

PAML Manual (Phylogenetic Analysis by Maximum Likelihood)

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0 Introduction

PAML is a package of programs for phylogenetic analyses of DNA or protein sequences using maximum likelihood (ML). The PAML web page explains what the programs can and cannot do, how to download and compile the programs, and how to report bugs. Those will not be duplicated in this documentation.

The program `baseml` is for analyzing nucleotide sequences. The program `codeml` is formed by merging two old programs: `codonml`, which implements the codon substitution model of Goldman and Yang (1994) for protein-coding DNA sequences, and `aaml`, which implements models for amino acid sequences. These two are now distinguished by a variable named `seqtype` in the control file `codeml.ctl`, that is, 1 for codon sequences and 2 for amino acid sequences. In this document I use `codonml` and `aaml` to mean `codeml` with `seqtype` = 1 and 2, respectively. The programs `baseml`, `codonml`, and `aaml` use similar algorithms to fit models, the difference being that the unit of evolution in the substitution model, referred to as a "site" in the sequence, is a nucleotide, a codon, or an amino acid for the three programs, respectively. Markov process models are used to describe substitutions between nucleotides, codons or amino acids, with substitution rates assumed to be either constant or variable among sites. A *discrete-gamma* model (Yang, 1994c) is used in `baseml`, `codonml` and `aaml` to accommodate rate variation among sites, by which rates for sites come from several (say, four or eight) categories used to approximate the continuous gamma distribution. When rates are variable at sites, the *auto-discrete-gamma* model (Yang, 1995) accounts for correlation of rates between adjacent sites.

The program `basemlg` implements the continuous gamma model of Yang (1993). It is slow and unfeasible for data of >6 or 7 species. The discrete-gamma model in `baseml` is recommended.

General assumptions of the models (programs) are

- Substitutions occur independently in different lineages;
- Substitutions occur independently among sites (except for the auto-discrete-gamma model which account for correlated substitution rates at neighboring sites);
- The process of substitution is described by a time-homogeneous Markov process. Further restrictions may be placed on the structure of the *rate matrix* of the process and lead to different substitution models;
- The process of substitution is stationary. In other words, the frequencies of nucleotides (`baseml`), codons (`codonml`), or amino acids (`aaml`) have remained constant over the time period covered by the data.
- The existence of a molecular clock (rate constancy among lineages) is not necessary but can be imposed. Variation (and dependence) of rates at sites is allowed by the discrete-gamma (or auto-discrete-gamma) models implemented in `baseml`, `codonml` and `aaml`.

The sequences must be aligned. If there are alignment gaps, they will either be removed from all sequences before analysis, with appropriate adjustment to the sequence length (if `cleandata` = 1), or treated as ambiguity characters (if `cleandata` = 0).

Other small programs in the package include `evolver` for simulating sequence data sets, `pamp` for parsimony-based analysis (Yang and Kumar 1996), and `yn00` for estimating synonymous and nonsynonymous substitution rates in pairwise comparisons using the method of Yang and Nielsen (2000).

This document is now mainly an explanation of the control variables in the control files for individual programs. Topics that seem too complicated to explain there are dealt with in a section in the Chapter "Models and Methods".

1 Files in the Package

The following files are included in the package:

Source codes:

```
baseml.c: various models for nucleotide sequences
codeml.c: models for codon (seqtype = 1) and amino acid (seqtype = 2) sequences
pamp.c: parsimony analyses of nucleotide or amino acid sequences
mcmctree.c: Markov chain Monte Carlo algorithm for Bayes estimation of
            phylogenies
evolver.c: simulation of sequence data and comparison of trees
basemlg.c: Nucleotide-based model with (continuous) gamma rates among sites
yn00.c: Estimation of dN and dS by the method of Yang and Nielsen (2000)
treesub.c: a few functions
treespace.c: a few more functions
tools.c: my toolkit
tools.h header file
eigen.c: routines for calculating eigen values and vectors
```

Compiling commands

```
Makefile: make file
paml.cc: batch file for compiling PAML using the cc compiler
paml.gcc: batch file for compiling PAML using the GNU gcc compiler
paml.acc: batch file for compilation PAML using the SUN acc compiler
```

Control files:

```
baseml.ctl: control file for running baseml and basemlg;
codeml.ctl: control file for codeml (i.e., codonml and aaml)
pamp.ctl: control file for pamp
yn00.ctl: control file yn00
mcmctree.ctl: control file for mcmctree
```

Data files for codeml (see the files for details):

```
grantham.dat amino acid distance matrix (Grantham 1974)
miyata.dat amino acid distance matrix (Miyata et al. 1980)
dayhoff.dat Empirical amino acid substitution matrix of Dayhoff et al. (1978)
jones.dat Empirical amino acid substitution matrix of Jones et al. (1992)
mtREV24.dat Empirical amino acid substitution matrix of Adachi and Hasegawa
            (1996b)
mtmam.dat Empirical amino acid substitution matrix for mitochondrial proteins of
            mammals
```

Data files for evolver (see the files for details):

```
MCbase.dat: data file for simulating nucleotide sequences
MCcodon.dat: data file for simulating codon sequences
MCaa.dat: data file for simulating amino acid sequences
```

Example tree structure files:

4s.trees: tree structure file for 4-sequence data
5s.trees: tree structure file for 5-sequence data

Documentations:

paml.readme: readme file
paml.html: paml web page, serving also as part of the manual (html file)
pamlDOC.pdf: this document

Example data sets:

Several example data sets are included. They were used in our papers to test new methods, and are included in the package for error-checking.

brown.nuc: the 895-bp mtDNA data of Brown et al. (1982), used in Yang et al. (1994) and Yang (1994c) to test models of variable rates among sites.

mtprim9.nuc: mitochondrial segment consisting 888 aligned sites from 9 primate species (Hayasaka et al. 1988), used by Yang (1994c) to test the discrete-gamma model and Yang (1995) to test the auto-discrete-gamma models.

abglobin.nuc: the concatenated alpha and beta globin genes, example data for condonml

HIVenvY7.nuc: HIV envelope genes, year 7 data, used by Nielsen and Yang (1998) in developing models of variable selective constraints among sites.

lysozymeSmall.nuc: primate lysozyme genes (Messier and Stewart 1997), analyzed by Yang (1998) in developing tests of positive selection along lineages. This is the "small data set" analyzed in that paper. See the control file lysozyme.ctl for details for specifying the different models.

stewart.aa: lysozyme sequences of mammals (Stewart et al. 1987), used by Yang et al. (1995) to test methods for reconstructing ancestral amino acid sequences.

abglobin.aa: the concatenated alpha- and beta-globins, translated from abglobin.nuc

Which files are needed?

You may copy the executables to a directory containing your data files. Please note that the program codeml may need some of the data files in the package such as grantham.dat, dayhoff.dat, jones.dat, mtREV24.dat, or mtmam.dat. You should probably copy these files together. Other programs do not need such data files apart from the sequence and tree files you specify in the control file.

Note also that the programs produce result files. Some other files with names rub, lnf, rst, or rates may also be created. You should not use these names for your files.

2 Using Programs in the Package

Sequence data format

Have a look at the example data files in the package (*.nuc, *.aa, and *.paup). As long as you get your data file into one of the formats, PAML programs should be able to read it. PAML now has limited support for the NEXUS file format used by PAUP and MacClade. Only the sequence data or trees are read, and command blocks are all ignored. PAML does not deal with comment blocks in the sequence data block, so try to avoid them.

Below is an example of the PHYLIP format (Felsenstein, 1993). The first line contains the number of species and the sequence length (possibly followed by option characters). With `codonml` (`codeml` with `seqtype = 1`), the sequence length in the sequence file refers to the number of nucleotides rather than the number of codons. The only options allowed in the sequence file are I, S, C and G. The sequences may be in either *interleaved* format (option I, example data file `abglobin.nuc`), or *sequential* format (option S, example data file `brown.nuc`). The default option is S. (Option G is used for combined analysis of multiple gene data and is explained below.) The following is an example data set in the sequential format. It has 4 sequences each of 60 nucleotides.

```
4 60
sequence 1
AAGCTTCACCGGCGCAGTCATTCTCATAAT
CGCCCACGGACTTACATCCTCATTACTATT
sequence 2
AAGCTTCACCGGCGCAATTATCCTCATAAT
CGCCCACGGACTTACATCCTCATTATTATT
sequence 3
AAGCTTCACCGGCGCAGTTGTTCTTATAAT
TGCCCACGGACTTACATCATCATTATTATT
sequence 4
AAGCTTCACCGGCGCAACCACCCTCATGAT
TGCCCATGGACTCACATCCTCCCTACTGTT
```

