Formal Grammars of English

Dr. Demetrios Glinos University of Central Florida

CAP6640 – Computer Understanding of Natural Language

Today

- Syntax
- Context-Free Grammars
- Grammar Rules for English
- Treebanks
- Grammar Equivalence and Normal Form
- Lexicalized Grammars

Constituents

- We do not understand words in isolation
- We group them into meaningful units called constituents
- We relate the units in hierarchical ways
- Consider the sentence

The man with the umbrella walked into the store.

Meaningful units: the man with the umbrella

walked into the store

Constituents may be further decomposed: the + man

with + the umbrella

walked + into the store

etc.

Syntax and Grammar

- Syntax
 - refers to the way words are arranged together
- Grammar
 - mechanism for determining valid and invalid arrangements (constituents)
 - Valid

The man with the umbrella walked into the store.

Invalid

into umbrella man the with the walked store the.

We use formal language theory to study grammars

Formal Language Theory

- Attributable to linguist Noam Chomsky (1956)
 - Language
 - a collection of sentences of finite length all constructed from a finite alphabet of symbols
 - Grammar
 - a mechanism that enumerates the sentences of a language
 - a grammar of language L can be regarded as a function whose range is exactly L
 - Formal grammar
 - a precisely defined grammar
 - Generative grammar
 - a formal grammar that can "generate" natural language expressions

Levels of Representation

- A sentence in a language has two levels of representation
 - Deep structure
 - a direct representation of the semantics underlying the sentence
 - Surface structure
 - the syntactical representation
- Deep structures are mapped onto surface structures via *transformations*
- Example:

Peter put the book on the table
The book was put on the table by Peter

same semantics

Formal Grammar

A formal grammar is a quad-tuple $G = (N, \Sigma, P, S)$, where

N is a finite set of non-terminalsfor which some production rule can be applied

Σ is a finite set of terminal symbols
disjoint from N
for which no production rule can be applied

P is a finite set of production rules of the form

$$w \in (N \cup \Sigma)^* \to w \in (N \cup \Sigma)^*$$

where w ("word") is a valid sequence of symbols in the language

 $S \in N$ is the start symbol

Formal Grammar

```
A formal grammar is a quad-tuple G = (N, \Sigma, P, S), where N is a finite set of non-terminals \Sigma is a finite set of terminals and is disjoint from N P is a finite set of production rules of the form w \in (N \cup \Sigma)^* \to w \in (N \cup \Sigma)^* S \in N is the start symbol
```

A formal language

- provides an axiom schema for generating a (usually infinite) set of finite-length sequences of symbols
- sequences may be constructed by successive applications of the production rules
- a rule may be applied by replacing an occurrence of the symbols on the lefthand side with those that appear on its right-hand side
- a sequence of rule applications is called a derivation
- the language so defined is the set of all "words" (sequences of terminals) that can be reached from the start symbol

Notation and Example

Notation

- Upper case nonterminals
- Lower case terminals
- S Start symbol

Example

Let L have terminals { a, b }, nonterminals { S, A, B }, start symbol S, and production rules:

$$S \to AB$$

 $S \to \varepsilon$ (where ε is the empty string)
 $A \to aS$
 $B \to b$

This grammar defines the language of all words of the form a^nb^n

The Chomsky Hierarchy

Each grammar type strictly includes all grammars below it in the hierarchy

Grammar	Languages	Automaton	Production rules (constraints)*
Type-0	Recursively enumerable	Turing machine	lpha ightarrow eta (no restrictions)
Type-1	Context-sensitive	Linear-bounded non-deterministic Turing machine	$lpha Aeta ightarrow lpha \gamma eta$
Type-2	Context-free	Non-deterministic pushdown automaton	$A o \gamma$
Туре-3	Regular	Finite state automaton	$egin{aligned} A ightarrow a \ & ext{and} \ A ightarrow a B \end{aligned}$

