

## Test Case

Please test your program with Input, and then check the answers with Output.

Listing 10 : Insert and delete a number of binary search tree

```
1 Input :  
2 4 5 1 0 6 7 2  
3 insert(44)  
4 delete(6)  
5 insert(3)  
6 delete(2)  
7  
8 Output :  
9 4 1 5 0 3 7 44
```

## 11. Heap sort

Given a sequence of n numbers, build a heap using an array and implement a heap sort that results in a sorted numbers in ascending order. The output includes two lines of the results: (1) the contents of the array that stores the heap in each step, and (2) the sorted numbers in ascending order.

## Test Case

Please test your program with Input1 and Input2, and then check the answers with Output1 and Output2.

Listing 11: Heap sort

```
1 Input1 :  
2 1 4 5 0 6 7 2  
3  
4 Output1 :  
5 0 1 2 4 6 7 5  
6 1 4 2 5 6 7  
7 2 4 7 5 6  
8 4 5 7 6  
9 5 6 7  
10 6 7  
11 7  
12 0 1 2 4 5 6 7
```

```

Input2 :
3 7 5 9 1

Output2 :
13 1 3 5 9 7
14 3 7 5 9
15 5 7 9
16 7 9
17 9
18 1 3 5 7 9

```

## 12. Equivalent Relations

Given  $n$  equivalent relations, find the equivalent classes. Each line in the input shows the equivalent relation that consists of a pair of numbers separated by a space. Each line in the output is an equivalent class.

**Note:** You must sort each equivalent class in ascending order, and **print the equivalent classes based on the smallest number of each class in ascending order.**

### Test Case

Please test your program with Input1 and Input2, and then check the answers with Output1 and Output2.

Listing 12: Equivalent Relations

```

1 Input1 :
2 0 4
3 3 1
4 6 10
5 8 9
6 7 4
7 6 8
8 3 5
9 2 11
10 11 0
11
12 Output1 :
13 0 2 4 7 11
14 1 3 5
15 6 8 9 10

```