Species names. Do not use special symbols like , : # () in a species name as they may confuse the programs. The maximum number of characters in a species name (LSPNAME) is specified at the beginning of the main programs `baseml.c` and `codeml.c`. The default value is 30. In PHYLIP, exactly 10 characters are used for a species name. You may change the value of LSPNAME to 10 in the source codes if you like. To make this discrepancy less a problem, PAML considers two consecutive spaces as the end of a species name, so that the species name does not have to have exactly 30 (or 10) characters. To make this rule work, you should not have two consecutive spaces *within* a species name. For example the above data set can have the following format too.

```
4 60

sequence 1  AAGCTTCACCGGCGCAGTCATTCTCATAAT
CGCCCACGGACTTACATCCTCATTACTATT

sequence 2  AAGCTTCACCGGCGCAATTATCCTCATAAT
CGCCCACGGACTTACATCCTCATTATTATT
sequence 3  AAGCTTCACC  GGCGCAGTTG  TTCTTATAAT
TGCCCACGGACTTACATCATCATTATTATT
sequence 4  AAGCTTCACCGGCGCAACCACCCTCATGAT
TGCCCATGGACTCACATCCTCCCTACTGTT
```

The second format is useful if the data are concatenated sequences of multiple genes, shown below for an example data set. This sequence has 1000 nucleotides from 4 genes, obtained from concatenating four genes with 100, 200, 300, and 400 nucleotides from genes 1, 2, 3, and 4.

respectively. The "lengths" for the genes must be on the line that starts with G, *i.e.*, on the second line of the sequence file. (This requirement allows the program to determine which of the two formats is being used.) The sum of the lengths for the genes should be equal to the number of nucleotides, amino acids, or codons in the combined sequence for baseml (or basemlg), aaml, and codonml, respectively.

```
5 1000 G
G 4 100 200 300 400
Sequence 1
TCGATAGATAGGTTTTAGGGGGGGGGGTAAAAAAAAA.....
```

The third format applies to protein-coding DNA sequences only (for baseml). You use option characters GC on the first line instead of G alone. The program will then treat the three codon positions differently in the nucleotide-based analysis. It is assumed that the sequence length is an exact multiple of three.

```
5 855 GC
human GTG CTG TCT CCT ...
```

Tree file and representations of tree topology

A *tree structure file* is used when `runmode = 0` or `1`. The file name is specified in the appropriate control file. Two methods for representing a tree topology are used in PAML.

Parenthesis notation: The first is the familiar parenthesis representation, that is used in virtually every phylogenetic software. The species can be represented using either their names or their indexes corresponding to the order of their occurrences in the sequence data file. If species names are used, they have to match exactly those in the sequence data file (including spaces or strange characters). Branch lengths are allowed. The following is a possible tree structure file for a data set of four species (human, chimpanzee, gorilla, and orangutan, occurring in this order in the data file). The first tree is a star tree, while the next four trees are the same.

```
4 5 // 4 species, 5 trees
(1234) // the star tree
((12)34) // species 1 and 2 are clustered together
((1,2),3,4) // Commas are needed with more than 9 species
((human,chimpanzee),gorilla,orangutan);
((human:.1,chimpanzee:.2):.05,gorilla:.3,orangutan:.5);
```

If the tree has branch lengths, some programs may ask you whether you want to use those branch lengths as fixed and estimate other parameters in the substitution model only. You will then have three options: ignore the branch lengths, use them as initial values, and fix them and estimate other parameters.

Whether the tree will be considered rooted or unrooted depends on whether a molecular clock is assumed. Without the clock, the trees are unrooted, and so ((12)34) is the same as (12(34)); with the clock, the trees are rooted and these two trees are different and both are different from (((12)3)4).

Branch labels: Sometimes (such as the local clock models specified by `clock = 2` in baseml and codeml and codon models with different ω s for branches), we need to label the branches. Branch labels are specified in the same way as branch lengths except that the symbol preceding the branch

label is # or \$ rather than : which indicates a branch length. The branch labels are consecutive integers starting from 0, which is the default label and does not have to be specified. For example, the following tree

```
((Hsa_Human, Hla_gibbon) #1, ((Cgu/Can_colobus, Pne_langur), Mmu_rhesus),
(Ssc_squirrelM, Cja_marmoset));
```

is from the tree file `lysozyme.trees`, with branch labels for fitting models of different d_N/d_S ratios (ω) for branches. The internal branch ancestral to human and gibbon has the ratio ω_1 while all other branches have the background ratio ω_0 . This fits the model in table 1C for the small data set of lysozyme genes in Yang (1998). I have found it convenient to create the tree file with labels and read the tree in using [TreeView](#) to check that the tree is right. However, TreeView recognizes labels for internal branches (nodes) only and do not allow the user to add labels. If you don't specify the labels in the tree structure, the program will ask for input from the keyboard. For large trees, this may be hard to use.

If the model requires labelling branches but the tree does not has any branch labels, the program will ask for input from the keyboard. See the explanations of the variable `model` for the program `codonml`.

Representation of tree topology by branches: A second way of representing the tree topology used in PAML is by enumerating its branches. This is mainly used in the result files for outputting the estimated branch lengths. For example, the tree ((12)34) is specified by its 5 branches:

```
5 6, 6 1, 6 2, 5 3, 5 4
```

The nodes in a tree are marked with consecutive natural numbers, with 1, 2, ..., s representing the s known sequences, in the same order as in the data. A number larger than s means an interior node, at which the sequence is unknown. In case some sequences in the data are ancestral to some others, this method is convenient. To use this format in the tree structure file, give the number of branches, and then the branches as specified by the end nodes. For example, the tree in the following `5s.trees` file has 4 branches, with taxon 5 to be the common ancestor of taxa 1, 2, 3, and 4:

```
5 1
4      5 1      5 2      5 3      5 4
```

baseml

The default control file for `baseml` is `basemlctl`, and an example is shown below. Note that spaces are required on both sides of the equal sign, and blank lines or lines beginning with "*" are treated as comments. Options not used can be deleted from the control file.

```
seqfile = brown.nuc * sequence data file name
outfile = mlb * main result file
treefile = brown.trees * tree structure file name

noisy = 3      * 0,1,2,3: how much rubbish on the screen
verbose = 0    * 1: detailed output, 0: concise output
runmode = 0    * 0: user tree; 1: semi-automatic; 2: automatic
                * 3: StepwiseAddition; (4,5):PerturbationNNI

model = 4      * 0:JC69, 1:K80, 2:F81, 3:F84, 4:HKY85, 5:TN93, 6:REV, 7:UNREST
Mgene = 0      * 0:rates, 1:separate; 2:diff pi, 3:diff kapa, 4:all diff

fix_kappa = 0  * 0: estimate kappa; 1: fix kappa at value below
```

```

kappa = 2.5    * initial or fixed kappa

fix_alpha = 1  * 0: estimate alpha; 1: fix alpha at value below
alpha = 0.    * initial or fixed alpha, 0:infinity (constant rate)
Malpha = 0    * 1: different alpha's for genes, 0: one alpha
ncatG = 5     * # of categories in the dG, AdG, or nparK models of rates

fix_rho = 1    * 0: estimate rho; 1: fix rho at value below
rho = 0.      * initial or fixed rho, 0:no correlation
nparK = 0     * rate-class models. 1:rK, 2:rK&fK, 3:rK&MK(1/K), 4:rK&MK

clock = 0     * 0:no clock, 1:clock; 2:local clock; 3:TipDate
nhomo = 0     * 0 & 1: homogeneous, 2: kappa for branches, 3: N1, 4: N2
getSE = 0     * 0: don't want them, 1: want S.E.s of estimates
RateAncestor = 0 * (0,1,2): rates (alpha>0) or ancestral states

Small_Diff = 9e-6
* cleandata = 1 * remove sites with ambiguity data (1:yes, 0:no)?
* ndata = 1
method = 0    * 0: simultaneous; 1: one branch at a time

```

The control variables are described below.

seqfile, **outfile**, and **treefile** specifies the names of the sequence data file, main result file, and the tree structure file, respectively.

noisy controls how much output you want on the screen. If the model being fitted involves much computation, you can choose a large number for **noisy** to avoid loneliness. **verbose** controls how much output in the result file.

runmode = 0 means evaluation of the tree topologies specified in the tree structure file, and **runmode** = 1 or 2 means heuristic tree search by the star-decomposition algorithm. With **runmode** = 2, the algorithm starts from the star tree, while if **runmode** = 1, the program will read a multifurcating tree from the tree structure file and try to estimate the best bifurcating tree compatible with it. **runmode** = 3 means stepwise addition. **runmode** = 4 means NNI perturbation with the starting tree obtained by a parsimony algorithm, while **runmode** = 5 means NNI perturbation with the starting tree read from the tree structure file. The tree search options do not work well, and so use **runmode** = 0 as much as you can. For relatively small data set, the stepwise addition algorithm seems usable.

model specifies the model of nucleotide substitution. See the section Nucleotide substitution models.

