## Supplementary Materials: Predicting similarity judgments in intertemporal choice with machine learning

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October 3, 2017

## R packages

This project used R (3.4.2, R Core Team, 2017) and the R-packages BayesFactor (0.9.12.2, Morey & Rouder, 2015), car (2.1.5, Fox & Weisberg, 2011), cowplot (0.8.0, Wilke, 2016), dplyr (0.7.4, Wickham & Francois, 2016), foreach (1.4.3, Analytics & Weston, 2015), ggplot2 (2.2.1, Wickham, 2009), lattice (0.20.35, Sarkar, 2008), lme4 (1.1.14, Bates, Mächler, Bolker, & Walker, 2015), MBESS (4.4.0, Kelley, 2017), papaja (0.1.0.9492, Aust & Barth, 2017), plyr (Wickham, 2011; 1.8.4, Wickham & Francois, 2016), rpart (Milborrow, 2017; 4.1.11, Therneau, Atkinson, & Ripley, 2017), rpart.plot (2.1.2, Milborrow, 2017), tidyr (0.7.1, Wickham, 2017), and xtable (1.8.2, Dahl, 2016).

Table S1: Amount Questions and Mean Ratings for Experiment 1

Small Value	Large Value	Mean Similarity Rating
3	4	0.88
3	5	0.70
3	6	0.50
3	7	0.26
3	8	0.16
3	9	0.25
3	10	0.05
3	11	0.03
3	12	0.08
3	13	0.12
4	5	0.94
5	6	0.92
5	14	0.03
6	8	0.90
6	9	0.63
7	11	0.42
8	29	0.00
9	20	0.05
10	11	0.95
10	12	0.89
10	18	0.14
10	20	0.22
12	16	0.68
12	28	0.11
13	17	0.55
14	18	0.64
15	16	0.92
15	18	0.73
15	19	0.62
15	20	0.48
15	22	0.21
15	24	0.08
15	26	0.06
15	27	0.14
15	28	0.05
15	30	0.17
15	31	0.08
15	32	0.08
15	34	0.08
17	18	0.88
17	30	0.03
18	21	0.80
18	40	0.06
22	53	0.00
23	48	0.09
26	62	0.16
50	90	0.14
52	61	0.42
62	66	0.85
82	90	0.71

Table S2: Delay Questions and Mean Ratings for Experiment 1

		Iean Ratings for Experim
Small Value	Large Value	Mean Similarity Rating
8	29	0.00
12	28	0.12
13	17	0.69
15	16	0.95
15	18	0.88
15	20	0.55
15	22	0.37
15	24	0.23
15	26	0.17
15	27	0.19
15	28	0.11
15	30	0.18
15	31	0.14
15	32	0.11
15	34	0.09
17	18	0.94
17	28	0.17
17	30	0.02
18	40	0.05
21	39	0.14
22	53	0.03
23	48	0.08
26	62	0.14
29	60	0.08
32	36	0.94
34	45	0.25
35	56	0.06
36	38	0.94
36	41	0.73
36	44	0.50
36	47	0.37
36	50	0.14
36	53	0.09
36	56	0.12
36	59	0.10
36	62	0.11
36	65	0.05
38	60	0.08
42	74	0.06
43	64	0.09
43	70	0.03
46	53	0.62
46	56	0.52
48	51	0.86
50	90	0.15
52	61	0.58
62	66	0.94
75	89	0.52
82	90	0.75

