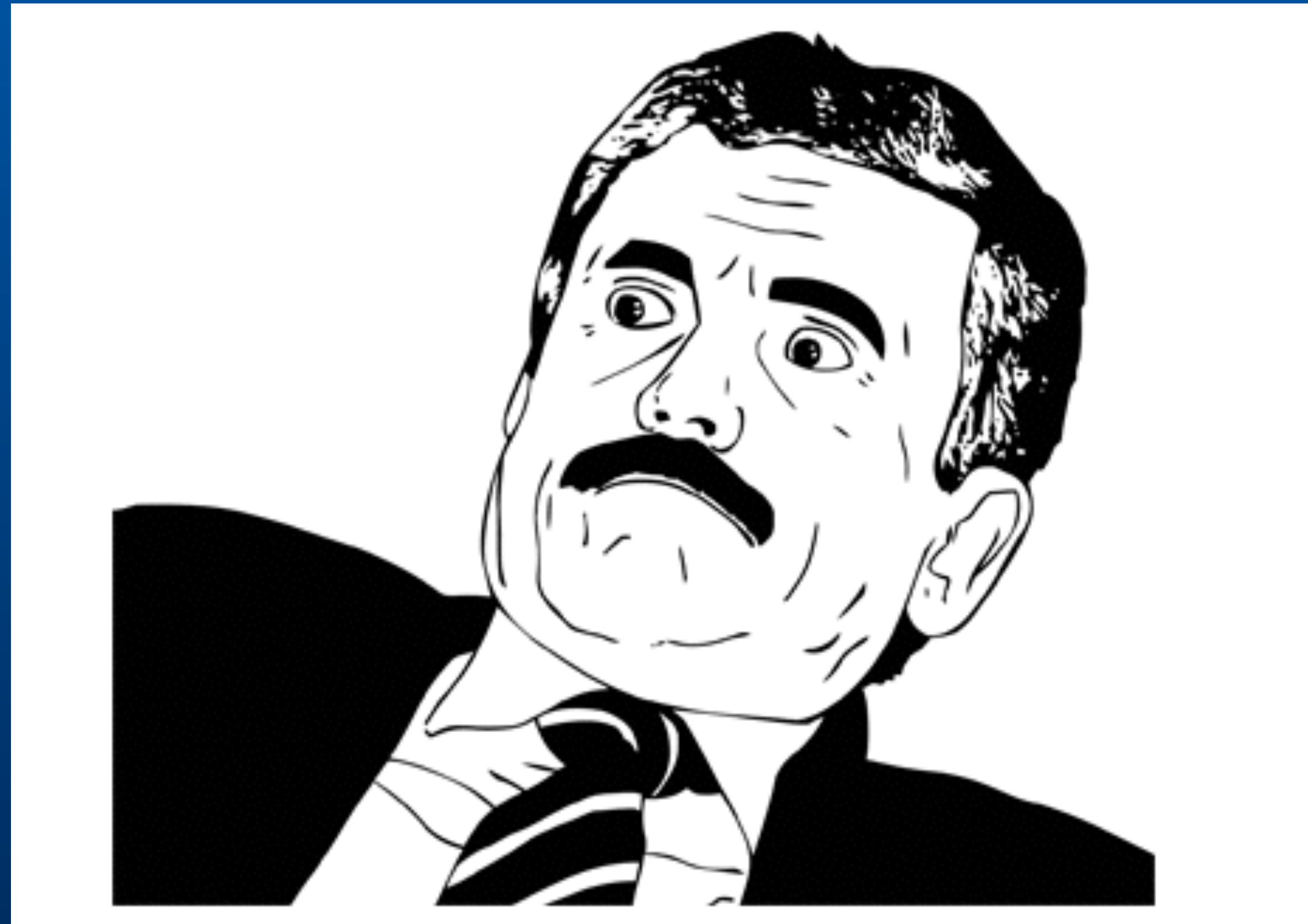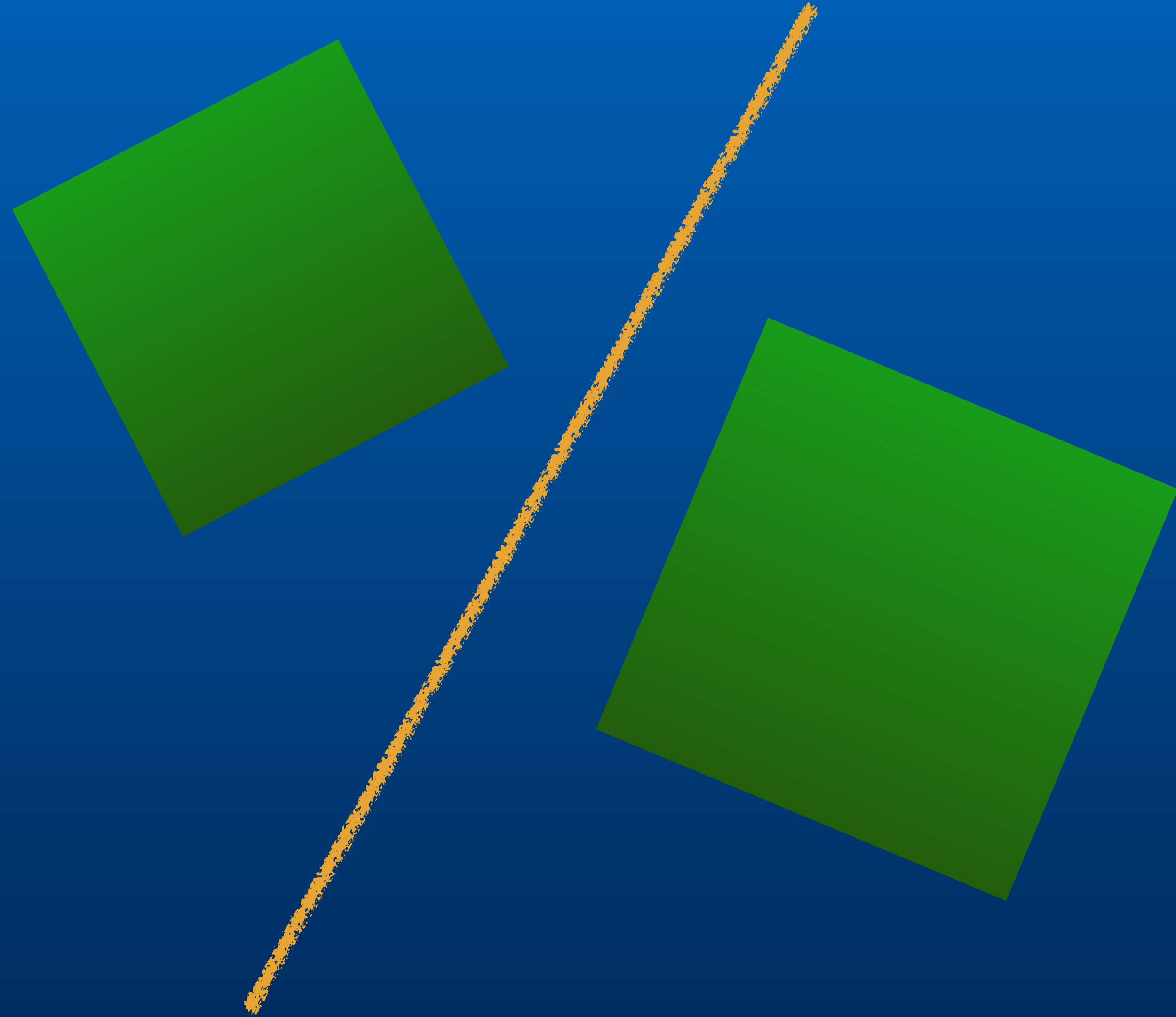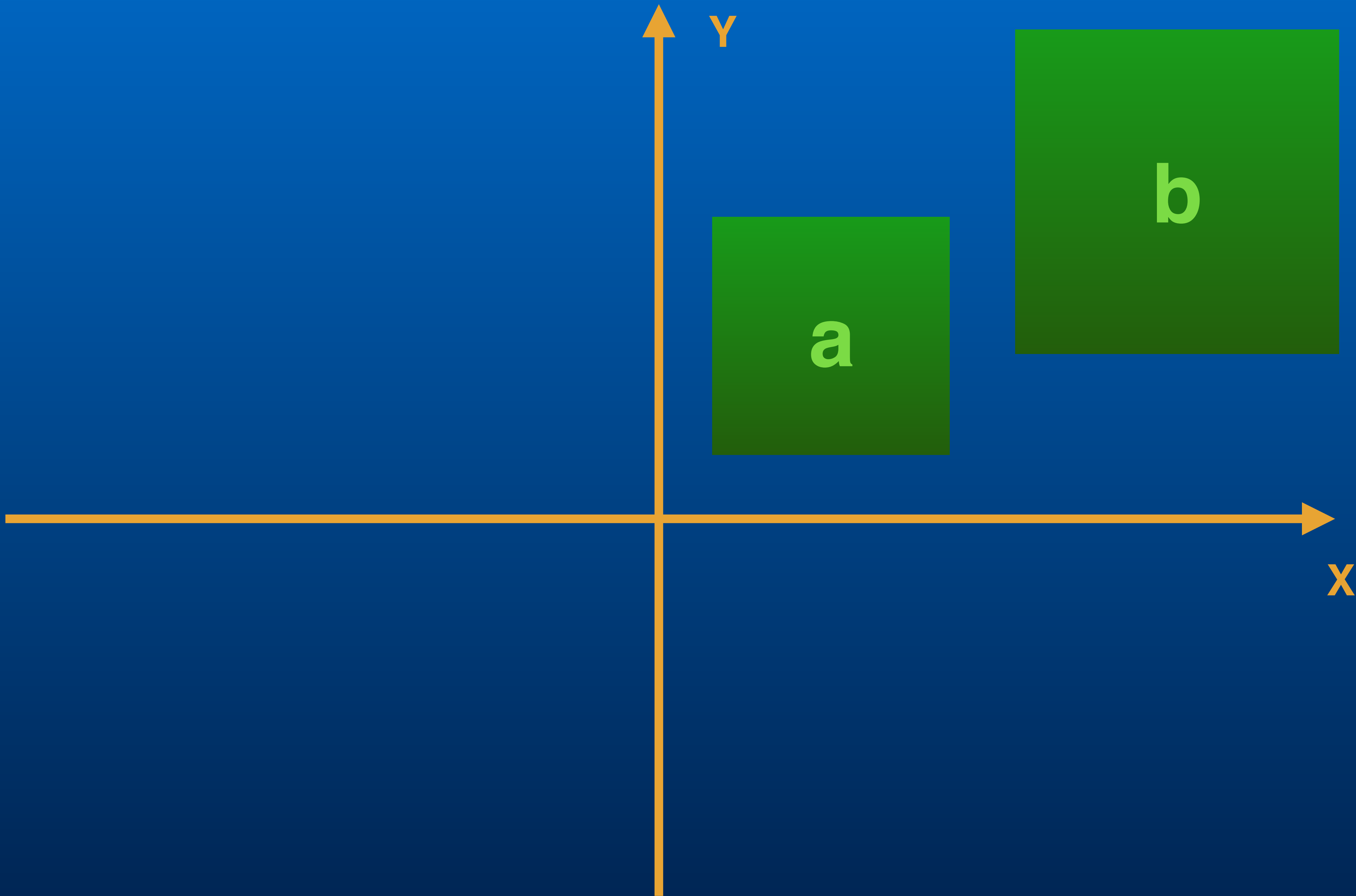# Advanced 2D collision detection.
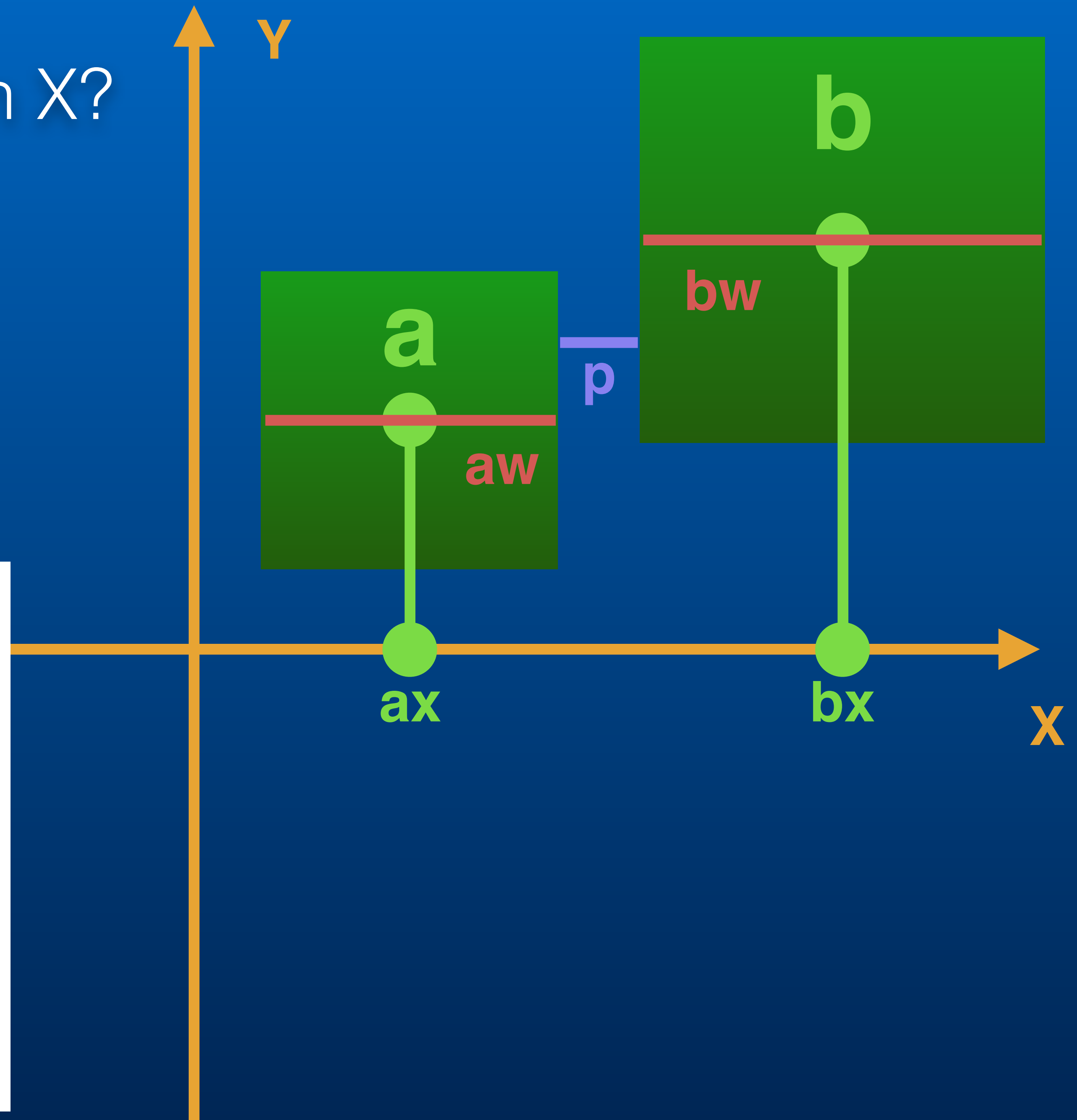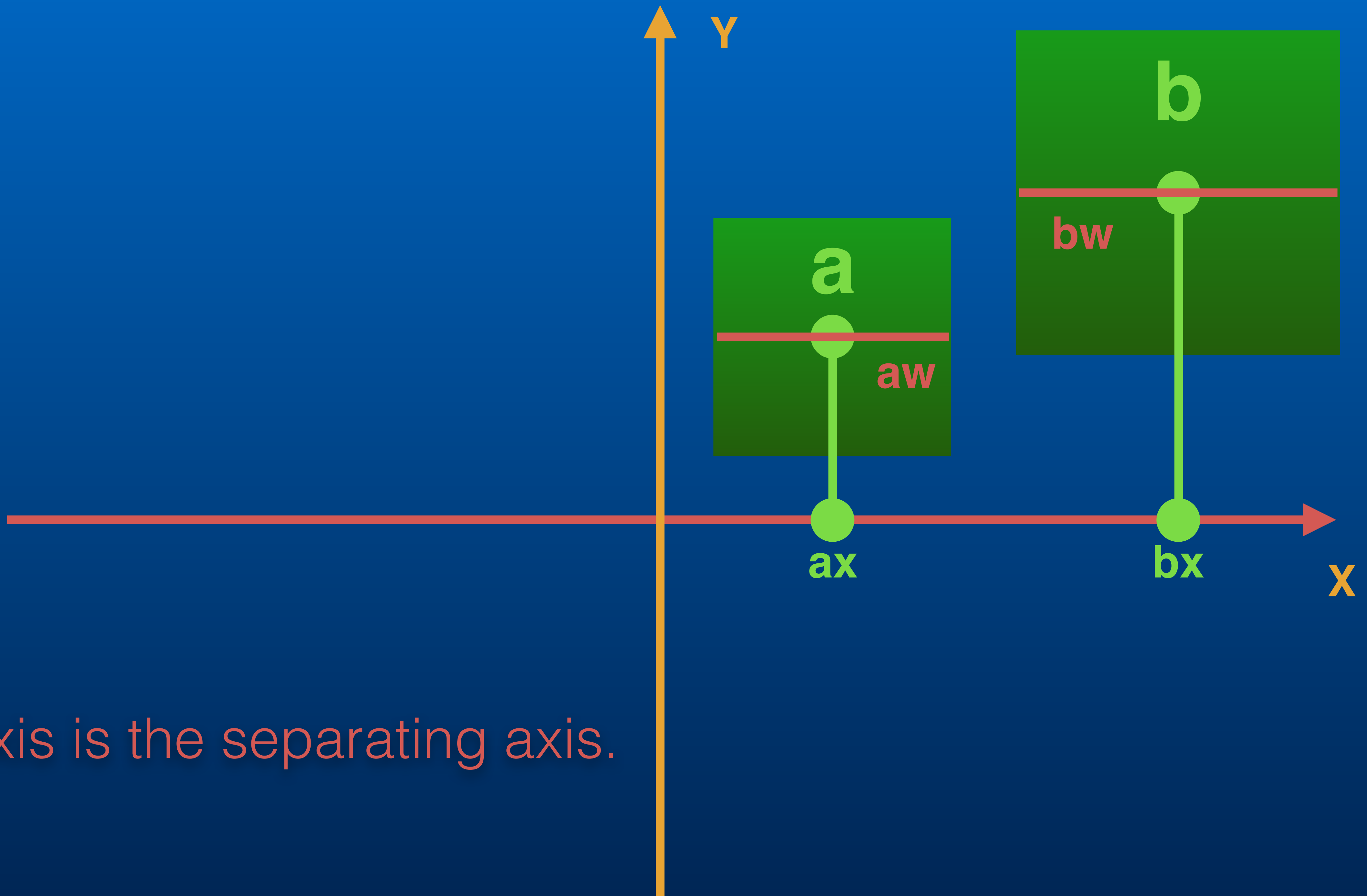
Separating axis theorem (SAT)

How far away are they on X?