Mgene is used in combination with option G in the sequence data file, for combined analysis of data from multiple genes or the three codon positions. More details are given later in the Models and Methods section. Choose 0 if option G is not used in the data file.

fix_kappa specifies whether κ in K80, F84, or HKY85 is given at a fixed value or is to be estimated by iteration from the data. If **fix_kappa** = 1, the value of another variable, **kappa**, is the given value, and otherwise the value of **kappa** is used as the initial estimate for iteration. The variables **fix_kappa** and **kappa** have no effect with JC69 or F81 which does not involve such a parameter, or with TN93 and REV which have two and five rate parameters respectively, when all of them are estimated from the data.

fix_alpha and **alpha** work in a similar way, where **alpha** refers to the shape parameter α of the gamma distribution for variable substitution rates across sites (Yang 1994c). The model of a single rate for all sites is specified as **fix_alpha** = 1 and **alpha** = 0 (0 means infinity), while the (discrete-) gamma model is specified by a positive value for **alpha**, and **ncatG** is then the number of categories for the discrete-gamma model (**baseml**).

fix_rho and **rho** work in a similar way and concern independence or correlation of rates at adjacent sites, where ρ (rho) is the correlation parameter of the auto-discrete-gamma model (Yang 1995). The model of independent rates for sites is specified as **fix_rho** = 1 and **rho** = 0; choosing **alpha** = 0 further means a constant rate for all sites. The auto-discrete-gamma model is specified by positive values for both **alpha** and **rho**. The model of a constant rate for sites is a special case of the (discrete) gamma model with $\alpha = \infty$ (**alpha** = 0), and the model of independent rates for sites is a special case of the auto-discrete-gamma model with $\rho = 0$ (**rho** = 0).

npark specifies nonparametric models for variable and Markov-dependent rates across sites: **npark** = 1 or 2 means several (**ncatG**) categories of independent rates for sites, while **npark** = 3 or 4 means the rates are Markov-dependent at adjacent sites; **npark** = 1 and 3 have the restriction that each rate category has equal probability while **npark** = 2 and 4 do not have this restriction (Yang, 1995). The variable **npark** takes precedence over **alpha** or **rho**.

clock specifies models concerning rate constancy among lineages. **clock** = 0 means no clock. **clock** = 1 means the global clock. **clock** = 2 implements local clock models (Yoder and Yang in press), which assumes that branches in the phylogeny conform with the clock assumption and has the default rate ($r_0 = 1$) except for several pre-defined branches which have different rates. Rates for branches are specified using branch marks in the tree file. **clock** = 3 implements Rambaut (2000)'s TipDate models. Evolution conforms to a global clock but sequences in the data are determined at different dates. The dates are specified at the end of the sequence names, based on Andrew's format. This model has one extra parameter (the mutation rate) than the global clock model (**clock** = 1).

nhomo is for **baseml** only, and concerns the frequency parameters in the F81, F84, HKY85, TN93, or REV models. The option **nhomo** = 1 fits a homogeneous model, but estimates the frequency parameters (π_T , π_C and π_A ; π_G is not a free parameter as the frequencies sum to 1) by maximum likelihood iteration. Normally (**nhomo** = 0) these are estimated by the averages of the observed frequencies. In both cases, you should count 3 free parameters for the base frequencies. The options **nhomo** = 3 or 4, in combination with F84 or HKY85, fit nonhomogeneous models of Yang and Roberts (1995). Substitutions are assumed to follow the pattern of F84 or HKY85, but with different frequency parameters assigned for different branches in the tree, to allow for unequal base frequencies in different sequences. The position of the root then makes a difference to the likelihood, and rooted trees are used. Because of the parameter richness, the model may only be used with small data sets when base frequencies are drastically different in different sequences. Choose **fix_kappa** = 1, which means one common **k** is assumed for all branches. The option **nhomo** = 4 assigns one set of frequency parameters for each node, which are the parameters for the rate matrix along the branch leading to the node or are the initial distribution if the node is the root of the tree. In the output, estimates of the frequency parameters are shown in the order of nodes $n + 1$, $n + 2$, ..., where n is the number of sequences.

nhomo = 2 uses one transition/transversion rate ratio (κ) for each branch in the tree for the K80, F84, and HKY85 models (Yang 1994b; Yang and Yoder 1999).

getSE tells whether we want estimates of the standard errors of estimated parameters. These are crude estimates, calculated by the curvature method, *i.e.*, by inverting the matrix of second derivatives of the log-likelihood with respect to parameters. The second derivatives are calculated by the difference method, and are not always reliable. Even if this approximation is reliable, tests relying on the SE's should be taken with caution, as such tests rely on the normal approximation to the maximum likelihood estimates. The likelihood ratio test should always be preferred. The option is not available and choose **getSE** = 0 when tree-search is performed.

RateAncestor = 1 also works with `runmode = 0` only. For models of variable rates across sites, the program will calculate rates for sites along the sequence (output in the file `rates`) and performs marginal ancestral reconstruction (output in `rst`). For models of one rate for all sites, `RateAncestor = 1` does both marginal and joint ancestral sequence reconstruction. The program lists results site by site. You can also use the variable `verbose` to control the amount of output. If you choose `verbose = 0`, the program will list the best nucleotide at each node for the variable sites only and results for constant sites are suppressed. If `verbose = 1`, the program will list all sites for the best nucleotide at each node. If `verbose = 2`, the program also lists the full posterior probability distribution for each site at each ancestral node (for marginal reconstruction).

Sine the algorithm for joint reconstruction may miss important reconstructions except for small data sets, I have added an option for the user to specify the reconstruction to be evaluated. Specify `RateAncestor = 2`, and you will be prompted to specify the site and the reconstruction to be evaluated.

For nucleotide based (`baseml`) analysis of protein coding DNA sequences (option `GC` in the sequence data file), I have added the calculation of posterior probabilities of ancestral amino acids. In this analysis, branch lengths and other parameters are estimated under a nucleotide substitution model, but the reconstructed nucleotide triplets are examined to infer the most likely amino acid encoded by the triplet. Posterior probabilities for stop codons are small and reset to zero to scale the posterior probabilities for amino acids. To use this option, you need add the control variable `icode` in the control file `baseml.ctl`. This is not listed in the above. The variable `icode` can take a value out of 0, 1, ..., 10, corresponding to the 11 genetic codes included in `paml` (See the control file `codeml.ctl` for the definition of different genetic codes). A nucleotide substitution model that is very close to a codon-substitution model can be specified as follows. You add the option characters `GC` at the end of the first line in the data file and choose `model = 4` (HKY85) and `Mgene = 4`. The model then assumes different substitution rates, different base frequencies, and different transition/transversion rate ratio (κ) for the three codon positions. Ancestral reconstruction from such a nucleotide substitution should be very similar to codon-based reconstruction. (Thanks to Belinda Change for many useful suggestions.)

Small_Diff is a small value used in the difference approximation of derivatives.

cleandata = 1 means sites involving ambiguity characters or alignment gaps are removed from all sequences. This leads to faster calculation. `cleaddata = 0` (default) uses those sites.

method: This variable controls the iteration algorithm for estimating branch lengths under a model of no clock. `method = 0` implements the old algorithm in PAML, which updates all parameters including branch lengths simultaneously. `method = 1` specifies an algorithm newly implemented in PAML, which updates branch lengths one by one. `method = 1` does not work under the clock models (`clock = 1, 2, 3`).

ndata: specifies the number of separate data sets in the file. This variable is useful for simulations. You can use `evolver` to generate 200 replicate data sets, and then set `ndata = 200` and use `baseml` to analyze them.

Output: The output should be self-explanatory. Descriptive statistics are always listed. The observed site patterns and their frequencies are listed, together with the proportions of constant patterns. Nucleotide frequencies for each species (and for each gene in case of multiple gene data) are counted and listed. $\ln(L_{\max})$ is the upper limit of the log likelihood and may be compared with the likelihood for the best (or true) tree under the substitution model to test the model's goodness of fit to data (Goldman, 1993a). You can ignore it if you don't know what it means.

With `getSE = 1`, the S.E.s are calculated as the square roots of the large sample variances and listed exactly below the parameter estimates. Zeros on this line mean errors, either caused by divergence of the algorithm or zero branch lengths. The S.E.s of the common parameters measure the reliability of the estimates. For example, $(\kappa - 1)/SE(\kappa)$, when κ is estimated under K80, can be compared with a normal distribution to see whether there is real difference between K80 and JC69. The test can be more reliably performed by comparing the log-likelihood values under the two models, using the likelihood ratio test. It has to be stressed that the S.E.'s of the estimated branch lengths should not be misinterpreted as an evaluation of the reliability of the estimated tree topology (e.g., Yang, 1994b, Goldman and Yang, 1994).

If the tree file has more than one tree, the programs `baseml` and `codeml` will calculate the bootstrap proportions using the RELL method (Kishino and Hasegawa 1989), as well as the method of Shimodaira and Hasegawa (1999) with a correction for multiple comparison. The bootstrap resampling accounts for possible data partitions (option G in the sequence data file). I did not bother to deal with ties, so if you include the same tree in the tree file more than once, you need to adjust the proportions for those trees yourself. The program `rell`, included in earlier versions, is now removed.

basemlg

`basemlg` uses the same control file `baseml.ctl`, as `baseml`. Tree-search or the assumption of a molecular clock are not allowed and so choose `runmode = 0` and `clock = 0`. Substitution models available for `basemlg` are JC69, F81, K80, F84 and HKY85, and a continuous gamma is always assumed for rates at sites. The variables `ncatG`, `given_rho`, `rho`, `nhomo` have no effect. The S.E.'s of parameter estimates are always printed out because they are calculated during the iteration, and so `getSE` has no effect.

