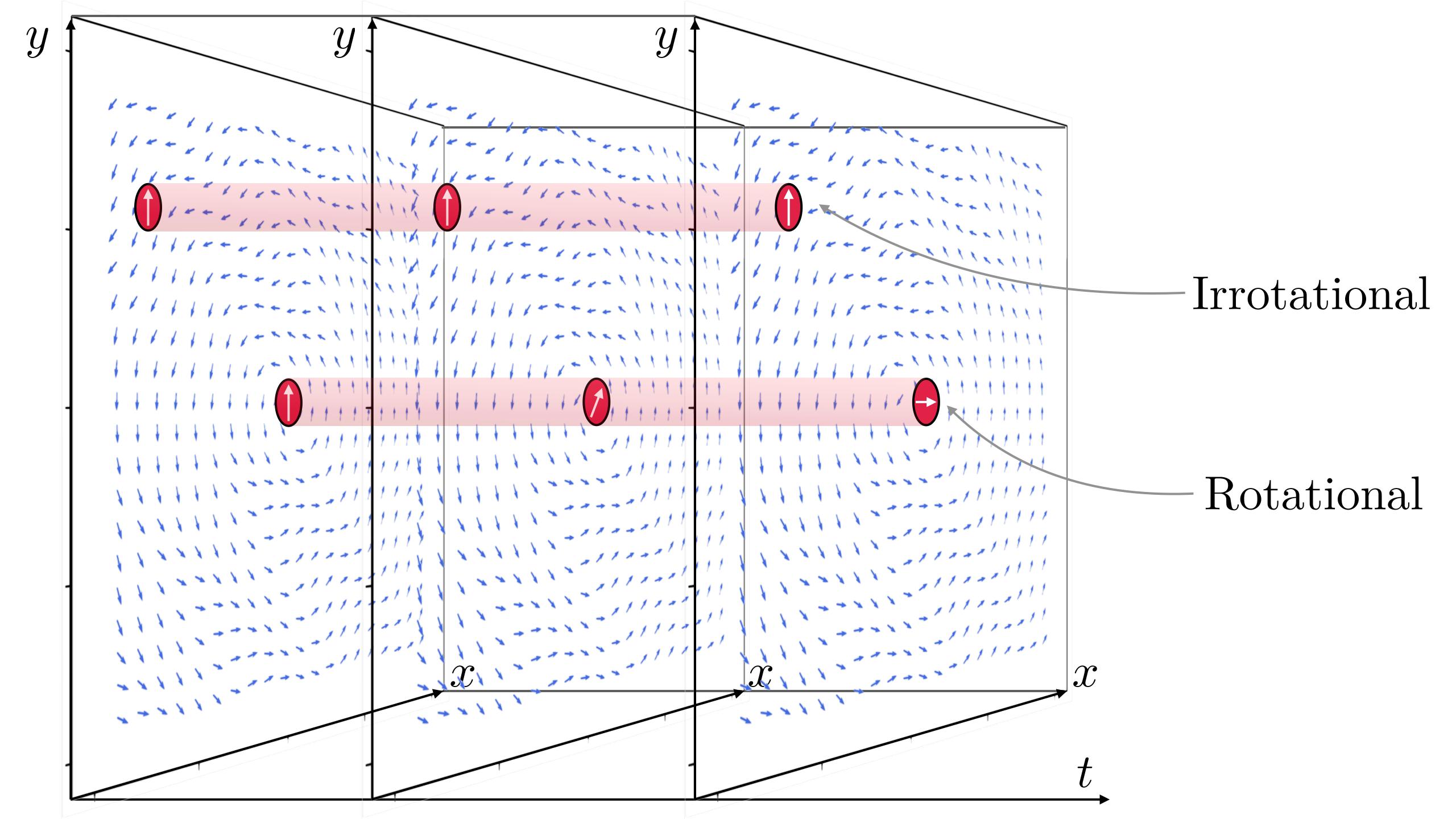