$$p = |x_1 - x_2| - \frac{w_1 + w_2}{2}$$
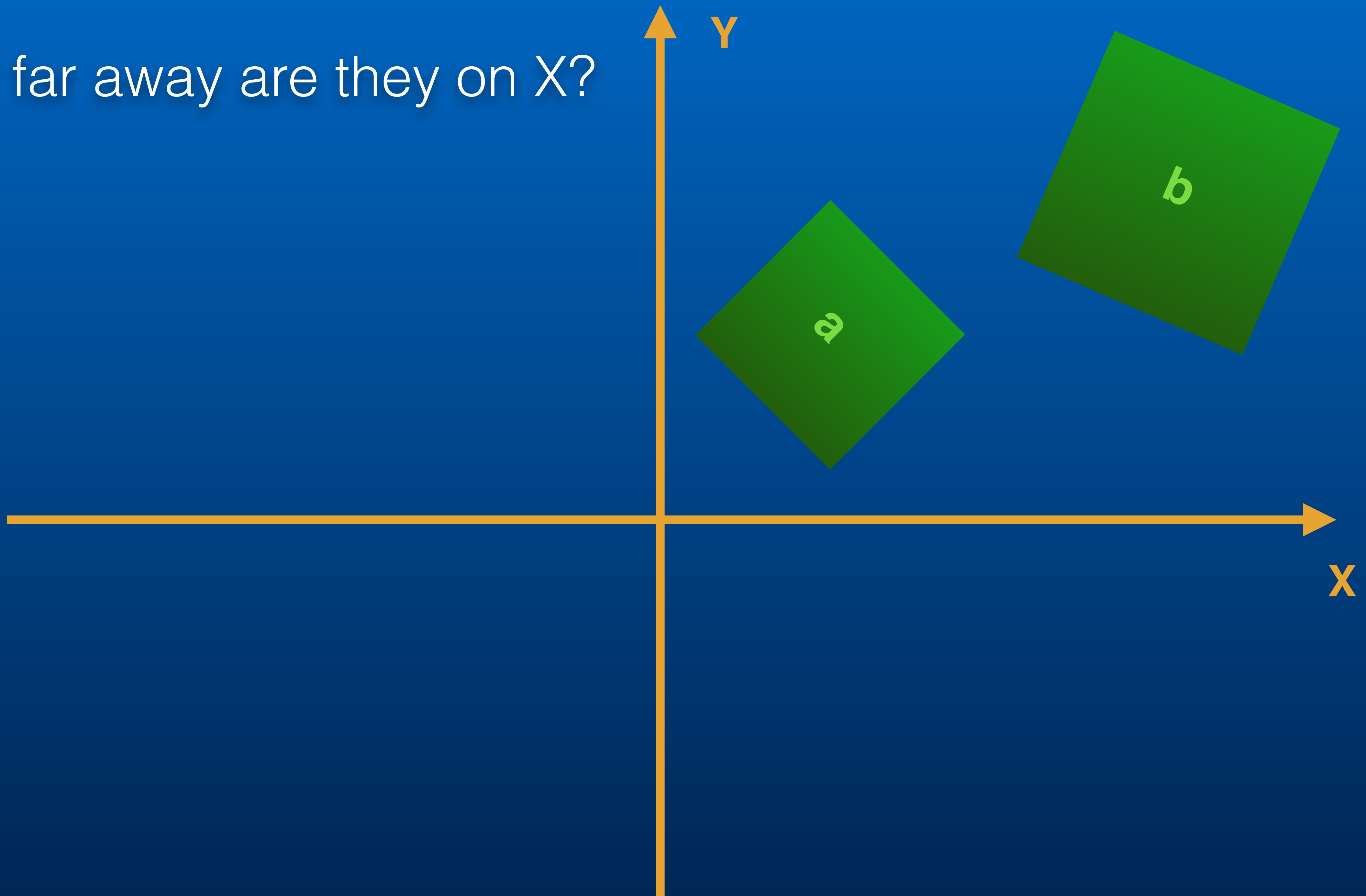
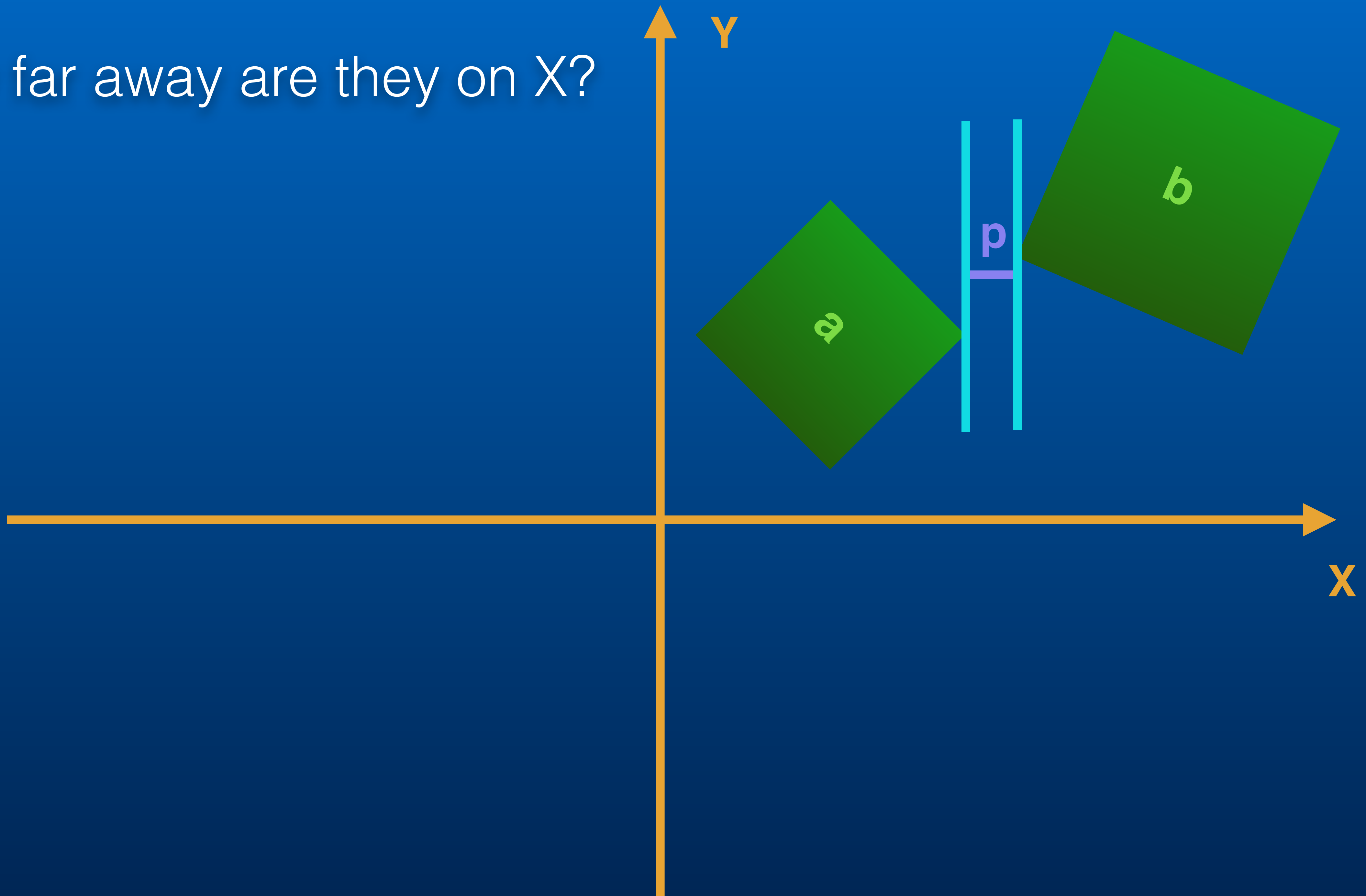if p >= 0, we are not colliding!

X axis is the separating axis.

Do the same on the Y-axis with box heights if X is not separating.

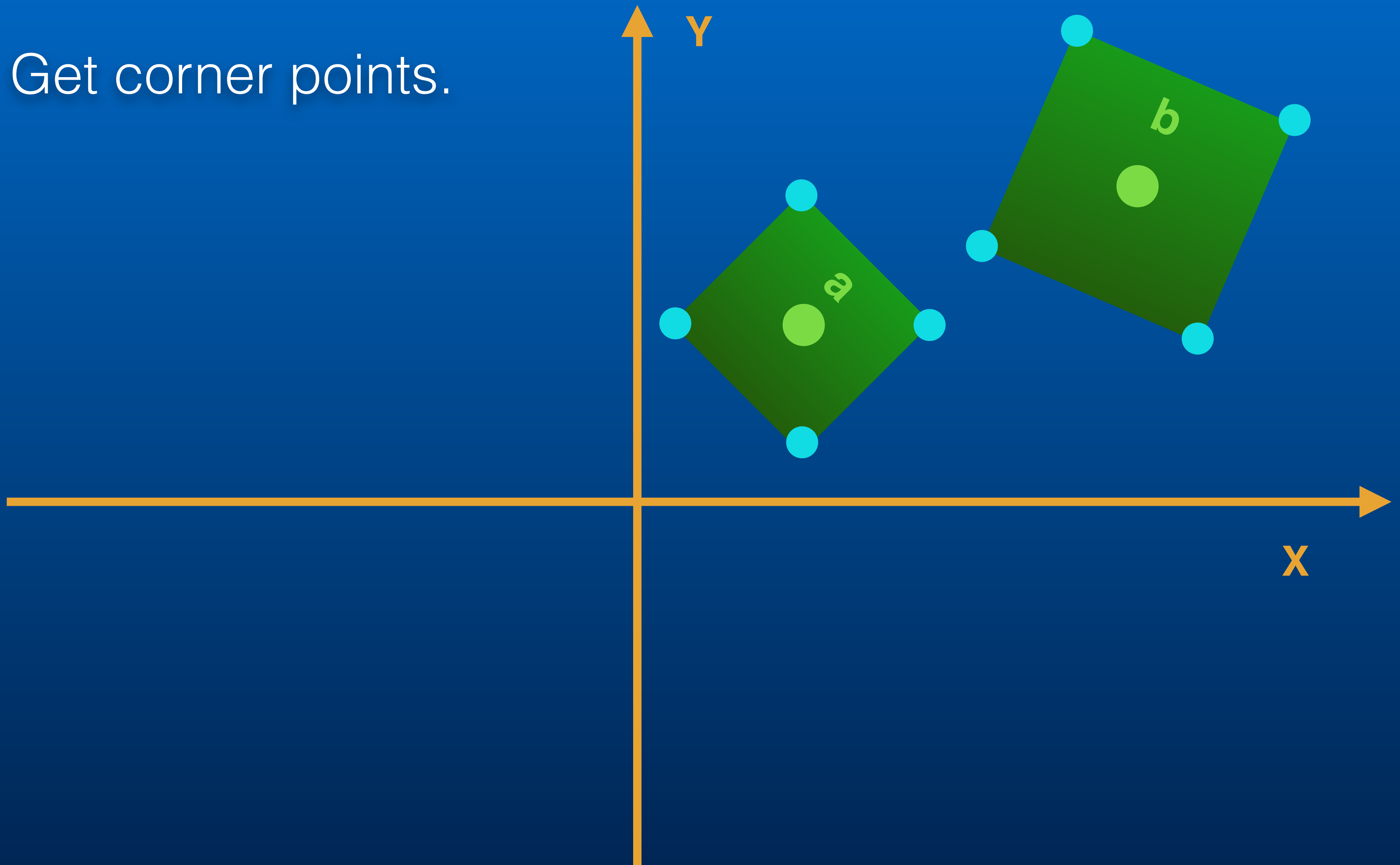If neither axis is separating, we have a collision!
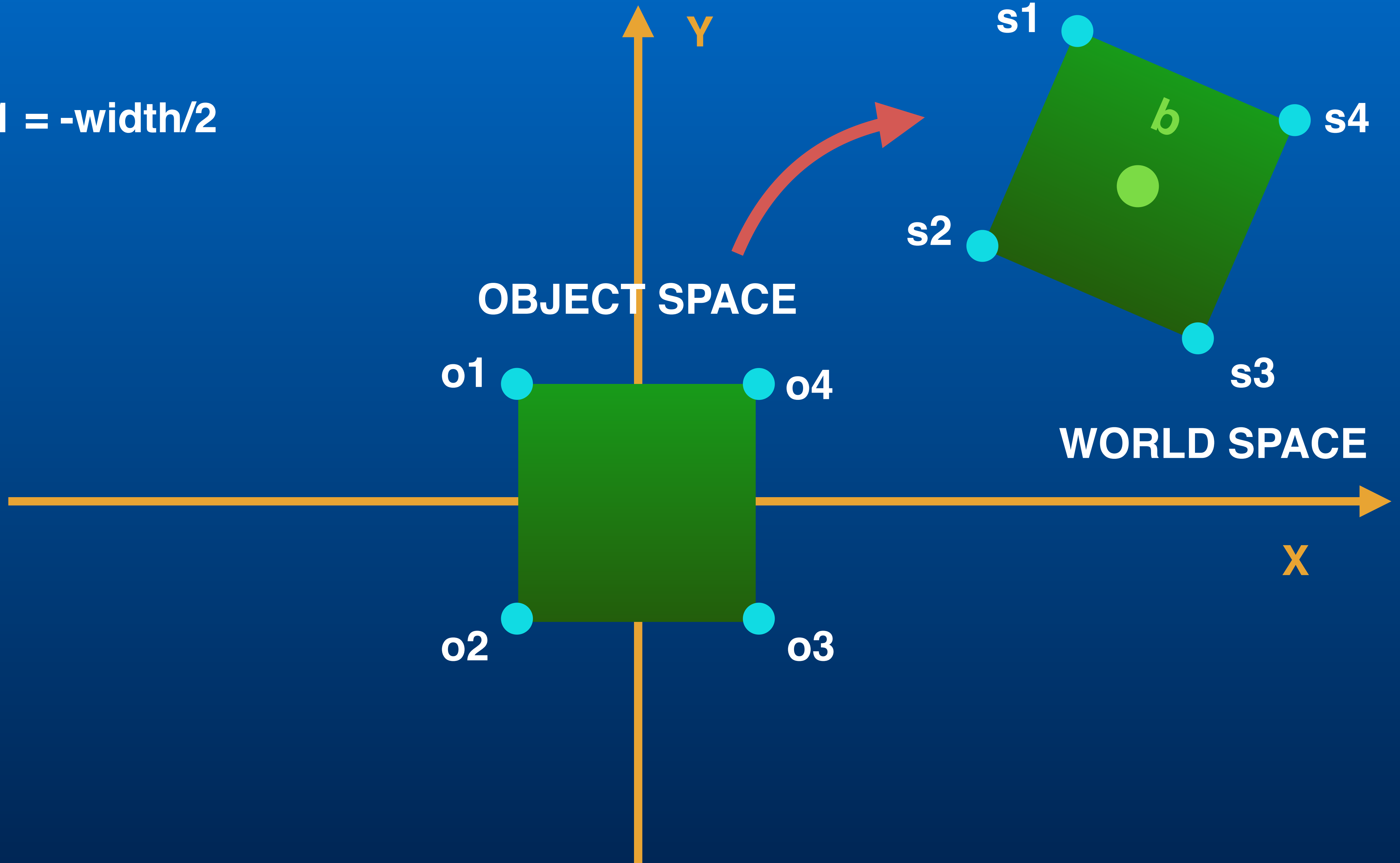
o1 = (-width/2, height/2)

s1 = b_matrix * o1

OBJECT SPACE

WORLD SPACE

Y

X

o1 o4

o2 o3

s1 s4

s2 s3

b
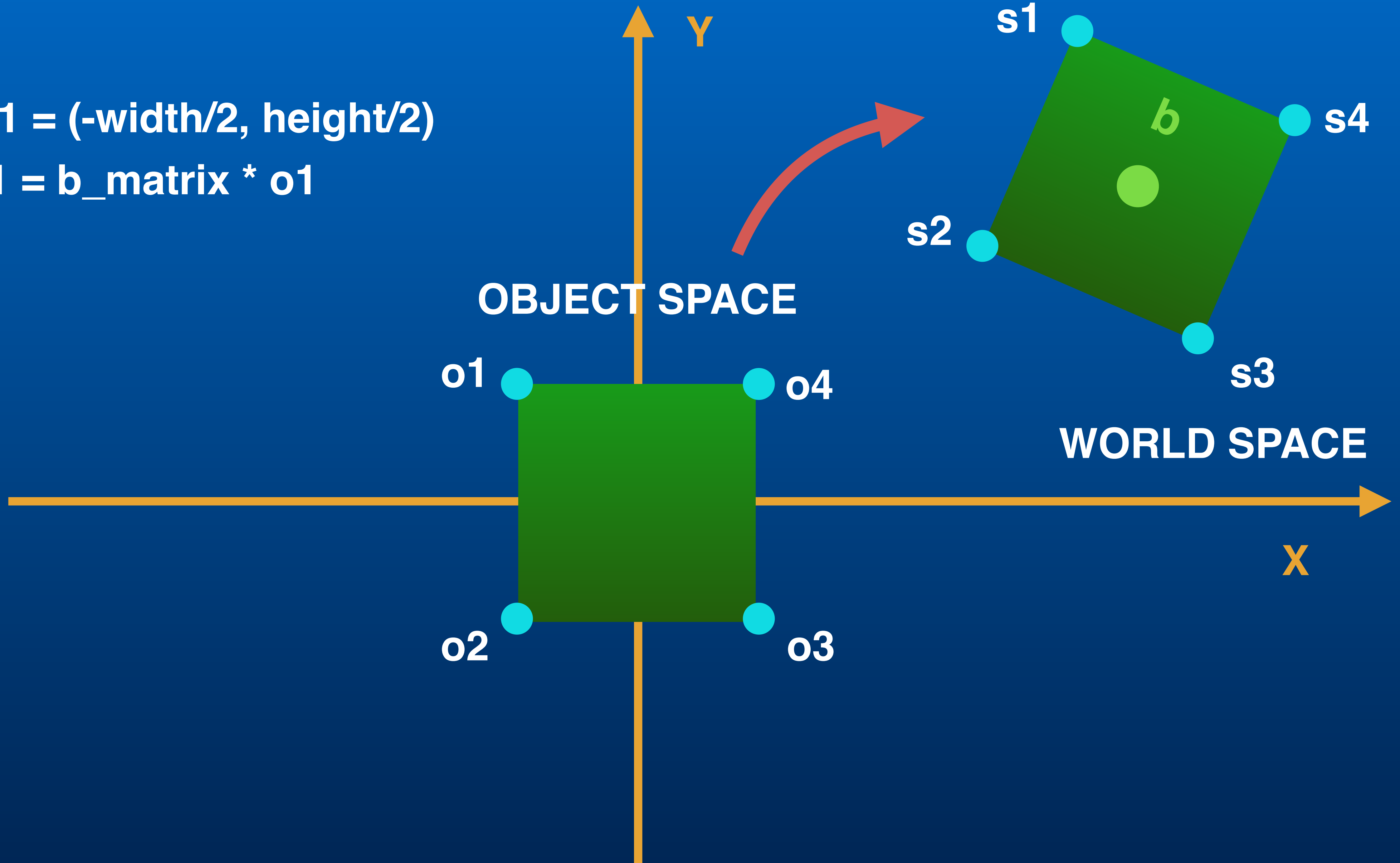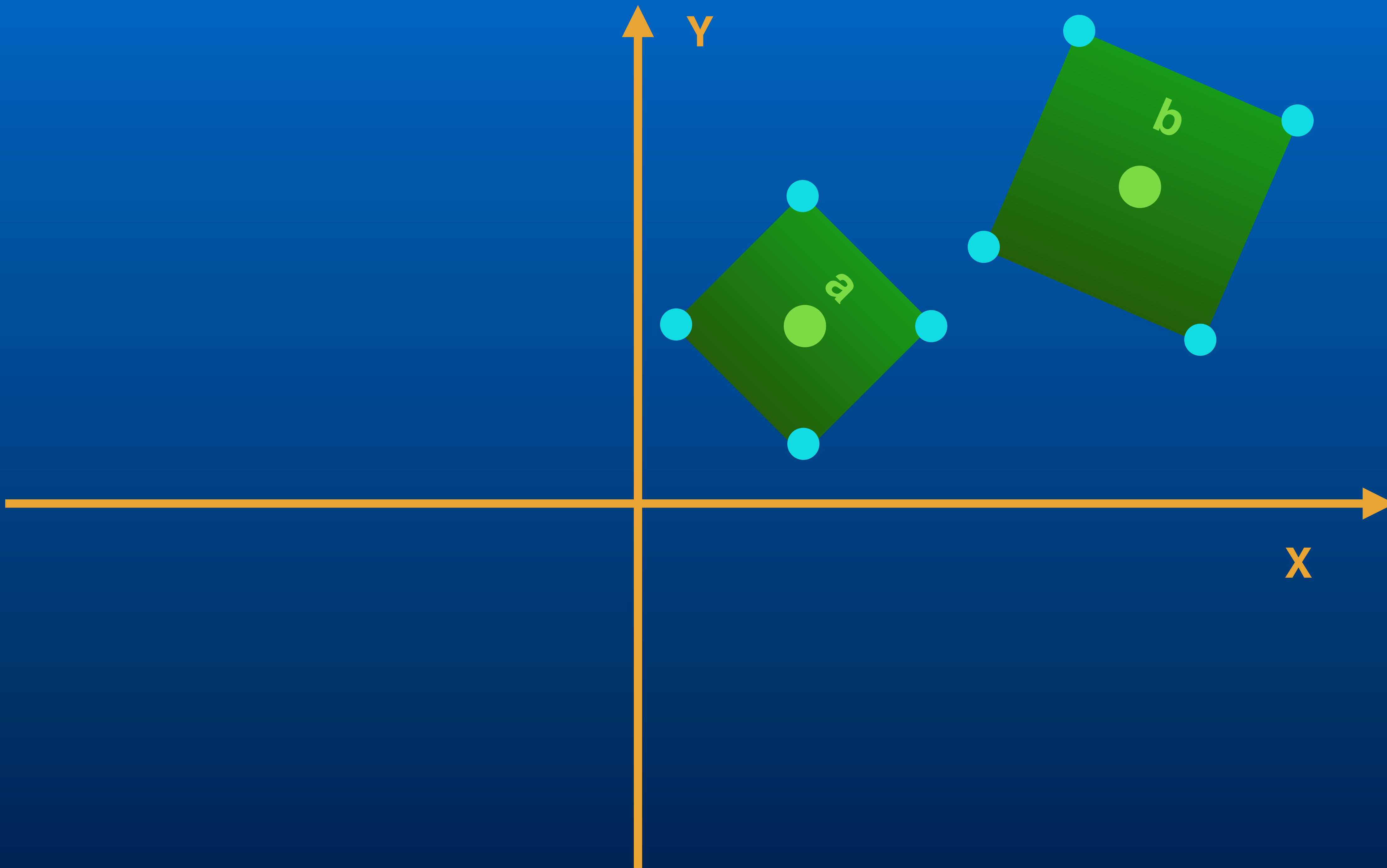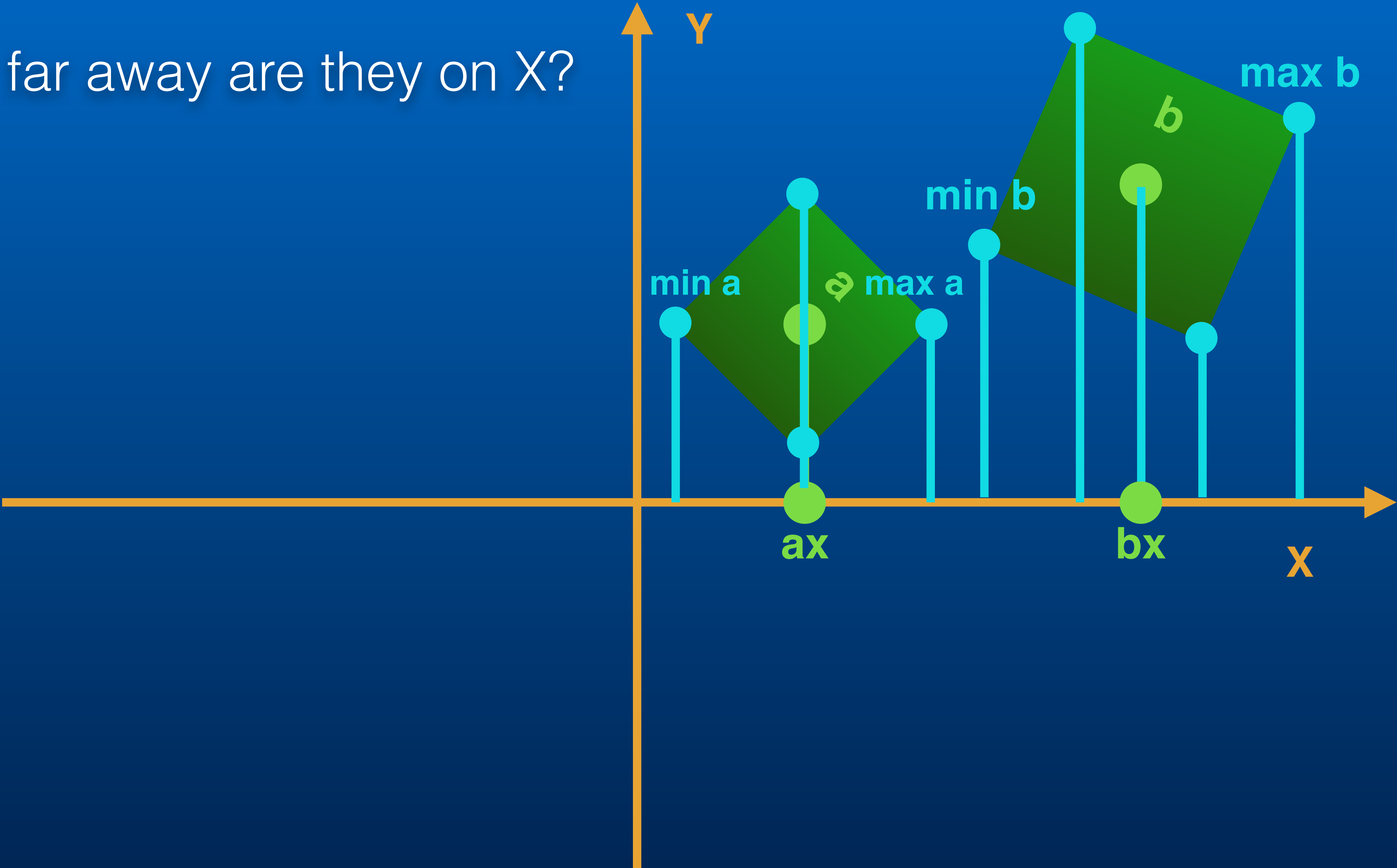
How far away are they on X?