Because of the intensive computation required by `basemlg`, the discrete-gamma model implemented in `baseml` is recommended for data analysis. If you choose to use `basemlg`, you should run `baseml` first, and then run `basemlg`. This allows `baseml` to collect initial values into a file named `in.basemlg`, for use by `basemlg`. Note that `basemlg` implements only a subset of models in `baseml`.

codeml (codonml and aaml)

Since the codon based analysis and the amino acid based analysis use different models, and some of the control variables have different meanings, it may be a good idea to use different control files for codon and amino acid sequences. The default control file for `codeml` is `codeml.ctl`, as shown below.

```
seqfile = stewart.aa * sequence data file name
outfile = mlc * main result file name
treefile = stewart.trees * tree structure file name

noisy = 9 * 0,1,2,3,9: how much rubbish on the screen
verbose = 0 * 1: detailed output, 0: concise output
runmode = 0 * 0: user tree; 1: semi-automatic; 2: automatic
              * 3: StepwiseAddition; (4,5):PerturbationNNI; -2: pairwise

seqtype = 2 * 1:codons; 2:AAs; 3:codons-->AAs
CodonFreq = 2 * 0:1/61 each, 1:F1X4, 2:F3X4, 3:codon table
aaDist = 0 * 0:equal, +:geometric; -:linear, 1-6:G1974,Miyata,c,p,v,a
aaRatefile = mtmam.dat * only used for aa seqs with model=empirical(_F)
                  * dayhoff.dat, jones.dat, mtmam.dat, or your own

model = 2
      * models for codons:
```

```

        * 0:one, 1:b, 2:2 or more dN/dS ratios for branches
* models for AAs or codon-translated AAs:
        * 0:poisson, 1:proportional,2:Empirical,3:Empirical+F
        * 6:FromCodon, 7:AAClasses, 8:REVaa_0, 9:REVaa(nr=189)

NSsites = 0 * 0:one w/1:neutral;2:selection; 3:discrete;4:freqs;
            * 5:gamma;6:2gamma;7:beta;8:beta&w;9:beta&gamma;
            * 10:beta&gamma+1; 11:beta&normal>1; 12:0&2normal>1;
            * 13:3normal>0

icode = 0 * 0:universal code; 1:mammalian mt; 2-10:see below
Mgene = 0 * 0:rates, 1:separate;

fix_kappa = 0 * 1: kappa fixed, 0: kappa to be estimated
kappa = 2 * initial or fixed kappa
fix_omega = 0 * 1: omega or omega_1 fixed, 0: estimate
omega = .4 * initial or fixed omega, for codons or codon-based AAs

fix_alpha = 1 * 0: estimate gamma shape parameter; 1: fix it at alpha
alpha = 0. * initial or fixed alpha, 0:infinity (constant rate)
Malpha = 0 * different alphas for genes
ncatG = 3 * # of categories in dG of NSsites models

fix_rho = 1 * 0: estimate rho; 1: fix it at rho
rho = 0. * initial or fixed rho, 0:no correlation

clock = 0 * 0:no clock, 1:clock; 2:local clock; 3:TipDate
getSE = 0 * 0: don't want them, 1: want S.E.s of estimates
RateAncestor = 0 * (0,1,2): rates (alpha>0) or ancestral states (1 or 2)

Small_Diff = .5e-6
* cleandata = 0 * remove sites with ambiguity data (1:yes, 0:no)?
* ndata = 10
method = 0 * 0: simultaneous; 1: one branch at a time

```

The variables `seqfile`, `outfile`, `treefile`, `noisy`, `Mgene`, `fix_alpha`, `alpha`, `Malpha`, `fix_rho`, `rho`, `clock`, `getSE`, `RateAncestor`, `Small_Diff`, `cleandata`, `ndata`, and `method` are used in the same way as in `baseml.ctl` and are described in the previous section. The variable `seqtype` specifies the type of sequences in the data; `seqtype = 1` means codon sequences (the program is then `codonml`); `2` means amino acid sequences (the program is then `aaml`); and `3` means codon sequences which are to be translated into proteins for analysis.

Codon sequences (`seqtype = 1`)

CodonFreq specifies the equilibrium codon frequencies in codon substitution model. These frequencies can be assumed to be equal ($1/61$ each for the standard genetic code, `CodonFreq = 0`), calculated from the average nucleotide frequencies (`CodonFreq = 1`), from the average nucleotide frequencies at the three codon positions (`CodonFreq = 2`), or used as free parameters (`CodonFreq = 3`). The number of parameters involved in those models of codon frequencies is 0, 3, 9, and 60 (under the universal code), for `CodonFreq = 0, 1, 2, and 3` respectively.

aaDist specifies whether equal amino acid distances are assumed (`= 0`) or Grantham's matrix is used (`= 1`) (Yang et al. 1998).

runmode = -2 performs ML estimation of d_S and d_N in pairwise comparisons. The program will collect estimates of d_S and d_N into the files `2ML.dS` and `2ML.dN`. Since many users seem interested in looking at d_N/d_S ratios among lineages, examination of the tree shapes indicated by branch lengths calculated from the two rates may be interesting although the analysis is *ad hoc*. If your species names have no more than 10 characters, you can use the output distance matrices as input to Phylip programs such as `neighbor` without change. Otherwise you need to edit the files to cut the names short.

The variable **model** concerns assumptions about the d_N/d_S rate ratios (or the w parameters) among branches (Yang 1998; Yang and Nielsen 1998). `model = 0` means one d_N/d_S ratio for all lineages (branches), 1 means one ratio for each branch (the free-ratio model), and 2 means an arbitrary number of ratios (such as the 2-ratios or 3-ratios models). When `model = 2`, you may specify the w ratios for branches using branch labels (see the section on [tree structure file](#)). This option seems rather easy to use. Otherwise, the program will ask the user to input a branch mark for the d_N/d_S ratio assumed for each branch. This should be an integral number between 0 to $k - 1$ if k different d_N/d_S ratios ($\omega_0 - \omega_{k-1}$) are assumed for the branches of the tree. This process may be frustrating if the tree is not very small. I run the program first to let it output the tree topology using the branch representation on the screen. I then prepare the branch labels in a file, say, `in`. Finally I run the program using redirection so that it will read the input from the prepared file

```
codeml < in
```

Redirection is not permitted on a MAC, but you can prepare the branch labels in a file and then copy and paste them into the session running the program. Furthermore, under this model, the variable `fix_omega` fixes the last d_N/d_S ratio (ω_{k-1}) at the value of `omega` specified in the file. This option can be used to test, for example, whether the ratio for a specific lineage is significantly different from one. It should, however, be noted that it is not proper to use the option `model = 1` to estimate d_N/d_S ratios for all branches to find out which ratios are greater than one, and then to use `model = 2` to test whether that difference is significant. This way the hypothesis is derived from the data and is tested using the same data. As a result, you tend to get significant results too often. Check the example data file `lysozymeSmall.nuc` and the control file `lysozyme.ctl` and try to reproduce results published in Yang (1998).

Nssites specifies models that allow the d_N/d_S ratio (w) to vary among sites (Nielsen and Yang 1998; Yang et al. 2000). `Nssites = m` corresponds to model M_m in Yang et al. (2000). The variable `ncatG` is used to specify the number of categories in the w distribution under some models. The values of `ncatG` used to perform our analyses are 3 for M3 (discrete), 5 for M4 (freq), 10 for the continuous distributions (M5: gamma, M6: 2gamma, M7: beta, M8:beta&w, M9:beta&gamma, M10: beta&gamma+1, M11:beta&normal>1, and M12:0&2normal>1, M13:3normal>0). This means M8 will have 11 site classes (10 from the beta distribution plus 1 additional class). The posterior probabilities for site classes as well as the expected w values for sites are listed in the file `rst`, which may be useful to pinpoint sites under positive selection, if they exist. To make it easy to run several `Nssites` models in one go, I compiled a program **codemlsites**, which asks you how many and which models to run at the start of the program. The number of categories used will then match those used in Yang et al. (2000). You are advised to use this program if you are not sure about the value of `ncatG`. The example data set for models of variable w ratios among sites (Nielsen and Yang 1998) is `HIVenvY7.unc`. This is the year 7 data, and the trees are at the end of the data file.

As noted in that paper, some of the models are hard to use, including M12 and M13. Recommended models are 0 (one-ratio), 1 (neutral), 2 (selection), 3 (discrete), 7 (beta), and 8 (beta& w). Some of the models like M2 and M8 are noted to be prone to the problem of multiple local optima. You are advised to run the program twice, once with an `omega` value < 1 and a second time with an `omega` value > 1 , and use the results corresponding to the highest likelihood.