* Meaning of symbols:

a = terminal

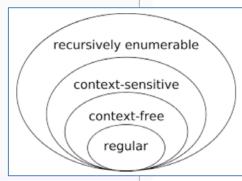
 α = terminal, non-terminal, or empty

 β = terminal, non-terminal, or empty

 γ = terminal or non-terminal

A = non-terminal

B = non-terminal



source: Wikipedia

Today

- Syntax
- Context-Free Grammars
- Grammar Rules for English
- Treebanks
- Grammar Equivalence and Normal Form
- Lexicalized Grammars

Context-Free Grammars

- Also known as "phrase-structure grammars"
- Basis of many formal models of the syntax of natural languages
 - also for computer programming languages
- Powerful enough to express sophisticated relations among words in a sentence
- Computationally tractable, supporting efficient algorithms for parsing
- Uses
 - grammar checking
 - semantic interpretation
 - dialogue understanding
 - machine translation

Example: ATIS L₀

- Air Traffic Information System (ATIS) (1990)
 - one of the earliest spoken language systems, for booking airline reservations

```
Noun → flights | breeze | trip | morning

Verb → is | prefer | like | need | want | fly

Adjective → cheapest | non-stop | first | latest

| other | direct

Pronoun → me | I | you | it

Proper-Noun → Alaska | Baltimore | Los Angeles

| Chicago | United | American

Determiner → the | a | an | this | these | that

Preposition → from | to | on | near

Conjunction → and | or | but
```

Figure 11.2 The lexicon for \mathcal{L}_0 .

Example: ATIS L₀

Grammar Rules	Examples
$S \rightarrow NPVP$	I + want a morning flight
NP → Pronoun Proper-Noun Det Nominal Nominal → Nominal Noun Noun	I Los Angeles a + flight morning + flight flights
VP → Verb Verb NP Verb NP PP Verb PP	do want + a flight leave + Boston + in the morning leaving + on Thursday
PP → Preposition NP	from + Los Angeles

Figure 11.3 The grammar for \mathcal{L}_0 , with example phrases for each rule.

Example: ATIS L₀

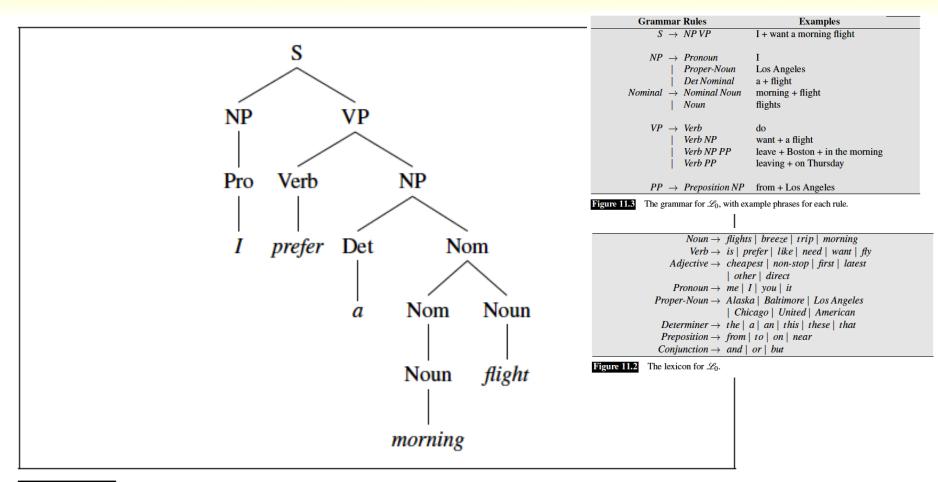


Figure 11.4 The parse tree for "I prefer a morning flight" according to grammar \mathcal{L}_0 .

