# Project Euler #252: Convex Holes

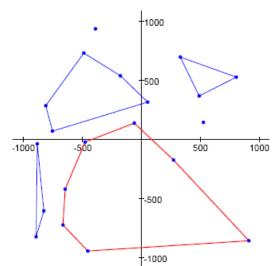


This problem is a programming version of Problem 252 from projecteuler.net

Given a set of points on a plane, we define a convex hole as a strictly convex polygon such that:

- 1. the vertices are from the set of given points;
- 2. the polygon is convex;
- none of the elements of the given set lie in the interior of the polygon. Non-vertex elements may lie on the boundary;
- 4. no three consecutive vertices are colinear.

As an example, the image below shows a set of twenty points and a few such convex holes. The convex hole shown as a red heptagon has an area equal to 1049694.5 square units, which is the highest possible area for a convex hole on the given set of points.



For our example, we used the first 20 points  $(T_{2k-1},T_{2k})$ , for  $k=1,2,\ldots,20$ , produced with the pseudo-random number generator (given  $S_0=290797$  and M=50515093):

$$S_{n+1} = S_n^2 \mod M$$
  
 $T_n = (S_n \mod 2000) - 1000$   
i.e. (527, 144), (-488, 732), (-454, -947), ...

Given integers M,  $S_0$  and N, generate N ordered pairs with the pseudo-random sequence with parameters M and  $S_0$ . Remove duplicate points. What is the maximum area of a convex hole with vertices from this set of points? How many different convex holes are there?

#### Input Format

Each test file contains 3 lines containing the integer values of N,  $S_0$  and M.

#### **Constraints**

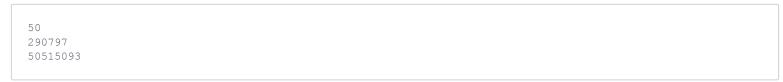
• 
$$0 < N < 450$$

- $0 < M \le 100000000$
- $0 < S_0 < M$

### **Output Format**

Print your solution in two lines. On the first line print the maximum convex hole area with exactly one digit after the decimal point. On the second line print the integer value of the number of convex holes.

## Sample Input 0



## Sample Output 0

```
584388.5
16186
```

# **Explanation 0**

All 50 of the generated points are unique. The largest area convex hole has area 584388.5 and there are 16186 different convex holes.