The continuous neutral and selection models of Nielsen and Yang (1998) are not implemented in the program.

icode specifies the genetic code. About a dozen genetic code tables are implemented, with 0 standing for the standard code and 1 for the mammalian mitochondrial code (see notes at the end of `codeml.ctl`).

RateAncestor: For codon sequences, ancestral reconstruction is not implemented for the models of variable d_N/d_S ratios among sites. The output under codon-based models usually shows the encoded amino acid for each codon. The output under "Prob of best character at each node, listed by site" has two posterior probabilities for each node at each codon (amino acid) site. The first is for the best codon. The second, in parentheses, is for the most likely amino acid under the codon substitution model. This is a sum of posterior probabilities across synonymous codons. In theory it is possible although rare for the most likely amino acid not to match the most likely codon.

Output for codon sequences (`seqtype = 1`): The codon frequencies in each sequence are counted and listed in a genetic code table, together with their sums across species. Each table contains six or fewer species. For data of multiple genes (option G in the sequence file), codon frequencies in each gene (summed over species) are also listed. The nucleotide distributions at the three codon positions are also listed. The method of Nei and Gojobori (1986) is used to calculate the number of synonymous substitutions per synonymous site (d_S) and the number of nonsynonymous substitutions per nonsynonymous site (d_N) and their ratio (d_N/d_S). These are used to construct initial estimates of branch lengths for the likelihood analysis but are not MLEs themselves. Note that the estimates of these quantities for the α - and β -globin genes shown in Table 2 of Goldman and Yang (1994), calculated using the MEGA package (Kumar et al., 1993), are not accurate.

Results of ancestral reconstructions (`RateAncestor = 1`) are collected in the file `rst`. Under models of variable d_N/d_S ratios among sites (`NSsites` models), the posterior probabilities for site classes as well as positively selected sites are listed in `rst`.

Amino acid sequences (`seqtype = 2`)

model specifies the model of amino acid substitution: 0 for the Poisson model assuming equal rates for any amino acid substitutions (Bishop and Friday, 1987); 1 for the proportional model in which the rate of change to an amino acid is proportional to the frequency of that amino acid. Model = 2 specifies a class of empirical models, and the empirical amino acid substitution rate matrix is given in the file specified by `aaRatefile`. Files included in the package are for the empirical models of Dayhoff et al. (1978) (`dayhoff.dat`) and Jones et al. 1992 (`jones.dat`) (see Kishino et al., 1990 for the construction). The file `mtmam.dat` has a matrix for mitochondrial proteins estimated by maximum likelihood from a data set of 20 mammals. The `mtREV24` model of the MOLPHY package is also provided (the file `mtREV24.dat`). These two are similar, and the difference is that the former is derived from proteins from mammals only while the latter came from more-diverse species including chicken, fish, frog, and lamprey. Due to differences in the implementation, you may see small differences in log-likelihood values and branch lengths between `aaml` and `protml` in the MOLPHY package. Such differences are normal and you should use the same program to compare different trees. Under the `mtREV24` model, the two programs should give almost identical results.

If you want to specify your own substitution rate matrix, have a look at one of those files, which has notes about the file structure. Other options for amino acid substitution models should be ignored. To summarize, the variables `model`, `aaDist`, `CodonFreq`, `NSsites`, and `icode` are used for codon sequences (`seqtype = 1`), while `model`, `alpha`, and `aaRatefile` are used for amino acid sequences.

runmode also works in the same way as in `baseml.ctl`. Specifying `runmode = -2` will force the program to calculate the ML distances in pairwise comparisons. You can change the following variables in the control file `codeml.ctl`: `aaRatefile`, `model`, and `alpha`.

If you do pairwise ML comparison (`runmode = -2`) and the data contain ambiguity characters or alignment gaps, the program will remove all sites which have such characters from all sequences

before the pairwise comparison if `cleandata = 1`. This is known as "complete deletion". It will remove alignment gaps and ambiguity characters in each pairwise comparison ("pairwise" deletion) if `cleandata = 0`. (In a likelihood analysis of multiple sequences on a phylogeny, alignment gaps are treated as ambiguity characters if `cleandata = 0`, and both alignment gaps and ambiguity characters are deleted if `cleandata = 1`. Note that removing alignment gaps and treating them as ambiguity characters both underestimate sequence divergences. Ambiguity characters in the data make the likelihood calculations quite a bit slower.

Output for amino acid sequences (`seqtype = 2`): The output file is self-explanatory and very similar to the result files for the nucleotide- and codon-based analyses. The models for amino acid substitution based on the PAM matrices of Dayhoff et al. (1978) or Jones et al. (1992) do not involve any parameters in the substitution rate matrix. When `RateAncestor = 1`, results for ancestral reconstruction are in the file `rst`. Calculated substitution rates for sites under models of variable rates for sites are in `rates`.

evolver

The program `evolver` simulates nucleotide, codon, and amino acid sequences with user-specified tree topology, branch lengths, and substitution model and parameters. It generates multiple data sets in one file in either PAML (output `mc.paml`) or PAUP* (output `mc.paup`) format. If you choose the PAUP* format, the program will look for files with the following names: `paupstart` (which the program copies to the start of the data file), `paupblock` (which the program copies to the end of each simulated data set), and `paupend` (which the program incorporate at the end of the file. This makes it possible to use PAUP* to analyze all data sets in one run. Parameters for simulation are specified in three files: `MCbase.dat`, `MCcodon.dat`, and `MCAA.dat` for simulating nucleotide, codon, and amino acid sequences, respectively. Run the default options first and also look at those files as well as the screen output.

This program evolved from the old boring program `listtree` and still has the option of generating random trees from a model of cladogenesis, the birth-death process with species sampling (Yang and Rannala, 1997).

yn00

The program `yn00` implements the method of Yang and Nielsen (2000) for estimating synonymous and nonsynonymous substitution rates between two sequences (d_S and d_N). The method of Nei and Gojobori (1986) is also included. The ad hoc method implemented in the program accounts for the transition/transversion rate bias and codon usage bias, and is an approximation to the ML method accounting for the transition/transversion rate ratio and assuming the F3x4 codon frequency model. We recommend that you use the ML method (`runmode = -2`, `CodonFreq = 2` in `codeml.ctl`) as much as possible even for pairwise sequence comparison.

```
seqfile = abglobin.nuc * sequence data file name
outfile = yn           * main result file
verbose = 0 * 1: detailed output (list sequences), 0: concise output

icode = 0 * 0:universal code; 1:mammalian mt; 2-10:see below
weighting = 0 * weighting pathways between codons (0/1)?
commonf3x4 = 0 * use one set of codon freqs for all pairs (0/1)?
```

The control file `yn00.ctl`, an example of which is shown above, specifies the sequence data file name (`seqfile`), output file name (`outfile`), and the genetic code (`icode`). Sites (codons) involving alignment gaps or ambiguity nucleotides in any sequence are removed from all sequences.

The variable `weighting` decides whether equal weighting or unequal weighting will be used when counting differences between codons. The two approaches will be different for divergent sequences, and unequal weighting is much slower computationally. The transition/transversion rate ratio k is estimated for all sequences in the data file and used in subsequent pairwise comparisons. I hope to add an option to allow k to be estimated for each pair. `commonf3x4` specifies whether codon frequencies (based on the F3x4 model of `codonml`) should be estimated for each pair or for all sequences in the data. Besides the main result file, the program also generates three distance matrices: `2YN.dS` for synonymous rates, `2YN.dN` for nonsynonymous rates, `2YN.t` for the combined codon rate (t is measured as the number of nucleotide substitutions per codon). It should be possible to use those files directly with distance programs such as `NEIGHBOR` in Felsenstein's `PHYLIP` package.

mcmctree

The program `mcmctree` performs Bayesian estimation of phylogenies (Rannala and Yang, 1996; Yang and Rannala, 1997). The birth-death process with species sampling is used to specify the prior distribution of phylogenies ("labeled histories", which are rooted tree topologies with the interior nodes ordered according their associated speciation times), and the posterior probabilities of the labeled histories are compared to select the maximum posterior probability tree. The program implementing the method of Rannala and Yang (1996) is not distributed as the algorithm involves extensive computation. Instead, `mcmctree` implements a refined method (Yang and Rannala 1997), which uses Markov chain Monte Carlo to select candidate labeled histories, and Monte Carlo integration to integrate over the distribution of the ancestral speciation times.