$$p = |x_1 - x_2| - \frac{w_1 + w_2}{2}$$

if p >= 0, we are not colliding!
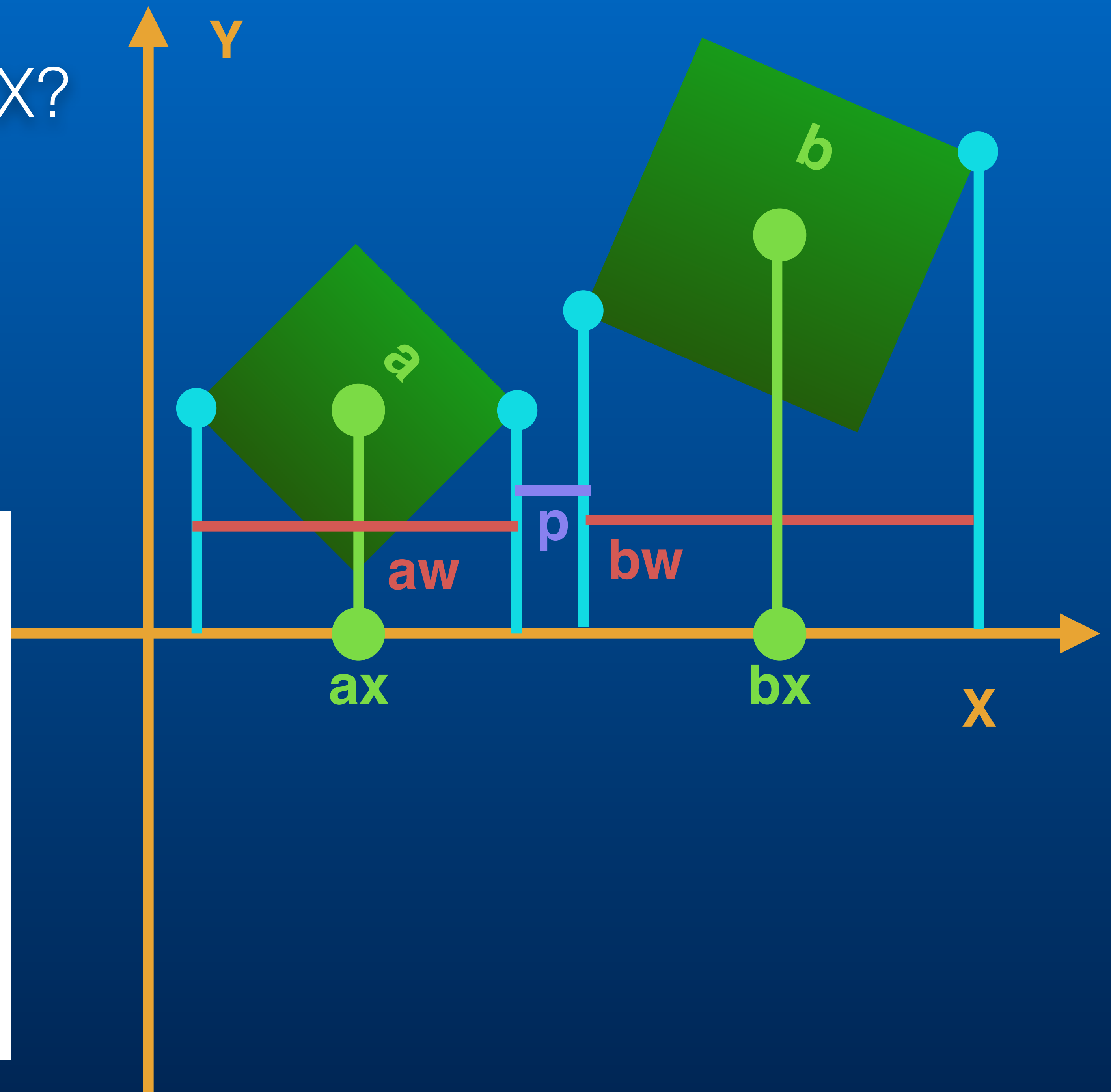
How far away are they on X?

$$p = |x_1 - x_2| - \frac{w_1 + w_2}{2}$$

if p >= 0, we are not colliding!

We cannot check rotated separation on X and Y axes!

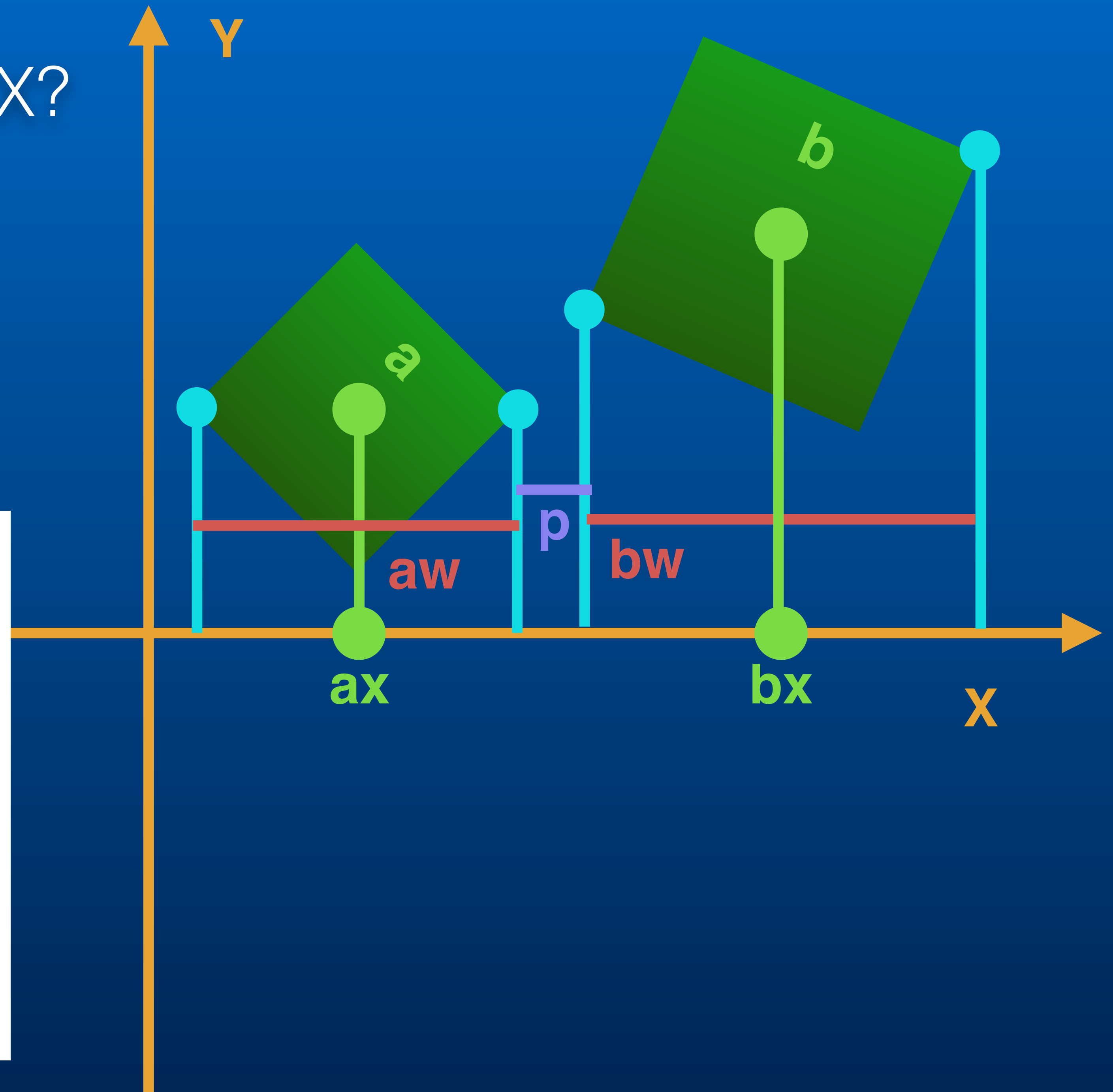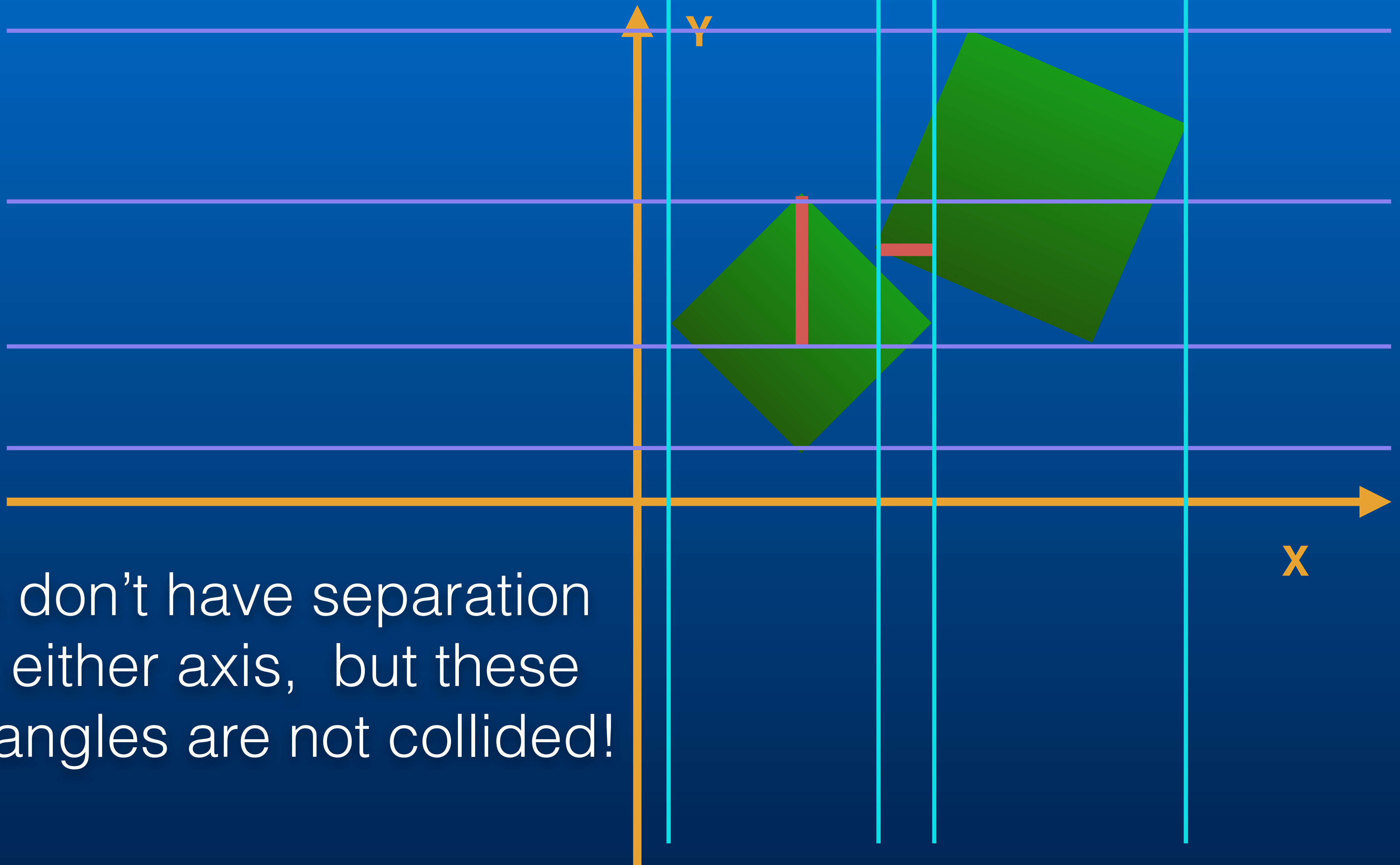We don't have separation on either axis, but these rectangles are not collided!

We need to check on both axes of each rectangle.
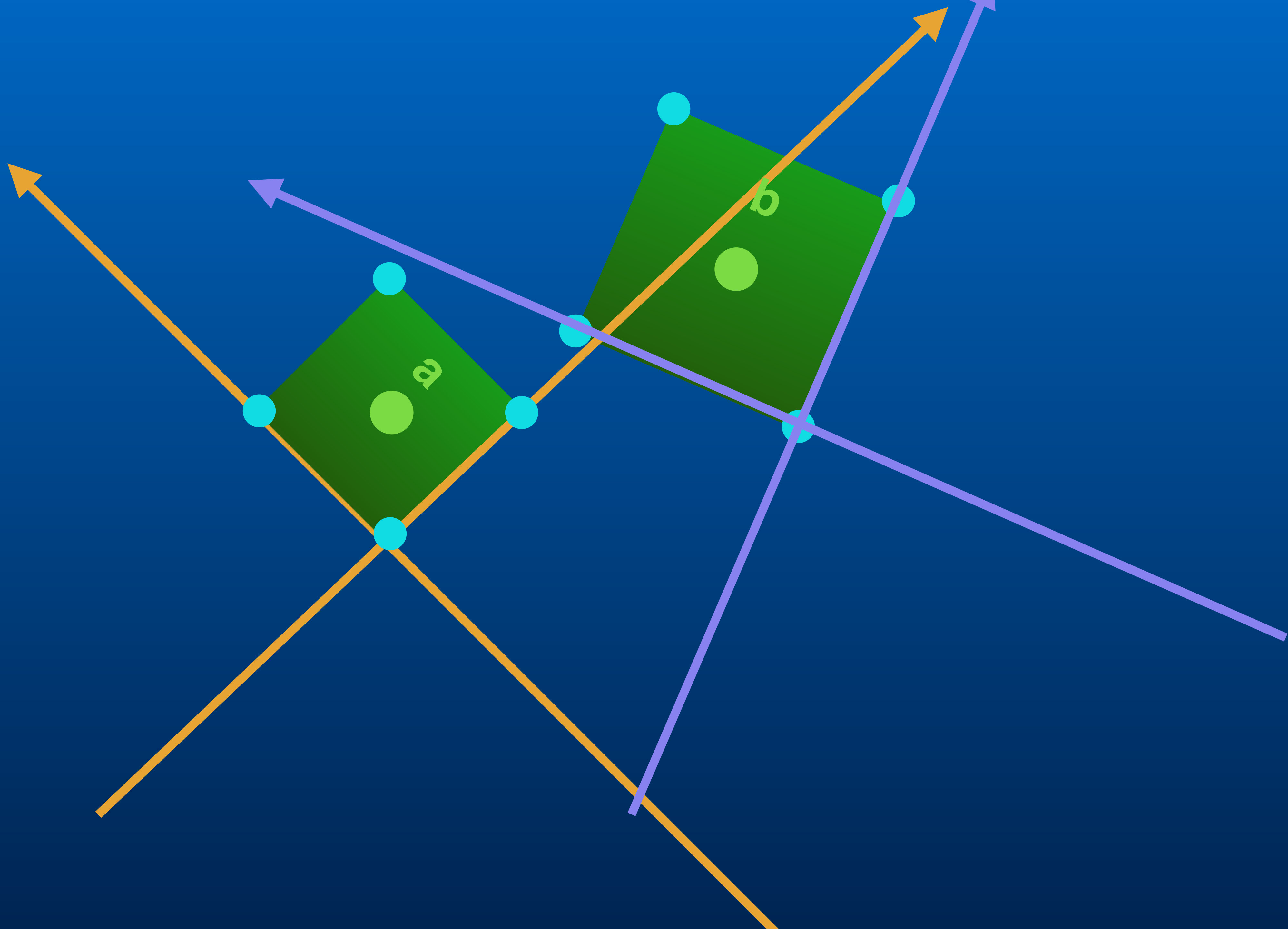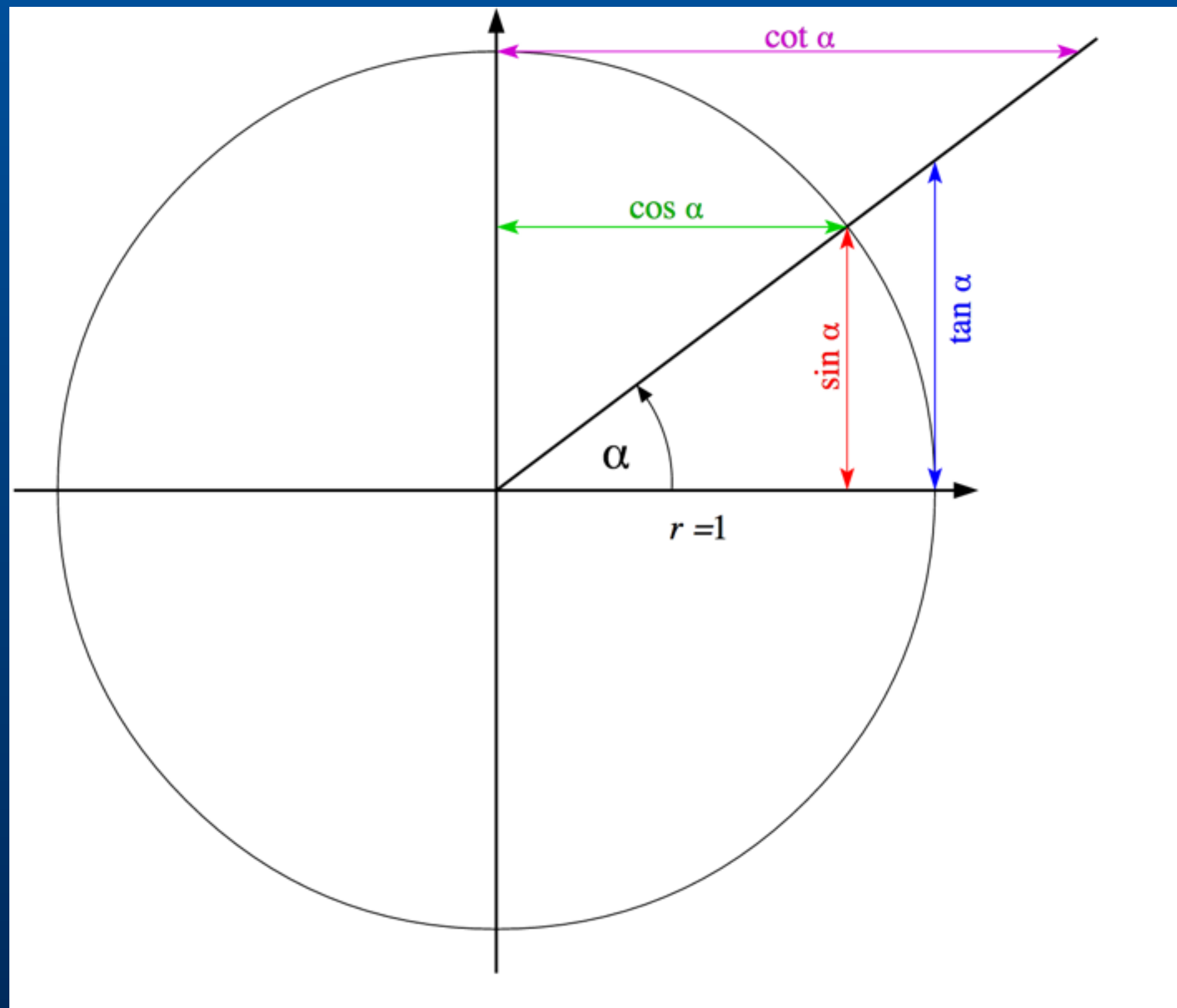
What is an axis?