Table S3: Amount Questions and Mean Ratings for Experiment 2

,			mean narmys for Experm
	Small Value	Large Value	Mean Similarity Rating
	1	2	0.88
	1	10	0.03
	2	3	0.92
	2	10	0.02
	3	4	0.93
	3	6	0.46
	3	10	0.06
	4	5	0.89
	4	10	0.07
	5	10	0.13
	6	9	0.56
	6	10	0.37
	7	10	0.59
	7	14	0.04
	8	10	0.79
	9	10	0.92
	9	12	0.58
	9	18	0.04
	10	15	0.34
	10	20	0.04
	11	20	0.02
	12	15	0.69
	12	20	0.06
	13	20	0.08
	14	20	0.10
	14	21	0.06
	15	20	0.36
	16	20	0.53
	17	20	0.70
	18	20	0.84
	18	27	0.12
	19	20	0.88
	20	25	0.46
	21	28	0.26
	27	30	0.78
	27	36	0.13
	28	35	0.27
	36	45	0.14
	45	50	0.63
	63	70	0.46
	81	90	0.51

Table S4: Delay Questions and Mean Ratings for Experiment 2

0     1     0.84       0     2     0.64       0     3     0.42       0     4     0.32       0     5     0.23       0     6     0.08       0     7     0.07       0     8     0.04       0     9     0.03       0     10     0.03       1     2     0.91       1     10     0.06       2     3     0.92       2     10     0.11       3     4     0.93       3     6     0.63       3     10     0.07       4     5     0.92       4     10     0.11       5     10     0.29       6     9     0.71       6     10     0.48       7     10     0.71       7     14     0.13       8     10     0.86       9     10 <td< th=""><th></th><th></th><th>tean Katings for Experim</th></td<>			tean Katings for Experim
0   2   0.64     0   3   0.42     0   4   0.32     0   5   0.23     0   6   0.08     0   7   0.07     0   8   0.04     0   9   0.03     0   10   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15	Small Value	Large Value	Mean Similarity Rating
0   3   0.42     0   4   0.32     0   5   0.23     0   6   0.08     0   7   0.07     0   8   0.04     0   9   0.03     0   10   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15			
0   4   0.32     0   5   0.23     0   6   0.08     0   7   0.07     0   8   0.04     0   9   0.03     0   10   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21			
0   5   0.23     0   6   0.08     0   7   0.07     0   8   0.04     0   9   0.03     0   10   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.5 <td></td> <td></td> <td></td>			
0   6   0.08     0   7   0.07     0   8   0.04     0   9   0.03     0   10   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.58     18   27   0.13<			
0   7   0.07     0   8   0.04     0   9   0.03     0   10   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.58     18   27   0.13     20   25   0.6			0.23
0   8   0.04     0   9   0.03     0   10   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.58     18   27   0.13     20   25   0.64     21   28   0	0		0.08
0   9   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.53     12   15   0.81     14   21   0.14     15   0.58     18   27   0.13     20   25   0.64 </td <td></td> <td></td> <td></td>			
0   10   0.03     1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   <	0		0.04
1   2   0.91     1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   36   0.27     28   35   0.30     36   45	0	9	0.03
1   10   0.06     2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   36   0.27     28   35   0.30     36   45   0.32     45	0		0.03
2   3   0.92     2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   36   0.27     28   35   0.30     36   45   0.32     45   0.0   0.48      4	1	2	0.91
2   10   0.11     3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	1	10	0.06
3   4   0.93     3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   0.02   0.48		3	0.92
3   6   0.63     3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48		10	0.11
3   10   0.07     4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	3	4	0.93
4   5   0.92     4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	3	6	0.63
4   10   0.11     5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	3	10	0.07
5   10   0.29     6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	4	5	0.92
6   9   0.71     6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	4	10	0.11
6   10   0.48     7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	5	10	0.29
7   10   0.71     7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	6	9	0.71
7   14   0.13     8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	6	10	0.48
8   10   0.86     9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	7	10	0.71
9   10   0.92     9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	7	14	0.13
9   12   0.73     9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	8	10	0.86
9   18   0.11     10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	9	10	
10   15   0.53     12   15   0.81     14   21   0.14     15   20   0.58     18   27   0.13     20   25   0.64     21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	9	12	0.73
12 15 0.81   14 21 0.14   15 20 0.58   18 27 0.13   20 25 0.64   21 28 0.37   27 30 0.81   27 36 0.27   28 35 0.30   36 45 0.32   45 50 0.72   63 70 0.48	9	18	0.11
14 21 0.14   15 20 0.58   18 27 0.13   20 25 0.64   21 28 0.37   27 30 0.81   27 36 0.27   28 35 0.30   36 45 0.32   45 50 0.72   63 70 0.48	10	15	0.53
15 20 0.58   18 27 0.13   20 25 0.64   21 28 0.37   27 30 0.81   27 36 0.27   28 35 0.30   36 45 0.32   45 50 0.72   63 70 0.48	12	15	0.81
18 27 0.13   20 25 0.64   21 28 0.37   27 30 0.81   27 36 0.27   28 35 0.30   36 45 0.32   45 50 0.72   63 70 0.48	14	21	0.14
20 25 0.64   21 28 0.37   27 30 0.81   27 36 0.27   28 35 0.30   36 45 0.32   45 50 0.72   63 70 0.48	15	20	0.58
21   28   0.37     27   30   0.81     27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	18	27	0.13
27 30 0.81   27 36 0.27   28 35 0.30   36 45 0.32   45 50 0.72   63 70 0.48	20	25	0.64
27   36   0.27     28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	21	28	0.37
28   35   0.30     36   45   0.32     45   50   0.72     63   70   0.48	27	30	0.81
36   45   0.32     45   50   0.72     63   70   0.48	27	36	0.27
36   45   0.32     45   50   0.72     63   70   0.48	28	35	0.30
45 50 0.72 63 70 0.48			
63   70   0.48			
0.04	81	90	0.64

