text{net}) \\ &= \tanh(182.7) \\ &= 1.0\end{aligned}$$

Correct!

$$\begin{aligned}w_1 &\leftarrow w_1 + \alpha(d - y)x_1 \\ &= 0.7 + 0.3 \times (1 - 1.0) \times 170 \\ &= 0.7\end{aligned}$$

$$\begin{aligned}w_2 &\leftarrow w_2 + \alpha(d - y)x_2 \\ &= 0.7 + 0.3 \times (1 - 1.0) \times 90 \\ &= 0.7\end{aligned}$$

$$\begin{aligned}b &\leftarrow b + \alpha(d - y) \\ &= 0.7 + 0.3 \times (1 - 1.0) \\ &= 0.7\end{aligned}$$

w_1	w_2	b
0.7	0.7	0.7

Iteration 2

$$(x_1, x_2, d) = (190, 95, -1)$$

$$\begin{aligned}\text{net} &= w_1 x_1 + w_2 x_2 + b \\ &= 0.7 \times 190 + 0.7 \times 95 + 0.7 \\ &= 200.2\end{aligned}$$

$$\begin{aligned}y &= \tanh(\text{net}) \\ &= \tanh(200.2) \\ &= 1.0\end{aligned}$$

Incorrect!

$$\begin{aligned}w_1 &\leftarrow w_1 + \alpha(d - y)x_1 \\ &= 0.7 + 0.3 \times (-1 - 1.0) \times 190 \\ &= -113.3\end{aligned}$$

$$\begin{aligned}w_2 &\leftarrow w_2 + \alpha(d - y)x_2 \\ &= 0.7 + 0.3 \times (-1 - 1.0) \times 95 \\ &= -56.3\end{aligned}$$

$$\begin{aligned}b &\leftarrow b + \alpha(d - y) \\ &= 0.7 + 0.3 \times (-1 - 1.0) \\ &= 0.1\end{aligned}$$

w_1	w_2	b
-113.3	-56.3	0.1

Iteration 3

$$(x_1, x_2, d) = (160, 50, -1)$$

$$\begin{aligned}w_1 &\leftarrow w_1 + \alpha(d - y)x_1 \\ &= -113.3 + 0.3 \times (-1 - -1.0) \times 160 \\ &= -113.3\end{aligned}$$

$$\begin{aligned}\text{net} &= w_1 x_1 + w_2 x_2 + b \\ &= -113.3 \times 160 + -56.3 \times 50 + 0.1 \\ &= -20942.9\end{aligned}$$

$$\begin{aligned}y &= \tanh(\text{net}) \\ &= \tanh(-20942.9) \\ &= -1.0\end{aligned}$$

Incorrect!

w_1	w_2	b
-113.3	-56.3	0.1

Iteration 4

$$\begin{aligned}(x_1, x_2, d) &= (180, 70, -1) \\ \text{net} &= w_1 x_1 + w_2 x_2 + b \\ &= -113.3 \times 180 + -56.3 \times 70 + 0.1 \\ &= -24334.9\end{aligned}$$

$$\begin{aligned}y &= \tanh(\text{net}) \\ &= \tanh(-24334.9) \\ &= -1.0\end{aligned}$$

Incorrect!

w_1	w_2	b
-113.3	-56.3	0.1

Iteration 5

$$\begin{aligned}(x_1, x_2, d) &= (170, 90, 1) \\ \text{net} &= w_1 x_1 + w_2 x_2 + b \\ &= -113.3 \times 170 + -56.3 \times 90 + 0.1 \\ &= -24327.9\end{aligned}$$

$$\begin{aligned}y &= \tanh(\text{net}) \\ &= \tanh(-24327.9) \\ &= -1.0\end{aligned}$$

Incorrect!

w_1	w_2	b
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$$\begin{aligned}w_2 &\leftarrow w_2 + \alpha(d - y)x_2 \\ &= -56.3 + 0.3 \times (-1 - -1.0) \times 50 \\ &= -56.3\end{aligned}$$

$$\begin{aligned}b &\leftarrow b + \alpha(d - y) \\ &= 0.1 + 0.3 \times (-1 - -1.0) \\ &= 0.1\end{aligned}$$

$$\begin{aligned}w_1 &\leftarrow w_1 + \alpha(d - y)x_1 \\ &= -113.3 + 0.3 \times (-1 - -1.0) \times 180 \\ &= -113.3\end{aligned}$$

$$\begin{aligned}w_2 &\leftarrow w_2 + \alpha(d - y)x_2 \\ &= -56.3 + 0.3 \times (-1 - -1.0) \times 70 \\ &= -56.3\end{aligned}$$

$$\begin{aligned}b &\leftarrow b + \alpha(d - y) \\ &= 0.1 + 0.3 \times (-1 - -1.0) \\ &= 0.1\end{aligned}$$

$$\begin{aligned}w_1 &\leftarrow w_1 + \alpha(d - y)x_1 \\ &= -113.3 + 0.3 \times (1 - -1.0) \times 170 \\ &= -11.3\end{aligned}$$

$$\begin{aligned}w_2 &\leftarrow w_2 + \alpha(d - y)x_2 \\ &= -56.3 + 0.3 \times (1 - -1.0) \times 90 \\ &= -2.3\end{aligned}$$

$$\begin{aligned}b &\leftarrow b + \alpha(d - y) \\ &= 0.1 + 0.3 \times (1 - -1.0) \\ &= 0.7\end{aligned}$$

w_1	w_2	b
-11.3	-2.3	0.7