An axis is just a unit vector representing a direction.

An axis is just a unit vector representing a direction.
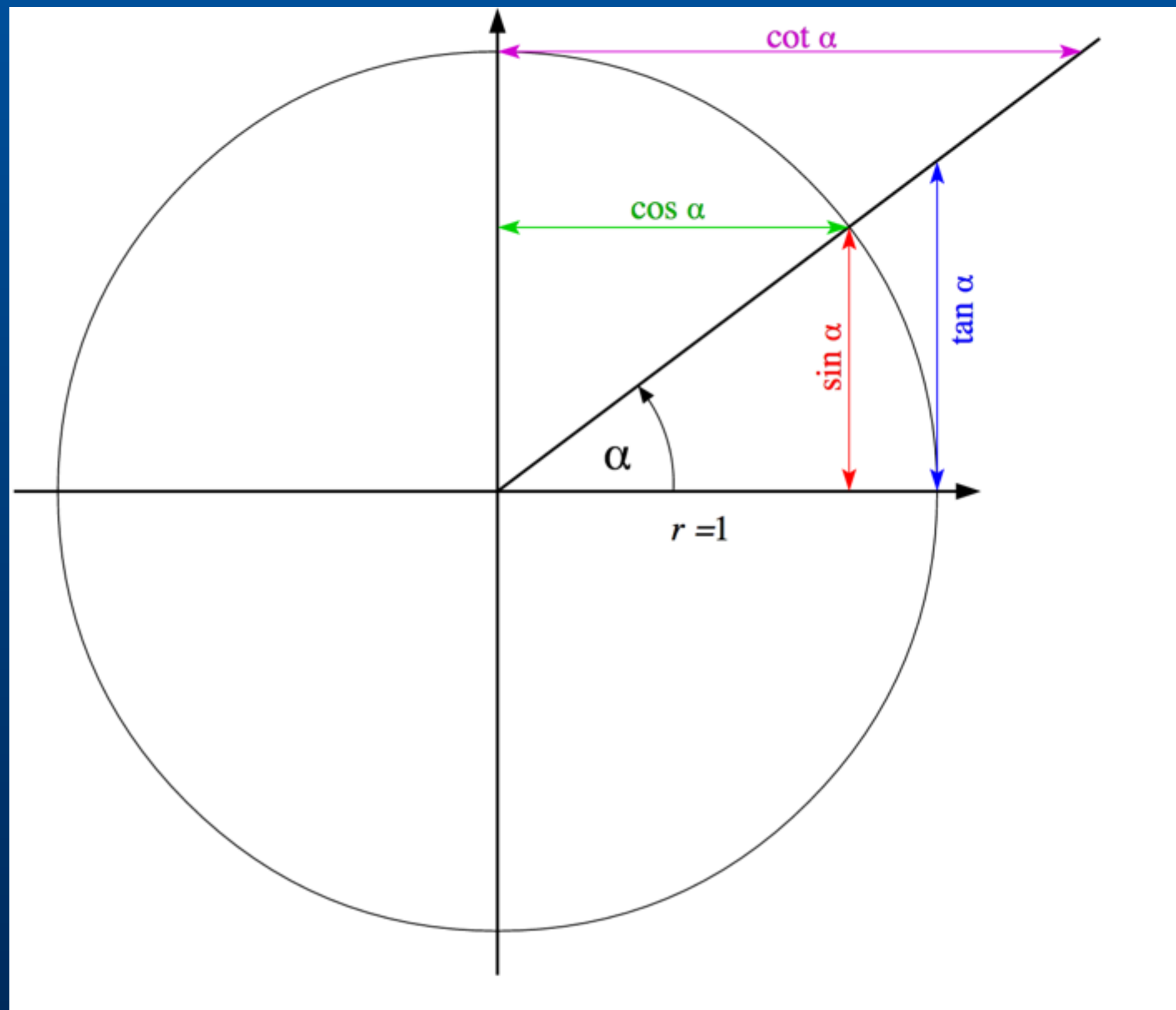
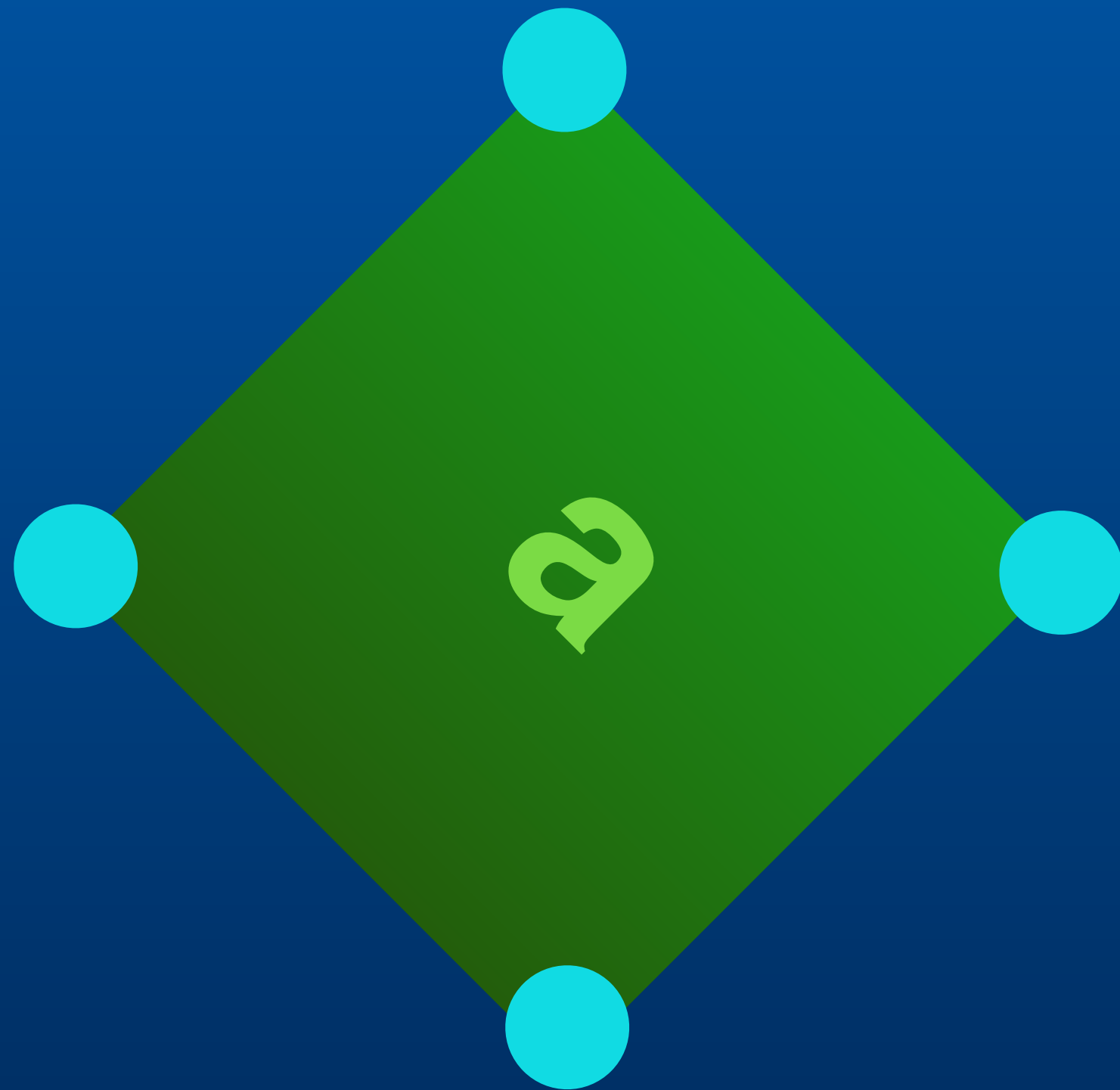Our usual X axis is (1.0, 0.0) and Y is (0.0, 1.0).

An axis that's at a 45 degree angle (PI/4) can be represented by (cos(PI/4), sin(PI/4)).
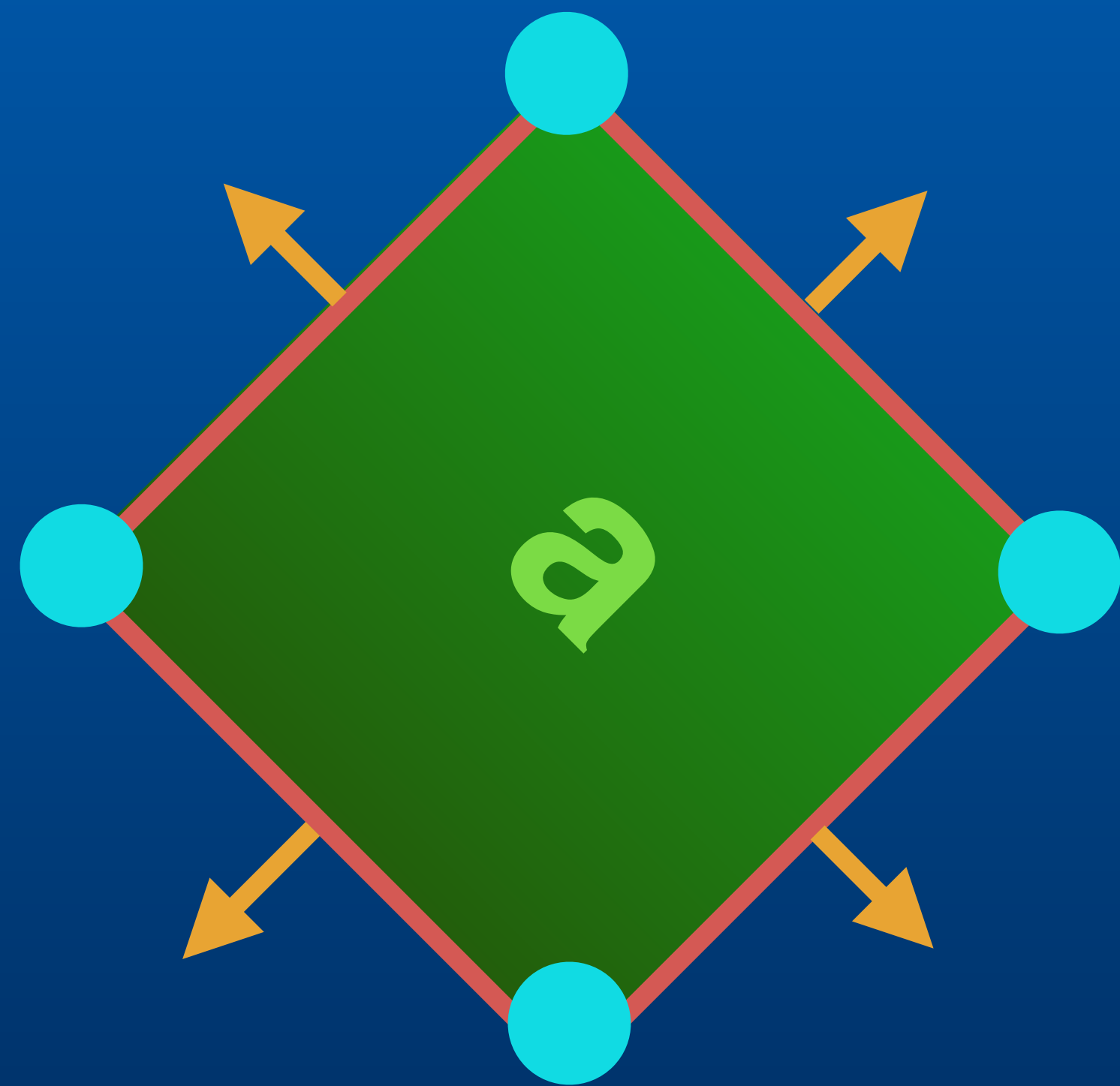
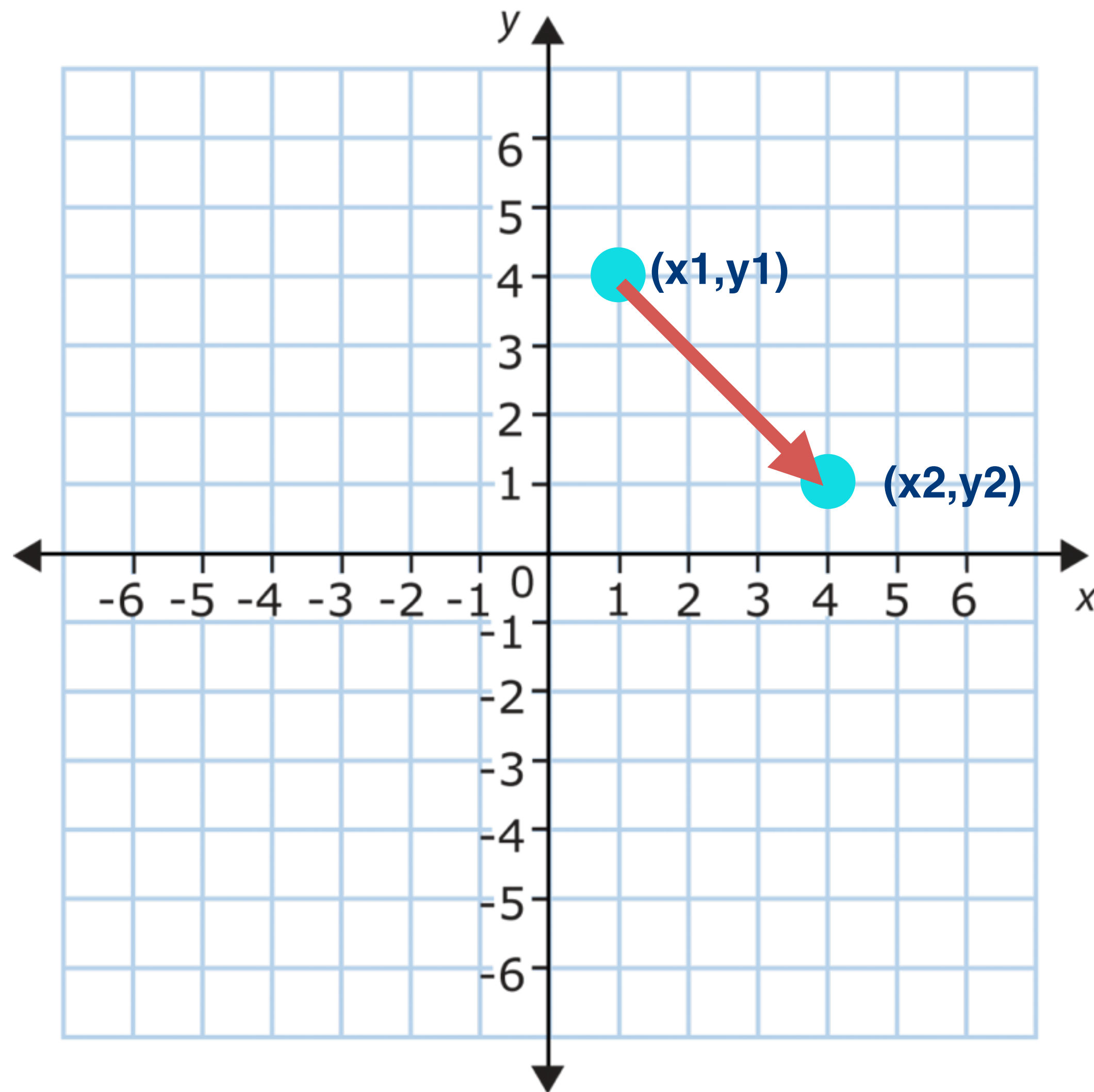# How do we figure out our rectangle axes?

Normals.

Polygon

Polygon edges or sides.

Edge normals.

Normalized (unit) vectors perpendicular to the edge.

An edge is a vector from one vertex to another.

edge_x = x2-x1
edge_y = y2-y1
edge = (edge_x, edge_y)

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edge_x = x2-x1
edge_y = y2-y1
edge = (edge_x, edge_y)
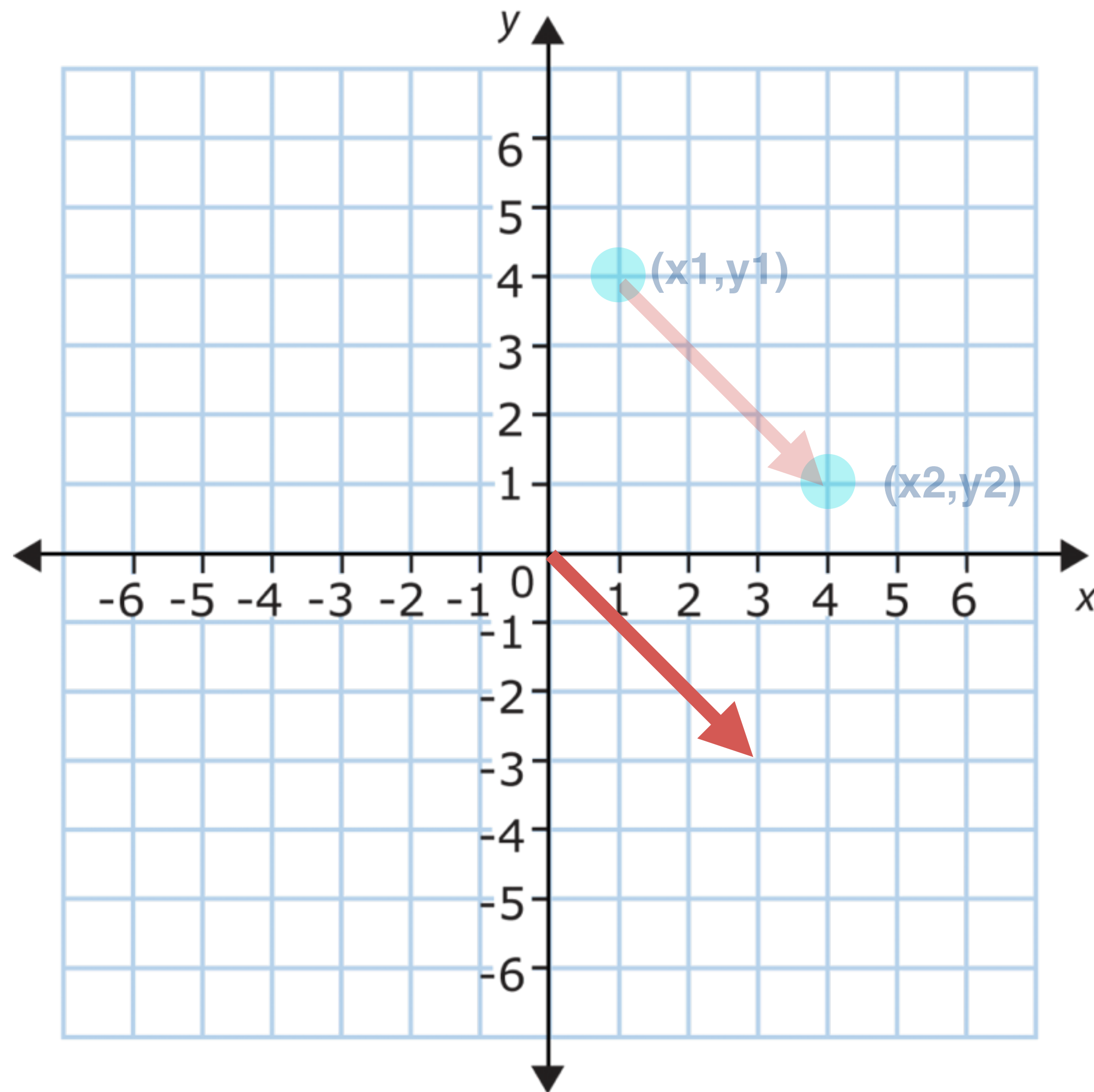
An edge is a vector from one vertex to another.

edge_x = x2-x1
edge_y = y2-y1
edge = (edge_x, edge_y)