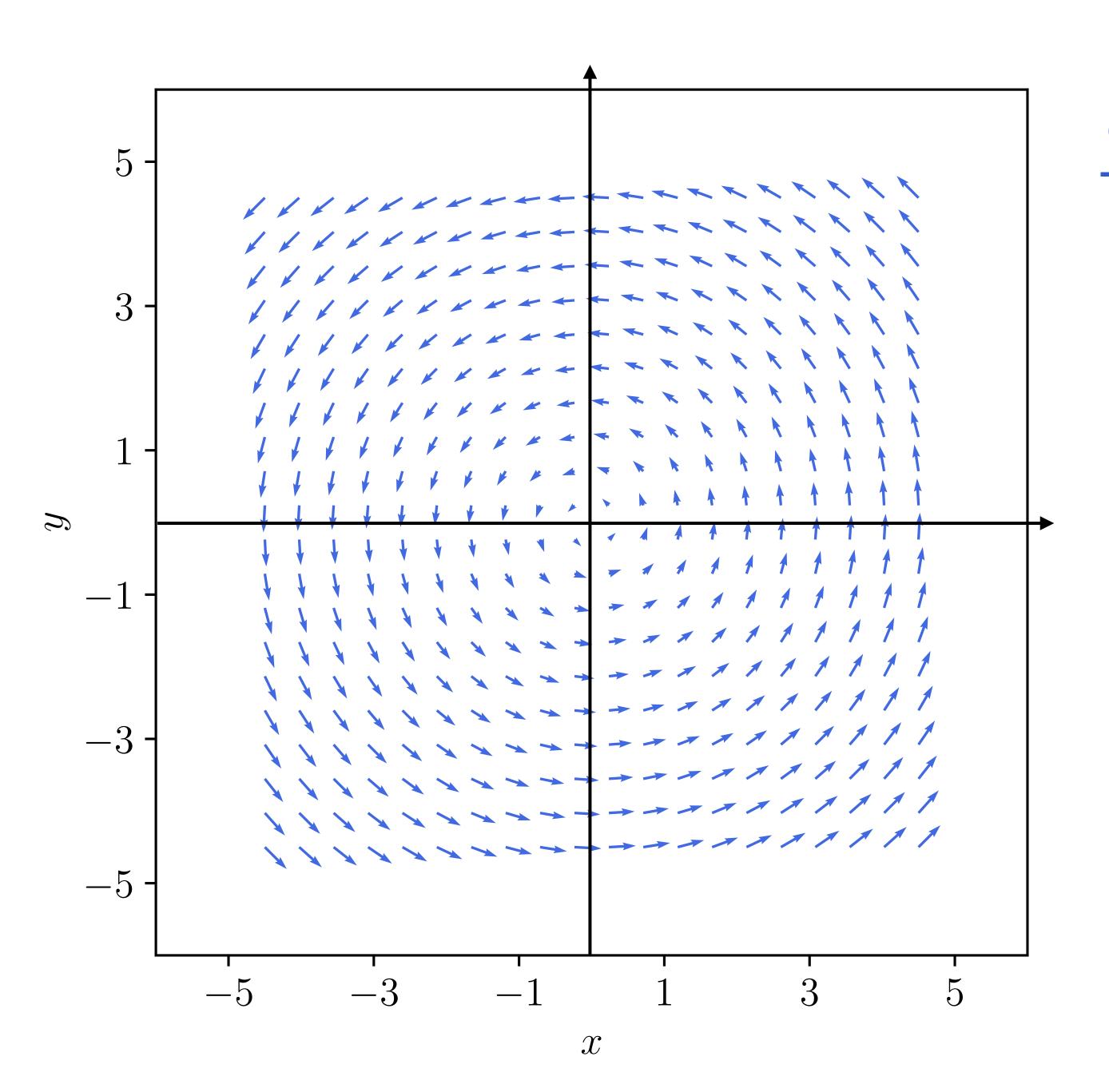