The default control file name is `mcmctree.ctl`, and a sample copy is shown below.

```
seqfile = mtprim9.nuc * sequence data file name
outfile = mcmctree.out * main result file name
treefile = 9s.trees * tree structure file name
LHfile = Lhs * LH file name. read (MCMC=0) or overwritten (MCMC=1)
MCMC = 0 * 0: read LHs from LHfile, 1: use MCMC to generate Lhs
beta = 0.15 * prob{change labeled history}, used only if MCMC=1
delta0 = 1 * small number for MCMC, used only if MCMC=1
delta1 = .2 * smaller number for comparing candidate LHs

model = 2 * 0:JC69, 1:K80, 2:F81, 3:F84, 4:HKY85

kappa = 2. * given kappa and omega in GY94.
alpha = 0 * given alpha, 0:infinity
ncatG = 8 * # of categories in the dG or AdG models of rates

hierarch = 0 * 1:hierarchical; 0:empirical Bayes analysis
birth = 6.7 * lineage birth rate
death = 2.5 * lineage death rate
sample = .06 * sampling proportion
mutate = .24 * mutation rate (# of mutations from root to present)
```

The variables `seqfile`, `outfile`, `treefile`, `model`, `kappa`, `alpha`, and `ncatG` are defined as in `baseml.ctl` for program `baseml`. The program first collects a set of candidate labeled histories. If `MCMC = 0`, the candidate labelled histories are read from the file `LHfile`, while if `MCMC = 1`, they are generated from the Markov chain Monte Carlo, with the Monte Carlo integration over ancestral speciation times evaluated at a low accuracy level (controlled by `delta0`). The program then calculates the (relative) posterior probabilities of these candidate labelled histories, with the Monte Carlo integration evaluated at a higher accuracy level (controlled by `delta1`). The Markov chain moves with probability `beta` to another labelled history of the same tree topology, or to a labelled history of a different tree topology through a nearest neighbor interchange. `hierarch` controls

whether an empirical Bayes analysis or a hierarchical Bayes analysis is to be performed. `birth`, `death`, and `sample` are parameters of the prior distribution specified by the birth-death process with species sampling.

3 Models and Methods

This section provides some background information about the analysis that the programs in the `paml` package perform.

Nucleotide substitution models

Markov process models of nucleotide substitution implemented in PAML include JC69 (Jukes and Cantor, 1969), K80 (Kimura, 1980), F81 (Felsenstein, 1981), F84 (Felsenstein, DNAML program since 1984, PHYLIP Version 2.6), HKY85 (Hasegawa et al., 1985), Tamura and Nei (1993), and REV (Yang, 1994a). The rate matrices of these models are given below

JC69 :

$$Q = \begin{pmatrix} . & 1 & 1 & 1 \\ 1 & . & 1 & 1 \\ 1 & 1 & . & 1 \\ 1 & 1 & 1 & . \end{pmatrix}$$

K80 :

$$Q = \begin{pmatrix} . & k & 1 & 1 \\ k & . & 1 & 1 \\ 1 & 1 & . & k \\ 1 & 1 & k & . \end{pmatrix}$$

F81 :

$$Q = \begin{pmatrix} . & p_C & p_A & p_G \\ p_T & . & p_A & p_G \\ p_T & p_C & . & p_G \\ p_T & p_C & p_A & . \end{pmatrix}$$

F84:

$$Q = \begin{pmatrix} . & (1+k/p_Y)p_C & p_A & p_G \\ (1+k/p_Y)p_T & . & p_A & p_G \\ p_T & p_C & . & (1+k/p_R)p_G \\ p_T & p_C & (1+k/p_R)p_A & . \end{pmatrix}$$

with $p_Y = p_T + p_C$ and $p_R = p_A + p_G$.

HKY85:

$$Q = \begin{pmatrix} . & kp_C & p_A & p_G \\ kp_T & . & p_A & p_G \\ p_T & p_C & . & kp_G \\ p_T & p_C & kp_A & . \end{pmatrix}$$

$$\text{TN93:} \quad Q = \begin{pmatrix} \cdot & k_1 p_C & p_A & p_G \\ k_1 p_T & \cdot & p_A & p_G \\ p_T & p_C & \cdot & k_2 p_G \\ p_T & p_C & k_2 p_A & \cdot \end{pmatrix}$$

$$\text{REV (GTR):} \quad Q = \begin{pmatrix} \cdot & ap_C & bp_A & cp_G \\ ap_T & \cdot & dp_A & ep_G \\ bp_T & dp_C & \cdot & p_G \\ cp_T & ep_C & p_A & \cdot \end{pmatrix}$$

The element q_{ij} ($i \neq j$) represents the rate of substitution from nucleotide i to j , with the diagonals q_{ii} specified by the mathematical requirement that each row of Q sums to zero. The nucleotides are ordered T, C, A, G. The transition probability matrix over time t is then given as $P(t) = \{p_{ij}(t)\} = \exp(Qt)$, where $p_{ij}(t)$ is the probability that nucleotide i will become nucleotide j after time t . The sequence data does not permit separation of rate (Q) and time (t), and so Q specifies relative rates only. In the programs, Q is multiplied by a constant so that the average rate of substitution is 1 when the process is in equilibrium. This scaling means that time t , or the branch length in a tree, is measured by the expected number of nucleotide substitutions per site. Q thus represents the pattern of substitution, while the amount of evolution is reflected in time or the branch length. The frequency parameters p_T, p_C, p_A, p_G (with the sum to be 1) give the equilibrium distribution of the process for the F81, F84, HKY85, TN93 and REV models; the equilibrium distribution under the JC69 and K80 models has equal frequencies (1/4) for the four nucleotides. Parameters a, b, c, d, e in REV, k in F84 or HKY85, and k_1 and k_2 in TN93 may be termed rate ratio parameters. So the JC69, K80, F81, F84, HKY85, TN93 and REV models contain 0, 1, 0, 1, 1, 2, 5 rate ratio parameters respectively, and 0, 0, 3, 3, 3, 3, 3 frequency parameters respectively. Normally the frequency parameters are estimated using the averages of the observed frequencies, which should be very close to the true maximum likelihood estimates if the assumptions of homogeneity and stationarity are acceptable.

Parameter k in the K80 and HKY85 models is equivalent to a/b in the notation of Kimura (1980) and Hasegawa et al. (1985). The present notation is more convenient in a maximum likelihood analysis as the ratio is assumed to be constant for different branches of the tree. F84 is the model implemented in J. Felsenstein's DNAML program. The rate matrix for this model was given by Hasegawa and Kishino (1989), Kishino and Hasegawa (1989), Yang (1994b, 1994c) and Tateno et al. (1994). Thorne et al. (1992) described the transition probability matrix, and Yang (1994c) and Tateno et al. (1994) derived formulae for estimating sequence distances under the model. REV is the general time-reversible process model (also known as GTR; Yang, 1994a; see also Tavare, 1986; Zharkikh, 1994). It is used in baseml only. It seems sufficiently general to enable accurate estimation of the substitution pattern from real data. See Gillespie (1986), Tavare (1986), Rodriguez et al. (1990), Yang (1994a), and Zharkikh (1994) for reviews of substitution models.

Unfortunately there are a few different definitions of the "transition/transversion rate ratio". The worst is the ratio of the observed numbers of transitional and transversional differences between two sequences, without correcting for multiple hits, also known as P/Q in Kimura's (1980) notation (see, e.g., Wakeley 1994). The measure used in baseml is k as specified in the above formulas for K80 or HKY85. In Kimura's (1980) notation, $k = a/b$. A third measure (R) is the ratio averaged over base frequencies; this is the ratio of the expected number of transitions to the expected number of transversions if one observes the substitution process over time. In Kimura's (2000) notation, $R = a/(2b)$. PHYLIP and PAUP* use R and name it the "transition/transversion rate ratio", while referred to k as the "transition/transversion rate parameter". For a general substitution model $Q = \{q_{ij}\}$, k and R are related by the formula

$$R = (p_{TC} + p_{CT} + p_{AG} + p_{GA}) / (p_{TA} + p_{TG} + p_{CA} + p_{CG} + p_{AT} + p_{AC} + p_{GT} + p_{GC}).$$

Special examples are listed in the following table.

Model	Average transition/transversion rate ratio (R)
JC69	$\frac{1}{2}$
K80	$k/2$
F81	$(p_T p_C + p_A p_G) / (p_Y p_R)$
F84	$[p_T p_C (1 + k/p_Y) + p_A p_G (1 + k/p_R)] / (p_Y p_R)$
HKY85	$(p_T p_C + p_A p_G) k / (p_Y p_R)$
TN93	$(p_T p_C k_1 + p_A p_G k_2) / (p_Y p_R)$
REV (GTR)	$(p_T p_{CA} + p_A p_G) / (p_T p_{AB} + p_T p_{GC} + p_C p_{Ad} + p_C p_{Ge})$

The case of no transition-transversion bias is represented by $k = 1$ and $R = \frac{1}{2}$ under K80; $k = 1$ and $R = (p_T p_C + p_A p_G) / (p_Y p_R)$ under HKY85; and $k = 0$ and $R = (p_T p_C + p_A p_G) / (p_Y p_R)$ under F84.

