(45 minutes)

2023/09/25

除了選擇,填充和簡答題之外,你的答案必須提供完整說明,如果只有答案沒有任何說明得零分!

1. (5+5=10 points) (a) Sketch the graph of $f(x) = e^{|x|}$. Is it a one-to-one function? Why or why not?

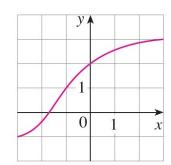
(b) Find the inverse function $g^{-1}(x)$ of $g(x) = \ln(x+3)$.

- 2. (5+5=10 points) Solve for x: (a) $e^{2x} 3e^x + 2 = 0$ (b) $1 2 \ln x < 3$

3. (4+3+3=10 points) 簡答題.

The graph of f is given.

- (a) What are the domain and range of f^{-1} ?
- (b) What is the value of $f^{-1}(2)$?
- (c) What is the value of $f^{-1}(-1)$?



4. (5+5=10 points) If $f(x) = e^x \sin x$, find f'(x) and f''(x).

5. (10 points) Find an equation of the tangent line to the curve $y=x\sqrt{x}$ that is parallel to the line y=1+3x.)

6. (5+5=10 points) Find the derivatives:

(a)
$$y = (x + 2\sqrt{x})e^x$$

(b)
$$f(x) = \frac{5t}{t^3 - t - 1}$$