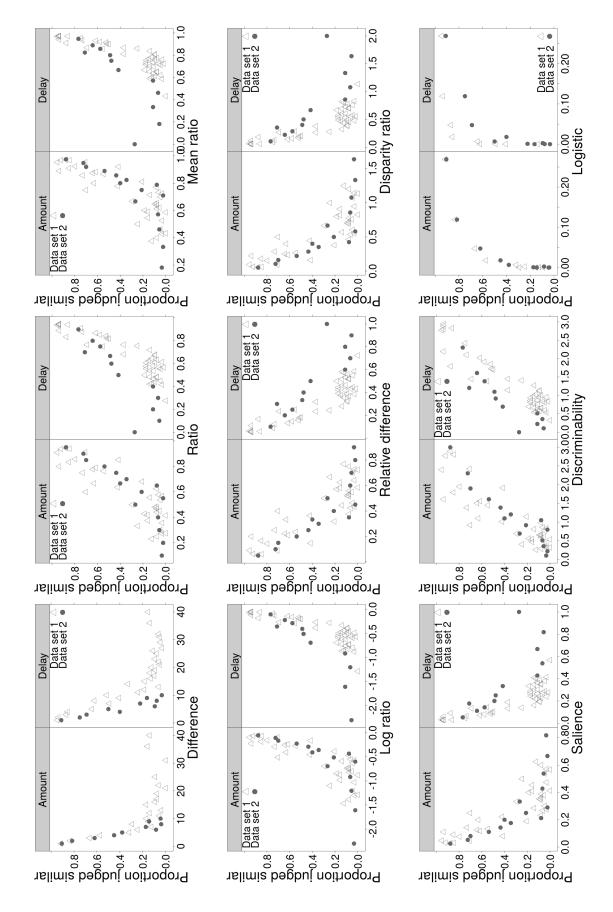


Figure S1: Attribute effects on similarity judgments. Dots represent mean proportion of pairs judged as similar for each attribute value.