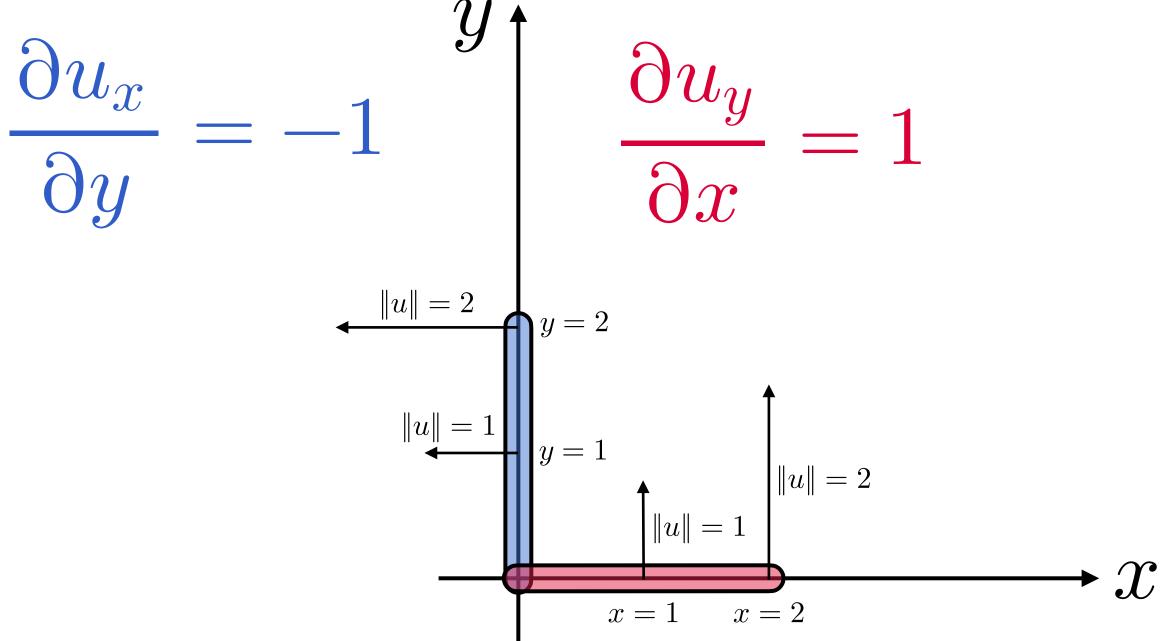