Syntactic Parsing

Definition:

If $A \to \beta$ is a production of R and α and γ are any strings in the set $(\Sigma \cup N)^*$, then we say that $\alpha A \gamma$ directly derives $\alpha \beta \gamma$, and we write $\alpha A \gamma \Rightarrow \alpha \beta \gamma$

Definition:

Let $\alpha_1, \alpha_2, ..., \alpha_m$ be strings in $(\Sigma \cup N)^*, m \ge 1$, such that

$$\alpha_1 \Rightarrow \alpha_2, \alpha_2 \Rightarrow \alpha_3, \dots, \alpha_{m-1} \Rightarrow \alpha_m$$

then we say that α_1 derives α_m , and we write $\alpha_1 \Rightarrow^* \alpha_m$

Definition:

The language generated by grammar G is $\mathcal{L}_G = \{w | w \text{ is in } \Sigma^* \text{ and } S \Rightarrow^* w\}$

Syntactic parsing

the problem of mapping from a string of words to its parse tree is called

Today

- Syntax
- Context-Free Grammars
- Grammar Rules for English
- Treebanks
- Grammar Equivalence and Normal Form
- Lexicalized Grammars

English has 4 major sentence-level constructions

1. Declarative

- basic form is S → NP VP, where we typically call the NP the "subject"
- examples
 - I want a flight from Ontario to Chicago
 - The flight should depart at eleven a.m. tomorrow
 - The return flight should leave at around seven p.m.

2. Imperative

- basic form is $S \rightarrow VP$; typically has no subject; used for commands, etc.
- examples
 - Show the lowest fares
 - Give me Sunday's flights from New York City to Las Vegas
 - List all flights between five and seven p.m.

3. Yes-No question

- basic form is S → Aux NP VP; begins with auxiliary verb, then subject NP, then VP
- examples
 - Do any of these flights have stops?
 - Does American's flight eighteen twenty five serve dinner?
 - Can you give me the same information for United?

4. Wh-questions

- contains a "wh-phrase"
 - includes a "wh-word": who, whose, when, where, what, which, how, why
- wh-subject-question (S → Wh-NP VP)
 - identical to declarative structure, except first NP contains a wh-word
 - examples:
 - What airlines fly from Burbank to Denver?
 - Whose flights serve breakfast?
- wh-non-subject-question (S → Wh-NP Aux NP VP)
 - wh-phrase is not the subject; auxiliary appears before the subject NP
 - example
 - What flights do you have from Burbank to Tacoma Washington?

Note the long-distance dependency: the leading Wh-NP is the object of the VP

Clauses and Sentences

- Sentence constructions ("S → " rules)
 - represent a "complete thought"
 - correspond to the lingistic notion of a *clause*
 - can be embedded within a larger sentence
 - e.g., "I said I prefer a morning flight."

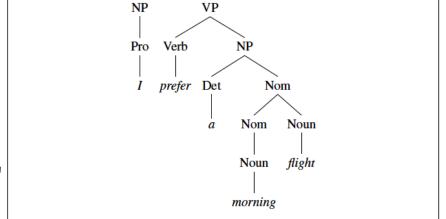


Figure 11.4 The parse tree for "I prefer a morning flight" according to grammar \mathcal{L}_0 .

- In other words
 - S is a node in a parse tree below which the main verb of the S has all of its arguments

The Noun Phrase

• L₀ contains these NP productions:

- The complexity is in the "Det Nominal" rule
- Determiner
 - can be simple: a, an, the, those, this, some, any, ...
 - e.g., those flights, a stop, the plane
 - can be filled by more complex expressions
 - Det \rightarrow NP 's
 - e.g., United's pilot's union (which also illustrates NP recursion)
 - optional when the noun is plural or mass noun
 - e.g., Show me flights from New York to Denver on weekdays

The Noun Phrase

- Nominal
 - follows the determiner

- Nominal → Nominal Noun morning + flight
 | Noun flights
- contains any pre- and post-head noun modifiers
 - before the head noun ("postdeterminers")
 - cardinal numbers, ordinal numbers, quantifiers, and adjectives
 - e.g., the first flight, many fares, the longest layover
 - adjectives can be grouped into an adjective phrase (AP), which can have an adverb before the adjective
 - e.g., the *least expensive* fare

multiple PPs

- after the head noun ("postmodifiers")
 - prepositional phrases,
- e.g., all flights from Cleveland to Newark
 - non-finite clauses,
 e.g., any flights arriving after eleven a.m.
 - relative clauses
 e.g., a flight that serves breakfast

The Nominal (cont'd)

