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Homework 3

COT 5405

1)

If $OPT(j)$ is equal to the maximum number of robots that can be destroyed for the instance of the problem on $x[1], x[2], \dots, x[j]$, and $f(j)$ is a function so that if j seconds have passed since the EMP was last used, it can destroy up to $f(j)$ robots. So, where k is the number of seconds since the EMP was used, $\min(x[k], f(j))$ would be how many robots could be killed that turn.

n = total number of seconds

$OPT(0) = 0$

for $j = 1; j \leq n; j++$

for $i = j; i \geq 0; i--$

$$OPT(j) = \max(OPT(i) + \min(x[j], f(j-i)))$$

Return $OPT(n)$

Runs in $O(n^2)$ time

2)

n = final day where the tank needs to be empty

a = starting day where the tank is assumed empty

b = day when the tank is filled

$b > a$

P = price of delivery

L = max capacity of storage tank

$S(a, b-1)$ = the cost to store the gas from day a to day b

$OPT(a)$ = the optimal solution for days a through n where the tank is empty on day a

$OPT(1)$ = starting day where the tank has to be filled on this day

for $a = n; a \geq 0; a--$ (Note: here b is found as well as the number of gallons to buy)

$$OPT(a) = P + (\sum_{j=a}^{b-1} g_j \leq L) S(a, b-1)$$

After all OPT values are found, start at $OPT(1)$, from there $OPT(b)$, then $OPT(b) \dots$ until n is reached. Each time you get to another b day (day the tank was filled), note how many gallons were bought and which day it was. Runs in $O(n^2)$

3)

a)

Given the following example:

	Week 1	Week 2	Week 3	Week 4	Total
l	10	1	10	10	
h	5	50	100	1	
Algorithm Answer	0	50	10	10	70
Correct Answer	10	0	100	10	120

The algorithm doesn't look far enough into the future. In this case, the algorithm incorrectly chose to pick the \$50 task, when if it looked a little further it would see that a much better \$100 task could have been chosen instead.

b)

$OPT(i)$ = the max cumulative revenue of the current week and previous weeks

$l[i]$ = low stress value of week i

$h[i]$ = high stress value of week i

n = total weeks

if OPT goes out of bounds assume value = 0

for $i=1; i \leq n; i++$

$$OPT(i) = \max(l[i] + OPT(i-1), h[i] + OPT(i-2))$$

return $OPT(n)$

This algorithm calculates the maximum value as it iterates through the weeks. And it calls previous OPT values in $O(1)$ time. Runs in $O(n)$ time.