## $\vec{u} = \vec{u}(t_n)$ 10 -Stream line at specific time $t = t_n$ Path line $\frac{d\vec{r}(x(t), y(y))}{d\vec{r}(x(t), y(t))} = \vec{u}(x(t), y(t))$ 10

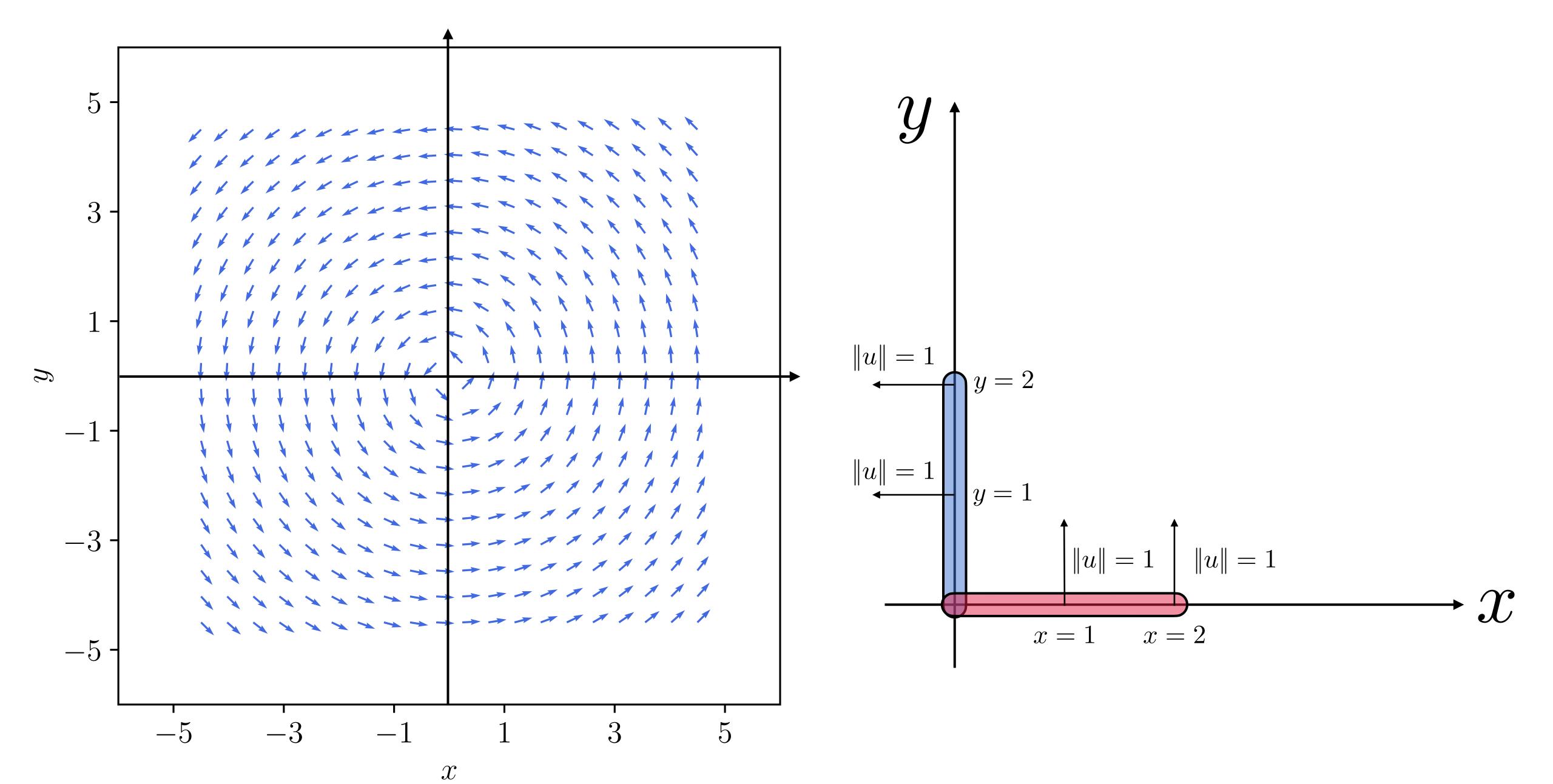
 $u_y(x,y)$ 







$$\operatorname{curl} \vec{u} = \frac{\partial u_y}{\partial x} - \frac{\partial u_x}{\partial y} = 2$$