- Non-finite postmodifiers
 - gerundive
 - postmodifier consists of a VP that begins with the gerundive (-ing)
 - examples:
 - any of those leaving on Thursday
 - flights arriving within the next two hours
 - infinitive
 - postmodifier consists of a VP that begins with the infinitive (to+)
 - e.g., the last flight to arrive in Boston
 - -ed form
 - postmodifier consists of a VP that begins with the past participle (-ed)
 - e.g., the aircraft used by this flight

The Nominal (cont'd)

- Postnominal relative clause
 - also called "restrictive relative clause"
 - typically begins with a relative pronoun (e.g., that and who),
 - can serve as the subject of the embedded verb
 - examples:
 - a flight that serves breakfast
 - flights that leave in the morning
 - can serve as the object of the embedded verb
 - e.g., the earliest American Airlines flight that I can get
- Predeterminers
 - word classes that modify and appear before NPs
 - typically involve number or amount; "all" is a common example
 - examples: all the flights; all flights; all non-stop flights

Example: Complex NP

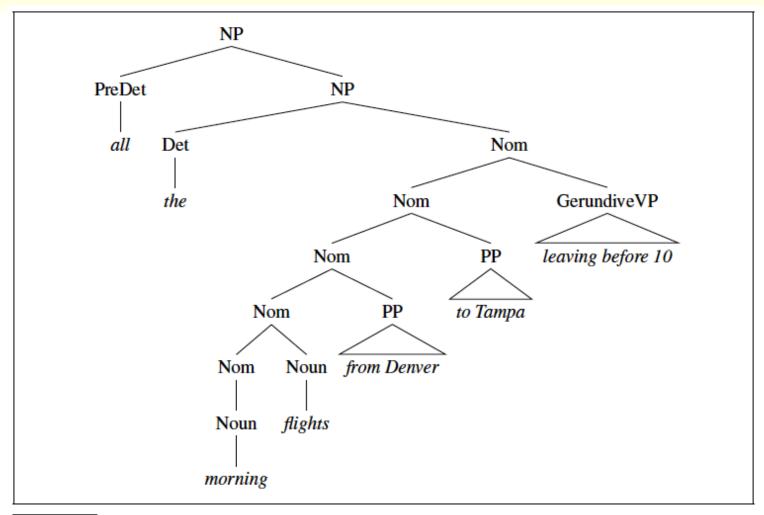


Figure 11.5 A parse tree for "all the morning flights from Denver to Tampa leaving before 10".

The Verb Phrase

L₀ contains these VP productions:

```
VP \rightarrow Verb do 

| Verb NP want + a flight 

| Verb NP PP leave + Boston + in the morning 

| Verb PP leaving + on Thursday
```

- sentential complements (VP → Verb S)
 - entire embedded sentences that can also follow VPs
 - e.g., You said you had a two hundred sixty six dollar fare
- VPs can also be followed by other VPs
 - common for verbs like want, would like, try, intend, need, etc.
 - e.g., I want to fly from Milwaukee to Orlando

Verb Subcategorization Frames

Frame	Verb	Example
Ø	eat, sleep	I ate
NP	prefer, find, leave	Find [NP the flight from Pittsburgh to Boston]
NP NP	show, give	Show $[NP]$ me] $[NP]$ airlines with flights from Pittsburgh]
$PP_{\text{from}} PP_{\text{to}}$	fly, travel	I would like to fly $[PP]$ from Boston $[PP]$ to Philadelphia
NP PP _{with}	help, load	Can you help [NP me] [PP with a flight]
VPto	prefer, want, need	I would prefer [VPto to go by United airlines]
VPbrst	can, would, might	I can [VPbrst go from Boston]
S	mean	Does this mean [$_S$ AA has a hub in Boston]

Figure 11.6

Subcategorization frames for a set of example verbs.

source: J&M (3d Ed. draft)

Notes:

- traditional "transitive" and "intransitive" distinctions have been replaced by finer-grained subcategorizations, as above
- Not every verb is compatible with every VP subcategorization
 - e.g., "want" can have NP or VP_{to} complements
 - e.g., "find" cannot take VP_{to} complement