Its normals are the vectors perpendicular to that vector.
normal1 = (edge_y, -edge_x)

and

normal2 = (-edge_y, edge_x)
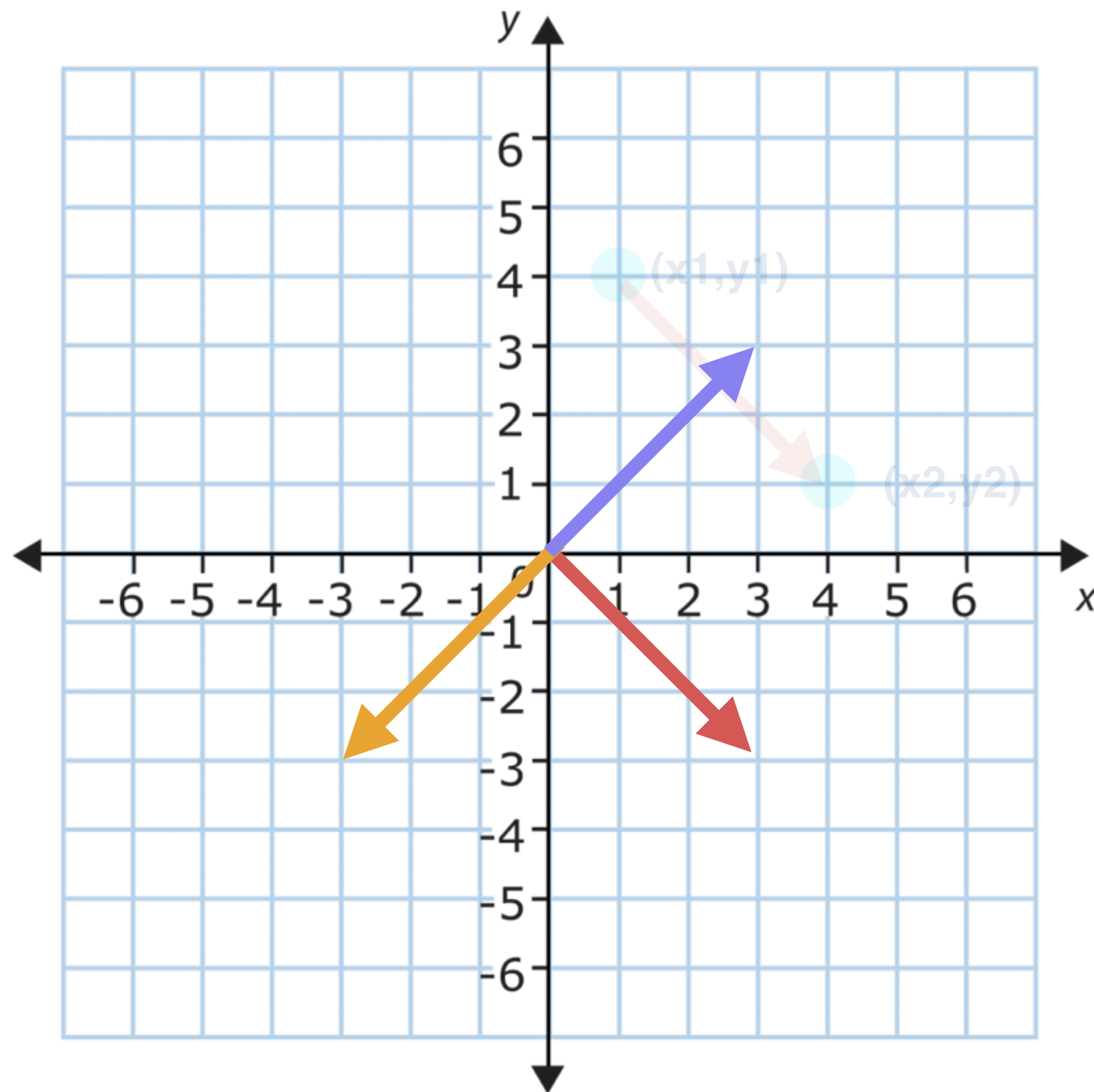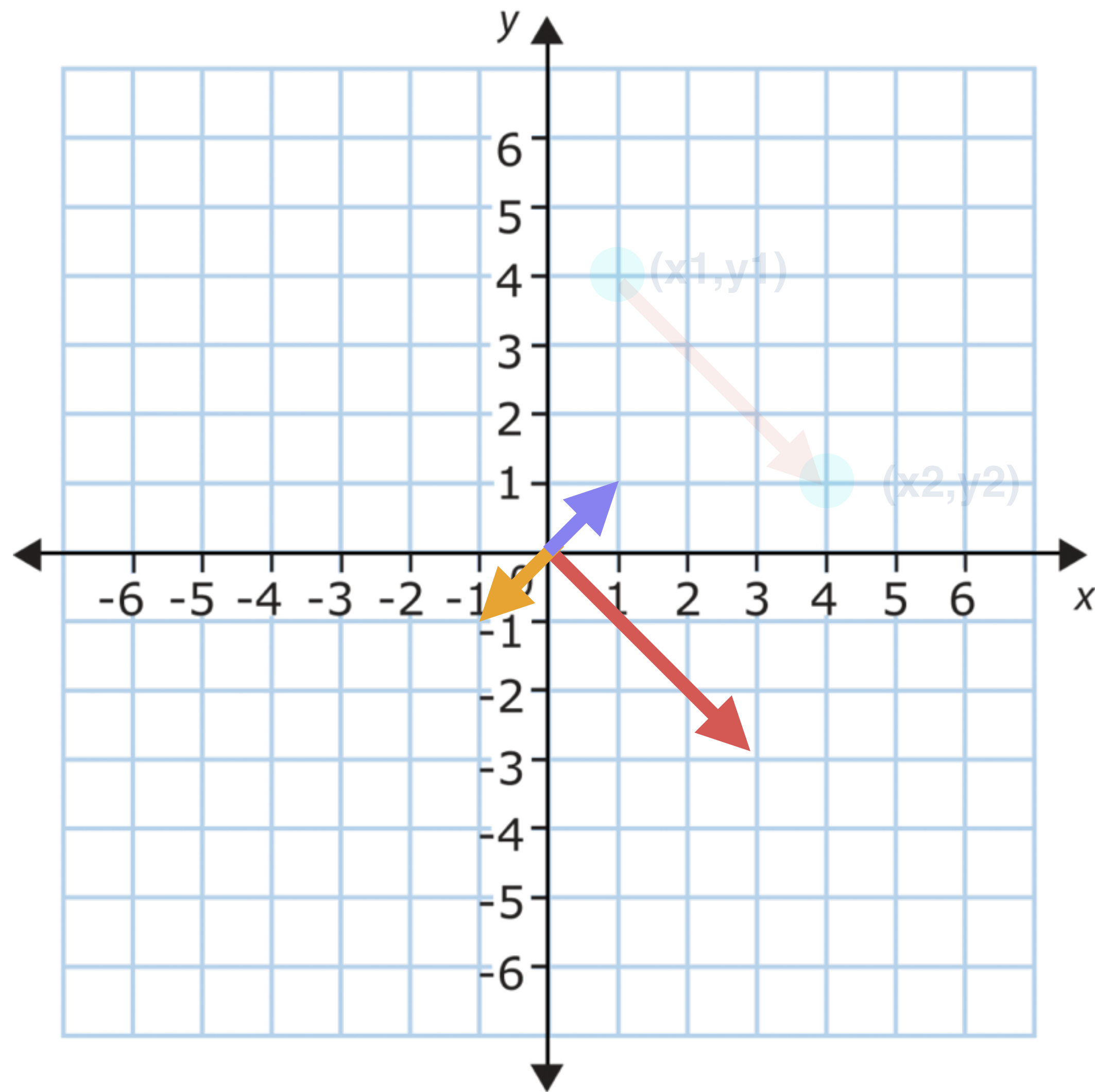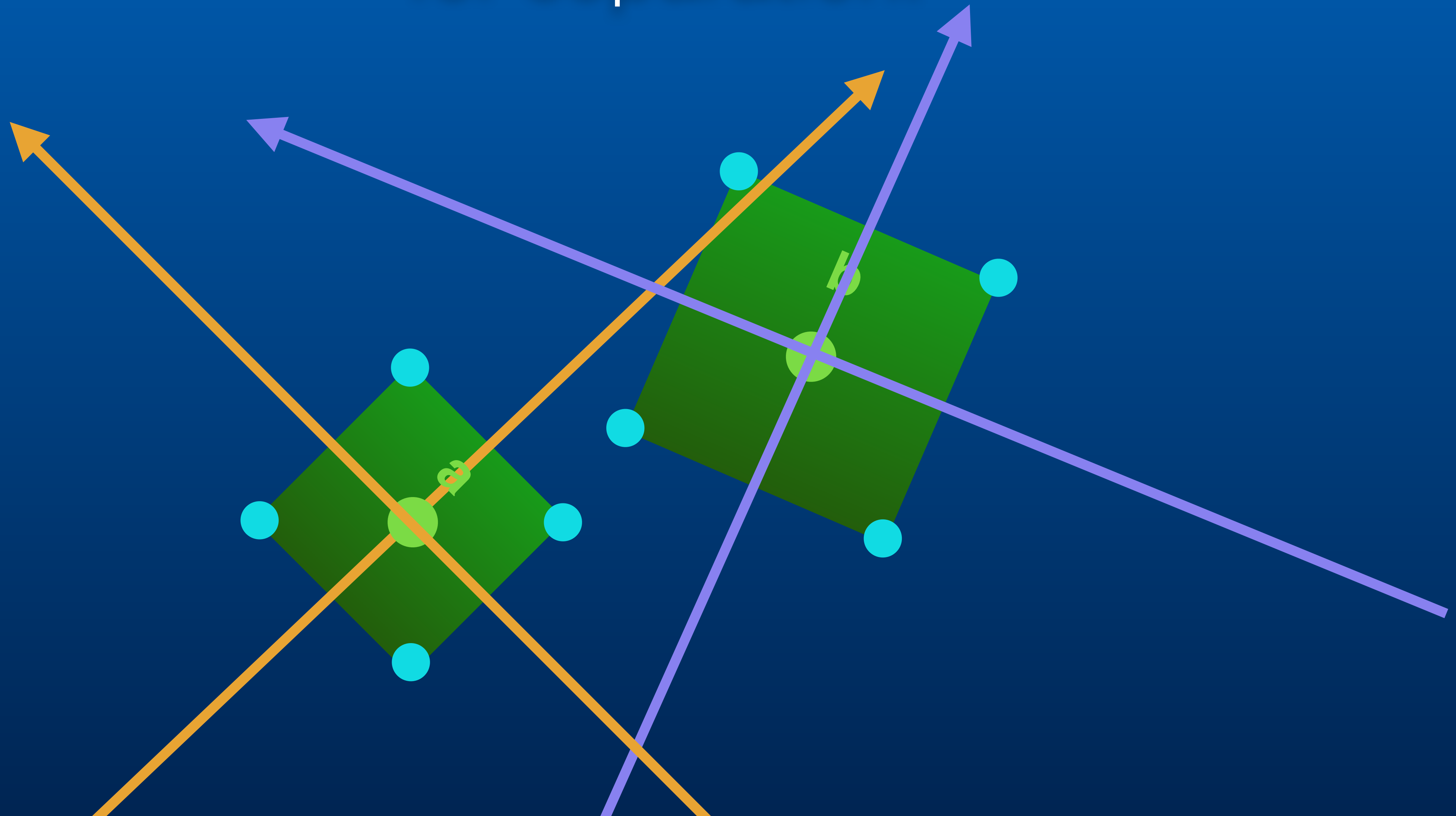
Now, normalize the normals.

length = sqrt(x*x + y*y)
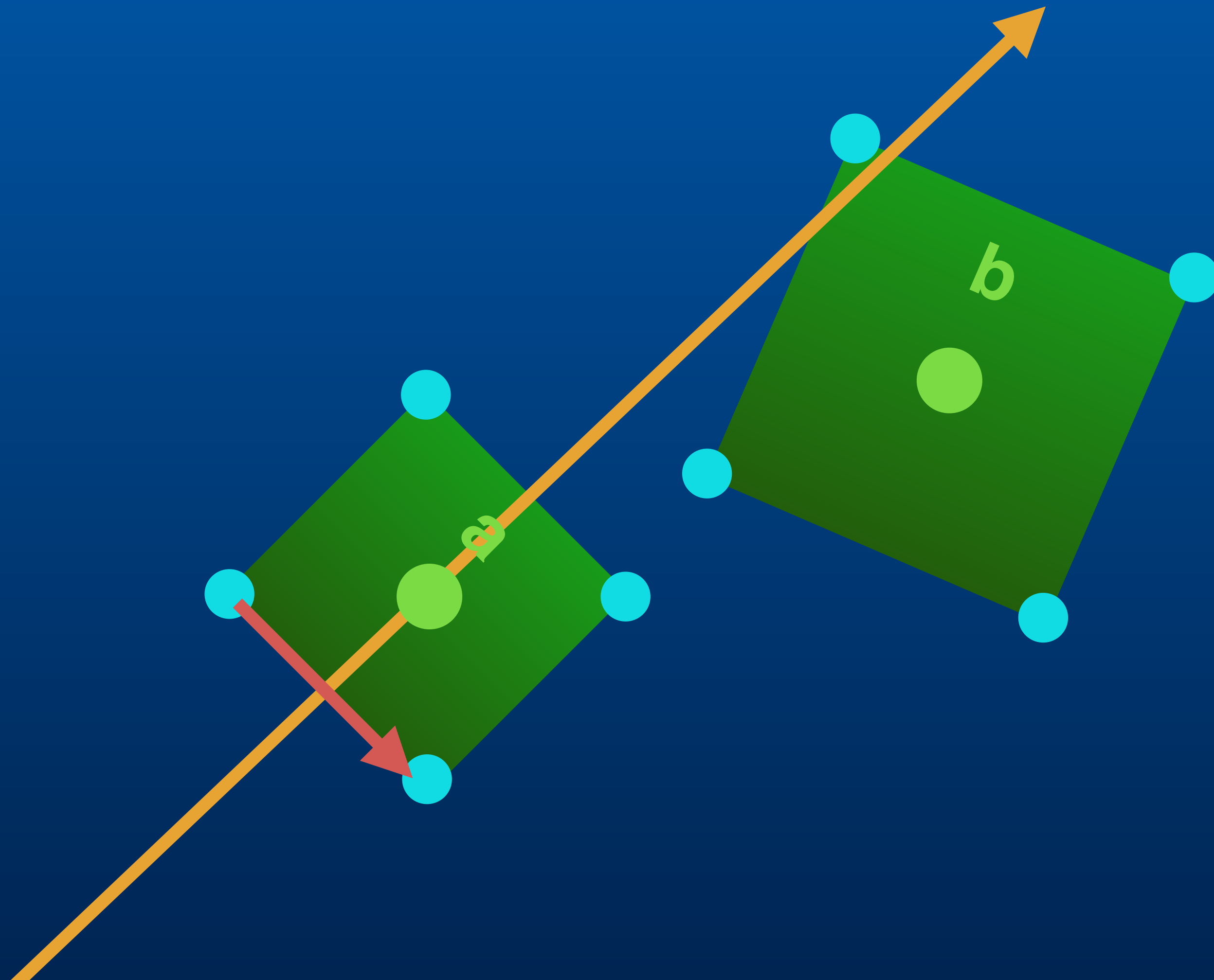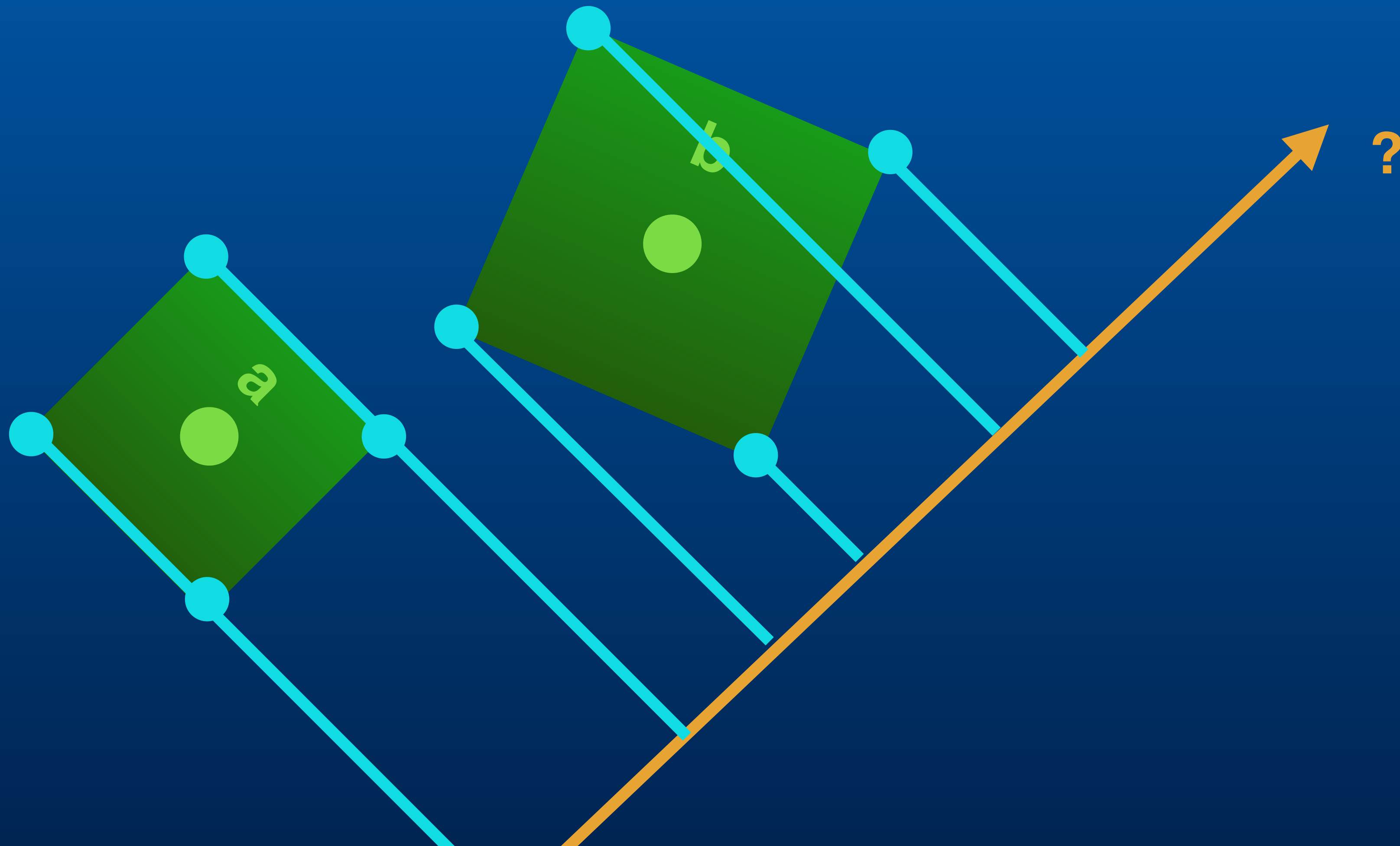x /= length
y /= length

Our normals are the axes on which we check for separation.

For each edge find the normal.