$$y = 1$$

$$||u|| = 1$$

$$y = 1$$

$$||u|| = 1$$

$$||u|| = 1$$

$$x = 1$$

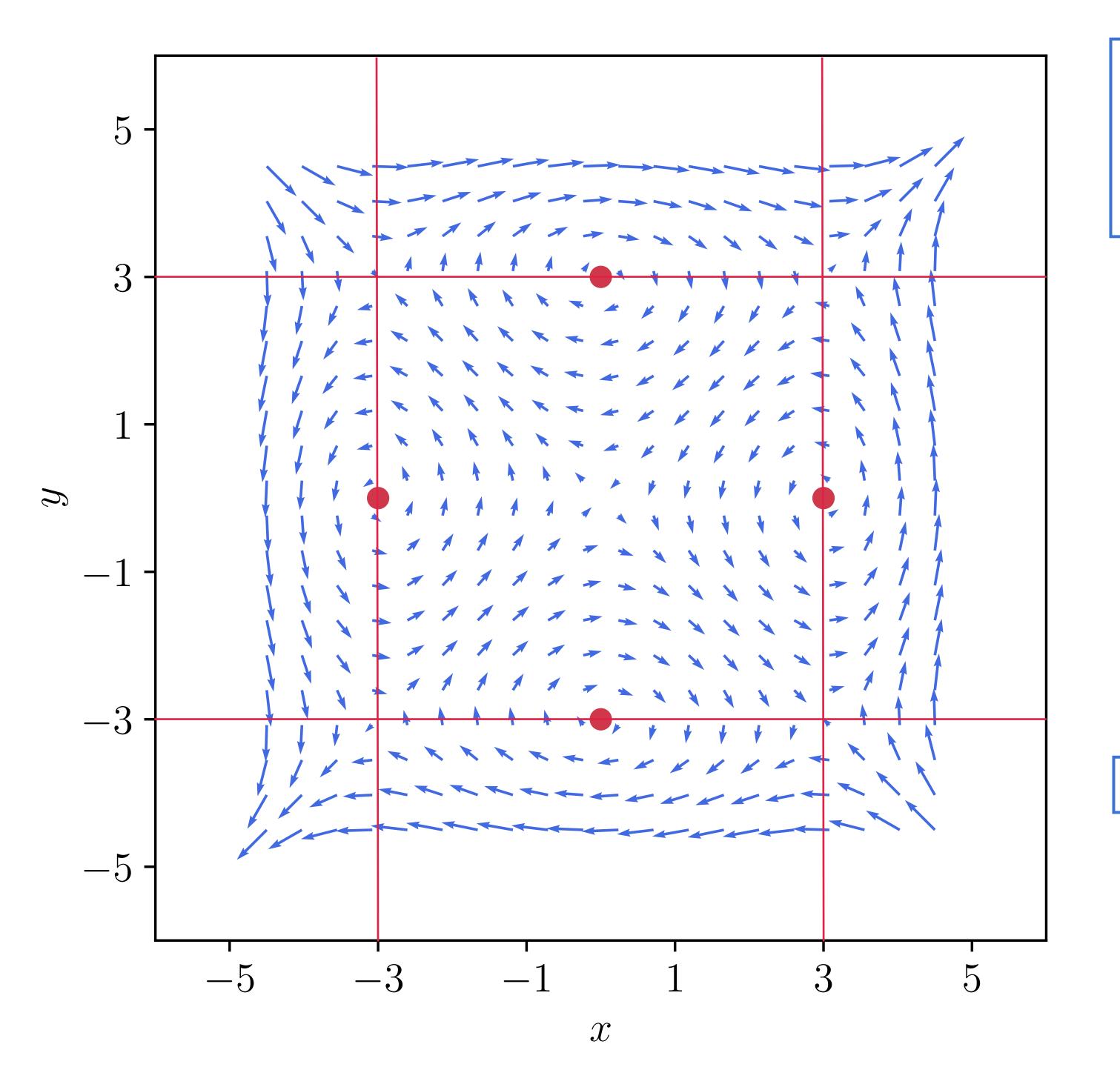
$$x = 2$$

$$\frac{\partial u_y}{\partial x} = -\frac{y^2}{(x^2 + y^2)^{3/2}} \xrightarrow{x=0} -\frac{1}{y^2}$$

$$\frac{\partial u_x}{\partial y} = \frac{x^2}{(x^2 + y^2)^{3/2}} \xrightarrow{y=0} \frac{1}{x}$$

$$\operatorname{curl} \vec{u} = \left(\frac{y^2}{(x^2 + y^2)^{3/2}}\right) - \left(-\frac{x^2}{(x^2 + y^2)^{3/2}}\right)$$

$$= \frac{1}{\sqrt{x^2 + y^2}}$$



$$\vec{u}(x(t), y(y)) = \frac{d\vec{r}}{dt} \quad \begin{cases} \frac{dx}{dt} = y^3 - 9y \\ \frac{dy}{dt} = x^3 - 9x \end{cases}$$