Coordination

- Coordinating conjunctions
 - and, but, or
 - can join NPs, VPs, and Ss to form larger constructions of the same type
 - example NP coordination
 - please repeat the flights and costs
 - I need to know the aircraft and the flight number
 - example VP coordination
 - What flights do you have leaving Denver and arriving in San Francisco?
 - example S coordination
 - I am interested in a flight from Dallas to Washington and I'm also interested in going to Baltimore

Today

- Syntax
- Context-Free Grammars
- Grammar Rules for English
- Treebanks
- Grammar Equivalence and Normal Form
- Lexicalized Grammars

Treebank

- A syntactically annotated corpus
- Made possible by a sufficiently robust CFG that ensures that every sentence will have at least one parse
- Typically generated using automated parsers, with human linguists to hand-correct the parses
- Treebank projects
 - Penn Treebank
 - corpora include Brown, Switchboard, ATIS, Wall Street Journal for English, plus various Chinese and Arabic corpora
 - Prague Dependency Treebank for Czech
 - Negra Treebank for German
 - Susanne Treebank for English

Penn Treebank Example: WSJ

```
( (S ('' '')
    (S-TPC-2
      (NP-SBJ-1 (PRP We) )
      (VP (MD would)
        (VP (VB have)
          (S
            (NP-SBJ (-NONE- *-1))
            (VP (TO to)
              (VP (VB wait)
                (SBAR-TMP (IN until)
                  (S
                    (NP-SBJ (PRP we) )
                    (VP (VBP have)
                      (VP (VBN collected)
                        (PP-CLR (IN on)
                          (NP (DT those)(NNS assets))))))))))))
   (, ,) ('' '')
    (NP-SBJ (PRP he) )
    (VP (VBD said)
      (S (-NONE- *T*-2)))
    (...)
```

Figure 11.9 A sentence from the Wall Street Journal portion of the LDC Penn Treebank.

Note the use of the empty -NONE- nodes.

Treebanks as Grammars

- The annotated sentences in a treebank implicitly constitute a grammar
- We can extract the grammar's production rules from these sentences
- But such extracted grammars are very "flat"
 - very many rules
 - very long rules
 - e.g., 4,500 different rules for expanding VPs
 - example:

Rule: $VP \rightarrow VBP PP PP PP PP ADVP PP$

Which comes from VP in:

This mostly happens because we go from football in the fall to lifting in the winter to football again in the spring.

 As a result, it is common to make modifications to a grammar extracted from a treebank

Heads and Head Finding

- Basic idea: each syntactic constituent can be associated with a lexical "head"
 - e.g., that a N is the head of an NP, a V is the head of a VP
 - a basic notion in linguistics since the early 20th century
 - central to grammar formalisms
 - Head-Driven Phrase Structure Grammar
 - dependency relations in grammars
 - in computational linguistics
 - for probabilistic parsing
 - for dependency parsing

Finding Lexical Heads

- A simple model of lexical heads (Charniak 1997, Collins 1999)
 - augment each CFG rule with the word in the phrase that is grammatically the most important
 - heads are passed up the parse tree
 - each nonterminal is annotated with a single word: its lexical "head"

- Basic approach
 - each CFG rule must be augmented to identify one right-side constituent to be the head daughter

Finding Lexical Heads

- Alternative lexicalization approach
 - Parse the sentence
 - After parsing, use a simple set of handwritten rules to "decorate" each node with the appropriate head
- Example: Collins's rule for determining the head of an NP:
 - If the last word is tagged POS, return last-word.
 - Else search from right to left for the first child which is an NN, NNP, NNPS, NX, POS, or JJR.
 - Else search from left to right for the first child which is an NP.
 - Else search from right to left for the first child which is a \$, ADJP, or PRN.
 - Else search from right to left for the first child which is a CD.
 - Else search from right to left for the first child which is a JJ, JJS, RB or QP.
 - Else return the last word

source: J&M (3d Ed. draft)