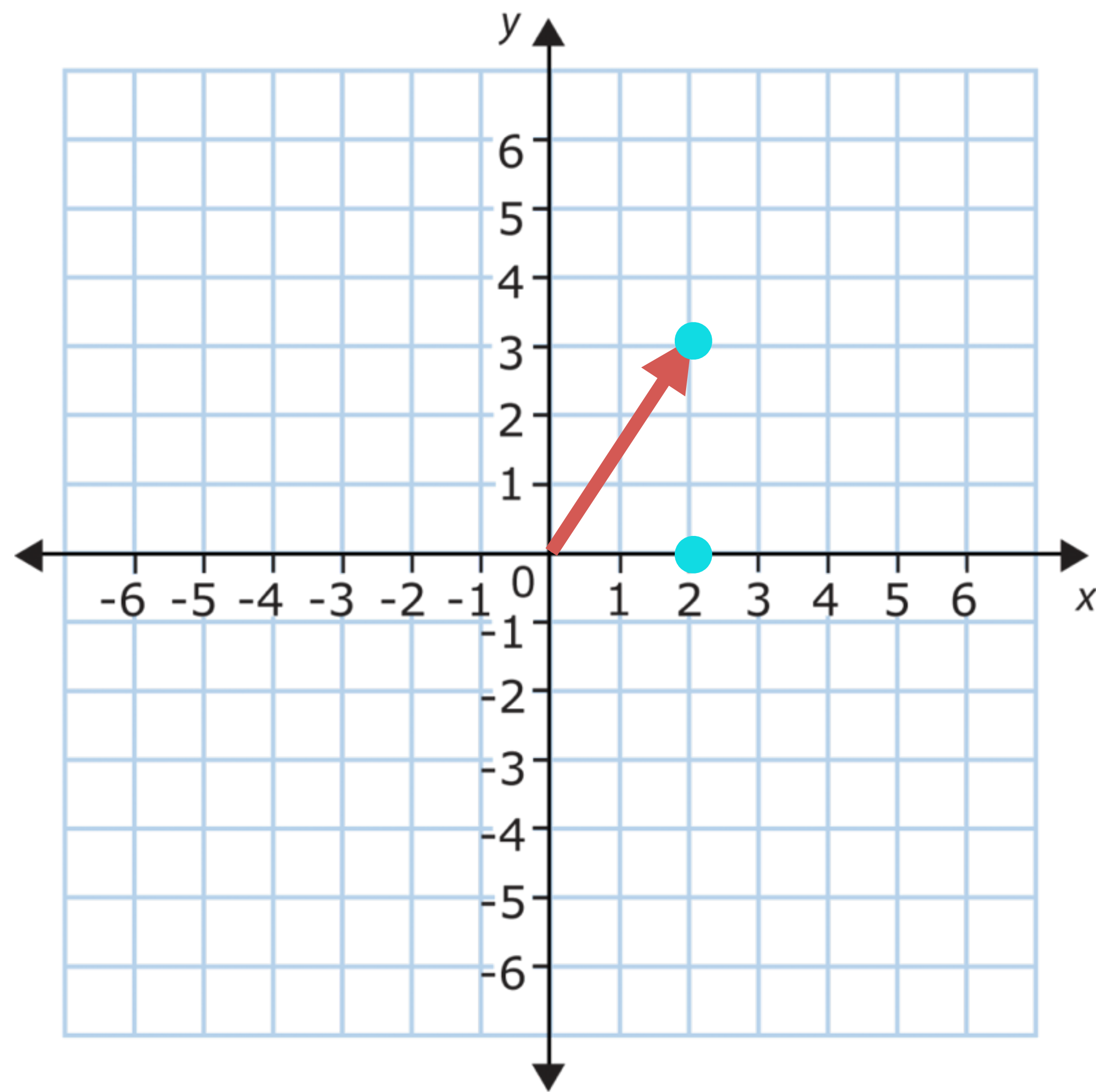# Projecting onto an arbitrary axis.
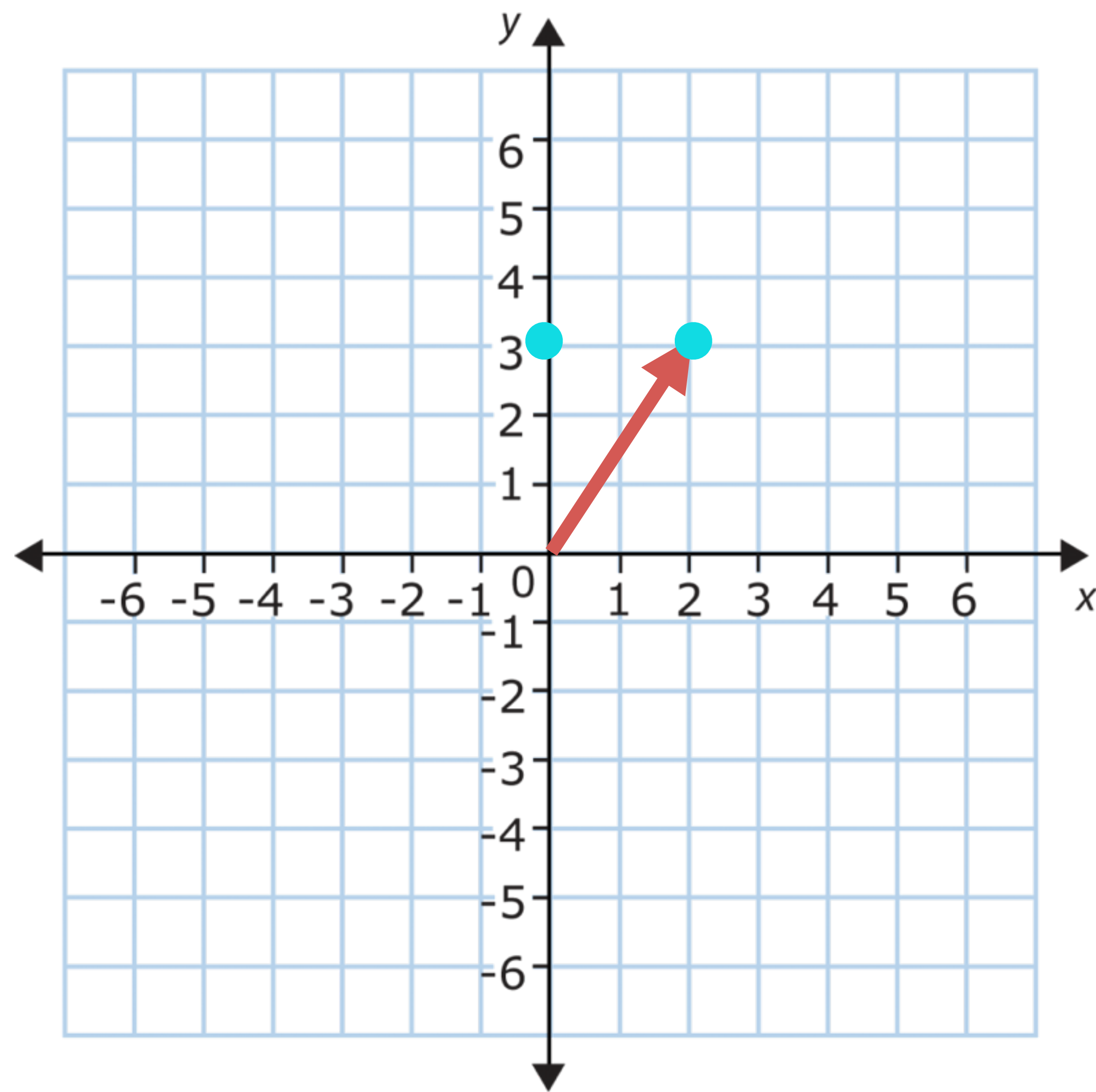
The dot product.

(x1*x2) + (y1*y2)
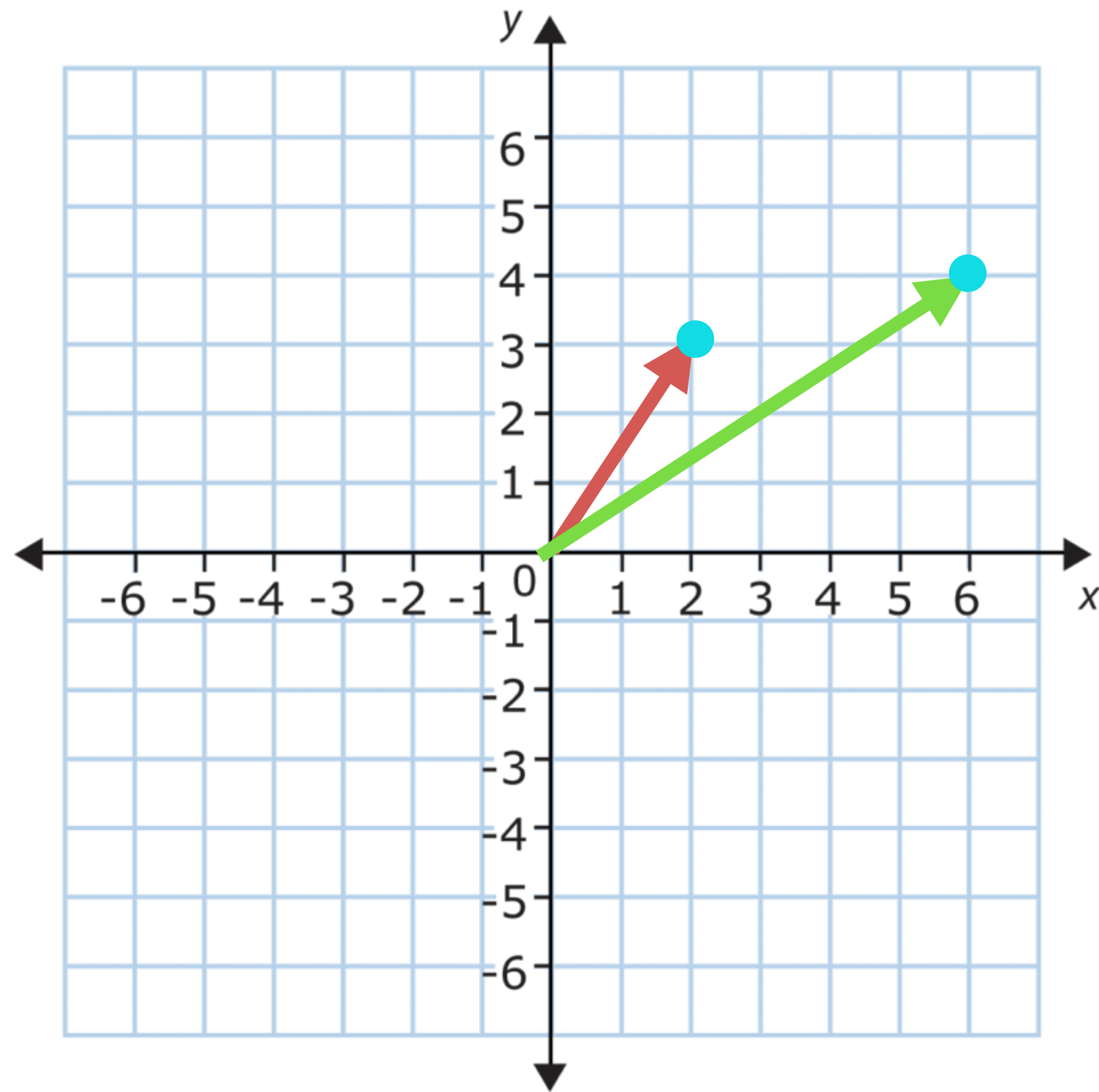
Applies one vector to another.

$(2,3) \cdot (1,0) = (2*1) + (3 * 0) = 2$

$(2,3) \cdot (0,1) = (2*0) + (3 * 1) = 3$

Normalize (6,4):

length = sqrt(6*6 + 4*4) = 7.2111
x = 6 / 7.2111 = 0.832
y = 4 / 7.2111 = 0.5547

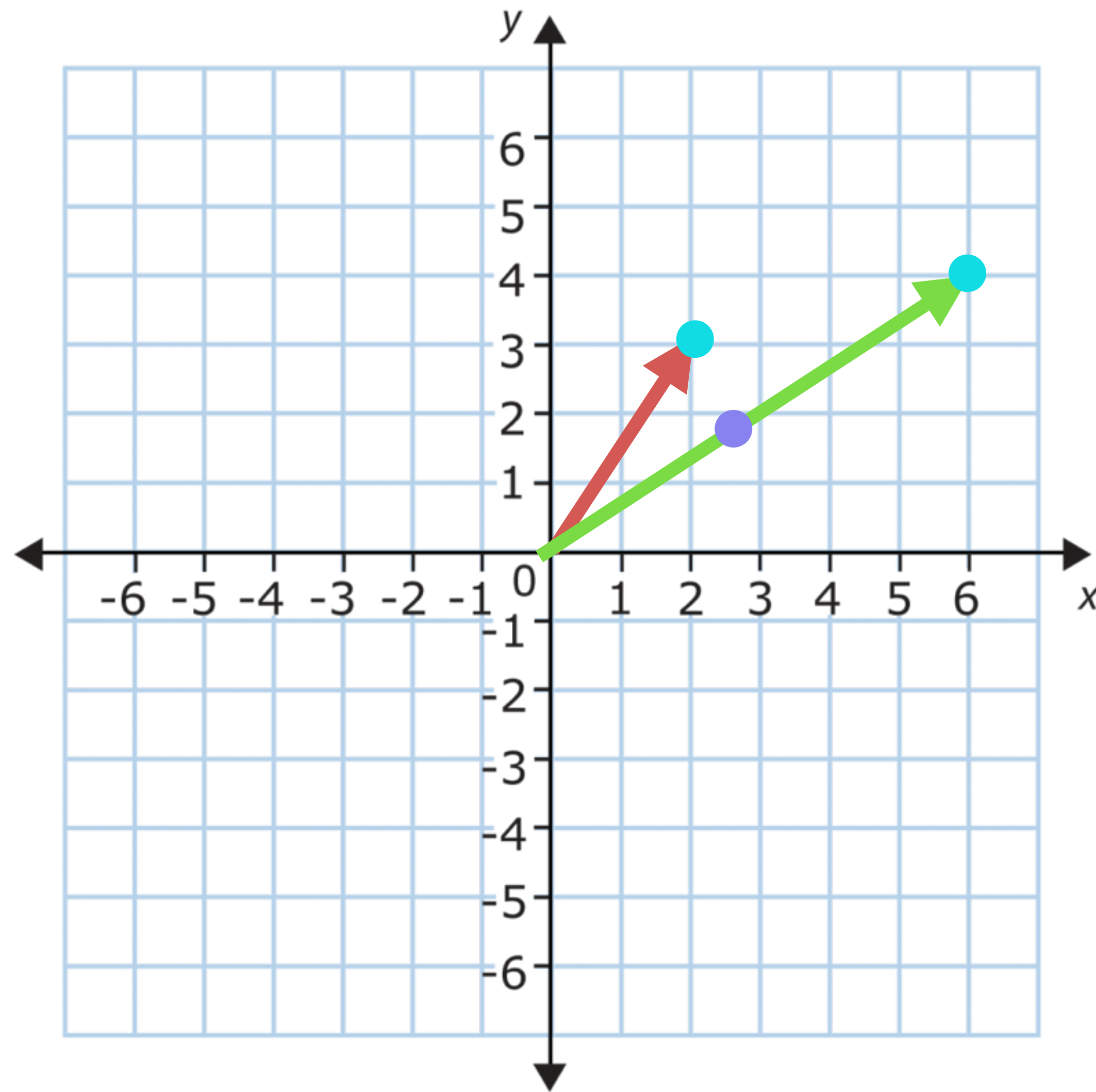(2,3) · (0.832,0.555) = (2*0.832) + (3 * 0.555)
= 1.664 + 1.665 = **3.329**

Normalize (6,4):

length = sqrt(6*6 + 4*4) = 7.2111
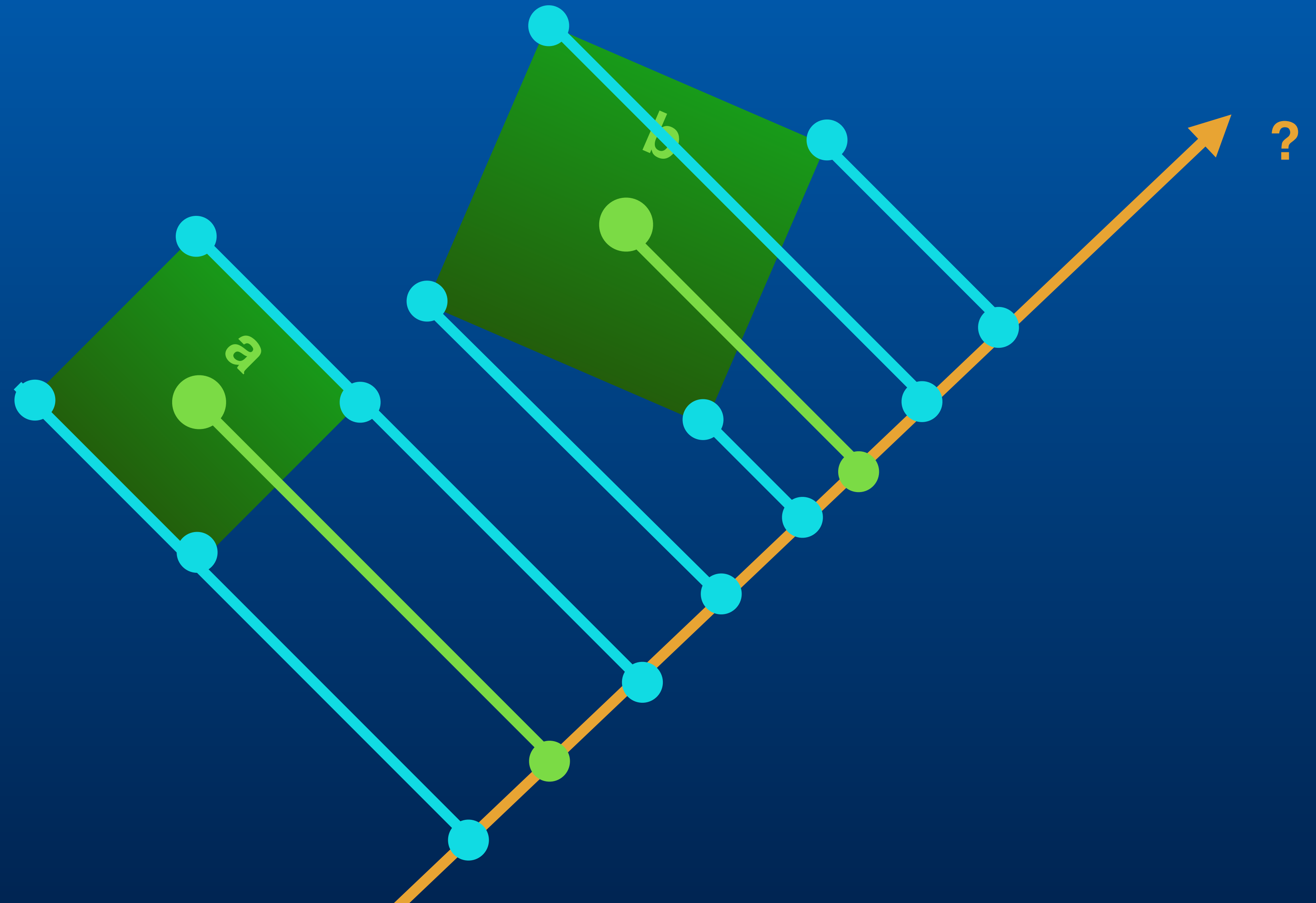**x = 6 / 7.2111 = 0.832**
y = 4 / 7.2111 = 0.5547

$(2,3) \cdot (0.832, 0.555) = (2*0.832) + (3 * 0.555)$
= 1.664 + 1.665 = **3.329**

(0.832,0.555) * 3.329 = (2.769, 1.847)
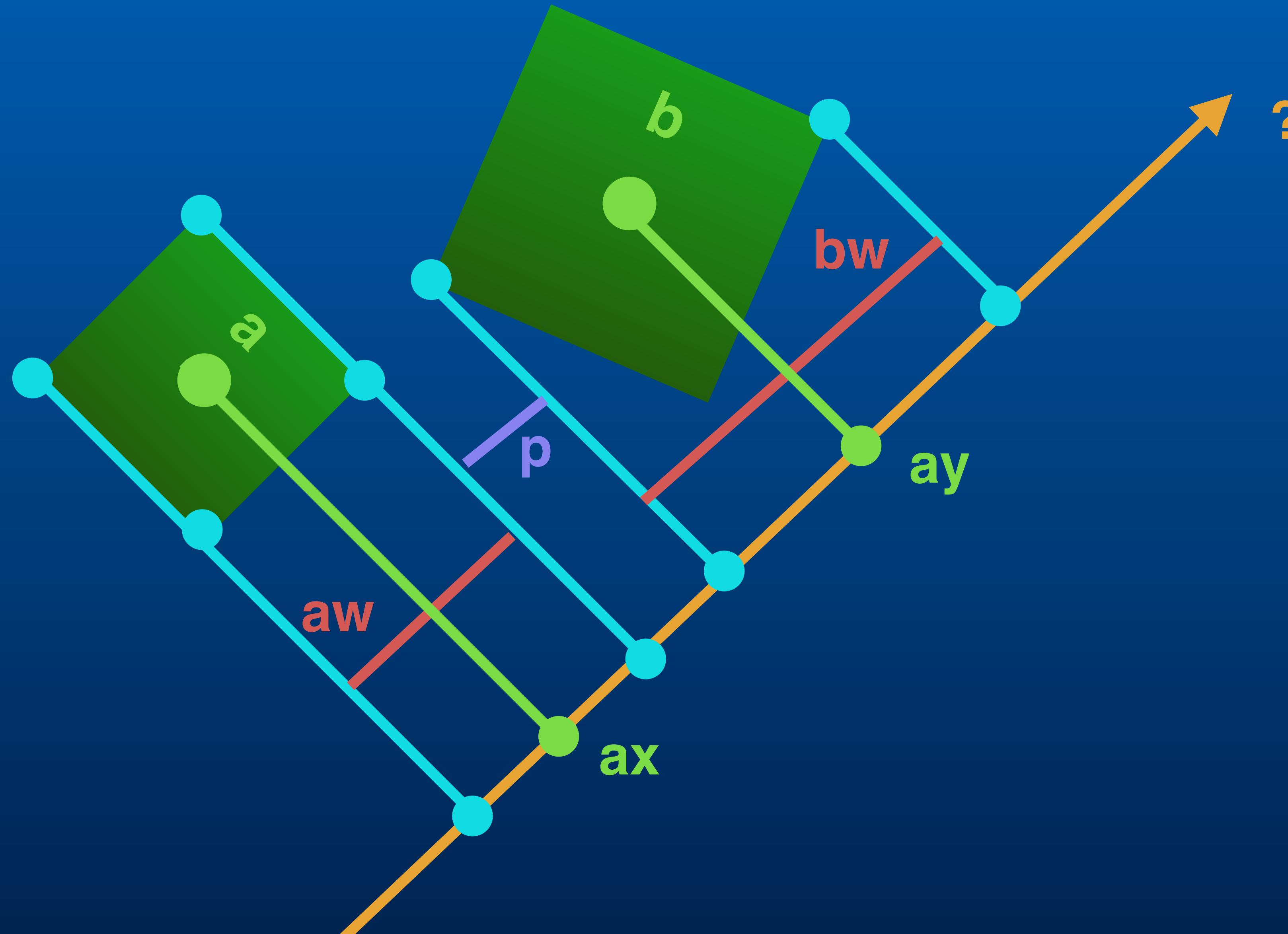
Find dot product of each corner with the normalized axis vector.