Codon substitution models

The model of Goldman and Yang (1994) specifies the probability of substitution between the sense codons, by using the matrix of amino acid distances of Grantham (1974). The model does not seem to fit real data well, however, and the user is advised to use the following simpler version, which is equivalent to use equal distances for any pair of amino acids. The substitution rate from codon i to codon j is given as

$$q_{ij} = \begin{cases} 0, & \text{if the two codons differ at more than one position,} \\ p_j, & \text{for synonymous transversion,} \\ k p_j, & \text{for synonymous transition,} \\ w p_j, & \text{for nonsynonymous transversion,} \\ w k p_j, & \text{for nonsynonymous transition,} \end{cases}$$

The equilibrium frequency of codon j (p_j) can be considered a free parameter, but can also be calculated from the nucleotide frequencies at the three codon positions (control variable CodonFreq). Under this model, the relationship holds that $w = d_N/d_S$, the ratio of nonsynonymous/synonymous substitution rates. This model forms the basis for more sophisticated models implemented in codeml, such as those that allow the w ratio to vary among branches in the phylogeny (Yang 1998; Yang and Nielsen 1998) implemented through the variable model, and those that allow the w ratio to vary among sites (among codons or amino acids in the protein), implemented through the variable Nssites.

Amino acid substitution models

“Empirical” models based on the Dayhoff substitution matrix (model = 2) or its updated version of Jones et al. (1992) are constructed using the same strategy. The transition probability matrix over a very short time period such as one PAM, i.e., $P(0.01)$, is used to approximate the matrix of instantaneous rates (Q). The empirical matrices of Dayhoff et al. (1978) and Jones et al. (1992) were made to satisfy the reversibility condition, that is,

$$p_i q_{ij} = p_j q_{ji}$$

for any i and j , so that my implementations may be slightly different from that of Kishino et al. (1990). These models assume a fixed pattern of amino acid substitution. The package also include two similar empirical models for mitochondrial proteins. The first is given by the file `mtREV24.dat` and is the mtREV24 model of Adachi and Hasegawa (1996a, b) estimated from a diverse range of species including mammals, chicken, frog, fish, and lamprey. The matrix was estimated by maximum likelihood from real data. The second is given by the file `mtmam.dat` and is estimated from 20 mammalian species using maximum likelihood under the REV model with variable rates among sites (Yang et al. 1998). You can check those files for more details, or if you want to supply your own empirical matrix.

"Mechanistic" models of amino acid substitution requires consideration of both the mutational distance between the amino acids as determined by the locations of their encoding codons in the genetic code table, and the effects that the potential change may have on the structure and function of the protein, which may be related to the physical, chemical and structural differences between amino acids. It seems natural that such a model should be formulated at the level of codons. The program `aaml` implements a few such models, specified by the variable `aaDist`.

Models of variable substitution rates across site (see Yang 1996b for review) are implemented for both nucleotide (`baseml`) and amino acid (`aaml`) sequences. Although the option variables such as `fix_alpha` and `alpha` are also available for codon models (`codonml`), the gamma model for codons is unrealistic as it applies the same gamma rate to both synonymous and nonsynonymous substitutions, with their rate ratio held constant among sites. You are recommended to use the `Nssites` models instead, which assume homogeneous synonymous rates but variable nonsynonymous rates.

Models for combined analyses of heterogeneous data (multiple genes or codon positions)

Several models are described by Yang (1996a) and implemented in programs `baseml` and `codeml` (`codonml` and `aaml`) for analyzing heterogeneous data sets (such as those of multiple genes or different codon positions). The implementation and description below refer to the case of multiple genes, but in the case of nucleotide-based models (`baseml`), the method can be used to analysed data of different codon positions. These models account for different aspects of heterogeneity among the different data sets and are useful for testing hypotheses concerning the similarities and differences in the evolutionary process of different data sets.

The simplest model which assumes complete homogeneity among genes can be fitted by concatenating different genes into one sequence without using the option `G` (and by specifying `Mgene = 0` in the control file). The most general model is equivalent to a separate analysis. This can be done by fitting the same model to each data set (each gene), but can also be done by specifying `Mgene = 1` with the option `G` in the combined data file. The sum of the log-likelihood values over different genes is then the log likelihood of the most general model considered here. Models accounting for some aspects of the heterogeneity of multiple genes are fitted by specifying `Mgene` in combination with the option `G` in the sequence data file. `Mgene = 0` means a model that assumes different substitution rates but the same pattern of nucleotide substitution for different genes. `Mgene = 2` means different frequency parameters for different genes but the same rate ratio parameters (k in the K80, F84, HKY85 models or the rate parameters in the TN93 and REV models). `Mgene = 3` means different rate ratio parameters and the same frequency parameters. `Mgene = 4` means both different rate ratio parameters and different frequency parameters for different genes. Parameters and assumptions made in these models are summarized in the following table, with the HKY85 model used as an example. When substitution rates are assumed to vary from site to site, the control variable `Malpha` specifies whether

one gamma distribution will be applied across all sites ($M_{\alpha} = 0$) or a different gamma distribution is used for each gene (or codon position).

Sequence file	Control file	Parameters across genes
No G	Mgene = 0	everything equal
Option G	Mgene = 0	the same κ and π , but different c_s (proportional branch lengths)
Option G	Mgene = 2	the same κ , but different π_s and c_s
Option G	Mgene = 3	the same π , but different κ_s and c_s
Option G	Mgene = 4	different κ , π_s , and c_s
Option G	Mgene = 1	different κ , π_s , and different (unproportional) branch lengths

The different c_s for different genes mean that branch lengths estimated for different genes are proportional. Parameters p represent the equilibrium nucleotide frequencies, which are estimated using the observed frequencies ($n_{\text{homo}} = 0$). The transition/transversion rate ratio k in HKY85 can be replaced by the two or five rate ratio parameters under the TN93 or REV models, respectively. The likelihood ratio test can be used to compare these models, using an approach called the analysis of deviance, which is very similar to the more familiar analysis of variance.

Global and local clocks, and dated sequences

PAML (baseml and codeml) implements three ML models regarding rate constancy among lineages. `clock = 0` means no clock and each branch has an independent rate. For a binary tree with n species (sequences), this model has $(2n - 3)$ parameters (branch lengths). `clock = 1` means the global clock, and all branches have the same rate. This model has $(n - 1)$ parameters corresponding to the $(n - 1)$ internal nodes in the binary tree. So a test of the molecular clock assumption, which compares those two models, should have d.f. = $n - 2$.

Between those two extremes are the local clock models, specified by `clock = 2` (Yoder and Yang in press), which assume that branches in the phylogeny conform with the clock assumption and has the default rate ($r_0 = 1$) except for several pre-defined branches which have different rates. Rates for branches are specified using branch labels in the tree file, and, if they are not, can be inputted from the keyboard. For example, the tree (((1,2) #1, 3), 4) specifies rate r_1 for the branch ancestral to species 1 and 2 while all other branches have the default rate r_0 , which does not have to be specified. The user need to specify which branch has which rate, and the program estimates the unknown rates (such as r_0 and r_1 in the above example). You need to be careful when specifying rates for branches to make sure that all rates are estimable by the model; if you specify too many rate parameters, especially for branches around the root, it may not be possible to estimate all of them and you will have a problem with identifiability. The number of parameters for a binary tree in the local clock model is $(n - 1)$ plus the number of extra rate parameters for branches. In the above tree of 4 species, you have only one extra rate parameter r_1 , and so the local clock model has $(n - 1) + 1 = n = 4$ parameters. Of course the no-clock model has 5 parameters while the global clock has 3 parameters for that tree.

The option `clock = 3` implements Andrew Rambaut's TipDate models (Rambaut 2000). For viral sequences determined in different years, a global molecular clock model can be fitted to the data with the dates of sequence determination used in the likelihood calculation. The dates are specified at the end of the sequence names, based on Andrew's format. See the file `exampleTipDate.phy` for the format, which is from Rambaut's package TipDate <<http://evolve.zps.ox.ac.uk/software/TipDate/main.html>>. This model has one extra parameter (the mutation rate) than the global clock model (`clock = 1`). Thanks to Andrew for help with the implementation.

Reconstruction of ancestral sequences

Nucleotides or amino acids of extinct ancestors can be reconstructed using information of the present-day sequences. Parsimony reconstructs ancestral character states by the criterion that the number of changes along the tree at the site is minimized. Algorithms based on this criterion were developed by Fitch (1971) and Hartigan (1973), and are implemented in the program `pamp`. The likelihood approach uses branch lengths and the substitution pattern for ancestral reconstruction. It was developed by Yang et al. (1995) and is implemented in `baseml` for nucleotide sequences and in `aaml` (`codeml.c` with `seqtype = 2`) for amino acid sequences. Results are collected in the file `rst`.

Marginal reconstruction: This approach assigns a nucleotide or amino acid to an interior node at a site according to its posterior probabilities (eq. 4 in Yang et al. 1995). The algorithm implemented in `paml` works under both the model of a constant rate for sites and the gamma-rates model. If `verbose = 1`, the output will include the full probability distribution at each node at each site.