Collins Lexicalized Parse

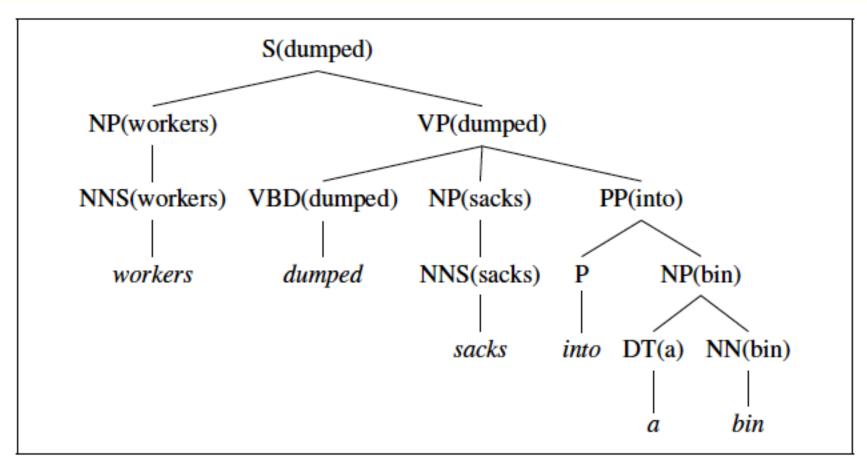


Figure 11.11 A lexicalized tree from Collins (1999).

source: J&M (3d Ed. draft)

Today

- Syntax
- Context-Free Grammars
- Grammar Rules for English
- Treebanks
- Grammar Equivalence and Normal Form
- Lexicalized Grammars

Grammar Equivalence

- Recall: a formal language is a (possibly infinite) set of strings
- It is possible that two different CFGs generate the same language

- weak equivalence
 - 2 grammars generate the same set of strings

- strong equivalence
 - 2 grammars generate the same set of strings
 - assign the same phrase structure to each sentence

Normal Form for Grammars

- Chomsky Normal Form (CNF)
 - productions are of form $A \rightarrow B C$ $A \rightarrow a$
 - no production produces the empty string (i.e., do not have $A \to \varepsilon$)
- Result is binary branching (useful for parsing)
- Any CFG can be converted into a weakly equivalent CNF

Example:
$$A \rightarrow B C D$$

can be converted to
$$A \rightarrow B X$$

 $X \rightarrow C D$

Today

- Syntax
- Context-Free Grammars
- Grammar Rules for English
- Treebanks
- Grammar Equivalence and Normal Form
- Lexicalized Grammars

Lexicalized Grammars

- CFGs have difficulty handling
 - agreement (person, number, tense)
 - subcategorization
 - long-distance dependencies

- "Lexicalized" grammar formalisms attempt to make better use of the lexicon
 - Lexical-Function Grammar (LFG)
 - Head-Driven Phrase Structure Grammar (HPSG)
 - Tree-Adjoining Grammar (TAG)
 - Combinatory Categorial Grammar (CCG)

Combinatory Categorial Grammar

Major elements

- a set of categories
- a lexicon that associates words with categories
- a set of rules for how categories combine in context

Categories

 either atomic elements or single-argument functions that return a category as a value given a desired category as input

Given set of categories \mathcal{C} and a set of atomic elements \mathcal{A} , where $\mathcal{A} \subseteq \mathcal{C}$, we define

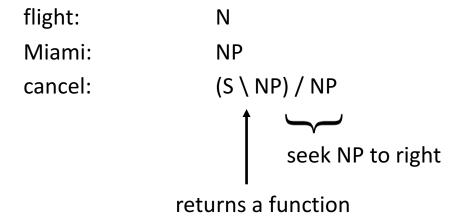
$$(X / Y), (X \setminus Y) \in \mathcal{C}, \text{ if } X, Y \in \mathcal{C}$$

where

 $(X \ / \ Y)$ is the function that seeks a constituent Y to right of X, and returns X $(X \setminus Y)$ is the function that seeks a constituent Y to left of X, and returns X

Categorial Grammar: Lexicon

- The lexicon assigns categories to words
 - can assign to atomic or functional categories
 - a word can be assigned to multiple categories
- Example lexical entries



- The returned function can combine with NP on left to return an S as result
- This formalism captures verb subcategorization information for the transitive verb "cancel"