How far away are they on this axis?

$$p = |x_1 - x_2| - \frac{w_1 + w_2}{2}$$
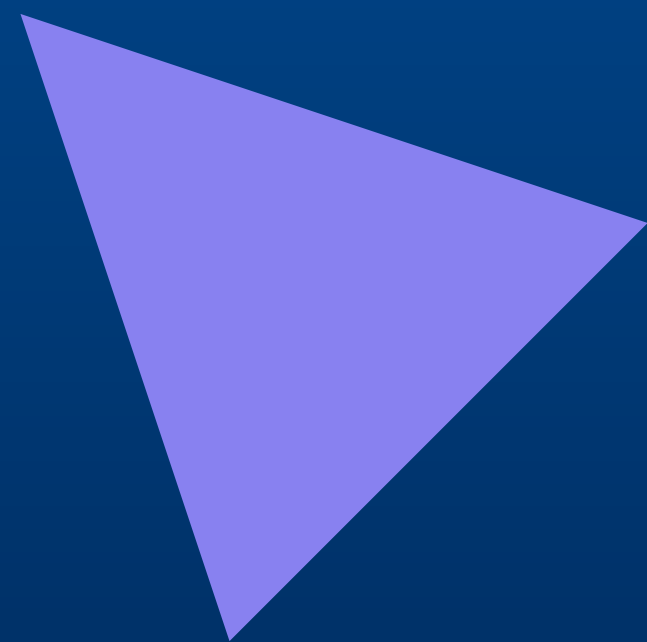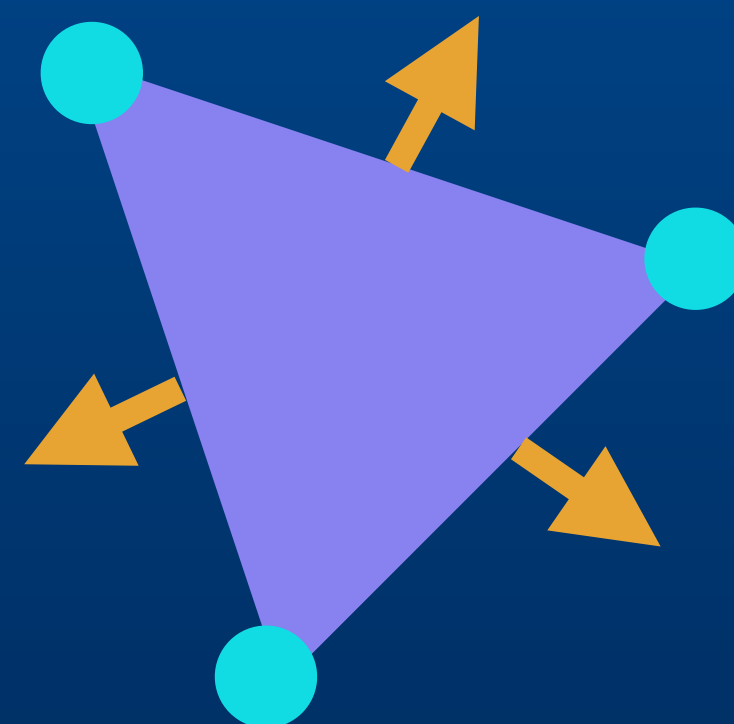
if p >= 0, we are not colliding!

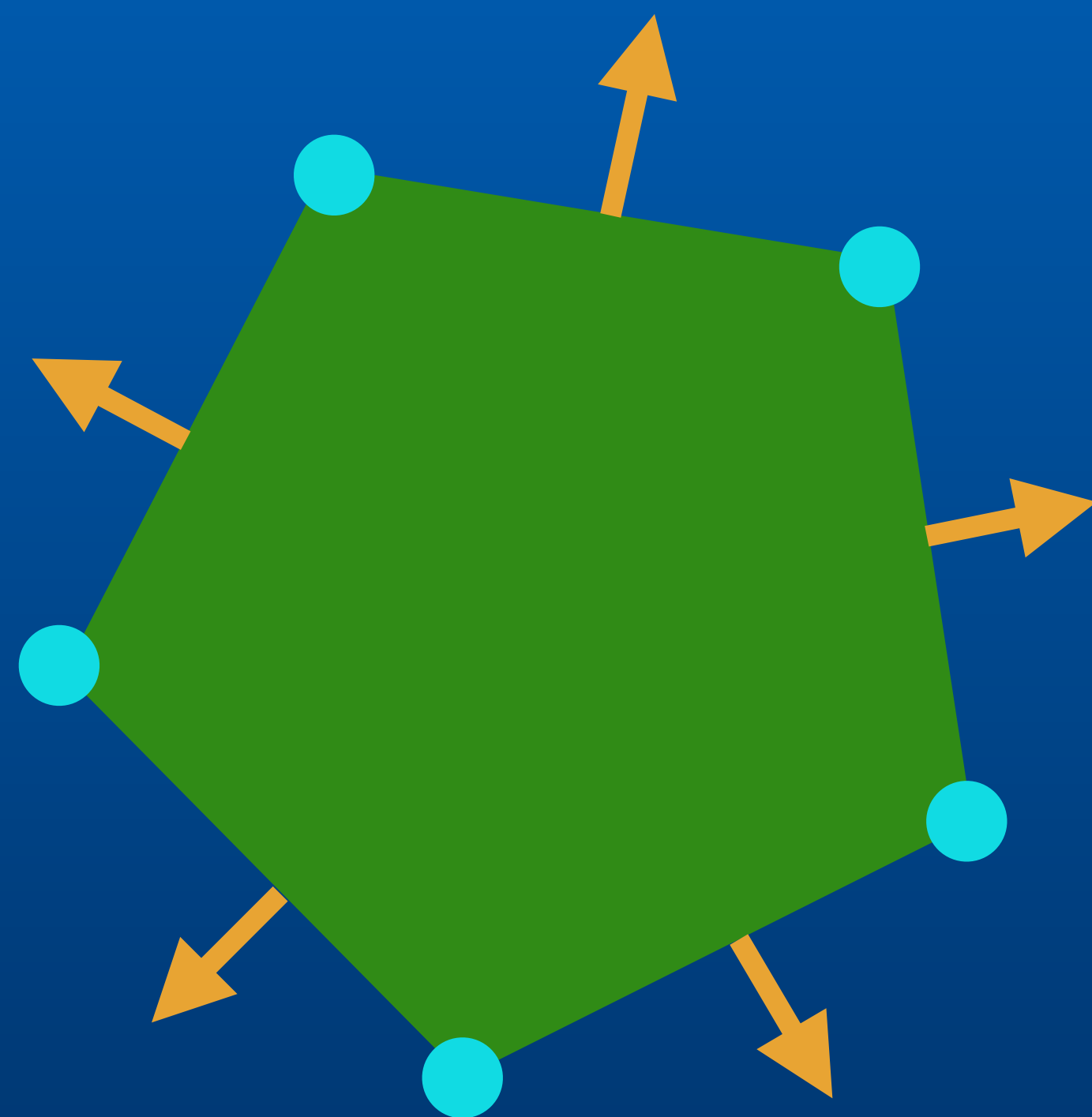Check the separation on each of the 4 normal axes (we don't have to check all 8 since 2 sides of each rectangle are parallel.

If on any axis, there is a separation, the collision is not occurring.

Arbitrary polygon collision.
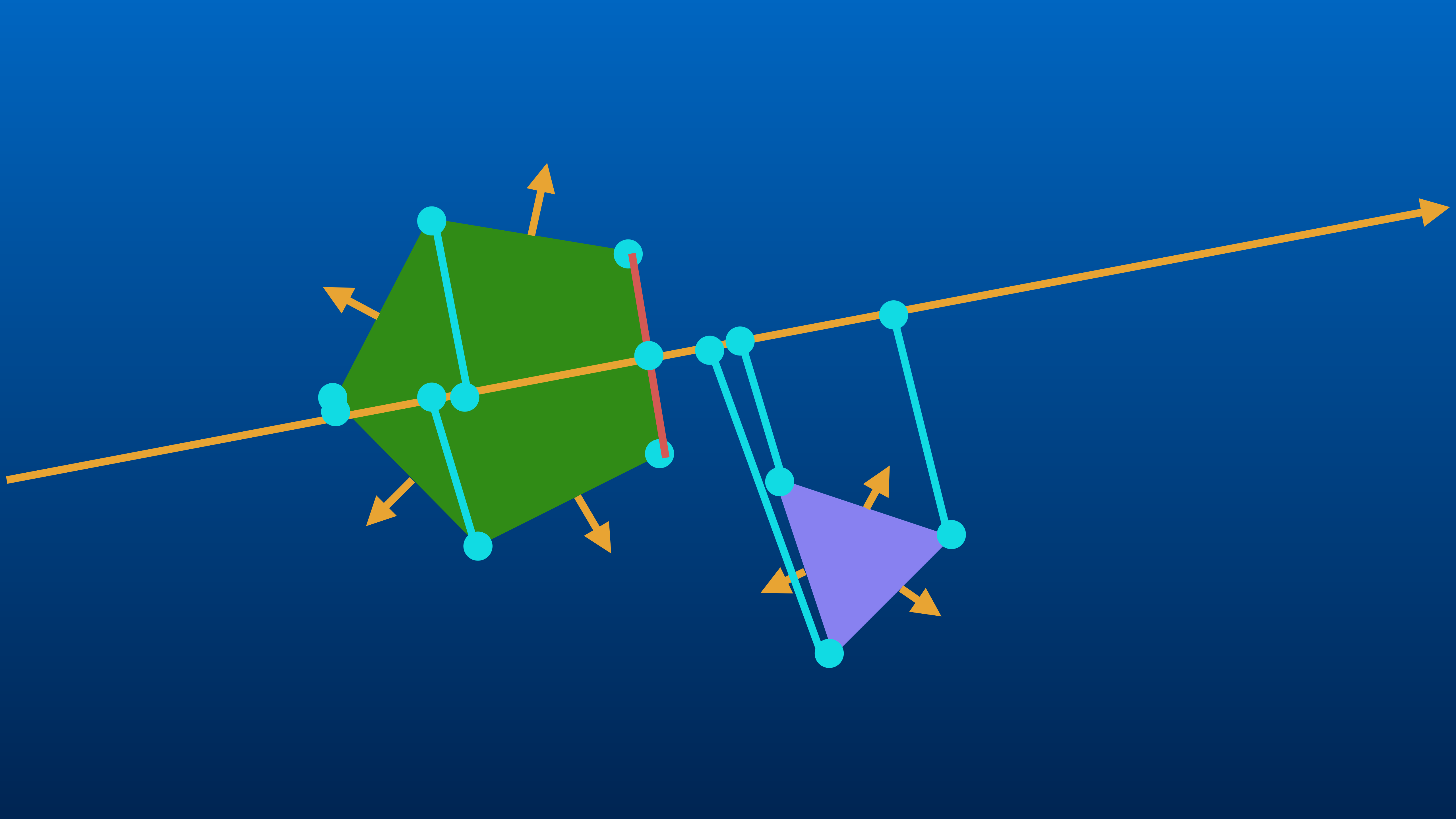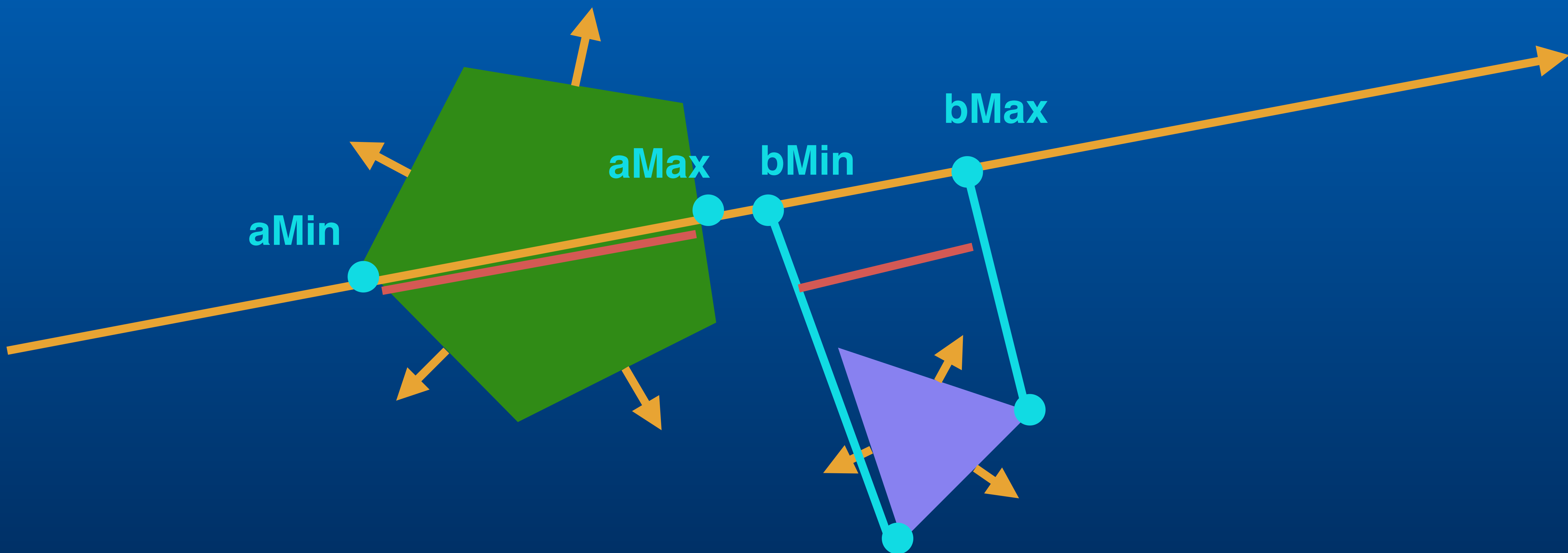
If aMin <= bMax and aMax >= bMin, we have a collision on this axis

Only works with convex polygons!

(every internal angle < 180 degrees and it's not self intersecting)
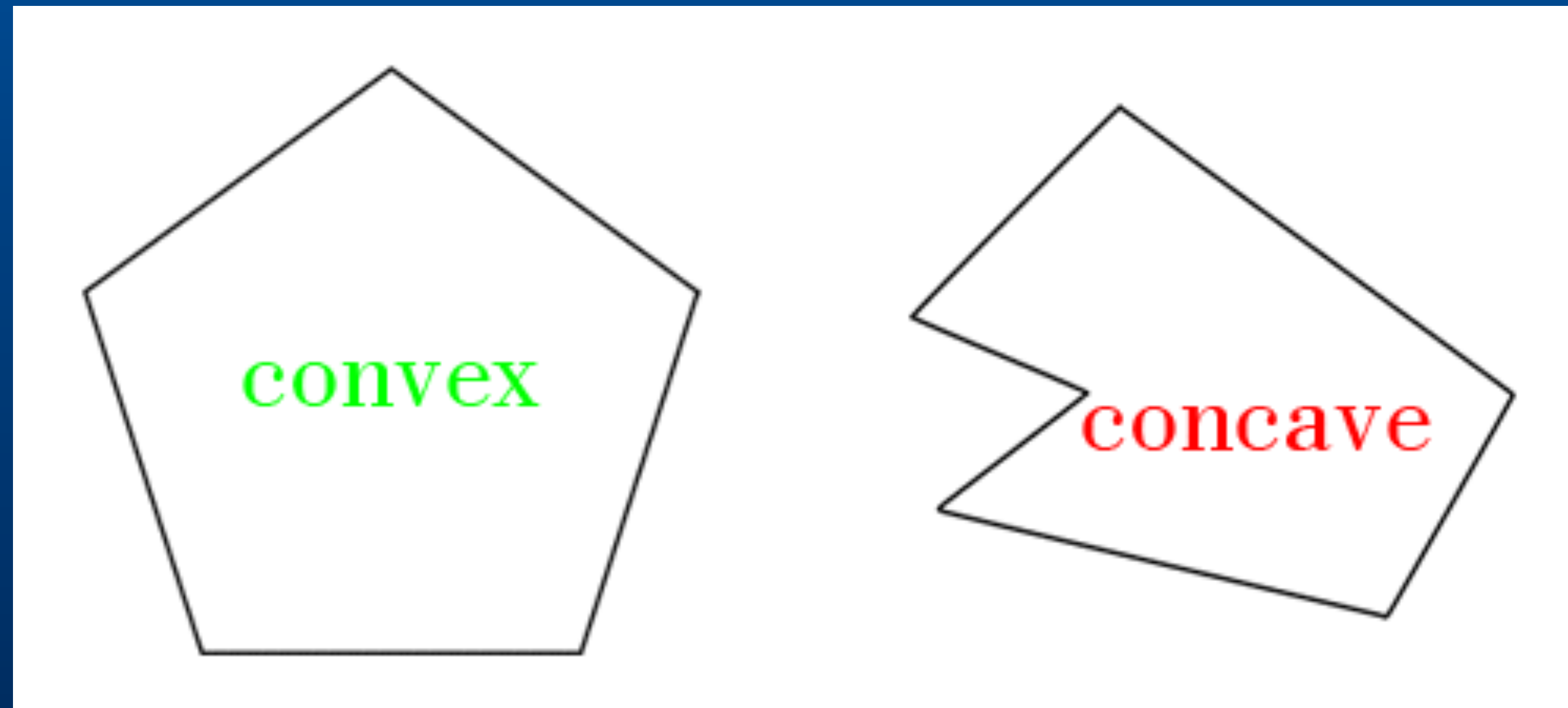
Responding to collisions.
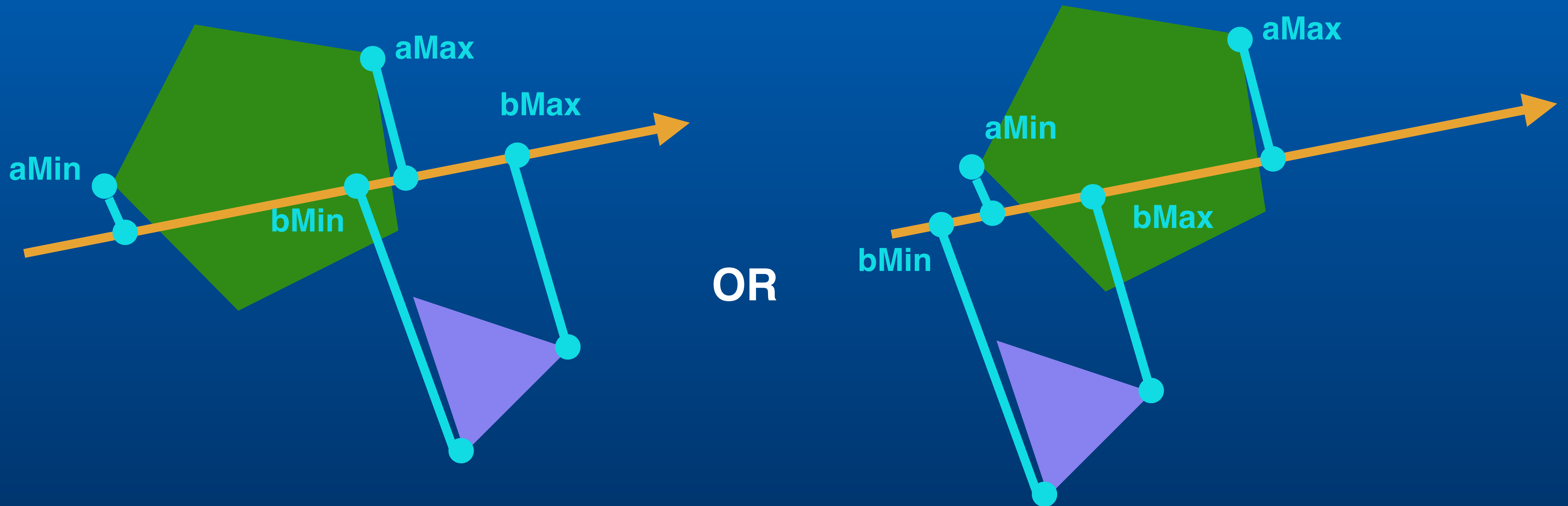
If aMin <= bMax and aMax >= bMin, we have a collision on this axis