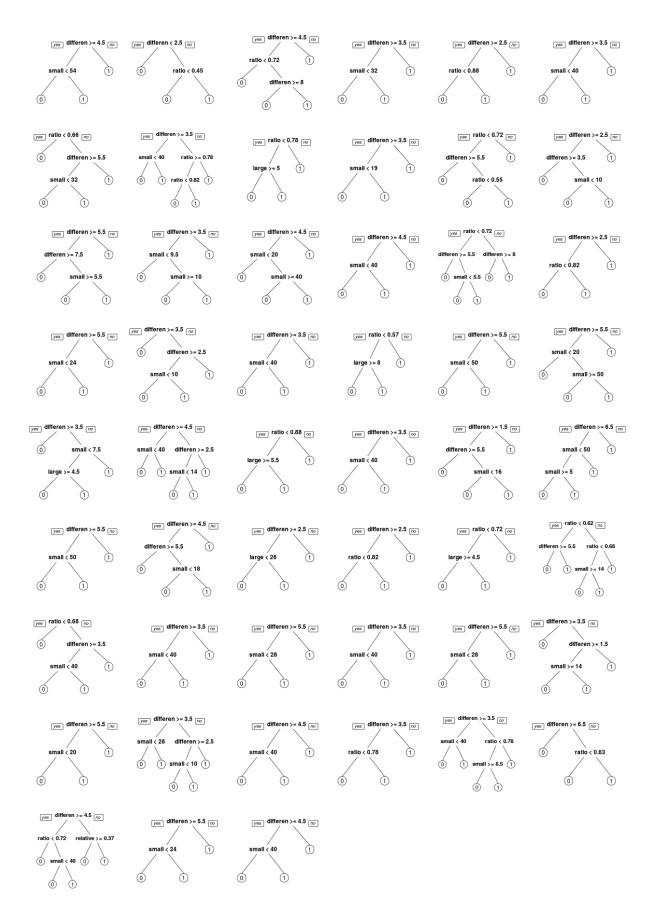


Figure S2: Amount judgment trees for participants with at least two nodes.

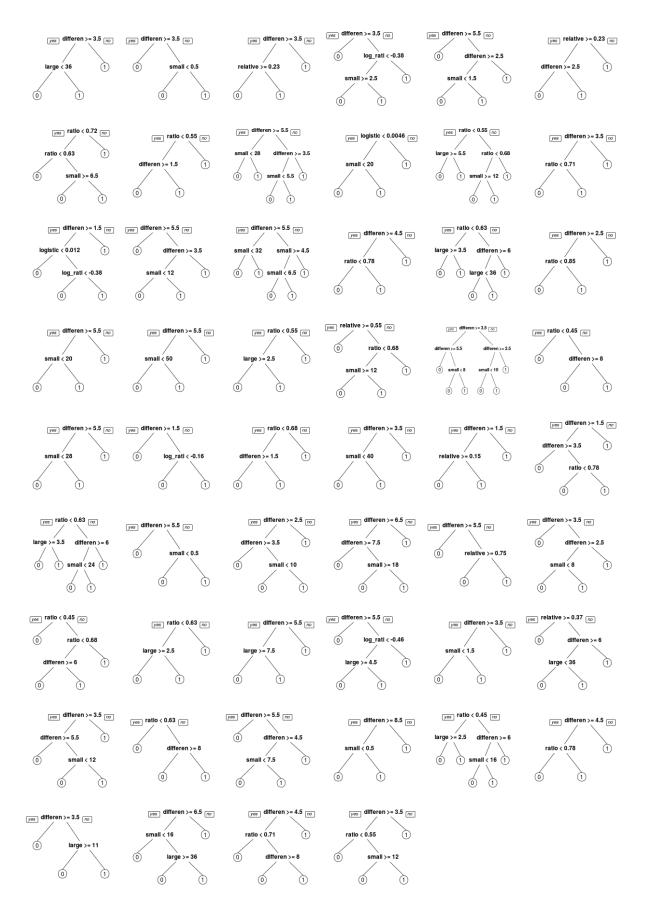


Figure S3: Delay judgment trees for participants with at least two nodes.

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