Joint reconstruction: This approach considers the assignment of a set of characters to all interior nodes at a site as a reconstruction (eq. 2 in Yang et al. 1995), and the implementation in `paml` works under the model of a constant rate for sites only. (It should work under models for multiple genes or data partitions as well.) The program makes a guess at the likely character states at the interior nodes of the tree, and then uses those to generate possible reconstructions to be evaluated. The current rules are: (1) with fewer than 15 interior nodes in the tree for nucleotide sequences or 7 for amino acid sequences, the program evaluates all reconstructions that can be generated by assigning to each interior node all nucleotides (or amino acids) that are observed at the site in any of the sequences; (2) for even larger trees, the program uses the parsimony algorithm to generate the equivocal character states at each interior node, and then evaluates reconstructions that can be generated from those equivocal states. The strategy may miss important reconstructions when the data contain more than several species; an indicator of the occurrence of this problem is that the sum of probabilities for the listed reconstructions at a site is not close to one. Note that the problem is possible failure to evaluate some reconstructions with high probabilities, but the probabilities for the evaluated reconstructions are correct. An option (`RateAncestor = 2`) allows the user to specify the site and reconstruction to be evaluated.

The marginal and joint approaches are expected to produce very similar results. Since the marginal reconstruction is always reliable and works with models of variable rates among sites, it is recommended for data analysis.

Iteration algorithms for parameter estimation

The maximum likelihood method estimates parameters by maximizing the likelihood function. This is multi-dimensional optimisation problem that has to be solved numerically (except for the simplest possible case; see Yang 2000). PAML implements two iteration algorithms. The first one (`method = 0`) is a general-purpose minimization algorithm that deals with upper and lower bounds for parameters but not general equality or inequality constraints. The algorithm requires first derivatives, which are calculated using the difference approximation, and accumulates information about the curvature (second derivatives) during the iteration using the BFGS updating scheme. At each iteration step, it calculates a search direction, and does a one-dimensional search along that direction to determine how far to go. At the new point, the process is repeated, until there is no improvement in the log-likelihood value, and changes to the parameters are very small. The algorithm updates all parameters including branch lengths simultaneously.

Another algorithm (method = 1) works if an independent rate is assumed for each branch (clock = 0) (Yang submitted). This algorithm cycles through two phases. Phase I estimates branch lengths with substitution parameters (such as the transition/transversion rate ratio k and the gamma shape parameter a) fixed. Phase II estimates substitution parameters using the BFGS algorithm, mentioned above, with branch lengths fixed. The procedure is repeated until the algorithm converges. In phase I of the algorithm, branch lengths are optimized one at a time. The advantage of the algorithm is that when the likelihood is calculated for different values of one single branch length, as is required when that branch length only is optimised, much of likelihood calculations on the phylogeny is the same and can be avoided by storing intermediate results in the computer memory. A cycle is completed after all branch lengths are optimized. As estimates of branch lengths are correlated, several cycles are needed to achieve convergence of all branch lengths in the tree, that is, to complete phase I of the algorithm.

If branch lengths are the only parameters to be estimated, that is, if substitution parameters are fixed, the second algorithm (method = 1) is much more efficient. Thus to perform heuristic tree search using stepwise addition, for example, you are advised to fix substitution parameters (such as k and a). The second algorithm is also more efficient if the data contain many sequences so that the tree has many branch lengths.

Tree search algorithms

One heuristic tree search algorithm implemented in `baseml`, `codonml` and `aaml` is a divisive algorithm, called "star-decomposition" by Adachi and Hasegawa (1996a). The algorithm starts from either the star tree (`runmode` = 2) or a multifurcation tree read from the tree structure file (`runmode` = 1). The algorithm joins two taxa to achieve the greatest increase in log-likelihood over the star-like tree. This will reduce the number of OTUs by one. The process is repeated to reduce the number of OTUs by one at each stage, until no multifurcation exists in the tree. This algorithm works either with or without the clock assumption. The stepwise addition algorithm is implemented with the option `runmode` = 3. Options `runmode` = 4 or 5 are used for nearest neighbor interchanges, with the initial tree determined with stepwise addition under the parsimony criterion (`runmode` = 4) or read from the tree structure file (`runmode` = 5). The results are self-explanatory.

Besides the fact that ML calculations are slow, my implementations of these algorithms are crude. If the data set is small (say, with <20 or 30 species), the stepwise addition algorithm (`runmode` = 3) appears usable. Choose `method` = 1 to use the algorithm that updates one branch at a time, and fix any substitution parameters (such as k and a) so that only branch lengths are estimated. While estimating k during the stepwise addition algorithm slows things down, estimating a in the algorithm may generate non-sensible results, since use of very few sequences at the start of the stepwise addition algorithm may lead to non-sensible a estimates.

4 Technical Notes

This section contains some technical notes for running PAML programs.

The `rub` file recording the progress of iteration

If you use a large value for the variable `noisy` (say >2), the programs `baseml` and `codeml` will log output to the screen, indicating the progress of the iteration process, i.e., the minimization of the negative log-likelihood. They will also print in the `rub` file, the size (norm) of the gradient or search direction (h), the negative log likelihood, and the current values of parameters for each round of

iteration. A healthy iteration is indicated by the decrease of both h and the negative log likelihood, and h is particularly sensitive. If you run a complicated model hard to converge or analyzing a large data set with hundreds or thousands of sequences, you may switch on the output. You can check this file to see whether the algorithm has converged. A typical symptom of failure of the algorithm is that estimates of parameters are at the preset boundaries, with values like 2.00000, 5.00000. When `method = 1`, the output in the `rub` file lists the log likelihood and parameter estimates only.

How to specify initial values

You may change values of parameters in the control file such as `kappa`, `alpha`, `omega`, etc. to start the iteration from different initial values. Initial values for the second and later trees are determined by the program, and so you do not have much control in this way.

You can collect initial values into a file called `in.baseml` if you are running `baseml` or `in.codeml` if you are running `codeml`. When this file exists, the program will read initial values from it. This may be useful if the iteration is somehow aborted, and then you can collect current values of parameters from the file `rub` into this file of initial values, so that the new iteration can have a better start and may converge faster. The file of initial values may also be useful if you experience problems with convergence. If you have already obtained parameter estimates before and do not want the program to re-estimate them and only want to do some analysis base on those estimates such as reconstructing ancestral sequences, insert -1 before the initial values.

The `rub` file records the iteration process and has one line for each round of iteration. Each line lists the current parameter values after the symbol `x`; you can copy those numbers into the file of initial values, and if you like, change one or a few of the parameter values too.

Fine-tuning the iteration algorithm

The iteration algorithm uses the difference approximation to calculate derivatives. This method changes the variable (x) slightly, say by a small number e , and see how the function value changes. One such formula is $df/dx = [f(x + e) - f(x)]/e$. The small number e should be small to allow accurate approximation but should not be too small to avoid rounding errors. You can change this value by adding a line in the control files `basemlctl` or `codemlctl`

```
Small_Diff = 1e-6
```

The iteration is rather sensitive to the value of this variable, and reasonable values are between $1e-5$ and $1e-7$. This variable also affects the calculation of the SE's for parameters, which are much more difficult to approximate than the first derivatives. If the calculated SE's are sensitive to slight change in this variable, they are not reliable.

If you compile the source codes, you can also change the lower and upper bounds for parameters. I have not put these variables into the control files. See the section on [Adjustable variables](#).

Adjustable variables in the source codes

This section is relevant only if you compile the source codes yourself. The maximum values of certain variables are listed as constants in uppercase at the beginning of the main programs (`baseml.c`, `basemlg.c`, `codeml.c`). These values can be raised without increasing the memory requirement by too much.

NS: maximum number of sequences (species)
LSPNAME: maximum number of characters in a species name
NGENE: maximum number of "genes" in data of multiple genes (option G)
NCATG: maximum number of rate categories in the (auto-) discrete-gamma model (baseml.c, codeml.c)

You may need to change the value of LSPNAME. Other variables that may be changed include the bounds for parameters, specified at the beginning of the function testx or SetxBound in the main programs (baseml.c and codeml.c). For example, these variables are defined in the function SetxBound in codeml.c:

```
double tb[]={.0001,9}, rgeneb[]={0.1,99}, rateb[]={1e-4,999};  
double alphab[]={0.005,99}, rhob[]={0.01,0.99}, omegab[]={.001,99};
```

The pairs of variables specify lower and upper bounds for variables (tb for branch lengths, rgeneb for relative rates of genes used in multiple gene analysis, alphab for the gamma shape parameter, rhob for the correlation parameter in the auto-discrete-gamma model, and omegab for the d_N/d_S ratio in codon based analysis).

PowerMAC memory allocation problem

When your data set is large, you may see a message like "oom ", which stands for "out of memory". If you think your data set should be manageable by the program/computer, you can change the memory that is allowed by the operating system for the program to use. If you select the file name and choose "File-Get information", you should see a pop up window. You can increase numbers in this window.

MS Windows version window auto-close

Run the Windows version from a DOS/Windows command box by typing the program names such as baseml. Do not run the programs by double clicking on the file names from Windows 95/98/2000/NT Explorer. Otherwise, the window will close automatically when the programs finish or abort and you won't have the chance to see any error messages.

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