FIND THE SMALLER PENETRATION FOR EACH AXIS

OR

$$aMax - bMin \ OR \ bMax - aMin$$

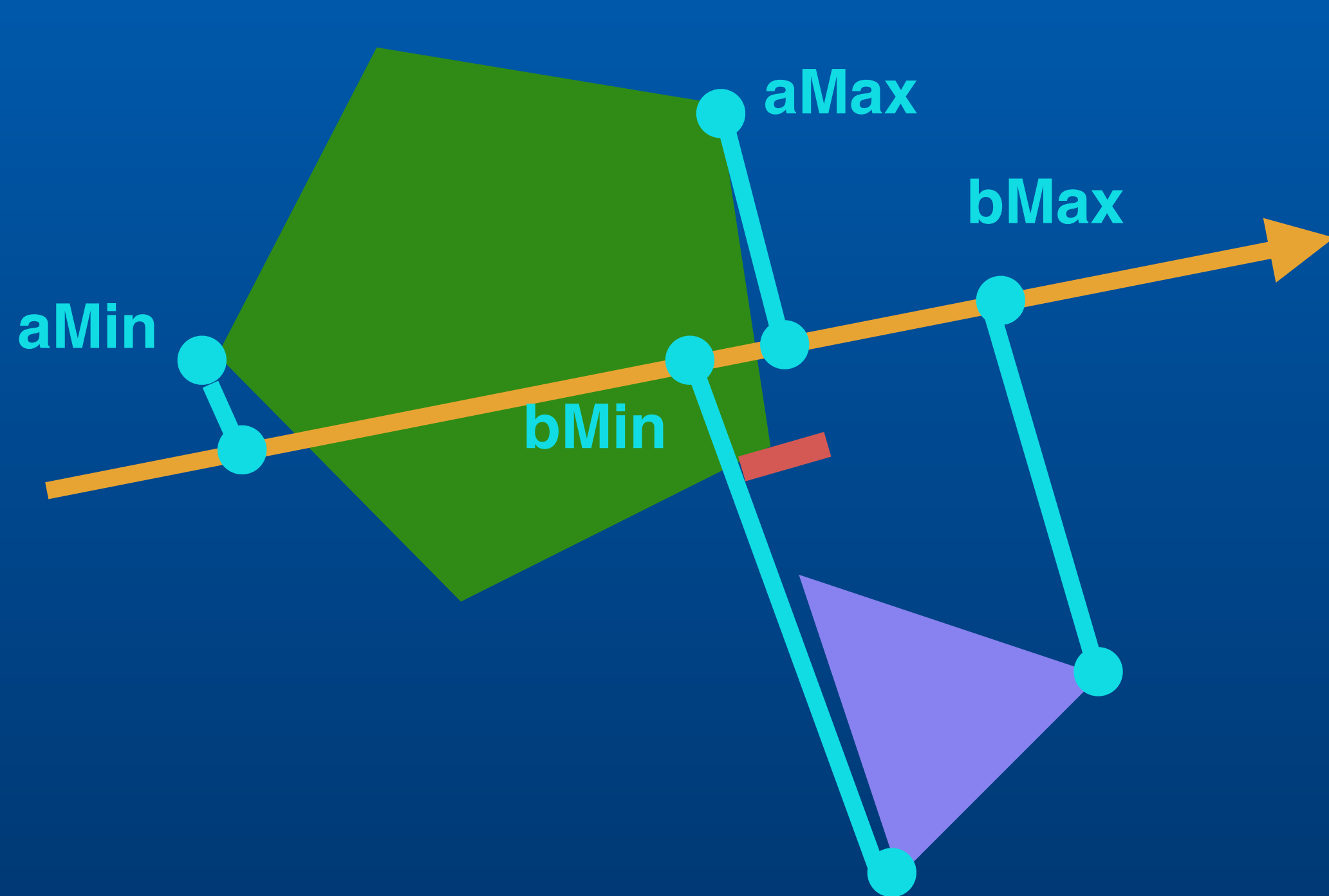THEN TRANSLATE IT BACK INTO WORLD SPACE COORDINATES BY MULTIPLYING BY THE AXIS NORMAL AND SAVE INTO A LIST
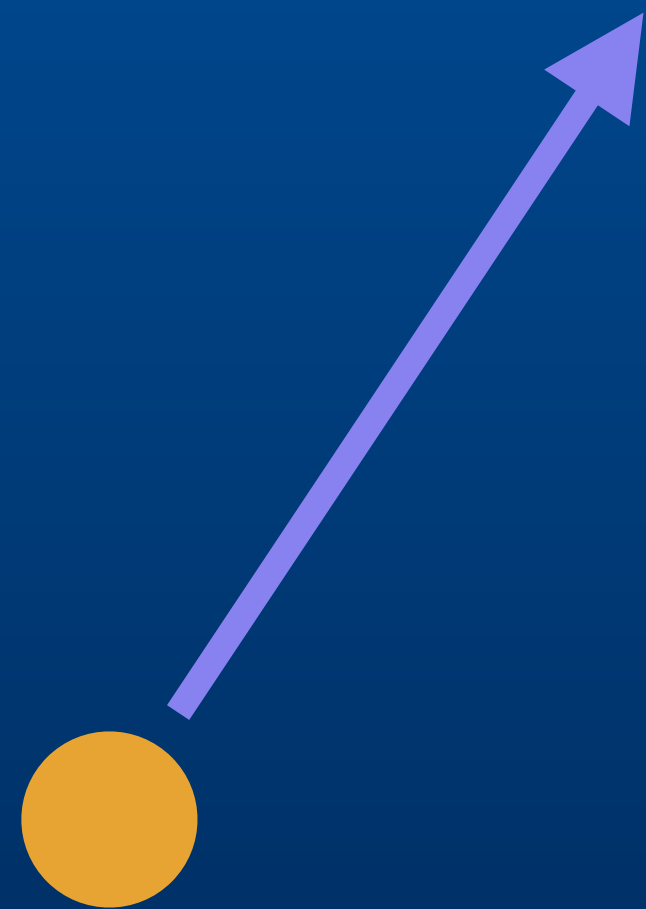
OUR ADJUST VECTOR IS THE SMALLEST PENETRATION VECTOR FROM ALL THE AXES!

Raycasting.

What is a ray?

A ray has an origin position and a direction.

It can be defined as a two vectors, one defining the position and another (unit!) vector defining the direction.
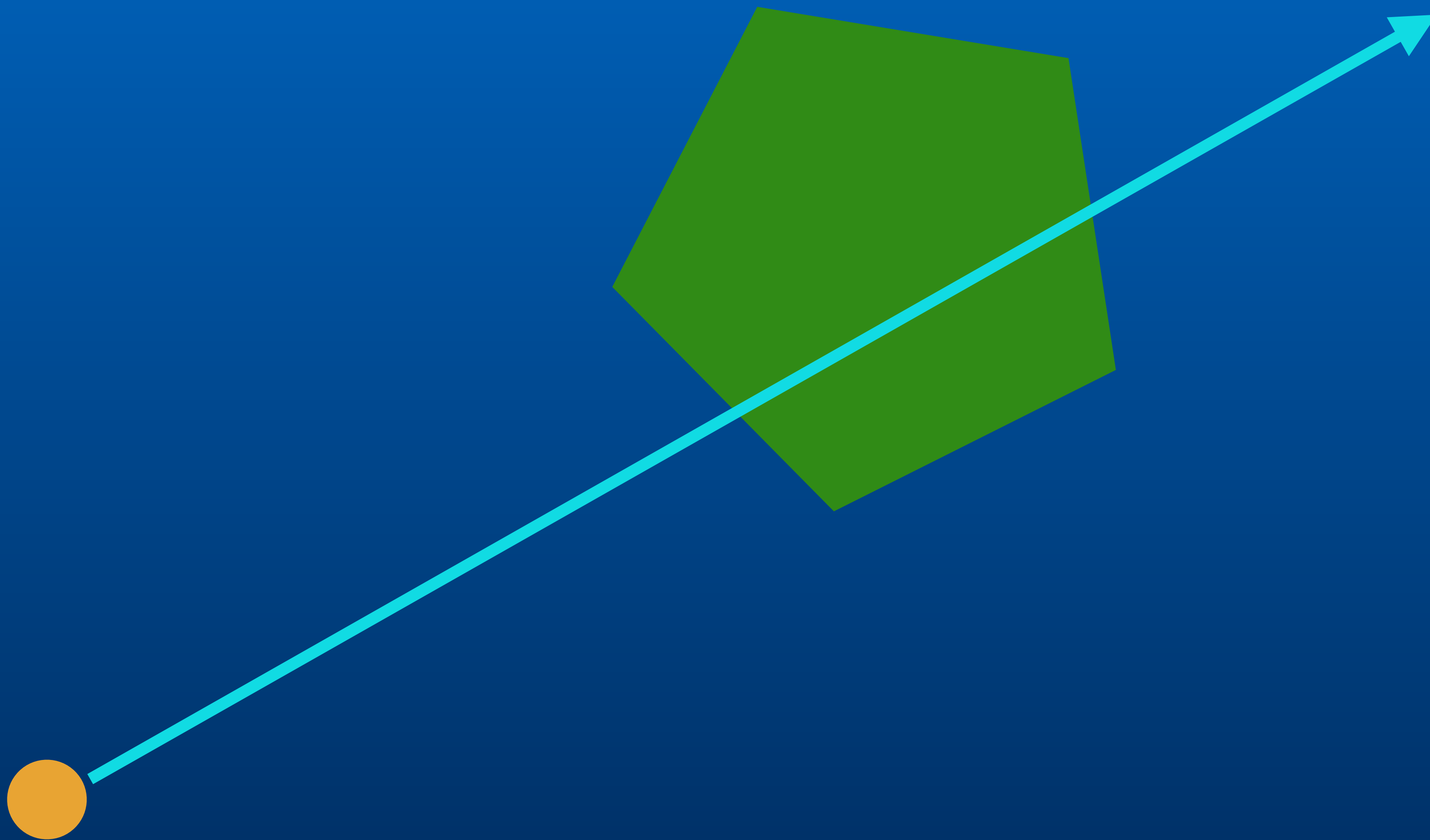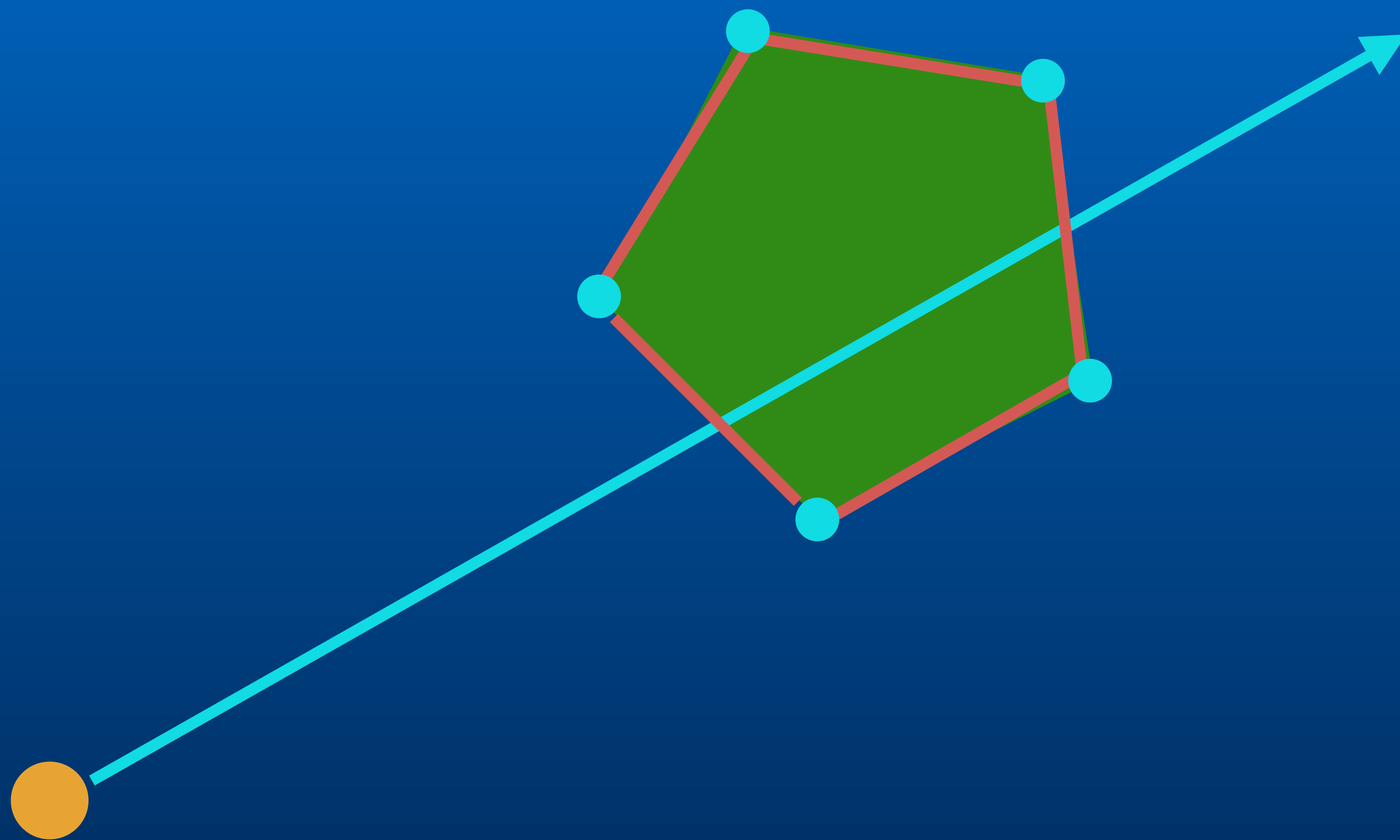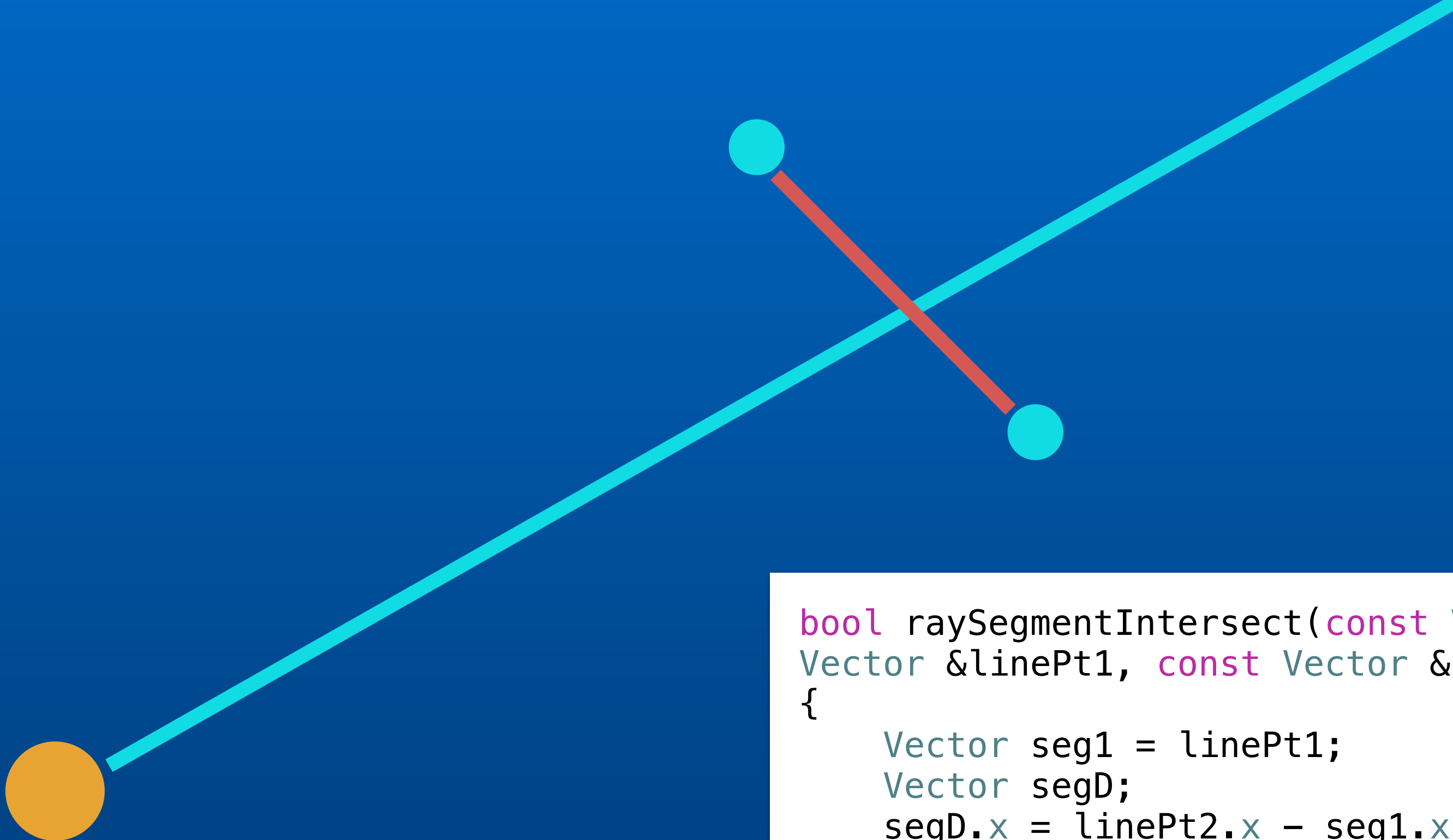
Ray/Polygon intersection test.

```cpp
bool raySegmentIntersect(const Vector &rayOrigin, const Vector &rayDirection, const
Vector &linePt1, const Vector &linePt2, float &dist)
{
    Vector seg1 = linePt1;
    Vector segD;
    segD.x = linePt2.x - seg1.x;
    segD.y = linePt2.y - seg1.y;

    float raySlope = rayDirection.y / rayDirection.x;
    float n  = ((seg1.x - rayOrigin.x)*raySlope + (rayOrigin.y - seg1.y)) / (segD.y -
segD.x*raySlope);

    if (n < 0 || n > 1)
        return false;

    float m = (seg1.x + segD.x * n - rayOrigin.x) / rayDirection.x;
    if (m < 0)
        return false;

    dist = m;
    return true;
}
```
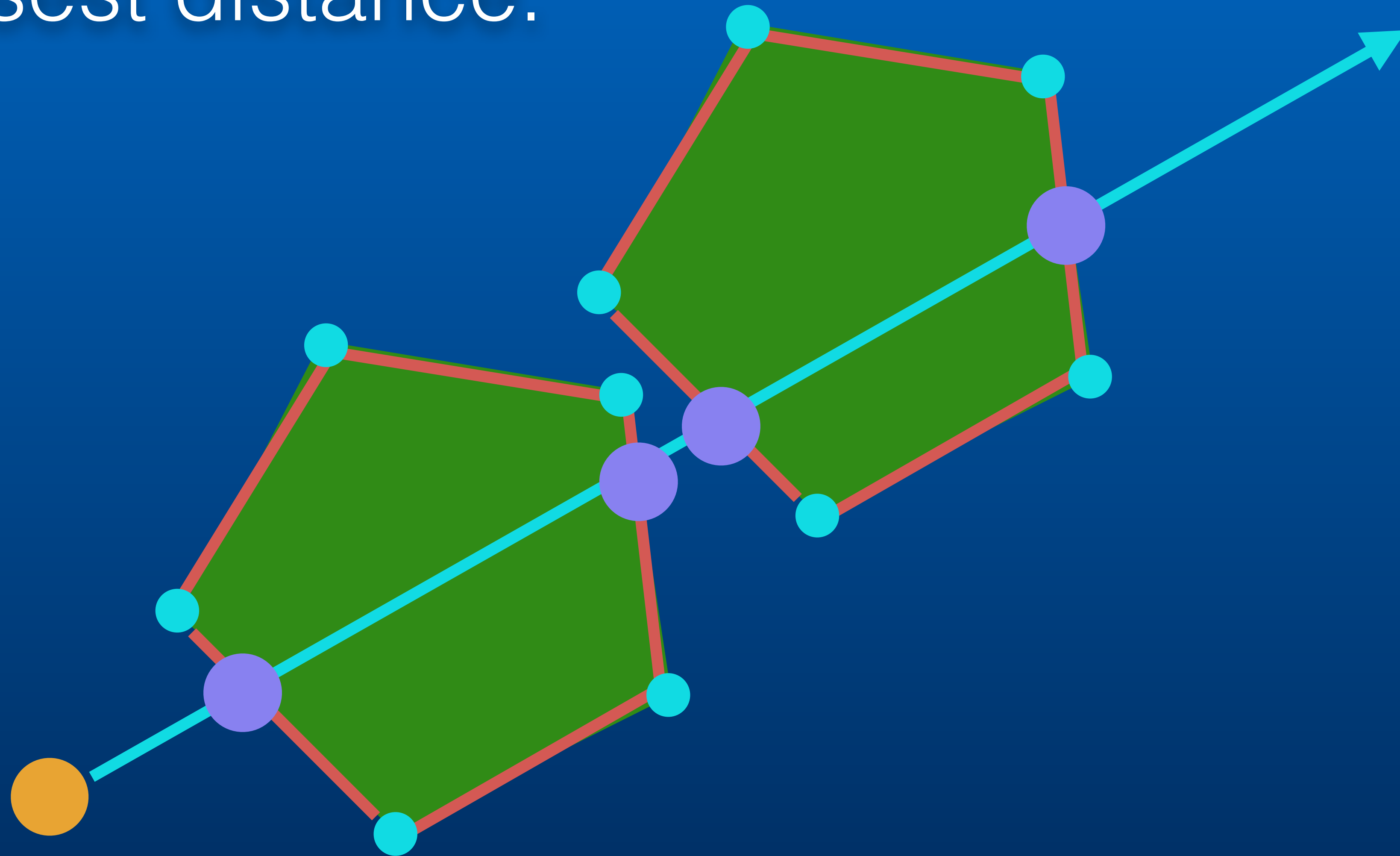
Use closest distance.

Assignment.

Make simple asteroids.

- You have two weeks.
- You must use transformation matrices and non-axis-aligned collisions!

Assignment #2.

- Start thinking about your final project.
- Send me your final project idea by next Thursday.