Categorial Grammar: Rules

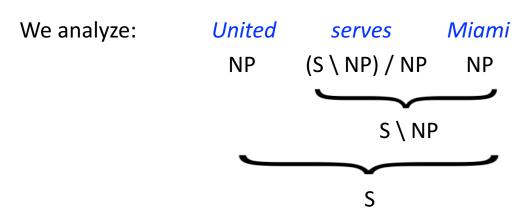
- Categorial grammar rules specify how functions and their arguments combine
- Only 2 rule templates for all categorial grammars

$$X/Y Y \Rightarrow X \leftarrow$$
 forward function application $Y X \setminus Y \Rightarrow X \leftarrow$ backward function application

Example

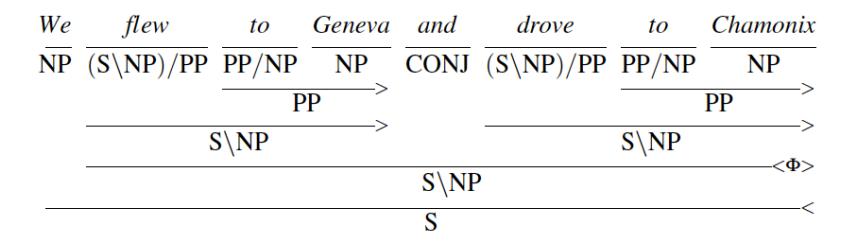
Given: *United* and *Miami* are both simple NPs

serves is transitive with category (S \ NP) / NP



Categorial Grammar: Conjunctions

• Conjunctions can be handled by the simple rule: $X \subset X \to X$



source: J&M (3d Ed. draft), Chap. 11

Combinatory Categorial Grammar

- Basic categorial grammar no more expressive than traditional CFG
 - grammatical facts just basically pushed down into the lexicon
- CCG is more expressive by including operations on functions
 - Composition operations

$$X/Y Y/Z \Rightarrow X/Z$$

 $Y\setminus Z X\setminus Y \Rightarrow X\setminus Z$

- Type raising operations
 - elevates simple categories to the status of functions

$$X \Rightarrow T/(T\backslash X)$$

 $X \Rightarrow T\backslash (T/X)$

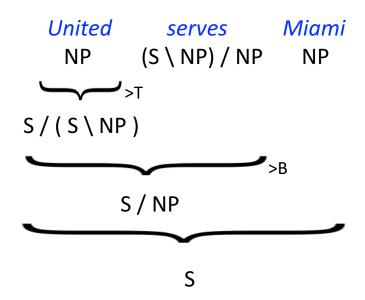
where T can be any atomic or functional category already in the grammar

CCG Example: Type raising

• We can use type raising to reinvent an NP as a function in its own right

$$NP \Rightarrow S/(S \setminus NP)$$

Type-raising alternative for previous example



Note how this provides a left-toright, word-by-word derivation that more closely mirrows how humans process language

CCG: Handling long-distance dependencies

• Consider the relarive clause: "the flight that United diverted"

$$divert$$
 (S\NP)/NP

transitive verb: subject NP to left + direct object NP to right

but here, the direct object NP ("the flight") has been moved to the beginning of the clause

derivation:

$$\frac{\frac{\textit{the}}{NP/N} \frac{\textit{flight}}{N}}{NP} \xrightarrow{\textit{INP} \setminus NP} \frac{\textit{that}}{(NP\backslash NP)/(S/NP)} \frac{\textit{United}}{NP} \xrightarrow{\textit{S}/(S\backslash NP)/NP} \frac{\textit{diverted}}{(S\backslash NP)/NP} \xrightarrow{S/NP} >B} \\ \frac{NP\backslash NP}{NP} \xrightarrow{NP\backslash NP} \xrightarrow{NP} >B$$

source: J&M (3d Ed. draft), Chap. 11

Summary of Formal Grammars

- Formal grammars can represent much of the richness of formal languages
- Traditional CFGs provide a baseline for many language features
- Lexicalized grammars can handle additional features
 - e.g., subcategorization, long-distance dependencies