$$\vec{r}_3 = x(t_3)\hat{e}_x + y(t_3)\hat{e}_y$$

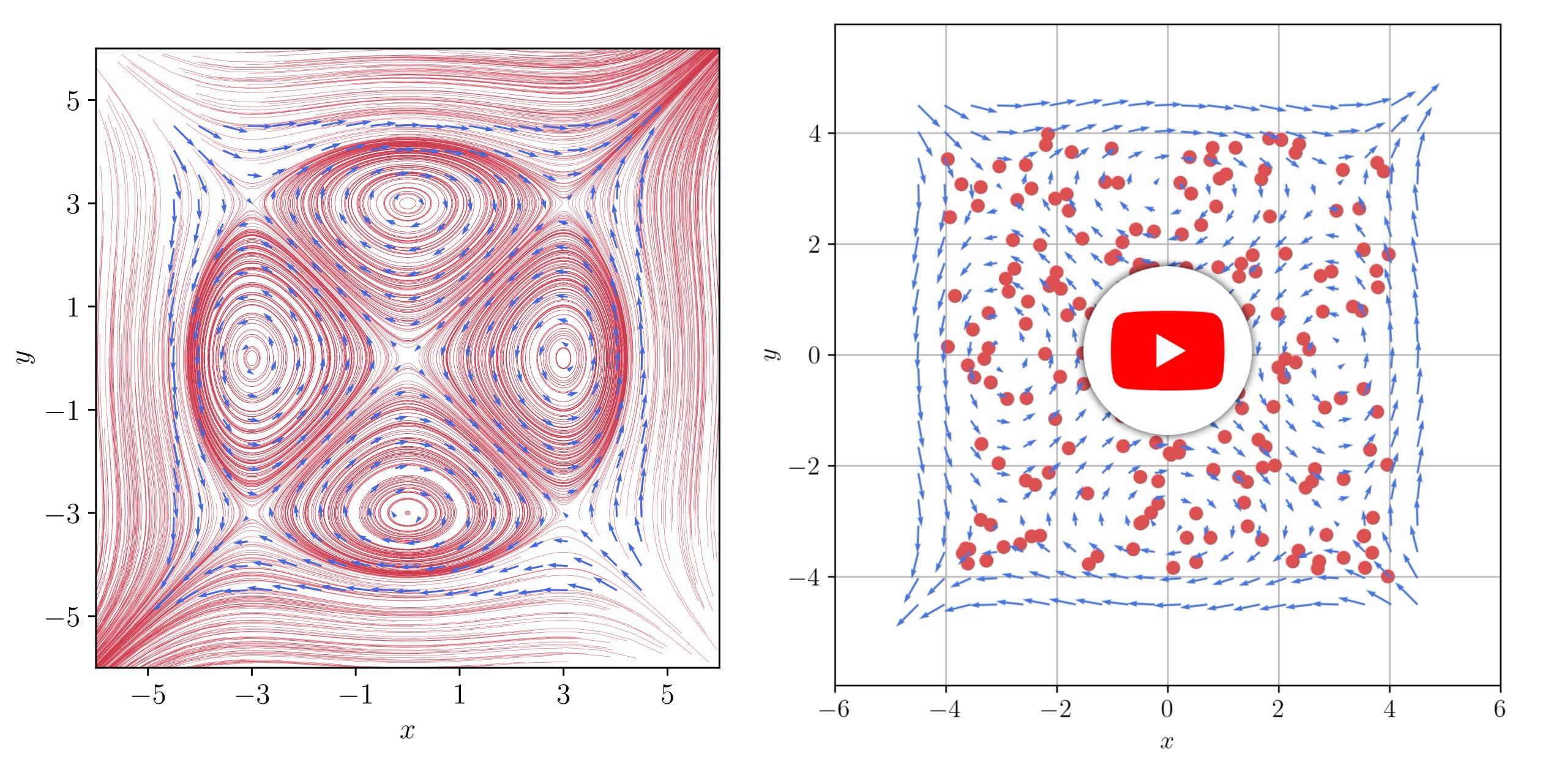
$$\vec{u} = \vec{u}(\vec{r}_3) \qquad t = t_3$$
Path line
$$\vec{r}_2 = x(t_2)\hat{e}_x + y(t_2)\hat{e}_y$$

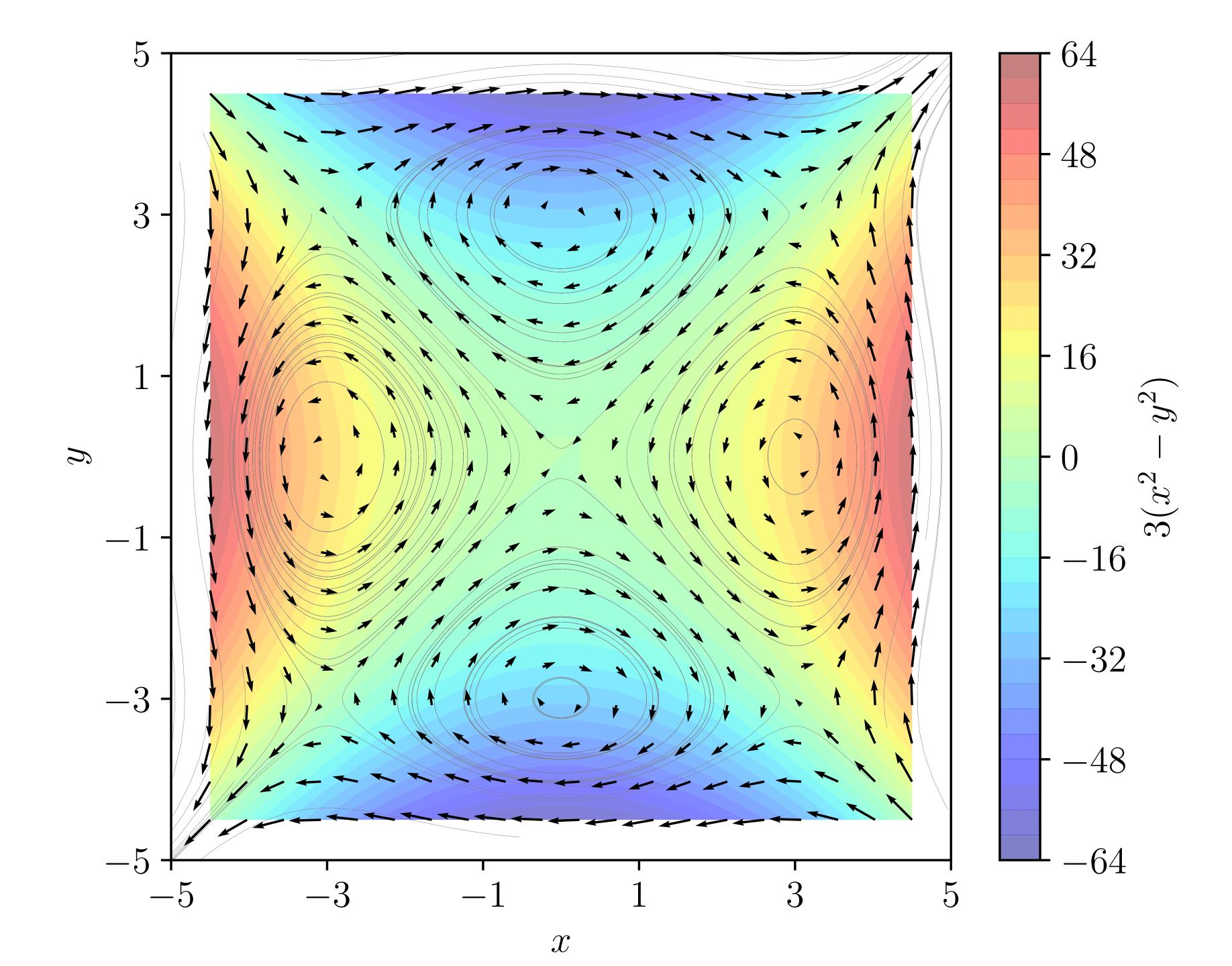
$$\vec{u} = \vec{u}(\vec{r}_2)$$

$$t = t_2$$

$$\vec{u} = \vec{u}(\vec{r}_1)$$

$$\vec{r}_1 = x(t_1)\hat{e}_x + y(t_1)\hat{e}_y$$





Cylindrical Spherical Cartesian coordiante coordiante coordiante  $\hat{e}_z$ z

